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CPSC 3300
Homework 1
Due 11:59PM Thursday, January 28
Submit your answers to Canvas

Please provide sufficient space on your homework solutions so that your calculations and answers are easily readable and so that grading will be easier. Furthermore, except for the simplest questions, giving only the answer without showing your work is not acceptable. For the best chance at partial credit, show the generic equation you are starting with and any derivations needed to handle the information as given in the question, then plug in the values from the question. You may, of course, use a calculator for the homework.

1. (30pt) A processor P has a 2.7 GHz clock rate and has a CPI of 1.2.

- (a) If the processor executes a program in 6 seconds, find the number of cycles and the number of instructions.

$$\begin{aligned}\text{Clock Cycles} &= \text{CPU Time} \times \text{Clock Rate} \\ &= 6\text{s} \times 2.7\text{GHZ} \\ &= 16.2 \times 10^9 \text{ cycles}\end{aligned}$$

To find instruction count (IC) use:

$$\begin{aligned}\text{IC} &= (\text{CPU Time} \times \text{Clock Cycle Time}) / \text{CPI} \\ \text{IC} &= (6\text{s} \times 2.7 \times 10^9) / 1.2 \\ \text{IC} &= (1.62 \times 10^{10}) / 1.2 \\ \text{IC} &= 1.35 \times 10^{10} \\ \text{or IC} &= 13,500,000,000\end{aligned}$$

- (b) What is the MIPS rate for the processor?

$$\begin{aligned}\text{MIPS} &= \text{Clock rate} / \text{CPI} \times 10^6 \\ \text{MIPS} &= 2.7 \times 10^9 / 1.2 \times 10^6 \\ \text{MIPS} &= 2250\end{aligned}$$

- (c) We are trying to reduce the execution time by 20% but this leads to an increase of 20% in the CPI. What clock rate should we have to get this time reduction?

$$\begin{aligned}\text{Execution time} &= (\text{instructions} \times \text{CPI}) / \text{clock rate} \\ \text{Execution time}(\text{new}) &= 0.8 \times \text{Execution time}(\text{old}) \\ \text{Therefore} \\ \text{CPI}(\text{new}) / \text{clock rate}(\text{new}) &= 0.8 \times \text{CPI}(\text{old}) / \text{clock rate}(\text{old}) \\ \text{CPI}(\text{new}) &= 1.2, \text{ so} \\ 1.2 / \text{clock rate}(\text{new}) &= 0.8 / \text{clock rate}(\text{old}) \\ \text{Clock rate}(\text{new}) &= 1.2 / 0.8 \times \text{clock rate}(\text{old}) \\ \text{Clock rate}(\text{new}) &= 1.5 \times \text{clock rate}(\text{old}) \\ \text{Therefore the old clock rate must increase by } &50\% \\ \text{Increasing } 2.7\text{GHZ by } 50\% &\text{ yields } \underline{4.05\text{GHZ}}\end{aligned}$$

2. (20pt) Consider two different implementation of the same instruction set architecture. The instructions can be divided into four classes according to their CPI (class A, B, C, and D). P1 has a clock rate of 2.5 GHz and CPIs of 1 (class A), 2 (class B), 3 (class C), and 5 (class D).

Given a program with a dynamic instruction count of 25 million instructions divided into classes as follows: 15% class A, 50% class B, 25% class C, and 10% class D.

- (a) What is the global CPI?

$$A = 1.5 \times 10^5, B = 5 \times 10^5, C = 2.5 \times 10^5, D = 10^5$$

$$\text{Time}(P1) = (1.5 \times 10^5 + 5 \times 10^5 \times 2 + 2.5 \times 10^5 \times 3 + 10^5 \times 4) / (2.5 \times 10^9)$$

$$\text{Time}(P1) = 9.2 \times 10^{-4}$$

$$\text{CPI}(P1) = (9.2 \times 10^{-4}) \times (2.5 \times 10^9) / 10^6$$

$$\text{CPI}(P1) = 2.3$$

- (b) Find the clock cycles required to run the program on P1.

Clock Cycles utilize part of the equation above.

$$A = 1.5 \times 10^5, B = 5 \times 10^5, C = 2.5 \times 10^5, D = 10^5$$

$$\text{Clock Cycles}(P1) = (1.5 \times 10^5 + 5 \times 10^5 \times 2 + 2.5 \times 10^5 \times 3 + 10^5 \times 4)$$

$$\text{Clock Cycles} = 2.3 \times 10^6$$

3. (20pt) Assume for a given processor the CPI of arithmetic instructions is 2, the CPI of load/store instructions is 6, and the CPI of branch instructions is 3. Assume a program has the following instruction breakdowns: 240 million arithmetic instructions, 70 million load/store instructions, 100 million branch instructions.

- (a) Suppose we find a way to double the performance of the arithmetic instructions. What is the speedup of our machine?

The old clock cycles was:

$$(2 \times 240) + (6 \times 70) + (3 \times 100) = 1200$$

To double arithmetic instructions our clock cycles becomes:

$$(1 \times 240) + (6 \times 70) + (3 \times 100) = 960$$

$$\text{Clock cycles}(\text{new})/\text{clock cycles}(\text{old}) = 960/1200 = 0.8$$

The speedup of the machine after doubling the performance of arithmetic instructions was 20%.

- (b) If in addition to the arithmetic instruction optimization we also find a way to double the performance of the load/store instructions, what is the overall speedup of our machine?

The old clock cycle (with optimization) was:

$$(1 \times 240) + (6 \times 70) + (3 \times 100) = 960$$

To double the load/store instructions:

$$(1 \times 240) + (3 \times 70) + (3 \times 100) = 750$$

$$\text{Clock cycles}(\text{new})/\text{clock cycles}(\text{old}) = 750/960 = 0.78125$$

The speedup of the machine was a further increase of 21.875%.

The overall speedup was 20% + 21.875% = 41.875%.

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4. (30pt) On machine newton using the **perf** tool, examine how compiler optimization levels and options change the number of instructions for the program **whetstone** and the number of CPU cycles to execute the program. Use gcc to compile your program. Refer to the following web page for information on how to use **perf** to count the number of instructions and cycles among other statistics: https://perf.wiki.kernel.org/index.php/Tutorial#Counting_with_perf_stat

I: Download the **whetstone** benchmark to your home directory:

<http://www.netlib.org/benchmark/whetstone.c>

Compile whetstone. You may need to explicitly specify the math library folder and link to it, e.g.,

```
gcc -o whetstone whetstone.c -lm
#link the math library with -lm
```

II: Examine the performance of **whetstone** looping 200,000 times

(./**whetstone 200000**) compiled with the following levels/options:

- a. -O0
- b. -O1
- c. -O2
- d. -O3
- e. -O3 -funroll-loops

Use a table to show the instruction count, #cycles, IPC, and time for each of the experiments, and calculate the speedup based on the execution time with -O0. Paste your screen shot at the end.

	IC	#Cycles	IPC	Time (ms)	Speedup
-O0	22,785,254,374	16,920,054,510	1.35	6363	0
-O1	10,957,309,469	8,819,209,982	1.24	3466	45.6%
-O2	6,056,123,284	6,141,991,202	0.99	2503	27.8%
-O3	6,021,948,416	6,127,308,031	0.98	2498	0.2%
-O3 - funroll- loops	5,015,729,716	5,442,507,576	0.92	2245	10.1%

Screenshots:

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```
Console
Enter command: perf stat ./whetstone 200000
Do not execute commands that require user-input or data transfer
Current directory: /home/pwoodru

/home/pwoodru$ gcc -Wall -O0 -o whetstone whetstone.c -lm
/home/pwoodru$ gcc -Wall -O0 -o whetstone whetstone.c -lm
/home/pwoodru$ gcc -Wall -O0 -o whetstone whetstone.c -lm
/home/pwoodru$ perf stat ./whetstone 200000

Loops: 200000, Iterations: 1, Duration: 6 sec.
C Converted Double Precision Whetstones: 3333.3 MIPS

Performance counter stats for './whetstone 200000':

    6356.188955 task-clock (msec)    #    0.999 CPUs utilized
         537    context-switches      #    0.084 K/sec
           0    cpu-migrations        #    0.000 K/sec
          79    page-faults          #    0.012 K/sec
16,920,054,510 cycles                 #    2.662 GHz              (83.35%)
 9,726,905,238 stalled-cycles-frontend # 57.49% frontend cycles idle (83.33%)
 2,140,139,280 stalled-cycles-backend  # 12.65% backend cycles idle (66.67%)
22,785,254,374 instructions          #    1.35 insns per cycle
           #    0.43 stalled cycles per insn (83.34%)
 2,460,954,672 branches               # 387.175 M/sec             (83.33%)
   198,573    branch-misses          #    0.01% of all branches  (83.36%)

 6.363367994 seconds time elapsed
```

```
/home/pwoodru$ gcc -Wall -O1 -o whetstone whetstone.c -lm
/home/pwoodru$ perf stat ./whetstone 200000

Loops: 200000, Iterations: 1, Duration: 3 sec.
C Converted Double Precision Whetstones: 6666.7 MIPS

Performance counter stats for './whetstone 200000':

 3460.495749 task-clock (msec)    #    0.998 CPUs utilized
        288    context-switches      #    0.083 K/sec
           0    cpu-migrations        #    0.000 K/sec
         75    page-faults          #    0.022 K/sec
 8,819,209,982 cycles                 #    2.549 GHz              (83.35%)
 4,545,662,944 stalled-cycles-frontend # 51.54% frontend cycles idle (83.36%)
 1,862,643,971 stalled-cycles-backend  # 21.12% backend cycles idle (66.74%)
10,957,309,469 instructions          #    1.24 insns per cycle
           #    0.41 stalled cycles per insn (83.36%)
 1,633,000,511 branches               # 471.898 M/sec             (83.36%)
   36,409    branch-misses          #    0.00% of all branches  (83.28%)

 3.465877827 seconds time elapsed
```

```
/home/pwoodru$ gcc -Wall -O2 -o whetstone whetstone.c -lm
/home/pwoodru$ perf stat ./whetstone 200000

Loops: 200000, Iterations: 1, Duration: 3 sec.
C Converted Double Precision Whetstones: 6666.7 MIPS

Performance counter stats for './whetstone 200000':

 2498.125735 task-clock (msec)    #    0.998 CPUs utilized
        212    context-switches      #    0.085 K/sec
           0    cpu-migrations        #    0.000 K/sec
         75    page-faults          #    0.030 K/sec
 6,141,991,202 cycles                 #    2.459 GHz              (83.34%)
 4,016,291,532 stalled-cycles-frontend # 65.39% frontend cycles idle (83.36%)
 1,864,407,036 stalled-cycles-backend  # 30.36% backend cycles idle (66.73%)
 6,056,123,284 instructions          #    0.99 insns per cycle
           #    0.66 stalled cycles per insn (83.36%)
 841,009,101 branches               # 336.656 M/sec             (83.35%)
   28,833    branch-misses          #    0.00% of all branches  (83.32%)

 2.502805475 seconds time elapsed
```

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```
/home/pwoodru$ gcc -Wall -O3 -o whetstone whetstone.c -lm
/home/pwoodru$ perf stat ./whetstone 200000
```

```
Loops: 200000, Iterations: 1, Duration: 3 sec.
C Converted Double Precision Whetstones: 6666.7 MIPS
```

Performance counter stats for './whetstone 200000':

2493.290543	task-clock (msec)	#	0.998 CPUs utilized	
210	context-switches	#	0.084 K/sec	
0	cpu-migrations	#	0.000 K/sec	
76	page-faults	#	0.030 K/sec	
6,127,308,031	cycles	#	2.458 GHz	(83.38%)
4,000,625,083	stalled-cycles-frontend	#	65.29% frontend cycles idle	(83.29%)
1,898,448,008	stalled-cycles-backend	#	30.98% backend cycles idle	(66.66%)
6,021,948,416	instructions	#	0.98 insns per cycle	
		#	0.66 stalled cycles per insn	(83.28%)
816,887,378	branches	#	327.634 M/sec	(83.38%)
29,889	branch-misses	#	0.00% of all branches	(83.40%)

2.497963006 seconds time elapsed

```
/home/pwoodru$ gcc -Wall -O3 -funroll-loops -o whetstone whetstone.c -lm
/home/pwoodru$ perf stat ./whetstone 200000
```

```
Loops: 200000, Iterations: 1, Duration: 3 sec.
C Converted Double Precision Whetstones: 6666.7 MIPS
```

Performance counter stats for './whetstone 200000':

2240.948425	task-clock (msec)	#	0.998 CPUs utilized	
190	context-switches	#	0.085 K/sec	
0	cpu-migrations	#	0.000 K/sec	
76	page-faults	#	0.034 K/sec	
5,442,507,576	cycles	#	2.429 GHz	(83.24%)
3,741,091,669	stalled-cycles-frontend	#	68.74% frontend cycles idle	(83.23%)
2,240,581,260	stalled-cycles-backend	#	41.17% backend cycles idle	(66.82%)
5,015,729,716	instructions	#	0.92 insns per cycle	
		#	0.75 stalled cycles per insn	(83.42%)
596,485,616	branches	#	266.176 M/sec	(83.41%)
30,878	branch-misses	#	0.01% of all branches	(83.31%)

2.245343023 seconds time elapsed