# The physica package

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# physica noun. Latin, study of nature.

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# 1. Introduction

<u>Typst</u> is typesetting framework aiming to become the next generation alternative to LATEX. It excels in its friendly user experience and performance.

The physica package provides handy Typst typesetting functions that make academic writing for natural sciences simpler and faster, by simplifying otherwise very complex and repetitive expressions in the domain of natural sciences.

This manual itself was generated using the Typst CLI and the physica package, so hopefully this document is able to provide you with a sufficiently self evident demonstration of how this package shall be used.

## 2. Using physica

With typst's package management:

# 3. The symbols

Some symbols are already provided as a Typst built-in. They are listed here just for completeness with annotation like <sup>typst</sup> this, as users coming from LATEX might not know they are already available in Typst out of box.

All symbols need to be used in **math mode** \$...\$.

#### 3.1. Braces

| Symbol              | Abbr.  | Example   | Notes  |
|---------------------|--------|---|--|
| typst abs (content) |        | $abs(phi(x)) \to  \varphi(x) $  | absolute   |
| typst norm(content) |        | $\mathrm{norm}(\mathrm{phi}(\mathbf{x})) \to \ \varphi(x)\ $  | norm   |
| Order(content)      |        | $\operatorname{Order}(\mathbf{x}^{2}) \to \mathcal{O}(x^2)$   | big O  |
| order(content)      |        | $\mathrm{order(1)} \to o(1)$  | small O  |
| Set(content)        |        | $\begin{split} & \operatorname{Set}(\mathbf{a}_{-}\mathbf{n}) , \operatorname{Set}(\mathbf{a}_{-}\mathbf{i}, \operatorname{forall} \mathbf{i}) \\ & \to \{a_n\}, \{a_i   \forall i\} \\ & \operatorname{Set}(\operatorname{vec}(1,\mathbf{n}), \operatorname{forall} \mathbf{n}) \\ & \to \left\{ \begin{pmatrix} 1 \\ n \end{pmatrix} \middle  \forall n \right\} \end{split}$ | math set, use Set not set since<br>the latter is a Typst keyword   |
| evaluated(content)  |        | evaluated(f(x))_0^oo<br>$ \rightarrow f(x) _0^\infty \\ \text{evaluated(f(x)/g(x))_0^1} \\ \rightarrow \frac{f(x)}{g(x)}\Big _0^1 $   | attach a vertical bar on the right to denote evaluation boundaries |
| expectationvalue    | expval | $\begin{array}{l} \text{expval(u)} \to \langle u \rangle \\ \text{expval(p,psi)} \to \langle \psi   p   \psi \rangle \end{array}$   | expectation value, also see braket Section 3.4 below               |

# 3.2. Vector notations

| Symbol                         | Abbr. | Example  | Notes   |
|--------------------------------|-------|--|---|
| typst vec ()                   |       | $\operatorname{vec}(1,2) \to \begin{pmatrix} 1 \\ 2 \end{pmatrix}$   | column vector                                     |
| vecrow()                       |       | vecrow(alpha, b) $ \to (\alpha,b) $ vecrow(sum_0^n i, b, delim:"[")  | row vector  |
|                                |       | $\rightarrow \left[\sum_{0}^{n} i, b\right]$   |   |
| ТТ                             |       | $v^T$ , $A^T$ $\to v^T$ , $A^T$  | transpose, also see<br>Section 3.7.1              |
| <pre>vectorbold(content)</pre> | vb    | vb(a),vb(mu_1) $ ightarrow a, \mu_1$   | vector, bold                                      |
| <pre>vectorunit(content)</pre> | vu    | vu(a),vu(mu_1) $ ightarrow \hat{a},\hat{\mu}_1$  | unit vector                                       |
| vectorarrow(content)           | va    | va(a),va(mu_1) $ ightarrow ec{a},ec{\mu}_1$  | vector, arrow<br>(not bold: see ISO 80000-2:2019) |
| grad                           |       | grad f $	o oldsymbol{ abla} f$   | gradient  |
| div                            |       | div vb(E) $ ightarrow oldsymbol{ abla} \cdot oldsymbol{E}$   | divergence  |
| curl                           |       | curl vb(B) $ ightarrow oldsymbol{ abla}	imes oldsymbol{B}$   | curl  |
| laplacian                      |       | diaer(u) = c^2 laplacian u $\rightarrow \ddot{u} = c^2 \nabla^2 u$   | Laplacian, not $^{	ext{typst}}$ laplace $\Delta$  |
| dotproduct                     | dprod | a dprod b $ ightarrow a \cdot b$   | dot product                                       |
| crossproduct                   | cprod | a cprod b $\longrightarrow a \times b$   | cross product                                     |
| innerproduct                   | iprod | $\begin{array}{l} \mathrm{iprod}(\mathbf{u},\ \mathbf{v}) \longrightarrow \langle u,v \rangle \\ \mathrm{iprod}(\mathrm{sum\_i}\ \mathrm{a\_i},\ \mathrm{b}) \\ \longrightarrow \left\langle \sum_i a_i,b \right\rangle \end{array}$ | inner product                                     |

# 3.3. Matrix notations

# 3.3.1. Determinant, (anti-)diagonal, identity, zero matrix

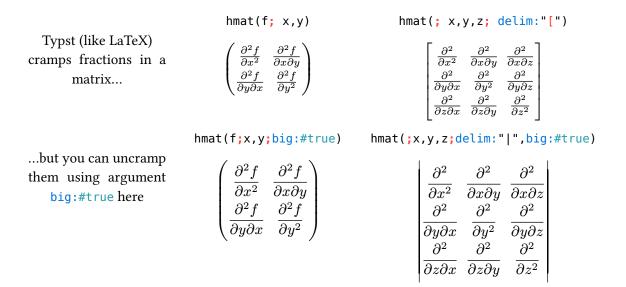
| Symbol                 | Abbr. | Example  | Notes                                |
|------------------------|-------|--|--------------------------------------|
| Π                      |       | $\mathbf{v}^{\wedge}TT, \ \mathbf{A}^{\wedge}TT \longrightarrow v^{T}, A^{T}$  | transpose, also see<br>Section 3.7.1 |
| typst mat()            |       |  | matrix                               |
| <pre>matrixdet()</pre> | mdet  | $mdet(1,x;1,y) \rightarrow \begin{vmatrix} 1 & x \\ 1 & y \end{vmatrix}$   | matrix determinant                   |
| diagonalmatrix()       | dmat  | $dmat(1,2) \rightarrow \begin{pmatrix} 1 \\ 2 \end{pmatrix}$   | diagonal matrix                      |
| antidiagonalmatrix()   | admat | $\begin{aligned} & \operatorname{dmat}(1,a,xi,\operatorname{delim}:"[",\operatorname{fill}:0) \\ & \to \begin{bmatrix} 1 & 0 & 0 \\ 0 & a & 0 \\ 0 & 0 & \xi \end{bmatrix} \\ & \operatorname{admat}(1,2) \to \begin{pmatrix} 1 \\ 2 \end{bmatrix} \\ & \operatorname{admat}(1,a,xi,\operatorname{delim}:"[",\operatorname{fill}:\operatorname{dot}) \\ & \to \begin{bmatrix} \cdot & 1 \\ \cdot & a & \cdot \\ \xi & \cdot & \cdot \end{bmatrix} \end{aligned}$ | anti-diagonal matrix                 |

#### 3.3.2. Jacobian matrix

jacobianmatrix(...), i.e. jmat(...).

#### 3.3.3. Hessian matrix

hessianmatrix(...), i.e. hmat(...).



#### 3.3.4. Matrix with an element builder

xmatrix(m, n, func), i.e. xmat(...). The element building function func takes two integers which are the row and column numbers starting from 1.

#let 
$$g = (i,j) \Rightarrow $g^(\#(i - 1)\#(j - 1))$$$
  
xmat(2, 2, #g)

$$\begin{pmatrix} g^{00} & g^{01} \\ g^{10} & g^{11} \end{pmatrix}$$

### 3.3.5. Rotation matrices, 2D and 3D

| rot2mat(theta)   | <pre>rot2mat(-a/2,delim:"[")</pre>   | <pre>rot2mat(display(a/2),delim:"[")</pre>   |
|--|--|--|
| $ \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix} $                        | $\begin{bmatrix} \cos(-\frac{a}{2}) & -\sin(-\frac{a}{2}) \\ \sin(-\frac{a}{2}) & \cos(-\frac{a}{2}) \end{bmatrix}$          | $\begin{bmatrix} \cos\frac{a}{2} & -\sin\frac{a}{2} \\ \sin\frac{a}{2} & \cos\frac{a}{2} \end{bmatrix}$  |
| <pre>rot3xmat(theta)</pre>   | <pre>rot3ymat(45^degree)</pre>   | <pre>rot3zmat(theta,delim:"[")</pre>   |
| $\begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta \\ 0 & \sin \theta & \cos \theta \end{pmatrix}$ | $\begin{pmatrix} \cos 45^{\circ} & 0 & \sin 45^{\circ} \\ 0 & 1 & 0 \\ -\sin 45^{\circ} & 0 & \cos 45^{\circ} \end{pmatrix}$ | $\begin{bmatrix} \cos\theta & -\sin\theta & 0 \\ \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$ |

#### 3.3.6. Gram matrix

$$\begin{array}{c} \text{grammat(alpha,beta)} & \text{grammat(v\_1,v\_2,v\_3,} \\ \begin{pmatrix} \langle \alpha,\alpha \rangle \ \langle \alpha,\beta \rangle \\ \langle \beta,\alpha \rangle \ \langle \beta,\beta \rangle \end{pmatrix} & \begin{bmatrix} \langle v_1,v_1 \rangle \ \langle v_1,v_2 \rangle \ \langle v_1,v_3 \rangle \\ \langle v_2,v_1 \rangle \ \langle v_2,v_2 \rangle \ \langle v_2,v_3 \rangle \\ \langle v_3,v_1 \rangle \ \langle v_3,v_2 \rangle \ \langle v_3,v_3 \rangle \end{bmatrix} & \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \end{pmatrix} \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_1 \rangle \ \|v_2\|^2 \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_2 \rangle \ \langle v_2,v_2 \rangle \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_2 \rangle \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ \langle v_2,v_2 \rangle \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2 \rangle \\ & \begin{pmatrix} \|v_1\|^2 \ \langle v_1,v_2$$

### 3.4. Dirac braket notations

| Symbol                     | Abbr. | Example   | Notes                                 |
|----------------------------|-------|---|---------------------------------------|
| bra(content)               |       | $\operatorname{bra}(u) 	o \langle u   $ $\operatorname{bra}(\operatorname{vec}(1,2)) 	o \left\langle \left(\begin{smallmatrix} 1 \\ 2 \end{smallmatrix}\right) \right $                           | bra                                   |
| ket(content)               |       | $\ker(u) 	o  u\rangle$ $\ker(vec(1,2)) 	o \left  \binom{1}{2} \right\rangle$  | ket                                   |
| braket()                   |       | $\begin{array}{l} \text{braket(a), braket(u, v)} \\ \to \langle a a\rangle, \langle u v\rangle \\ \text{braket(psi,A/N,phi)} \to \langle \psi\big \frac{A}{N}\big \varphi\big\rangle \end{array}$ | braket, with 1, 2, or 3 arguments     |
| ketbra()                   |       | ketbra(a), ketbra(u, v) $ \to  a\rangle\langle a ,  u\rangle\langle v $ ketbra(a/N, b) $\to \left \frac{a}{N}\right\rangle\langle b $   | ketbra, with 1 or 2 arguments         |
| expval(content)            |       | expval(u) $ ightarrow \langle u  angle$ expval(A,psi) $ ightarrow \langle \psi   A   \psi  angle$   | expectation                           |
| <pre>matrixelement()</pre> | mel   | mel(n, partial_nu H, m) $ ightarrow \langle n \partial_{ u}H m angle$   | matrix element, same as braket(n,M,n) |

### 3.5. Math functions

Typst built-in math operators: <a href="math.op">math.op</a>.

| Expressions | Results |
|-------------|---------|
|-------------|---------|

| sin(x), | sinh(x), | <pre>arcsin(x),</pre> | asin(x) | $\sin(x), \sinh(x), \arcsin(x), \sin(x)$  |
|---------|----------|-----------------------|---------|---|
| cos(x), | cosh(x), | arccos(x),            | acos(x) | $\cos(x), \cosh(x), \arccos(x), \cos(x)$  |
| tan(x), | tanh(x), | <pre>arctan(x),</pre> | atan(x) | $\tan(x), \tanh(x), \arctan(x), \tan(x)$  |
| sec(x), | sech(x), | arcsec(x),            | asec(x) | $\sec(x), \operatorname{sech}(x), \operatorname{arcsec}(x), \operatorname{asec}(x)$ |
| csc(x), | csch(x), | <pre>arccsc(x),</pre> | acsc(x) | $\csc(x), \operatorname{csch}(x), \operatorname{arccsc}(x), \operatorname{acsc}(x)$ |
| cot(x), | coth(x), | <pre>arccot(x),</pre> | acot(x) | $\cot(x), \coth(x), \operatorname{arccot}(x), \operatorname{acot}(x)$               |

| Expressions             | Results                                      | Notes   |
|-------------------------|--|---|
| typst Pr(x)             | $\Pr(x)$                                     | probability   |
| <sup>typst</sup> exp x  | $\exp x$                                     | exponential   |
| typst log x, lg x, ln x | $\log x, \lg x, \ln x$                       | logarithmic   |
| lb x                    | $\operatorname{lb} x$                        | binary logarithm  |
| <sup>typst</sup> det A  | $\det A$                                     | matrix determinant  |
| diag(-1,1,1,1)          | diag(-1, 1, 1, 1)                            | diagonal matrix, compact form (use dmat for the "real" matrix form) |
| trace A, tr A           | $\operatorname{trace} A,\operatorname{tr} A$ | matrix trace  |
| Trace A, Tr A           | $\operatorname{Trace} A,\operatorname{Tr} A$ | matrix trace, alt.  |
| rank A                  | $\operatorname{rank} A$                      | matrix rank   |
| erf(x)                  | $\operatorname{erf}(x)$                      | Gauss error function  |
| Res A                   | $\operatorname{Res} A$                       | residue (complex analysis)  |
| Re z, Im z              | ${\rm Re}z, {\rm Im}z$                       | real, imaginary (complex analysis)                                  |
| sgn x                   | $\operatorname{sgn} x$                       | sign function   |

## 3.6. Differentials and derivatives

| Symbol              | Abb | r.Example   | Notes  |
|---------------------|-----|---|--|
| differential()      | dd  | e.g. $df$ , $dx dy$ , $d^3x$ , $dx \wedge dy$<br>See Section 3.6.1  | differential                                       |
| variation()         | var | ${\sf var}({\sf f}) 	o \delta f$ ${\sf var}({\sf x},{\sf y}) 	o \delta x \delta y$  | <pre>variation, shorthand of dd(, d: delta)</pre>  |
| difference()        |     | $\begin{array}{l} \text{difference(f)} \rightarrow \Delta f \\ \text{difference(x,y)} \rightarrow \Delta x \Delta y \end{array}$  | <pre>difference, shorthand of dd(, d: Delta)</pre> |
| derivative()        | dv  | e.g. $\frac{\mathrm{d}}{\mathrm{d}x}, \frac{\mathrm{d}f}{\mathrm{d}x}, \frac{\Delta^k f}{\Delta x^k}, \mathrm{d}f/\mathrm{d}x$<br>See Section 3.6.2   | derivative   |
| partialderivative() | pdv | e.g. $\frac{\partial}{\partial x}$ , $\frac{\partial f}{\partial x}$ , $\frac{\partial^4 f}{\partial x^2 \partial y^2}$ , $\frac{\partial^5 f}{\partial x^2 \partial y^3}$ , $\frac{\partial}{\partial f} / \frac{\partial}{\partial x}$<br>See Section 3.6.3 | partial derivative, could be mixed order           |

### 3.6.1. Differentials

Functions: differential(\*args, \*\*kwargs), abbreviated as dd(...).

- positional *args*: the variable names, **optionally** followed by an order number e.g. 2, or an order array e.g. [2,3], [k], [m n, lambda+1].
- named *kwargs*:

- ► d: the differential symbol [default: upright(d)].
- p: the product symbol connecting the components [default: none].
- compact: only effective if p is none. If #true, will remove the TeXBook-advised thin spaces between the d-units [default: #false].

TeXBook advises [f]ormulas involving calculus look best when an extra thin space appears before dx or dy or d whatever (Chapter 18 p.168), and this package heeds this advice. If you don't want the spaces between the d-units, you may pass a compact:#true argument:  $drd\theta$  vs.  $drd\theta$  (compact).

#### Order assignment algorithm:

- If there is no order number or order array, all variables have order 1.
- If there is an order number (not an array), then this order number is assigned to *every* variable, e.g. dd(x,y,2) assigns  $x \leftarrow 2, y \leftarrow 2$ .
- If there is an order array, then the orders therein are assigned to the variables in order, e.g. dd(f,x,y,[2,3]) assigns  $x \leftarrow 2, y \leftarrow 3$ .
- If the order array holds fewer elements than the number of variables, then the orders of the remaining variables are 1, e.g. dd(x,y,z,[2,3]) assigns  $x \leftarrow 2, y \leftarrow 3, z \leftarrow 1$ .
- If a variable x has order 1, it is rendered as dx not  $d^{1}x$ .

#### **Examples**

#### 3.6.2. Ordinary derivatives

Function: derivative(f, \*args, \*\*kwargs), abbreviated as dv(...).

- *f*: the function, which can be #none or omitted,
- positional args: the variable name, **optionally** followed by an order number e.g. 2,
- named kwargs:
  - → d: the differential symbol [default: upright(d)].
  - s: the "slash" separating the numerator and denominator [default: none], by default it produces the normal fraction form  $\frac{\mathrm{d}f}{\mathrm{d}x}$ . The most common non-defaults are (1) \/, so as to create a flat form  $\mathrm{d}f/\mathrm{d}x$  that fits inline; and (2) large, so that "d/dx" operator is put in front of the (potentially very large) function expression, and the size of the parentheses are adapted to match the highest of the operator and the function expression.

**Order assignment algorithm:** there is just one variable, so the assignment is trivial: simply assign the order number (default to 1) to the variable. If a variable x has order 1, it is rendered as x not  $x^1$ .

(1) 
$$dv(,x)$$
,  $dv(,x,2)$ ,  $dv(f,x,k+1)$  (2)  $dv(,vb(r))$ ,  $dv(f,vb(r)_e, 2)$ 

$$\frac{\mathrm{d}}{\mathrm{d}x}, \frac{\mathrm{d}^2}{\mathrm{d}x^2}, \frac{\mathrm{d}^{k+1}f}{\mathrm{d}x^{k+1}} \qquad \qquad \frac{\mathrm{d}}{\mathrm{d}r}, \frac{\mathrm{d}^2}{\mathrm{d}r_e^2}$$

$$(3) \, \mathrm{dv}(\mathsf{f},\mathsf{x},\mathsf{2},\mathsf{s}: \backslash /), \, \, \mathrm{dv}(\mathsf{f},\mathsf{x}\mathsf{i},\mathsf{k}+\mathsf{1},\mathsf{s}: \backslash /) \qquad \qquad (4) \, \mathrm{dv}((\mathsf{sum} \, \mathsf{f_i} \, (\mathsf{x}) \, \, \mathrm{dd}(\mathsf{x})), \mathsf{x}, \mathsf{s}: \text{"large"})$$

$$\frac{\mathrm{d}^2 f/\mathrm{d}x^2}{\mathrm{d}x^2}, \frac{\mathrm{d}^{k+1}f/\mathrm{d}\xi^{k+1}}{\mathrm{d}\xi^{k+1}} \qquad \qquad \frac{\mathrm{d}}{\mathrm{d}x} \left(\sum f_i(x) \, \mathrm{d}x\right)$$

$$(5) \, \mathrm{dv}(\mathsf{x}, \mathsf{x}, \mathsf{d}: \mathsf{delta}), \, \, \mathrm{dv}(\mathsf{x}, \mathsf{x}, \mathsf{2}, \mathsf{d}: \mathsf{Delta}) \qquad \qquad (6) \, \mathrm{dv}(\mathsf{vb}(\mathsf{u}), \, \mathsf{t}, \mathsf{2}, \, \mathsf{d}: \mathsf{upright}(\mathsf{D}))$$

$$\frac{\delta}{\delta x}, \frac{\Delta^2}{\Delta x^2} \qquad \qquad \frac{\mathrm{D}^2 u}{\mathrm{D}t^2}$$

$$(7) \, \mathrm{dv}(\mathsf{vb}(\mathsf{u}), \mathsf{t}, \mathsf{2}, \mathsf{d}: \mathsf{upright}(\mathsf{D}), \mathsf{s}: \text{"large"})$$

$$\frac{\mathrm{D}^2 u}{\mathrm{D}t^2} \qquad \qquad \frac{\mathrm{D}^2}{\mathrm{D}t^2} \left(u + v\right)$$

#### 3.6.3. Partial derivatives (incl. mixed orders)

Function: partialderivative(f, \*args, \*\*kwargs), abbreviated as pdv(...).

- f: the function, which can be #none or omitted,
- positional *args*: the variable names, **optionally** followed by an order number e.g. 2, or an order array e.g. [2,3], [k], [m n, lambda+1].
- named kwargs:
  - d: the differential symbol [default: partial].
  - ightharpoonup s: the "slash" separating the numerator and denominator [default: none], by default it produces the normal fraction form  $\frac{\partial f}{\partial x}$ . The most common non-defaults non-defaults are (1) \/, so as to create a flat form  $\mathrm{d}f/\mathrm{d}x$  that fits inline, and (2) "large", so that "d/dx" operator is put in front of the (potentially very large) function expression, and the size of the parentheses are adapted to match the highest of the operator and the function expression.
  - total: the user-specified total order.
    - If it is absent, then (1) if the orders assigned to all variables are numeric, the total order number will be automatically computed; (2) if non-number symbols are present, computation will be attempted with minimum effort, and a user override with argument total may be necessary.

#### Order assignment algorithm:

- If there is no order number or order array, all variables have order 1.
- If there is an order number (not an array), then this order number is assigned to *every* variable, e.g. pdv(f,x,y,2) assigns  $x \leftarrow 2, y \leftarrow 2$ .
- If there is an order array, then the orders therein are assigned to the variables in order, e.g. pdv(f,x,y,[2,3]) assigns  $x \leftarrow 2, y \leftarrow 3$ .
- If the order array holds fewer elements than the number of variables, then the orders of the remaining variables are 1, e.g. pdv(f,x,y,z,[2,3]) assigns  $x \leftarrow 2, y \leftarrow 3, z \leftarrow 1$ .
- If a variable x has order 1, it is rendered as x, not  $x^1$ .

(1) 
$$\operatorname{pdv}(,x)$$
,  $\operatorname{pdv}(,t,2)$ ,  $\operatorname{pdv}(,\operatorname{lambda},[k])$  (2)  $\operatorname{pdv}(f,\operatorname{vb}(r))$ ,  $\operatorname{pdv}(\operatorname{phi},\operatorname{vb}(r)_e,2)$ 

$$\frac{\partial}{\partial x},\frac{\partial^2}{\partial t^2},\frac{\partial^k}{\partial \lambda^k}$$

$$\frac{\partial \varphi}{\partial r},\frac{\partial^2 \varphi}{\partial r^2_e}$$
(3)  $\operatorname{pdv}(,x,y)$ ,  $\operatorname{pdv}(,x,y,2)$  (4)  $\operatorname{pdv}(f,x,y,2)$ ,  $\operatorname{pdv}(f,x,y,3)$ 

$$\frac{\partial^2}{\partial x \partial y}, \frac{\partial^4}{\partial x^2 \partial y^2} \qquad \qquad \frac{\partial^4 \varphi}{\partial x^2 \partial y^2}, \frac{\partial^6 \varphi}{\partial x^3 \partial y^3}$$
 (5)  $\operatorname{pdv}(x,y,[2,]), \operatorname{pdv}(x,y,[1,2])$  (6)  $\operatorname{pdv}(x,y,[2,]), \operatorname{pdv}(x,y,[2,]), \operatorname{pdv}(x,[2,]), \operatorname{pdv}(x,[2,$ 

(15) integral\_V dd(V) (pdv(cal(L), phi) - partial\_mu (pdv(cal(L), (partial\_mu phi))))
= 0

$$\int_{V} dV \left( \frac{\partial \mathcal{L}}{\partial \varphi} - \partial_{\mu} \left( \frac{\partial \mathcal{L}}{\partial (\partial_{\mu} \varphi)} \right) \right) = 0$$

#### 3.7. Special show rules

#### 3.7.1. Matrix transpose with superscript T

Matrix transposition can be simply written as  $..^T$ , just like handwriting, and the only superscript T will be formatted properly to represent transposition instead of a normal capital letter T.

This  $\Box^T \Rightarrow \Box^\mathsf{T}$  conversion is disabled if the base is either

- a limits(...) or scripts(...) element, or
- an integration  $\int$  or sum  $\sum$  (not greek  $\Sigma$ ) or product  $\prod$  (not greek  $\Pi$ ) or vertical bar |, or
- an equation or lr(...) element whose last child is one of the above.

Overrides: if you really want to

- print a transpose explicitly: use symbol TT:  $A^T$ ;
- print a superscript letter T: use scripts(T): 2^scripts(T)  $\Rightarrow 2^T$ .

This feature needs to be enabled explicitly through a *show rule*.

If you only want to enable it within a content block's scope, you may do

```
#[
    #show: super-T-as-transpose // Enabled from here till the end of block.
    (A B)^T = B^T A^T
]
```

#### **Examples**

(1) 
$$(U \ V_n \ W')^T = W'^T \ V_n^T \ U^T$$

$$(\Sigma V_n W')^{\mathsf{T}} = W^{\mathsf{T}} V_n^{\mathsf{T}} \Sigma^{\mathsf{T}}$$

$$\begin{pmatrix} a \\ b \end{pmatrix}^{\mathsf{T}}, \begin{pmatrix} a & b \\ c & d \end{pmatrix}^{\mathsf{T}}$$

$$|a|^T, ||a||^T, F(t)|_0^T$$

$$\int^T, \sum^T, \prod^T$$

$$e^T, e^T$$

$$(M+N)^{\mathsf{T}}, (m+n)^{T}$$

### 3.7.2. Matrix dagger with superscript +

The conjugate transpose, also known as the Hermitian transpose, transjugate, or adjoint, of a complex matrix A is performed by first transposing and then complex-conjugating each matrix element. It is often denoted as  $A^*$ ,  $A^{\mathsf{H}}$ , and sometimes with a dagger symbol: A^dagger  $\Rightarrow A^{\dagger}$ .

Writing ...^dagger often visually clutters an equation in the source code form. Therefore, the package offers the ability to write ...^+ instead.

This  $\Box^+ \Rightarrow \Box^\dagger$  conversion is disabled if the base is either

- a limits(...) or scripts(...) element, or
- an equation or lr(...) element whose last child is one of the above.

This feature needs to be enabled explicitly through a *show rule*.

```
#show: super-plus-as-dagger
U^+U = U U^+ = I
```

If you only want to enable it within a content block's scope (e.g. you want to have — for ions or Moore–Penrose inverse outside the block), you may do

```
#[    #show: super-plus-as-dagger // Enabled from here till the end of block. U^+U = U U^+ = I
```

Overrides: if you really want to

- print a dagger explicitly: use the built-in symbol dagger as normal: A^dagger  $\Rightarrow A^{\dagger}$ ;
- print a superscript plus sign: use scripts(+):  $A^scripts(+) \Rightarrow A^+$ .

(1) U^+U = U U^+ = I   
 
$$U^{\dagger}U = UU^{\dagger} = I$$
 
$$\begin{pmatrix} 1+i & 1 \\ 2-i & 1 \end{pmatrix}^{\dagger} = \begin{pmatrix} 1-i & 2+i \\ 1 & 1 \end{pmatrix}$$

(3) 
$$\liminf_{N \to \infty} (N)^+$$
,  $\operatorname{scripts}(N)^+$  (4) #let eq =  $\operatorname{scripts}(N)$ ; eq^+

$$\stackrel{+}{N}, N^+$$

#### 3.8. Miscellaneous

#### 3.8.1. Reduced Planck constant (hbar)

In the default font, the Typst built-in symbol planck. reduce  $\hbar$  looks a bit off: on letter "h" there is a slash instead of a horizontal bar, contrary to the symbol's colloquial name "h-bar". This package offers hbar to render the symbol in the familiar form:  $\hbar$ . Contrast:

Typst's planck. reduce 
$$E=\hbar\omega$$
  $\frac{\pi G^2}{\hbar c^4}$   $Ae^{\frac{i(px-Et)}{\hbar}}$   $i\hbar\frac{\partial}{\partial t}\psi=-\frac{\hbar^2}{2m}\nabla^2\psi$  this package's hbar  $E=\hbar\omega$   $\frac{\pi G^2}{\hbar c^4}$   $Ae^{\frac{i(px-Et)}{\hbar}}$   $i\hbar\frac{\partial}{\partial t}\psi=-\frac{\hbar^2}{2m}\nabla^2\psi$ 

**Known limitation**: hbar uses the strike function, and show rules of strike will affect hbar. Therefore, you may have to revert your show rules for hbar. The following is an example.

```
#import "@preview/physica:0.9.5": hbar as old-hbar
#show strike: set text(gray)
#let hbar = {
    show strike: set text(black)
    old-hbar
}
```

\$hbar\$ is black, while \$#old-hbar\$ is gray.

#### 3.8.2. Tensors

Tensors are often expressed using the <u>abstract index notation</u>, which makes the contravariant and covariant "slots" explicit. The intuitive solution of using superscripts and subscripts do not suffice if both upper (contravariant) and lower (covariant) indices exist, because the notation rules require the indices be vertically separated: e.g.  $T_b^a$  and  $T_a^b$ , which are of different shapes. " $T_b^a$ " is flatly wrong, and T^(space w)\_(i space j) produces a weird-looking " $T_i^w$ " (note w, j vertically overlap).

Function: tensor(symbol, \*args).

- *symbol*: the tensor symbol,
- positional *args*: each argument takes the form of +... or -..., where a + prefix denotes an upper index and a prefix denotes a lower index.

(1) 
$$tensor(u,+a)$$
,  $tensor(v,-a)$  (2)  $tensor(h,+mu,+nu)$ ,  $tensor(g,-mu,-nu)$  
$$u^a,v_a \qquad \qquad h^{\mu\nu},g_{\mu\nu}$$
 (3)  $tensor(T,+a,-b)$ ,  $tensor(T,-a,+b)$  (4)  $tensor(T,-i,+w,-j)$  
$$T^a_{\ b},T_a^{\ b} \qquad \qquad T^w_{i\ j}$$
 (5)  $tensor((dd(x^\lambda)_a)$  (6)  $tensor(AA,+a,+b,-c,-d,+e,-f,+g,-h)$  
$$(dx^\lambda)_a \qquad \qquad \mathbb{A}^{ab\ e\ g}_{\ cd\ f\ h}$$

$$(7)$$
 tensor(R, -a, -b, +d)

$$R_{ab}^{\phantom{ab}d}$$

$$T^{1}_{I(1,-1)}^{a_{\perp}}$$

(9) grad\_mu A^nu = partial\_mu A^nu + tensor(Gamma, +nu, -mu, -lambda) A^lambda

$$\nabla_{\mu}A^{\nu} = \partial_{\mu}A^{\nu} + \Gamma^{\nu}_{\ \mu\lambda}A^{\lambda}$$

#### 3.8.3. Isotopes

Function: isotope (element, a: ..., z: ...).

- *element*: the chemical element (use ".." for multi-letter symbols)
- *a*: the mass number *A* [default: none].
- *z*: the atomic number *Z* [default: none].

Change log: Typst merged my PR, which fixed a misalignment issue with the surrounding text.

#### **Examples**

$$_{26}$$
Fe

$$^{211}_{83}\text{Bi} \rightarrow ^{207}_{81}\text{Tl} + ^{4}_{2}\text{He}$$

$$^{207}_{81}{
m Tl} 
ightarrow ^{207}_{82}{
m Pb} + {}^{0}_{-1}{
m e}$$

#### 3.8.4. The n-th term in Taylor series

Function: taylorterm(func, x, x0, idx).

- *func*: the function e.g. f, (f+q),
- *x*: the variable name e.g. x,
- x0: the variable value at the expansion point e.g.  $x_0$ , (1+a),
- *idx*: the index of the term, e.g. 0, 1, 2, n, (n+1).

If x0 or idx is an add/sub sequence e.g. -a, a+b, then the function automatically adds a parenthesis where appropriate.

#### **Examples**

(1) taylorterm(
$$f,x,x_0,0$$
)

$$f(x_0)$$

$$f^{(1)}(x_0)(x-x_0) \\$$

$$\frac{F^{(n)}(x_0^{\nu})}{n!}(x^{\nu}-x_0^{\nu})^n$$

$$\frac{f^{(n)}(x_0)}{n!}(x-x_0)^n$$

(5) taylorterm(f,x,1+a,2)

$$\frac{f^{(2)}(1+a)}{2!}(x-(1+a))^2$$

$$\frac{f_p^{(n-1)}(x_0)}{(n-1)!}(x-x_0)^{n-1}$$

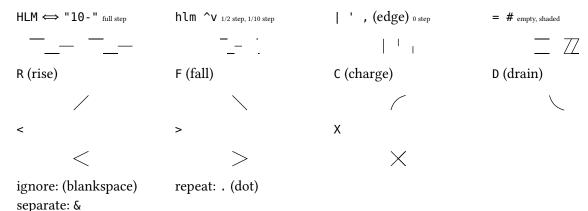
#### 3.8.5. Signal sequences (digital timing diagrams)

In engineering, people often need to draw digital timing diagrams for signals, like

Function: signals(str, step::..., style:...).

- str: a string representing the signals. Each character represents an glyph (see below).
- step (optional): step width, i.e. how wide each glyph is [default: #1em].
- color (optional): the stroke color [default: #black].

### Glyph characters



#### **Examples**

(1) signals("10.1"), signals("1|0|1|0R"), signals("CD"), signals("CD", step: #2em)

(2) signals("M'H|L|h|l|^|v,&|H'M'H|l,m,l|") (the ampersand & serves as a separator)

(3) signals("-|=|-", step: #2em), signals("-|#|-"), signals("-<=>-<=")

(4) signals("R1..F0..", step: #.5em)signals("R1.|v|1", step: #.5em, color:#fuchsia)



**(5)** 

```
"clk:" & signals("|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|0....|1....|1....|0....|1....|1...|0....|1....|1....|0....|1....|1....|0....|1....|1....|0....|1....|1....|0....|1....|1....|0....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|1....|
```

### 3.9. Symbolic addition

This package implements a very rudimentary, **bare-minimum-effort** symbolic addition function to aid the automatic computation of a partial derivative's total order in the absence of user override (see Section 3.6.3). Though rudimentary and unsophisticated, this should suffice for most use cases in partial derivatives.

Function: BMEsymadd([...]).

• ...: symbols that need to be added up e.g. [1,2],  $[a+1,b^2+1,2]$ .

(1) BMEsymadd([1]), BMEsymadd([2, 3]) 
$$\rightarrow 1,5$$

(2) BMEsymadd([a, b^2, 1]) 
$$\rightarrow a + b^2 + 1$$

(3) BMEsymadd([a+1,2c,b,2,b]) 
$$\rightarrow \qquad a+2b+2c+3$$

(4) BMEsymadd([a+1,2(b+1),1,b+1,15]) 
$$\rightarrow a+b+2(b+1)+18$$

(5) BMEsymadd([a+1,2(b+1),1,(b+1),15]) 
$$\rightarrow a+3(b+1)+17$$

(6) BMEsymadd([a+1,2(b+1),1,3(b+1),15]) 
$$\rightarrow a+5(b+1)+17$$

(7) BMEsymadd([2a+1,xi,b+1,a xi + 2b+a,2b+1]) 
$$\rightarrow$$
  $3a + 5b + \xi + a\xi + 3$ 

# 4. Acknowledgement

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- physics by Sergio C. de la Barrera,
- derivatives by Simon Jensen,
- tensor by Philip G. Ratcliffe et al.

# 5. License

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