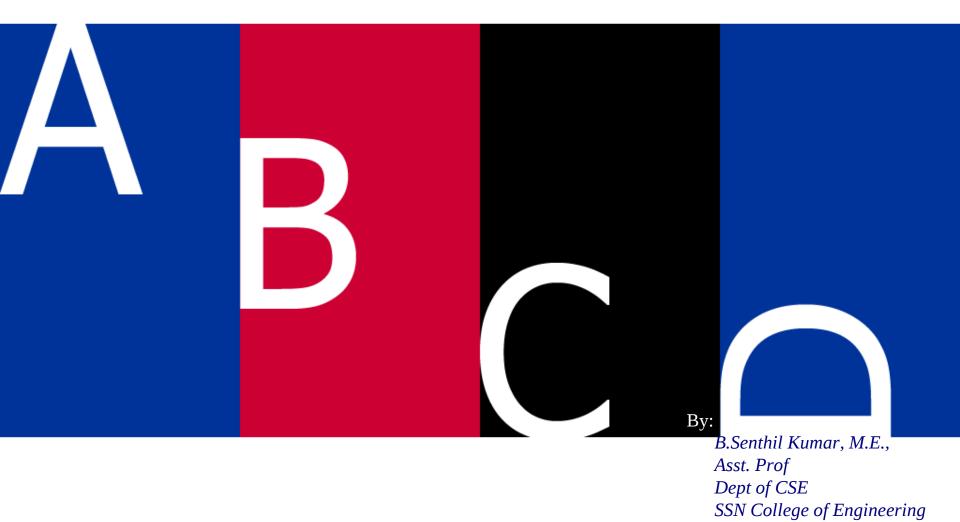
SSN Finite-State Morphological Parsing





Overview

- 1. Finite-State Morphological Parsing An Introduction
 - Lexicon, morphotactics and orthographic rules
- 2. The Lexicon and Morphotactics
- 3. Morphological parsing with Finite-State Transducers
 - Two-level morphology
 - Finite-State Transducer
- 4. Orthographic Rules and Finite-State Transducers
 - Spelling rules

) =____

Tell me and I forget. Teach me and I remember. Involve me and I learn.
-- Benjamin Franklin





Finite-State Morphological Parsing

- Parsing English morphology
 - The second column contains the stem of each word + assorted morphological *features*
 - Features specify additional information about stem
 - +N means word is a noun; +SG means singular

| Input | Morphological parsed output |
|---------|--|
| cats | cat +N +PL |
| cat | cat +N +SG |
| cities | city +N +PL |
| geese | goose +N +PL |
| goose | (goose +N +SG) or (goose +V) |
| gooses | goose +V +3SG |
| merging | merge +V +PRES-PART |
| caught | (caught +V +PAST-PART) or (catch +V +PAST) |





Finite-State Morphological Parsing

<u>с в А</u>

- We need at least the following to build a morphological parser:
 - **Lexicon**: the *list of stems and affixes*, together with basic information about them (Noun stem or Verb stem, etc.)
 - Morphotactics: the model of *morpheme ordering* that explains which classes of morphemes can follow other classes of morphemes.
 E.g., the rule that English plural morpheme follows the noun rather than preceding it.
 - Orthographic rules: these spelling rules are used to model the changes that occur in a word, usually when two morphemes combine (e.g., the y → ie spelling rule changes city + -s to cities).

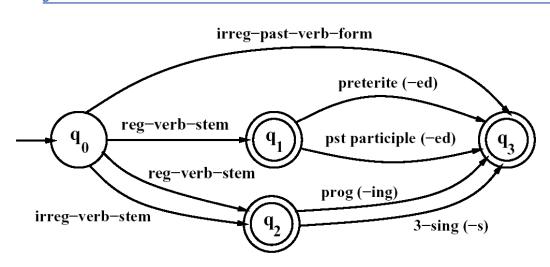
- A lexicon is a repository for words.
 - The simplest one would consist of an explicit list of every word of the language. *Inconvenient or impossible!*
 - Computational lexicons are usually structured with
 - a list of each of the stems and
 - Affixes of the language together with a representation of morphotactics telling us how they can fit together.
 - The most common way of modelling morphotactics is the finite-state automaton.

 $\begin{array}{c|c} reg-noun & plural \, (-s) \\ \hline \hline q_0 & q_1 \\ \hline irreg-pl-noun \\ \end{array}$

An FSA for English nominal inflection

irreg-sg-noun

| Reg-noun | Irreg-pl-noun | Irreg-sg-noun | plural |
|----------|---------------|---------------|--------|
| fox | geese | goose | -S |
| cat | sheep | sheep | |
| table | mice | mouse | |
| book | | | |

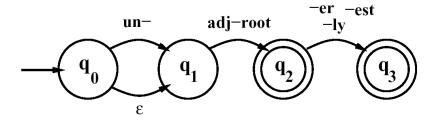


An FSA for English verbal inflection

| Reg-verb-stem | Irreg-verb-stem | Irreg-past-verb | past | Past-part | Pres-part | 3sg |
|---------------|-----------------|-----------------|------|-----------|-----------|-----|
| walk | cut | caught | -ed | -ed | -ing | -s |
| fry | speak | ate | | | | |
| talk | sing | eaten | | | | |
| impeach | | sang | | | | |
| | | spoken | | | | |
| | | | | | | |



- English derivational morphology is more complex than inflectional morphology
- So automata of modeling English derivation tends to be quite complex
 - Some even based on CFG
 - [Antworth,1990] A small part of morphotactics of English adjectives
 - Adjectives can have an optional prefix (un-)
 - An obligatory root (*big*, *cool*, *etc*)
 - And an optional suffix (-er, -est, or -ly)



An FSA for a fragment of English adjective Morphology #1

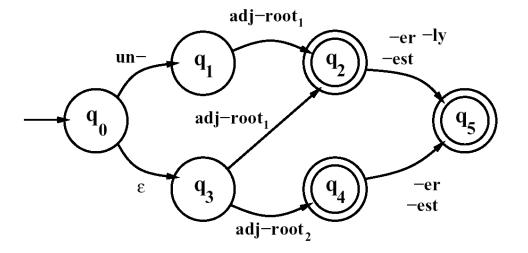
big, bigger, biggest cool, cooler, coolest, coolly red, redder, reddest clear, clearer, clearest, clearly, unclear, unclearly happy, happier, happiest, happily unhappy, unhappier, unhappiest, unhappily real, unreal, really





The Lexicon and Morphotactics

- The FSA#1 recognizes all the listed adjectives, and ungrammatical forms like *unbig*, *unfast*, *redly*, *smally* and *realest*.
- Thus #1 is revised to become #2.
- The complexity is expected from English derivation.



An FSA for a fragment of English adjective Morphology #2

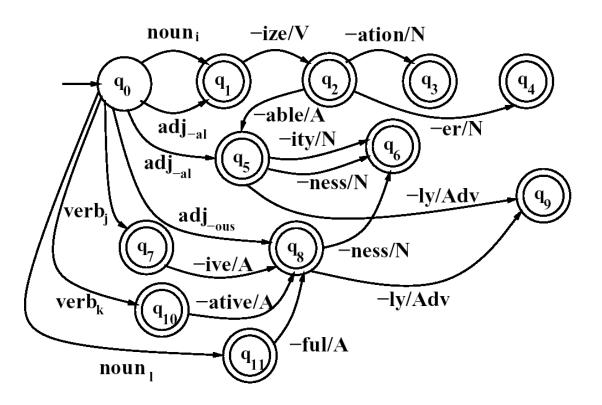
C

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The Lexicon and Morphotactics

D C B A



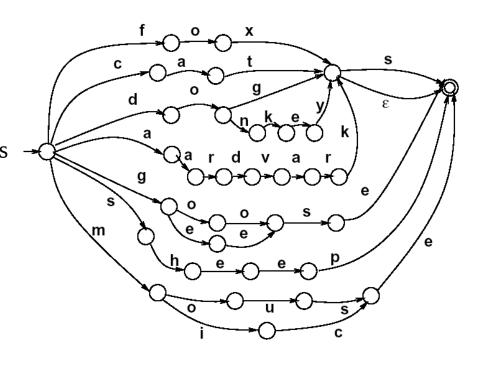
An FSA for another fragment of English derivational morphology



The Lexicon and Morphotactics

FSA can be used to solve the problem of morphological recognition:

- Determining whether
 an input string of letters
 makes up a *legitimate English word* or not
- The resulting FSA can then be defined as the level of the individual letter.



An FSA for English nominal inflection



- → Two-level morphology
- → Finite-State Transducer [FST]



D C B A

Given the input, for example, *cats*, we would like to produce :

- Two-level morphology, by Koskenniemi (1983)
 - Represent a word as a correspondence between a lexical level
 - represents a concatenation of morphemes making up a word
 - and the surface level
 - Represents the actual spelling of the final word.





Morphological Parsing with FST

- Morphological parsing is implemented by building mapping rules:
 - that <u>maps letter sequences</u> like *cats* on the surface level
 - into morpheme and features sequence like cat +N +PL on the lexical level.

```
Lexical \( \frac{1}{2} \) C \quad a \quad t \quad +N \quad +PL \quad \( \frac{1}{2} \)

Surface \( \frac{1}{2} \) C \quad a \quad t \quad s \quad \( \frac{1}{2} \)
```



- The automaton we use for performing the mapping between these two levels is the **finite-state transducer** or **FST**.
 - A transducer maps between one set of symbols and another;
 - An FST does this via a finite automaton.
 - Thus an FST can be seen as a two-tape automaton which recognizes or generates pairs of strings.
 - The FST has a more general function than an FSA:
 - An FSA defines a formal language
 - An FST defines a relation between sets of strings.
 - Another view of an FST:
 - A machine reads one string and generates another.



\mathbf{B}



Morphological Parsing with FST

D C B A

FST as recognizer:

- a transducer that takes a pair of strings as input and output *accept* if the string-pair is in the string-pair language, and a *reject* if it is not.

FST as generator:

a machine that outputs pairs of strings of the language. Thus the output is
 a yes or no, and a pair of output strings.

FST as translator:

A machine that reads a string and outputs another string.

FST as set relater:

A machine that computes relation between sets.

3



Morphological Parsing with FST

- A formal definition of FST (based on the **Mealy machine** extension to a simple FSA):
 - *Q*: a finite set of *N* states $q_0, q_1, ..., q_N$
 - Σ: a finite alphabet of complex symbols. Each complex symbol is composed of an input-output pair *i* : *o*; one symbol *I* from an input alphabet *I*, and one symbol *o* from an output alphabet *O*, thus Σ ⊆ *I* □*O*. *I* and *O* may each also include the epsilon symbol ε.
 - q_0 : the start state
 - F: the set of final states, $F \subseteq Q$
 - $\delta(q,i:o)$: the transition function or transition matrix between states. Given a state $q \in Q$ and complex symbol $i:o \in \Sigma$, $\delta(q,i:o)$ returns a new state $q' \in Q$. δ is thus a relation from $Q \times \Sigma$ to Q.

 B.E. VII Sem Natural Language Processing



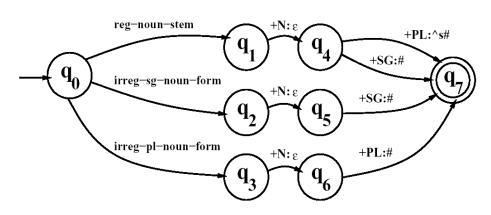
- FSAs are isomorphic to regular languages, FSTs are isomorphic to regular relations.
 - Regular relations are sets of pairs of strings, a natural extension of the regular language, which are sets of strings.
 - FSTs are closed under union, but generally they are not closed under difference, complementation, and intersection.
 - Two useful closure properties of FSTs:
 - **Inversion:** If T maps from I to O, then the inverse of T, T^{-1} maps from O to I.
 - **Composition:** If T_1 is a transducer from I_1 to O_1 and T_2 a transducer from I_2 to O_2 , then T_1 or T_2 maps from I_1 to O_2



- Inversion is useful because it makes it easy to convert a FST-as-parser into an FST-as-generator.
- Composition is useful because it allows us to take two transducers than run in series and replace them with one complex transducer. $T_1 \circ T_2(S) = T_2(T_1(S))$
- View an FST as having two tapes:
 - upper or lexical tape: characters from the left side of the a:b pairs
 - lower or surface tape: characters from the right side of the a:b pairs
 - Each symbol *a:b* expresses how the symbol *a* from one tape is mapped to the symbol *b* on the another tape



Morphological Parsing with FST



A lexical transducer for English nominal inflection T_{num}

| Reg-noun | Irreg-pl-noun | Irreg-sg-noun | | |
|----------|-----------------|---------------|--|--|
| fox | g o:e o:e s e | goose | | |
| cat | sheep | sheep | | |
| dog | m o:i u:ɛ s:c e | mouse | | |
| aardvark | | | | |







- The transducer will map:
 - plural nouns = stem + morphological marker +PL
 - singular nouns = stem + morphological marker +SG
- Thus a surface cats will map to cat +N +PL

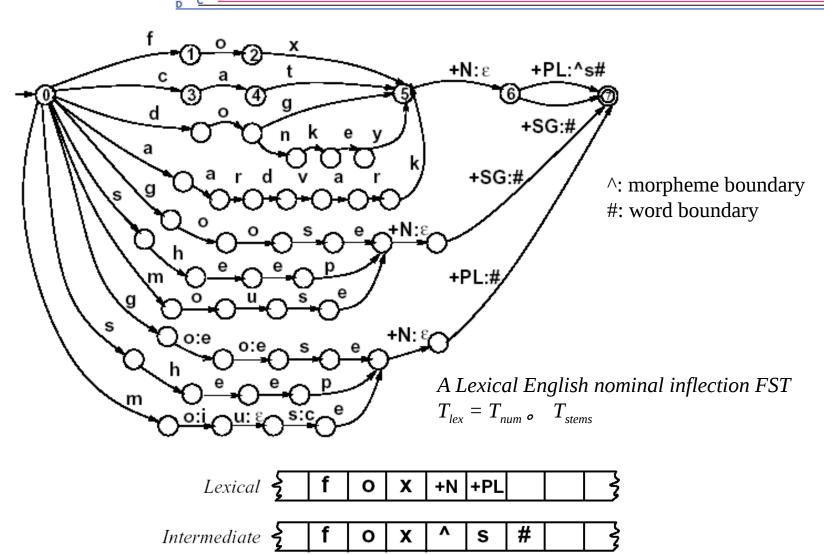
```
-c:c a:a t:t +N:epsilon +PL:^s#
```

- -c maps to itself, as do a and t, while morphological feature +N maps to nothing, and the feature +PL maps to s
- −The symbol ^ indicates *morpheme boundary*, while symbol # indicates a *word boundary*

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A

Morphological Parsing with FST





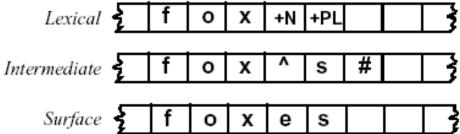
Orthographic Rules and FSTs

D C B A

Spelling rules (or orthographic rules)

| Name | Description of Rule | Example | |
|--------------------|---|----------------|--|
| Consonant doubling | 1-letter consonant doubled before -ing/-ed | beg/begging | |
| E deletion | Silent e dropped before -ing and -ed | make/making | |
| E insertion | e added after -s, -z, -x, -ch, -sh, before -s | watch/watches | |
| Y replacement | -y changes to -ie before -s, -i before -ed | try/tries | |
| K insertion | Verb ending with $vowel + -c$ add $-k$ | panic/panicked | |

Spelling changes can be thought as taking as input a simple concatenation of morphemes and producing as output a slightly-modified concatenation of morphemes.







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Orthographic Rules and FSTs

D C B A

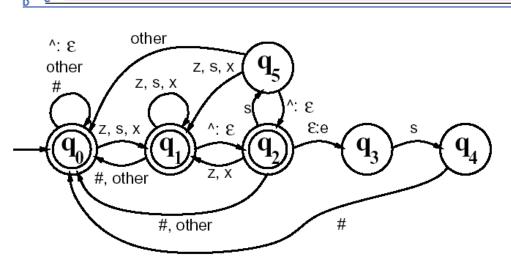
"insert an e on the surface tape just when the lexical tape has a morpheme ending in x (s or z) and the next morphemes is -s"

$$\varepsilon \rightarrow \varepsilon / \begin{cases} x \\ s \\ z \end{cases} \land \underline{\hspace{1cm}} s\#$$

"rewrite *a* and *b* when it occurs between *c* and *d*"[Chomsky and Halle (1968)]

$$a \rightarrow b / c _d$$

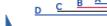
Orthographic Rules and FSTs



The transducer for the E-insertion rule

| State\Input | s:s | x:x | z:z | 3:.^ | ε: e | # | other |
|-------------|-----|-----|-----|------|-------------|---|-------|
| q_0 : | 1 | 1 | 1 | 0 | - | 0 | 0 |
| q_1 : | 1 | 1 | 1 | 2 | - | 0 | 0 |
| q_2 : | 5 | 1 | 1 | 0 | 3 | 0 | 0 |
| q_3 | 4 | - | - | - | - | - | - |
| $ q_4 $ | - | - | - | - | - | 0 | - |
| q_5 | 1 | 1 | 1 | 2 | - | - | 0 |

References





Speech and Language Processing, [Chapter 3]
 Daniel Jurafsky and James H. Martin





