

Global Data-flow Analysis

- A number of optimization can be achieved by knowing various pieces of information that can be obtained only by examining the entire program.
- For example, value for identifier A may be used in some part of the program, but to know where it has been defined, we need to examine the entire program.
- Solution is a **global data flow analysis**
- Method is **Ud-chaining**(use-definition chaining)
- For ud-chaining, **Reaching Definitions** should be found
- Then **data-flow equations** have to be determined iteratively

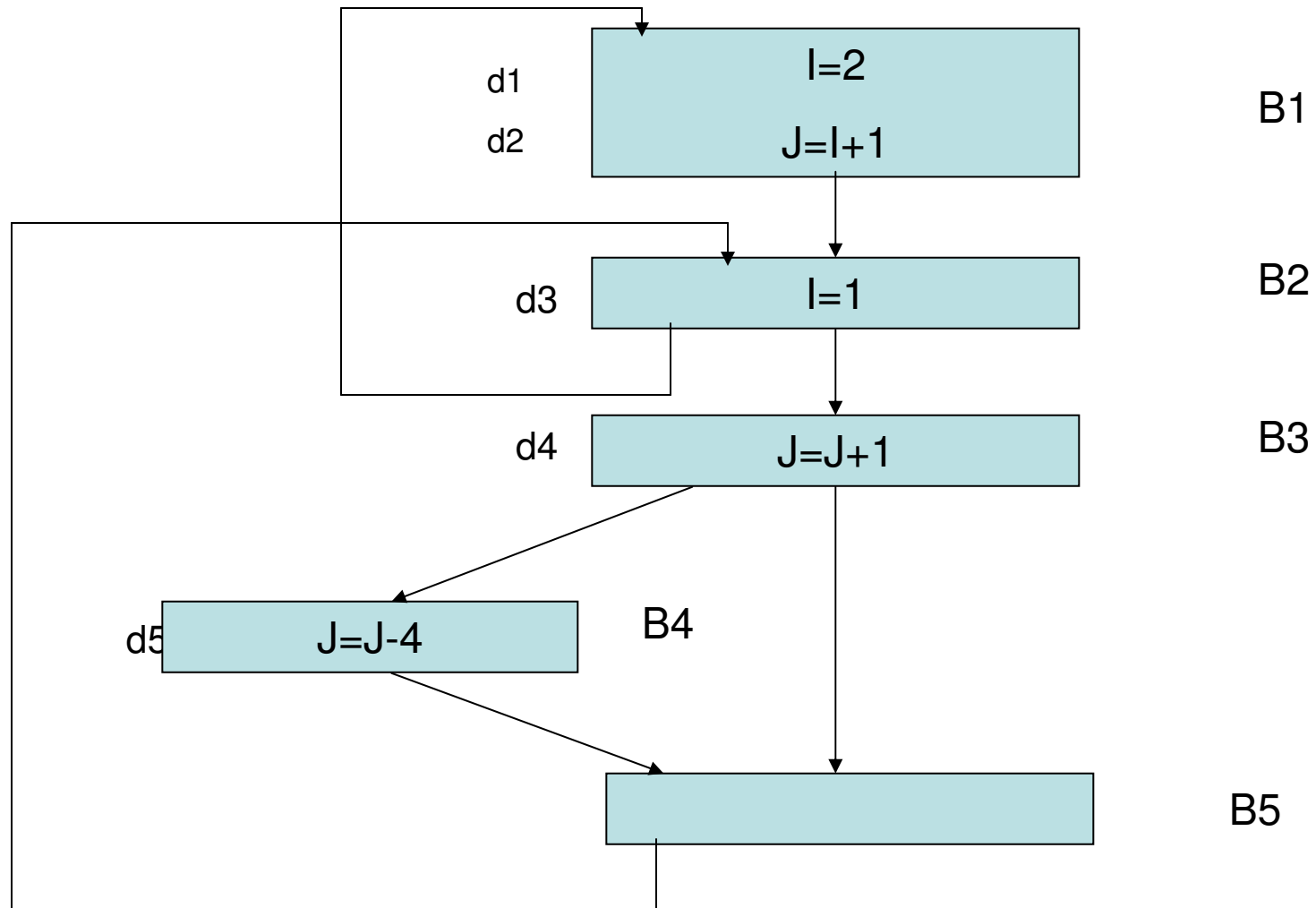
Reaching definition

1. Assign number to each definition
2. For simple variable A, make a list of all definitions anywhere in the program
3. Compute two sets for each basic block B
 - **GEN[B]**-set of generated definitions within basic block B that reach the end of the block
 - **KILL[B]**-set of definitions outside of B that have definition within B
 - Use **bit vectors** for representation
4. Compute set **IN[B]** for all blocks B-(all definitions reaching the point just before the first statement of Block B)
5. Compute set **OUT[B]** for all blocks B (the set of definitions reaching the point just after the last statement of B)
6. Repeat 4,5 iteratively until it gets converged

Data-flow equations

- $OUT[B] = IN[B] - KILL[B] \cup GEN[B]$ {- means NOT AND}
- $IN[B] = \cup OUT[P]$, P is a predecessor of B

Example



Step 1

Assign numbers to the definitions

- $d1 \rightarrow I=2$
- $d2 \rightarrow J=I+1$
- $d3 \rightarrow I=1$
- $d4 \rightarrow J=J+1$
- $d5 \rightarrow J=J-4$

Step 2

Make a list of all definitions

- I has the definitions
 - d1 in B1
 - d3 in B2
- J has the definitions
 - d2 in B1
 - d4 in B3
 - d5 in B4

Step 3

Compute GEN[B] and KILL[B]

Block B	GEN[B]	Bit Vector	KILL[B]	Bit Vector
B1	{d1,d2}	11000	{d3,d4,d5}	00111
B2	{d3}	00100	{d1}	10000
B3	{d4}	00010	{d2,d5}	01001
B4	{d5}	00001	{d2,d4}	01010
B5	∅	00000	∅	00000

Step 4,5

Compute data flow equations $IN[B]$ and $OUT[B]$

Initial assumptions:

$$IN[B] = \emptyset$$

$$OUT[B] = GEN[B]$$

With $B = B1$

$NEWIN = OUT[B2]$, $B2$ is the only predecessor

$$NEWIN = GEN[B2] = 00100$$

$$NEWIN \neq IN[B1]$$

$$IN[B1] = 00100$$

$$\begin{aligned} OUT[B1] &= IN[B1] - KILL[B1] \cup GEN[B1] \\ &= 00100 - 00111 + 11000 = 11000 \end{aligned}$$

With $B = B2$

$$\begin{aligned} NEWIN &= OUT[B1] + OUT[B5] , B1, B5 \text{ are predecessors of } B2 \\ &= 11000 + 00000 = 11000 \end{aligned}$$

$$IN[B2] = 11000$$

$$OUT[B2] = 11000 - 10000 + 00100 = 01100$$

Step 4,5 (cont.)

With B = B3

NEWIN = OUT[B2] = 01100

IN[B3] = 01100

OUT[B3] = 01100 - 01001 + 00010 = 00110

With B = B4

NEWIN = OUT[B3] = 00110

IN[B4] = 00110

OUT[B4] = 00110 - 01010 + 00001 = 00101

With B = B5

NEWIN = OUT[B3] + OUT[B4] = 00110 + 00101 = 00111

IN[B5] = 00111

OUT[B5] = 00111 - 00000 + 00000 = 00111

The use of J at d5 in block B4 is not preceded by a definition of J, so consider
IN[B4] = {d3, d4}, of these only d4 defines J, so the ud-chain for J in d5 = {d4}

Application: dead code elimination

Step 4,5

Compute data flow equations $IN[B]$ and $OUT[B]$

Block	INITIAL		PASS-I	
	$IN[B]$	$OUT[B]$	$IN[B]$	$OUT[B]$
B1	00000	11000	00100	11000
B2	00000	00100	11000	01100
B3	00000	00010	01100	00110
B4	00000	00001	00110	00101
B5	00000	00000	00111	00111

Block	PASS-II		PASS=III	
	$IN[B]$	$OUT[B]$	$IN[B]$	$OUT[B]$
B1	01100	11000	01111	11000
B2	11111	01111	11111	01111
B3	01111	00110	01111	00110
B4	00110	00101	00110	00101
B5	00111	00111	00111	00111