
Public Key Cryptography and RSA

Private-Key Cryptography

- traditional **private/secret/single key** cryptography uses **one** key
 - shared by both sender and receiver
 - if this key is disclosed communications are compromised
 - also is **symmetric**, parties are equal
 - hence does not protect sender from receiver forging a message & claiming is sent by sender
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Public-Key Cryptography

- probably most significant advance in the 3000 year history of cryptography
 - uses **two** keys – a public & a private key
 - **asymmetric** since parties are **not** equal
 - uses clever application of number theoretic concepts to function
 - complements **rather than** replaces private key crypto
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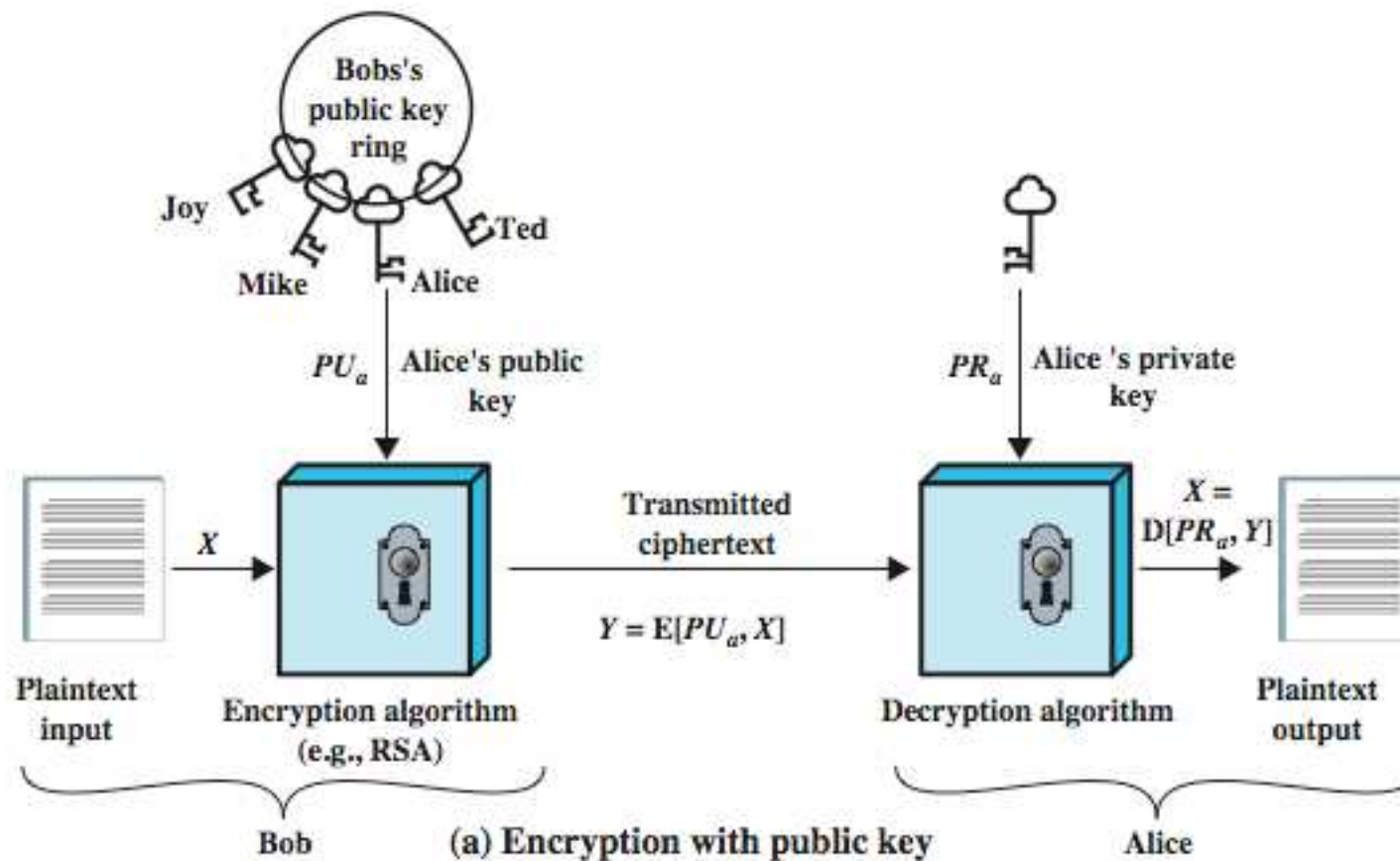
Why Public-Key Cryptography?

- developed to address two key issues:
 - **key distribution** – how to have secure communications in general without having to trust a KDC with your key
 - **digital signatures** – how to verify a message comes intact from the claimed sender
 - public invention due to Whitfield Diffie & Martin Hellman at Stanford Uni in 1976
 - known earlier in classified community
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Public-Key Cryptography

- **public-key/two-key/asymmetric** cryptography involves the use of **two** keys:
 - a **public-key**, which may be known by anybody, and can be used to **encrypt messages**, and **verify signatures**
 - a related **private-key**, known only to the recipient, used to **decrypt messages**, and **sign** (create) **signatures**
 - **infeasible to determine private key from public**
 - is **asymmetric** because
 - those who encrypt messages or verify signatures **cannot** decrypt messages or create signatures
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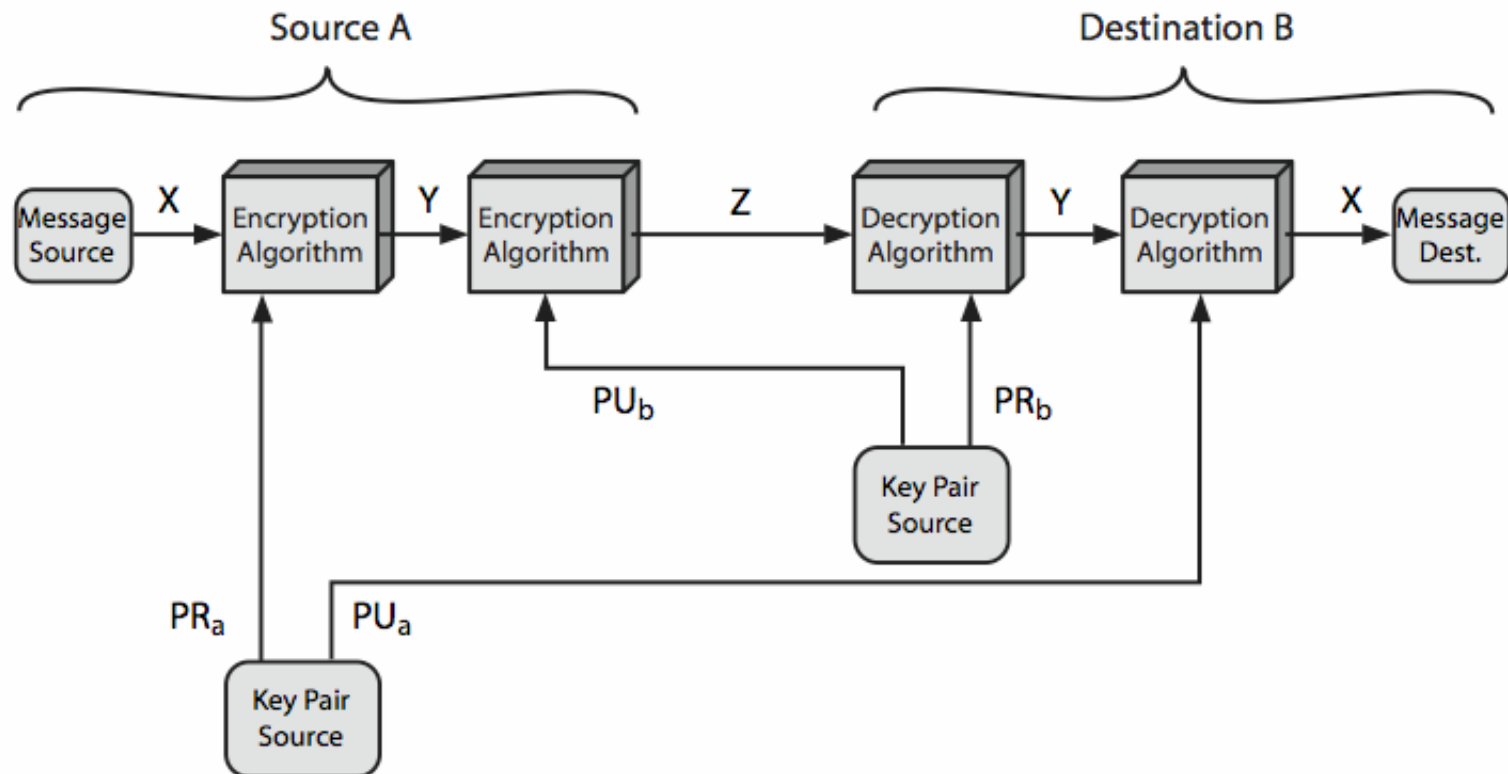
Public-Key Cryptography



Symmetric vs Public-Key

Conventional Encryption	Public-Key Encryption
<i>Needed to Work:</i> <ol style="list-style-type: none">1. The same algorithm with the same key is used for encryption and decryption.2. The sender and receiver must share the algorithm and the key. <i>Needed for Security:</i> <ol style="list-style-type: none">1. The key must be kept secret.2. It must be impossible or at least impractical to decipher a message if no other information is available.3. Knowledge of the algorithm plus samples of ciphertext must be insufficient to determine the key.	<i>Needed to Work:</i> <ol style="list-style-type: none">1. One algorithm is used for encryption and decryption with a pair of keys, one for encryption and one for decryption.2. The sender and receiver must each have one of the matched pair of keys (not the same one). <i>Needed for Security:</i> <ol style="list-style-type: none">1. One of the two keys must be kept secret.2. It must be impossible or at least impractical to decipher a message if no other information is available.3. Knowledge of the algorithm plus one of the keys plus samples of ciphertext must be insufficient to determine the other key.

Public-Key Cryptosystems



Public-Key Applications

- can classify uses into 3 categories:
 - **encryption/decryption** (provide secrecy)
 - **digital signatures** (provide authentication)
 - **key exchange** (of session keys)
- some algorithms are suitable for all uses, others are specific to one

Algorithm	Encryption/Decryption	Digital Signature	Key Exchange
RSA	Yes	Yes	Yes
Elliptic Curve	Yes	Yes	Yes
Diffie-Hellman	No	No	Yes
DSS	No	Yes	No

Public-Key Requirements

- Public-Key algorithms rely on two keys where:
 - it is computationally infeasible to find decryption key knowing only algorithm & encryption key
 - it is computationally easy to en/decrypt messages when the relevant (en/decrypt) key is known
 - either of the two related keys can be used for encryption, with the other used for decryption (for some algorithms)
 - these are formidable requirements which only a few algorithms have satisfied
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Public-Key Requirements

- need a trapdoor one-way function
- one-way function has
 - $Y = f(X)$ easy
 - $X = f^{-1}(Y)$ infeasible
- a trap-door one-way function has
 - $Y = f_k(X)$ easy, if k and X are known
 - $X = f_k^{-1}(Y)$ easy, if k and Y are known
 - $X = f_k^{-1}(Y)$ infeasible, if Y known but k not known
- a practical public-key scheme depends on a suitable trap-door one-way function

Security of Public Key Schemes

- like private key schemes brute force **exhaustive search** attack is always theoretically possible
 - but keys used are too large (>512bits)
 - security relies on a **large enough** difference in difficulty between **easy** (en/decrypt) and **hard** (cryptanalyse) problems
 - more generally the **hard** problem is known, but is made hard enough to be impractical to break
 - requires the use of **very large numbers**
 - hence is **slow** compared to private key schemes
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