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# Message Authentication and Hash Functions

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# Message Authentication

- message authentication is concerned with:
  - protecting the integrity of a message
  - validating identity of originator
  - non-repudiation of origin (dispute resolution)
- three alternative functions used:
  - message encryption
  - message authentication code (MAC)
  - hash function

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# Broader Set of Attacks

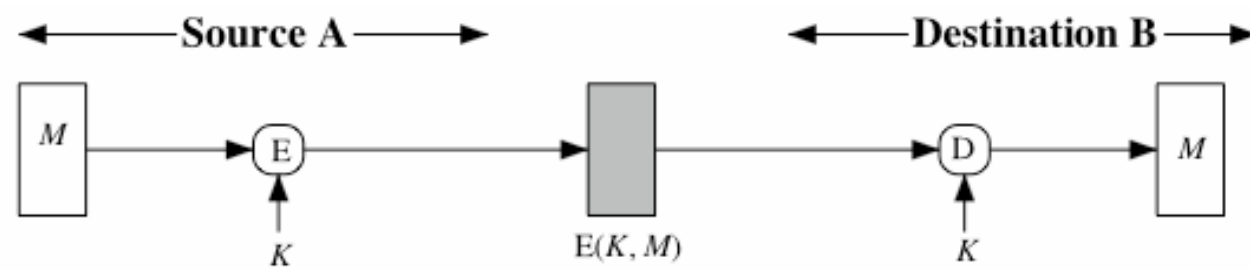
- disclosure
- traffic analysis
- masquerade
- content modification
- sequence modification
- timing modification
- source repudiation
- destination repudiation

# Message Encryption

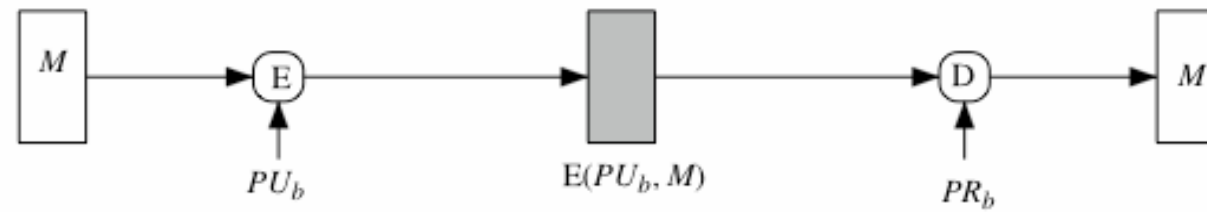
- message encryption by itself also provides a measure of authentication
- if symmetric encryption is used then:
  - receiver know sender must have created it
  - since only sender and receiver now key used
  - know content cannot of been altered
  - Provides both: sender authentication and message authenticity.

# Message Encryption

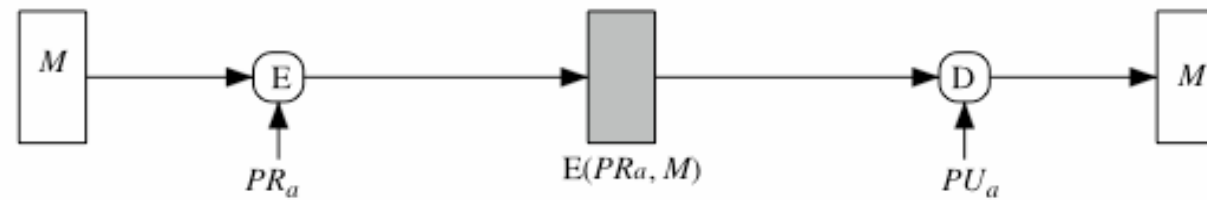
- if public-key encryption is used:
  - encryption provides no confidence of sender
  - since anyone potentially knows public-key
  - however if
    - sender **signs** message using his private-key
    - then encrypts with recipients public key
    - have both secrecy and authentication
  - but at cost of two public-key uses on message



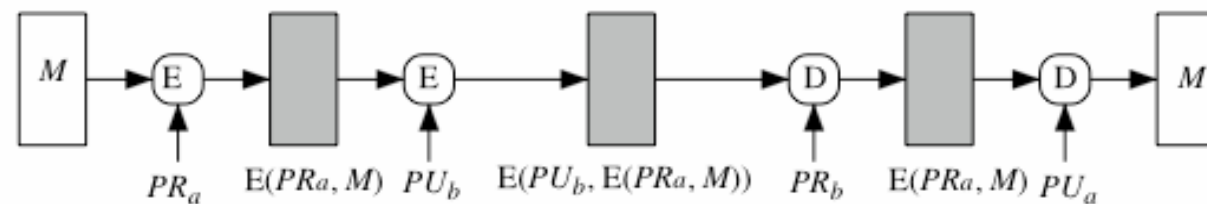
(a) Symmetric encryption: confidentiality and authentication



(b) Public-key encryption: confidentiality

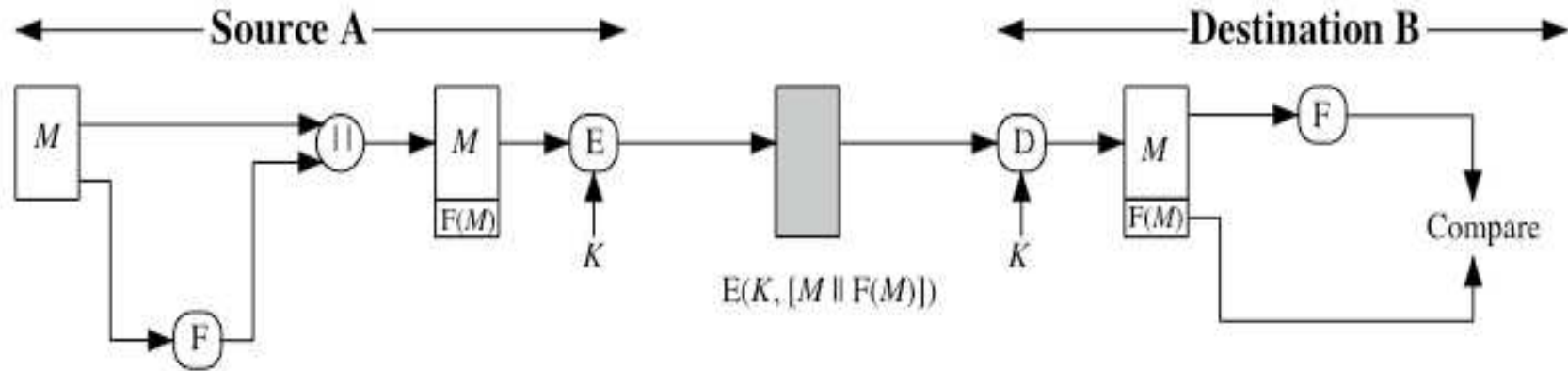


(c) Public-key encryption: authentication and signature

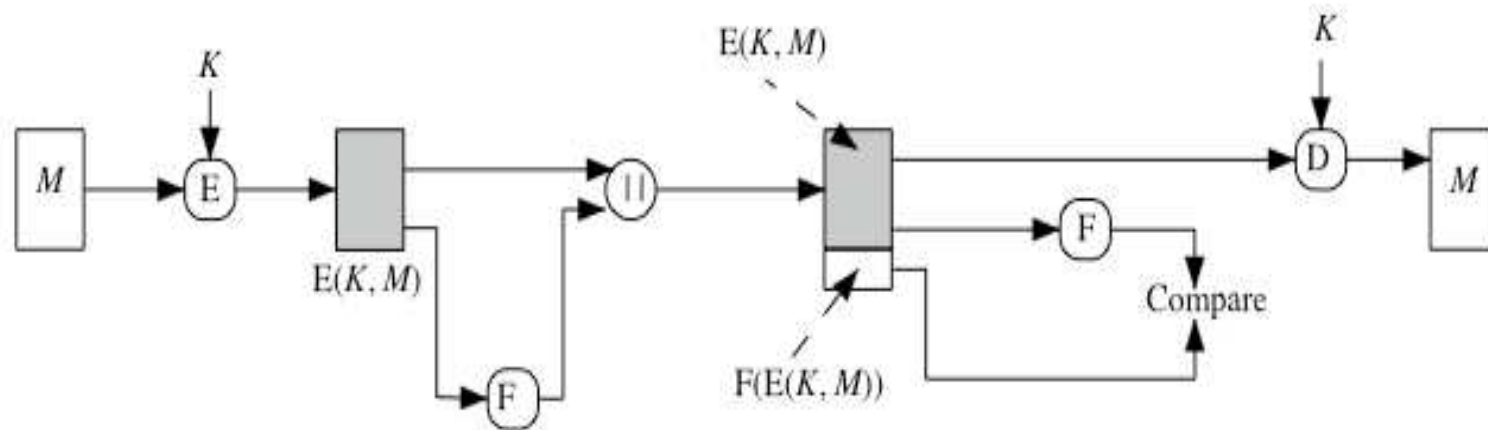


(d) Public-key encryption: confidentiality, authentication, and signature

# Internal and External Error control



(a) Internal error control



(b) External error control

# Confidentiality and Authentication

## Implications of Message

$A \rightarrow B: E(K, M)$

- Provides confidentiality
  - Only A and B share  $K$
- Provides a degree of authentication
  - Could come only from A
  - Has not been altered in transit
  - Requires some formatting/redundancy
- Does not provide signature
  - Receiver could forge message
  - Sender could deny message

(a) Symmetric encryption

$A \rightarrow B: E(PU_b, M)$

- Provides confidentiality
  - Only B has  $PR_b$  to decrypt
- Provides no authentication
  - Any party could use  $PU_b$  to encrypt message and claim to be A

(b) Public-key (asymmetric) encryption: confidentiality



# Confidentiality and Authentication Implications of Message

$A \rightarrow B: E(PR_a, M)$

- Provides authentication and signature
  - Only A has  $PR_a$  to encrypt
  - Has not been altered in transit
  - Requires some formatting/redundancy
  - Any party can use  $PU_a$  to verify signature

(c) Public-key encryption: authentication and signature

$A \rightarrow B: E(PU_b, E(PR_a, M))$

- Provides confidentiality because of  $PU_b$
- Provides authentication and signature because of  $PR_a$

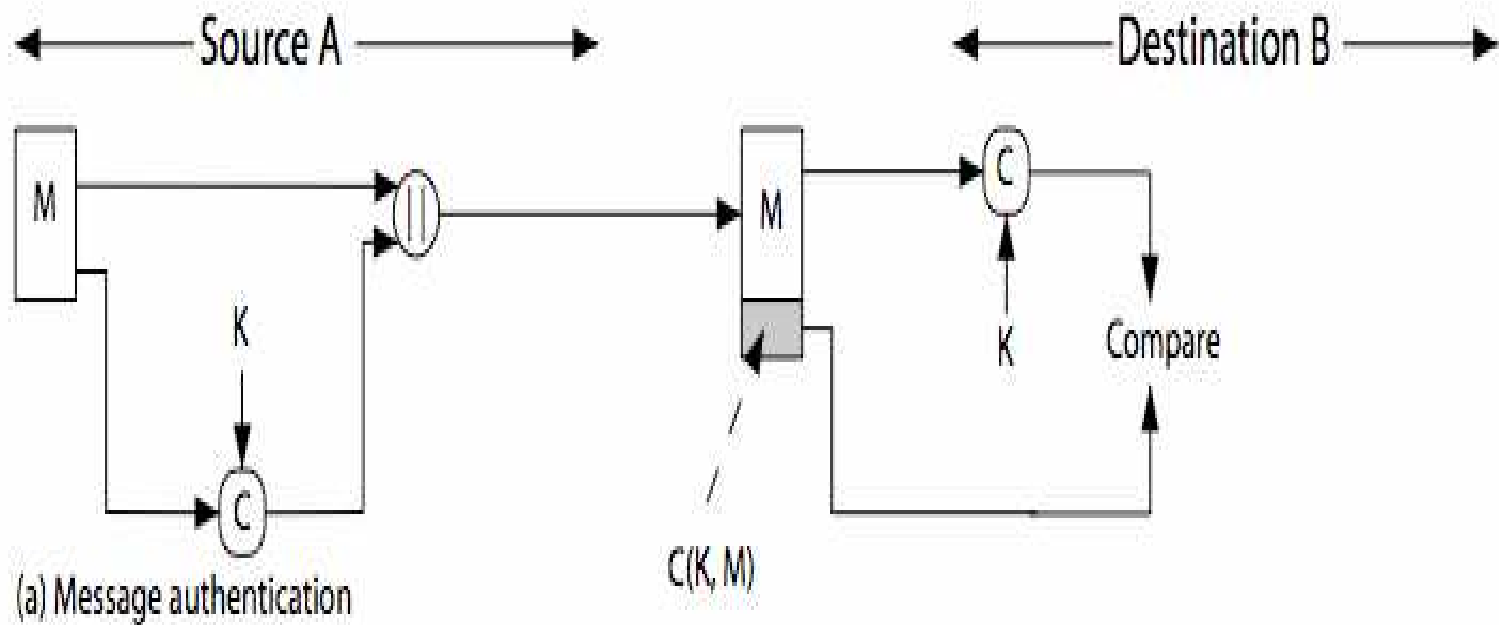
(d) Public-key encryption: confidentiality, authentication, and signature

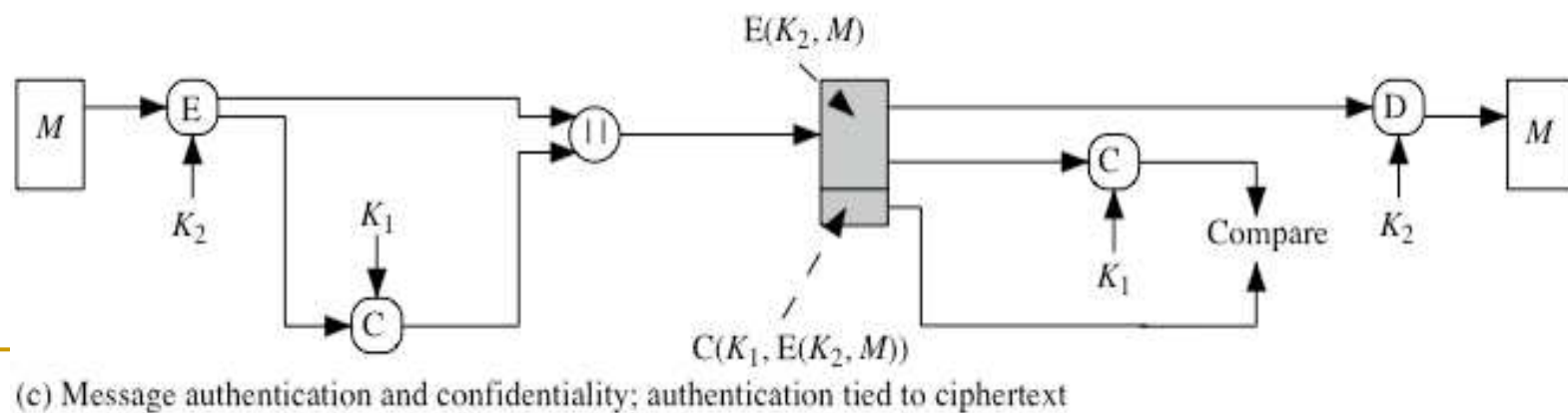
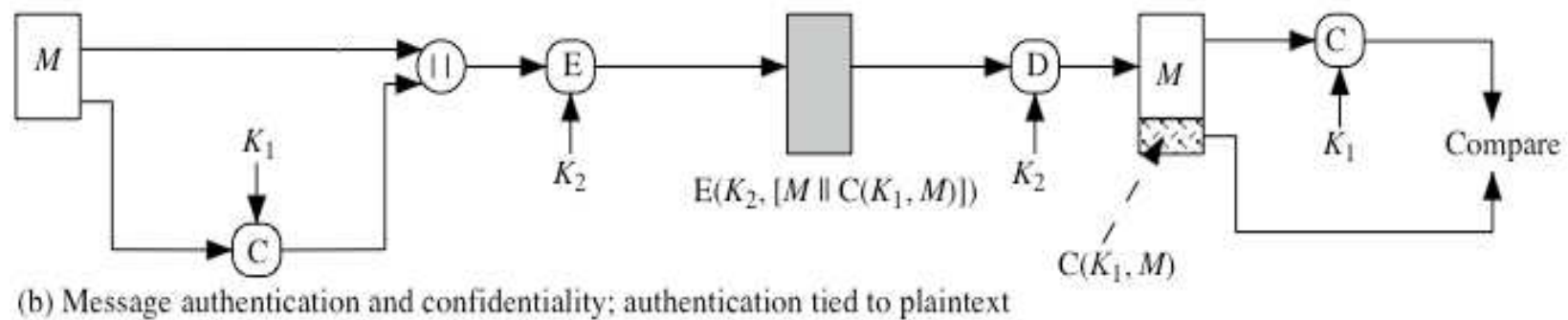
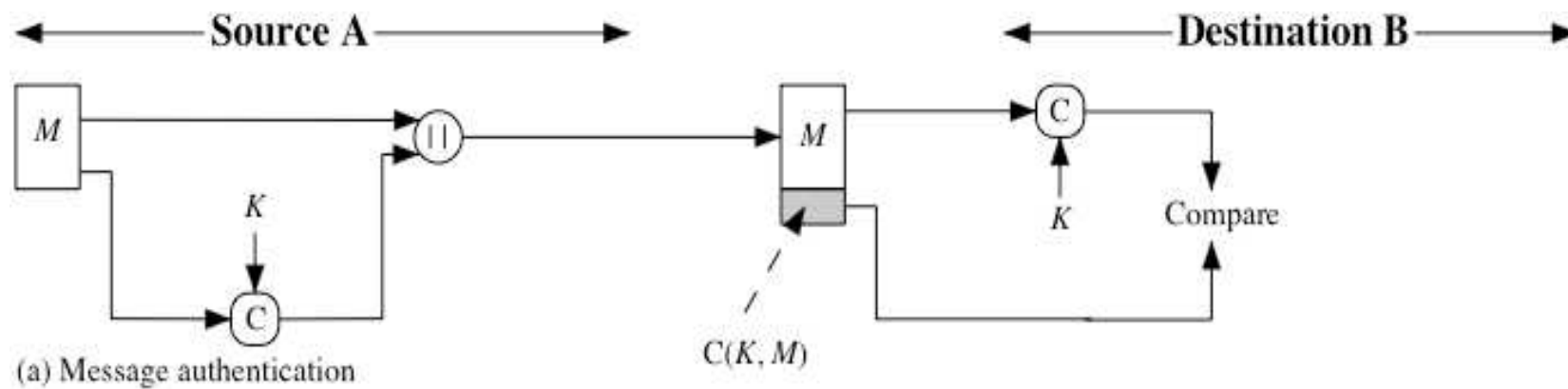
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# Message Authentication Code (MAC)

- a small fixed-sized block of data:
  - depends on both message and a secret key
  - like encryption though need not be reversible
- appended to message as a **signature**
- receiver performs same computation on message and checks it matches the MAC
- provides assurance that message is unaltered and comes from sender

# Message Authentication Code





# Message Authentication Codes

- MAC provides authentication
- Message can be encrypted for secrecy
  - generally use separate keys for each
  - can compute MAC either before or after encryption
  - is generally regarded as better done before
- why use a MAC?
  - sometimes only authentication is needed
  - sometimes need authentication to persist longer than the encryption (e.g., archival use)
- note that a MAC is not a digital signature

# MAC Properties

- a MAC is a cryptographic checksum

$$\text{MAC} = C_K(M)$$

- C is a function
  - condenses a variable-length message M
  - using a secret key K
  - to a fixed-sized authenticator
- many-to-one function
    - potentially many messages have same MAC
    - but finding these needs to be very difficult

# Requirements for MACs

- MAC needs to satisfy the following:
  1. knowing a message and MAC, is infeasible to find another message with same MAC
  2. MACs should be uniformly distributed
  3. MAC should depend equally on all bits of the message

# Basic Uses of Message Authentication Code C

$A \rightarrow B: M \parallel C(K, M)$   
•Provides authentication  
—Only A and B share  $K$

(a) Message authentication

$A \rightarrow B: E(K_2, [M \parallel C(K, M)])$   
•Provides authentication  
—Only A and B share  $K_1$   
•Provides confidentiality  
—Only A and B share  $K_2$

(b) Message authentication and confidentiality:  
authentication tied to plaintext

$A \rightarrow B: E(K_2, M) \parallel C(K_1, E(K_2, M))$   
•Provides authentication  
—Using  $K_1$   
•Provides confidentiality  
—Using  $K_2$

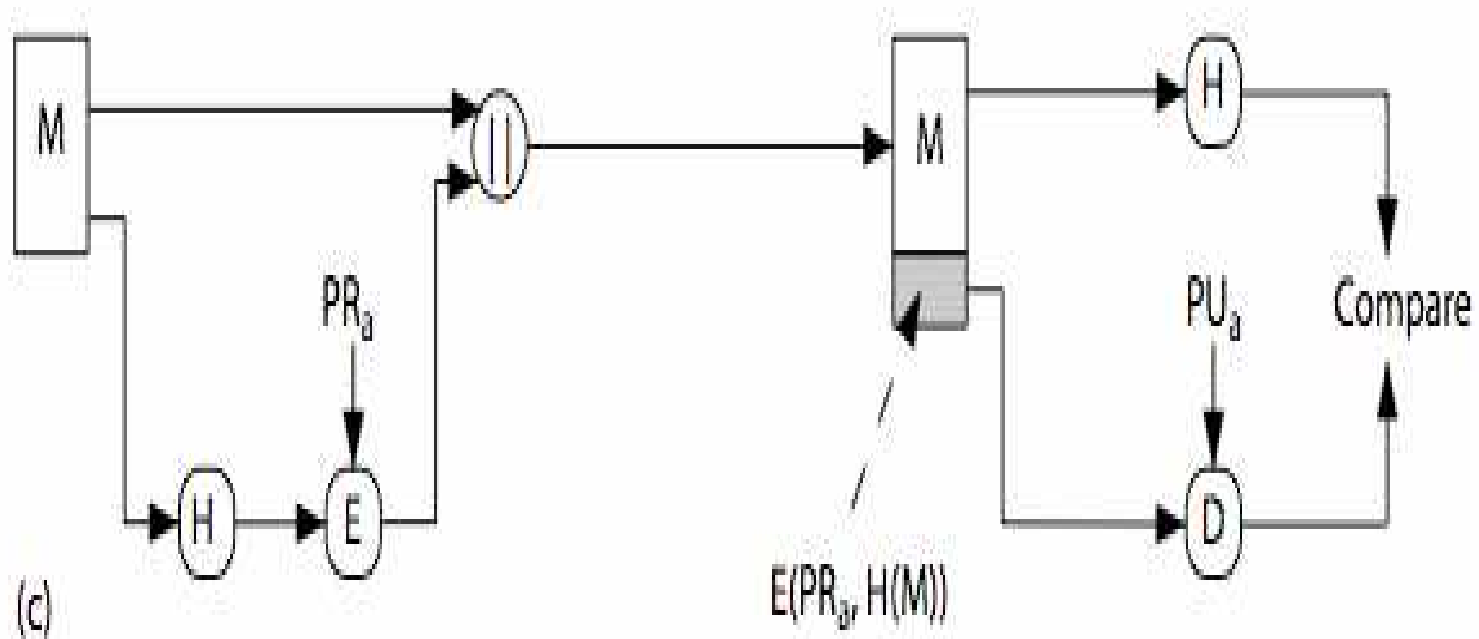
(c) Message authentication and confidentiality:  
authentication tied to ciphertext



# Hash Functions

- A hash function is like a MAC
- condenses arbitrary message to fixed size
$$h = H(M)$$
- usually assume that the hash function is public and not keyed
  - note that a MAC is keyed
- hash used to detect changes to message
- can use in various ways with message
- most often to create a digital signature

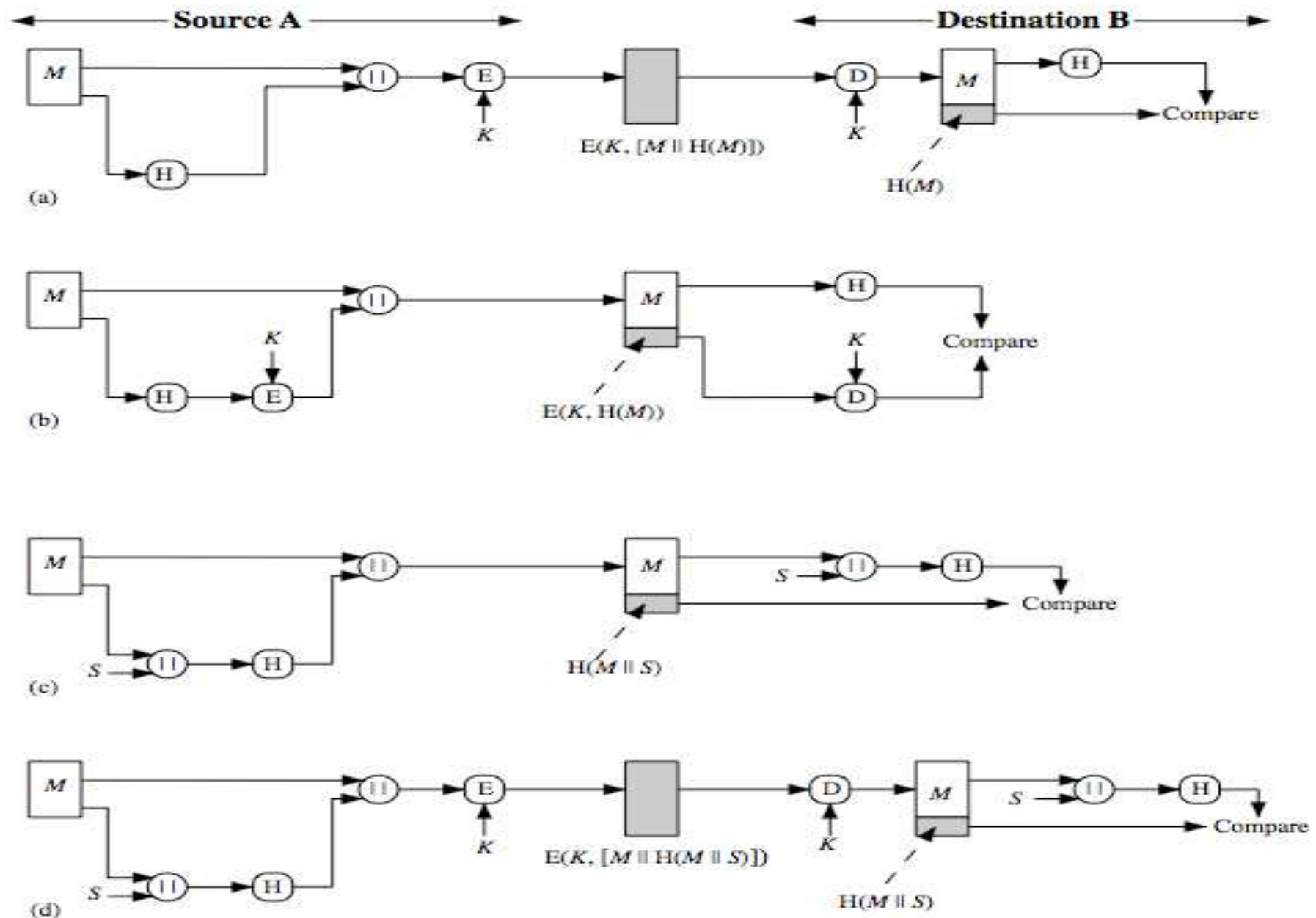
# Hash Functions & Digital Signatures



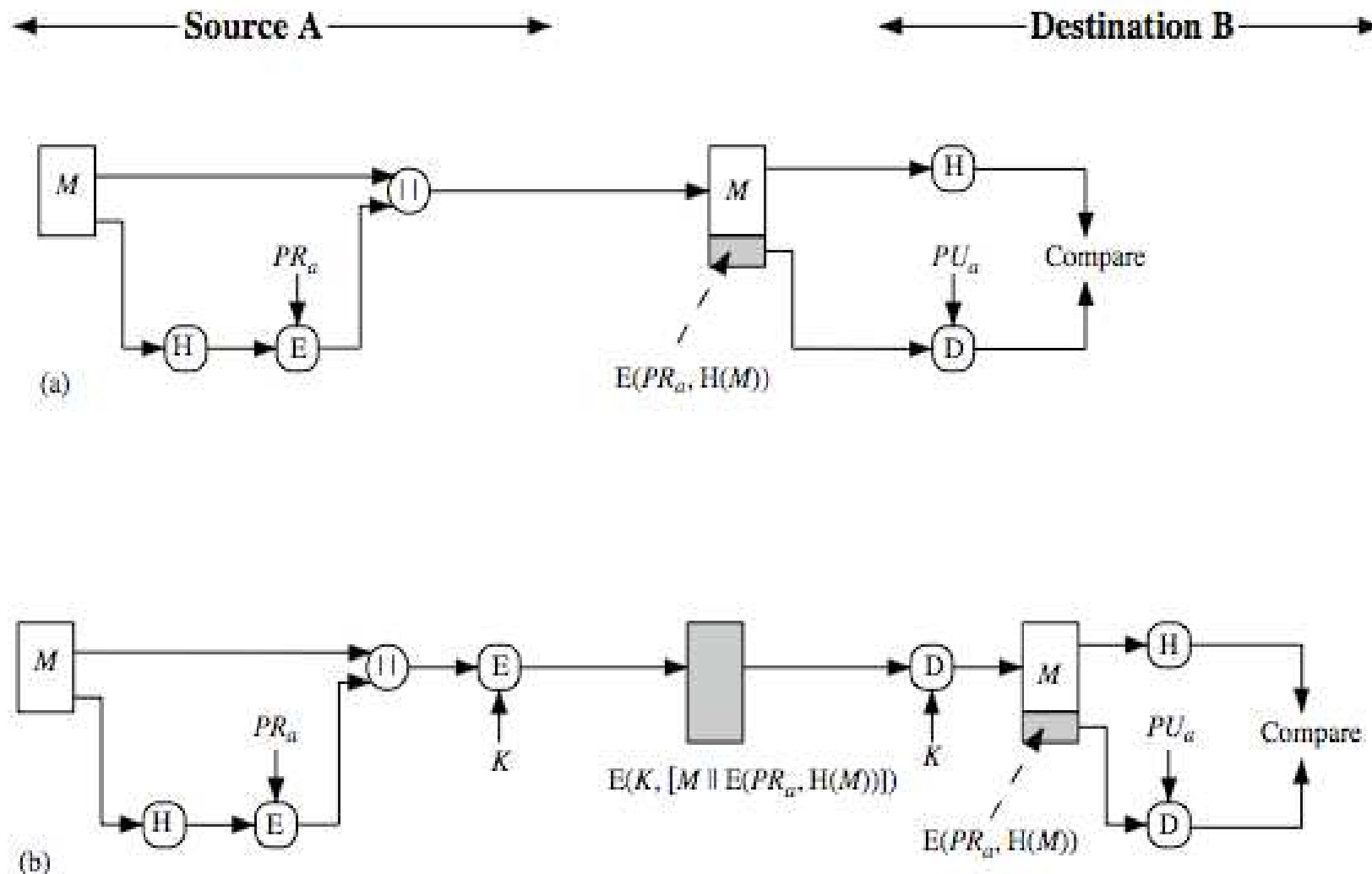
# Requirements for Hash Functions

1. can be applied to any size message  $M$
2. produces a fixed-length output  $h$
3. is easy to compute  $h=H(M)$  for any message  $M$
4. given  $h$  is infeasible to find  $x$  s.t.  $H(x)=h$ 
  - one-way property
5. given  $x$  is infeasible to find  $y$  s.t.  $H(y)=H(x)$ 
  - weak collision resistance
6. is infeasible to find any  $x, y$  s.t.  $H(y)=H(x)$ 
  - strong collision resistance

# Hash Functions & Message Authentication



# Hash Functions & Digital Signatures



# Basic Uses of Hash Function H

$A \rightarrow B: E(K, [M \parallel H(M)])$ <ul style="list-style-type: none"> <li>•Provides confidentiality                             <ul style="list-style-type: none"> <li>—Only A and B share <math>K</math></li> </ul> </li> <li>•Provides authentication                             <ul style="list-style-type: none"> <li>—<math>H(M)</math> is cryptographically protected</li> </ul> </li> </ul>	$A \rightarrow B: E(K, [M \parallel E(PR_a, H(M))])$ <ul style="list-style-type: none"> <li>•Provides authentication and digital signature</li> <li>•Provides confidentiality                             <ul style="list-style-type: none"> <li>—Only A and B share <math>K</math></li> </ul> </li> </ul>
(a) Encrypt message plus hash code	(d) Encrypt result of (c) - shared secret key
$A \rightarrow B: M \parallel E(K, H(M))$ <ul style="list-style-type: none"> <li>•Provides authentication                             <ul style="list-style-type: none"> <li>—<math>H(M)</math> is cryptographically protected</li> </ul> </li> </ul>	$A \rightarrow B: M \parallel H(M \parallel S)$ <ul style="list-style-type: none"> <li>•Provides authentication                             <ul style="list-style-type: none"> <li>—Only A and B share <math>S</math></li> </ul> </li> </ul>
(b) Encrypt hash code - shared secret key	(e) Compute hash code of message plus secret value
$A \rightarrow B: M \parallel E(PR_a, H(M))$ <ul style="list-style-type: none"> <li>•Provides authentication and digital signature                             <ul style="list-style-type: none"> <li>—<math>H(M)</math> is cryptographically protected</li> <li>—Only A could create <math>E(PR_a, H(M))</math></li> </ul> </li> </ul>	$A \rightarrow B: E(K, [M \parallel H(M \parallel S)])$ <ul style="list-style-type: none"> <li>•Provides authentication                             <ul style="list-style-type: none"> <li>—Only A and B share <math>S</math></li> </ul> </li> <li>•Provides confidentiality                             <ul style="list-style-type: none"> <li>—Only A and B share <math>K</math></li> </ul> </li> </ul>
(c) Encrypt hash code - sender's private key	(f) Encrypt result of (e)

# Birthday Attacks

- might think a 64-bit hash is secure
- but by **Birthday Paradox** is not
- **birthday attack** works thus:
  - given user prepared to sign a valid message  $x$
  - opponent generates  $2^{m/2}$  variations  $x''$  off  $x$ , all with essentially the same meaning, and saves them
  - opponent generates  $2^{m/2}$  variations  $y''$  off a desired
- fraudulent message  $y$ 
  - two sets of messages are compared to find pair with same hash (probability  $> 0.5$  by birthday paradox)
  - have user sign the valid message, then substitute the forgery which will have a valid signature
- conclusion is that need to use larger MAC/hash

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# Summary

- have considered:
  - ❑ message authentication using
  - ❑ message encryption
  - ❑ MACs
  - ❑ hash functions