

Tutorial 1

3 July 2017

1. Show that the complement of a bipartite graph need not be bipartite.
2. Suppose $N(n,k)$ is the number of non-isomorphic simple graph with n vertices and k edges. Find $N(4,3)$.
3. Using techniques from graph theory show that
$$1+2+\dots+n=n(n+1)/2.$$
4. Show that two simple graphs are isomorphic if & only if their complements are isomorphic.
5. Show that if a graph is disconnected its complement is connected.
6. A connected graph is said to be **minimally connected** if removal of any one edge from it disconnects the graph. Prove that a graph is a tree if & only if it is minimally connected.
7. Given a graph G its **line graph** $L(G)$ is a graph such that
 - a. for each edge in G there is a vertex in $L(G)$.
 - b. two vertices in $L(G)$ are adjacent if & only if their corresponding edges share a common endpoint in G .Show that if G is a Euler graph then $L(G)$ is an Euler graph.