

# Overview

- Background – Parsing
- Parsing as Search
  - Top-down Parsing
  - Bottom-up Parsing
- A Basic Top-Down Parser
  - Adding bottom-up filtering
- Problems: Basic Top-Down Parser
  - Left-recursion
  - Ambiguity
  - Repeated Parsing Subtrees
- Dynamic Programming

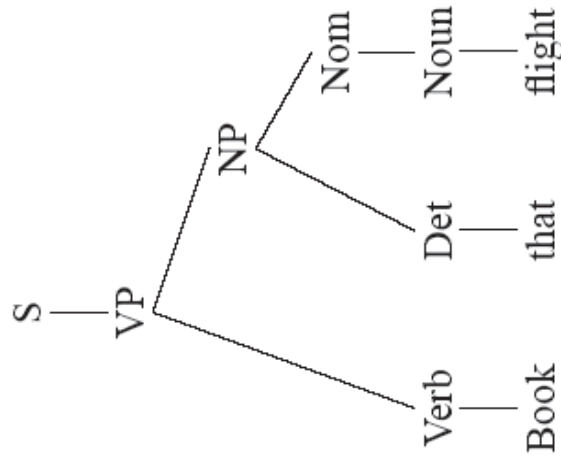
# Background

- ♦ Syntactic parsing
  - The task of recognizing a sentence and assigning a syntactic structure to it
- ♦ Since CFGs are a declarative formalism – do not specify how the parse tree for a given sentence should be computed
- ♦ Parse trees are useful in applications such as :
  - Grammar checking
  - Semantic analysis
  - Machine translation
  - Question answering
  - Information extraction

# Parsing as Search

- ◆ The parser can be viewed as searching through the space of all possible parse trees to find the correct parse tree for the sentence.
- ◆ **How can we use the grammar to assign the parse tree?**

$S \rightarrow NP VP$	$Det \rightarrow that   this   a$
$S \rightarrow Aux NP VP$	$Noun \rightarrow book   flight   meal   money$
$S \rightarrow VP$	$Verb \rightarrow book   include   prefer$
$NP \rightarrow Det Nominal$	$Aux \rightarrow does$
$Nominal \rightarrow Noun$	$Prep \rightarrow from   to   on$
$Nominal \rightarrow Noun Nominal$	$Proper-Noun \rightarrow Houston   TWA$
$NP \rightarrow Proper-Noun$	
$VP \rightarrow Verb$	
$VP \rightarrow Verb NP$	$Nominal \rightarrow Nominal PP$



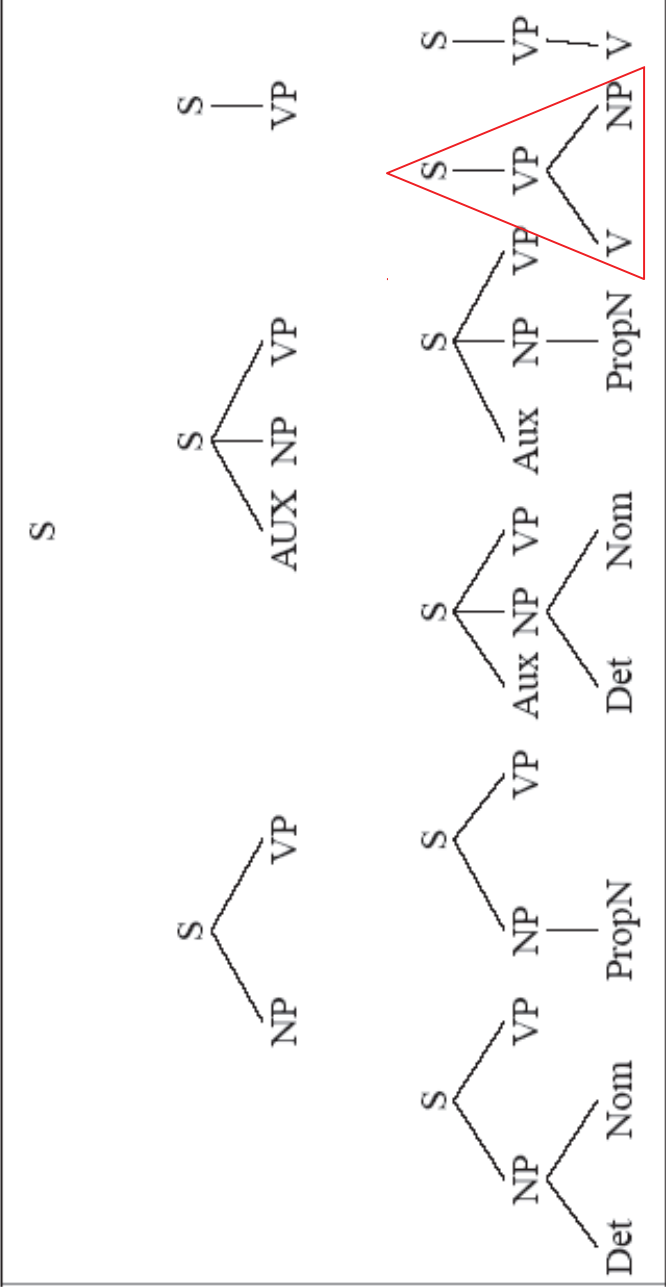
# Parsing as Search

- ◆ The goal of a parsing search is to find all trees whose root is the start symbol  $S$ , which cover exactly the words in input.
- ◆ Two kinds of constraints:
  - Data – input words as leaves (*book, that, flight*)
  - Grammar – must have one root, which must be the start symbol  $S$
- ◆ Leads to the two search strategies:
  - *Top-down* or goal-directed search
  - *Bottom-up* or data-directed search

# Top-down Parser

- ◆ Trying to build from the **root node S** down to the leaves
- ◆ Start by start symbol S.
- ◆ Find the grammar rules with S on the left-hand side and expand the constituents in new trees
- ◆ At each level or **ply**, use the right-hand sides of the rules to provide new sets of expectations
- ◆ Tree grows until reaches the part-of-speech categories at the bottom
- ◆ Trees whose leaves fail to match all the words in the input can be rejected

# Top-down Parser



$S \rightarrow NP VP$	$Det \rightarrow that   this   a$
$S \rightarrow Aux NP VP$	$Noun \rightarrow book   flight   meal   money$
$S \rightarrow VP$	$Verb \rightarrow book   include   prefer$
$NP \rightarrow Det Nominal$	$Aux \rightarrow does$
$Nominal \rightarrow Noun$	$Prep \rightarrow from   to   on$
$Nominal \rightarrow Noun Nominal$	$Proper-Noun \rightarrow Houston   TWA$
$NP \rightarrow Proper-Noun$	$Nominal \rightarrow Nominal PP$
$VP \rightarrow Verb$	
$VP \rightarrow Verb NP$	



# Bottom-up Parsing

- ◆ Starts with the words of the input and tries to build trees from the words up, by applying rules from the grammar
- ◆ Initially *for each input word* build partial trees with the part-of-speech
- ◆ For each ply, find the right-hand side of the rule that match the sequence of non-terminals
- ◆ Parse is success, if parser succeeds in building a tree rooted in the start symbol S

# Bottom-up Parsing

Book that flight

Noun Det Noun      Verb Det Noun  
|                                  |  
Book that flight      Book that flight

NOM                      NOM  
|                                  |  
Noun Det Noun      Verb Det Noun  
|                                  |  
Book that flight      Book that flight

NOM                      NP                      VP                      NOM  
|                                  |                                  |                                  |  
Noun Det      Noun      flight      Verb Det      Noun      flight  
|                                  |  
Book that      Book that

VP                      NP                      NP                      NP  
|                                  |                                  |                                  |  
Verb Det      Noun      flight      Verb Det      Noun      flight  
|                                  |  
Book that      Book that



# Top-down Vs Bottom-up

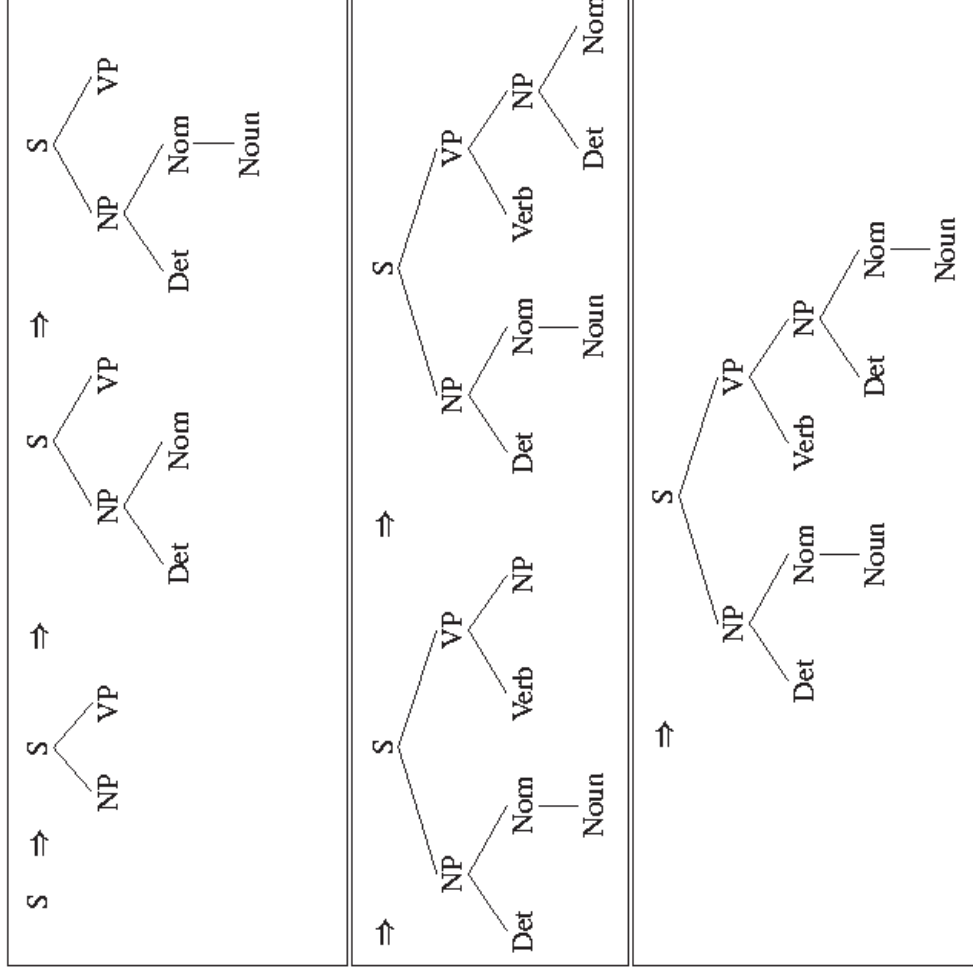
- ◆ **Comparisons**

- ◆ The top-down strategy never wastes time exploring trees that cannot result in an  $S$ .
  - Spend considerable effort on  $S$  trees that are not consistent with the input.
  - Generate trees before ever examining the input.
- ◆ The bottom-up strategy never suggest trees that are *not at least locally grounded* in the actual input
  - Trees that have no hope to leading to an  $S$  are generated with wild abandon.

# A Basic Top-Down Parser

- ◆ Solution: Incorporate features of both the top-down and bottom-up approaches
- ◆ In top-down depth-first approach:
  - Left-most unexpanded leaf node is expanded first
  - Grammar rules are applied according to their textual order

# A Basic Top-Down Parser



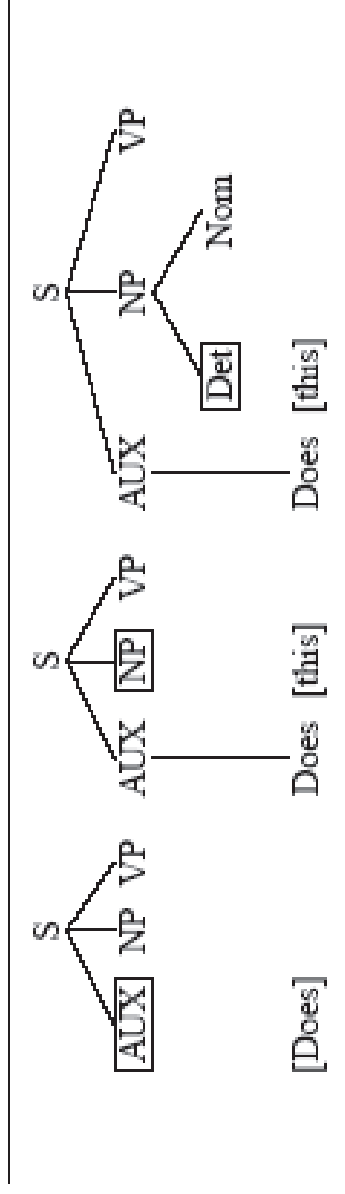
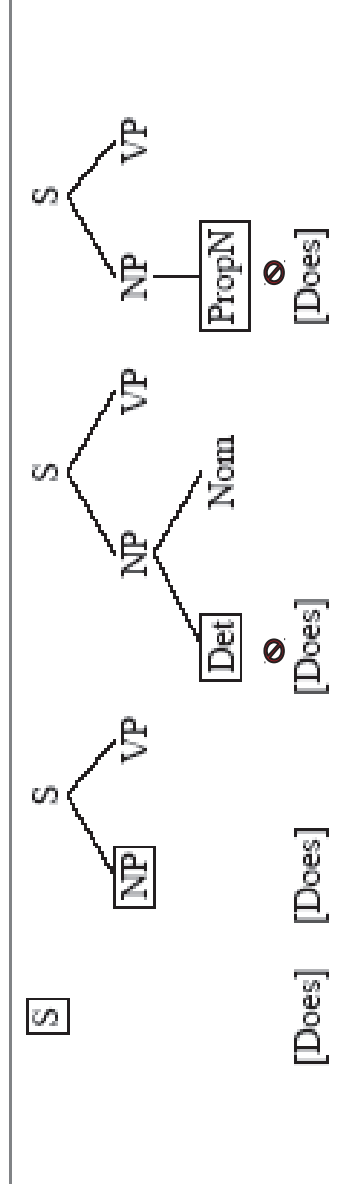
*A top-down depth-first derivation*

# A Basic Top-Down Parser

- ◆ Top-down, depth-first, left-to-right approach: expand the left-most unexpanded node in the tree
  - The node currently being expanded is shown in a box
  - The current input word is bracketed

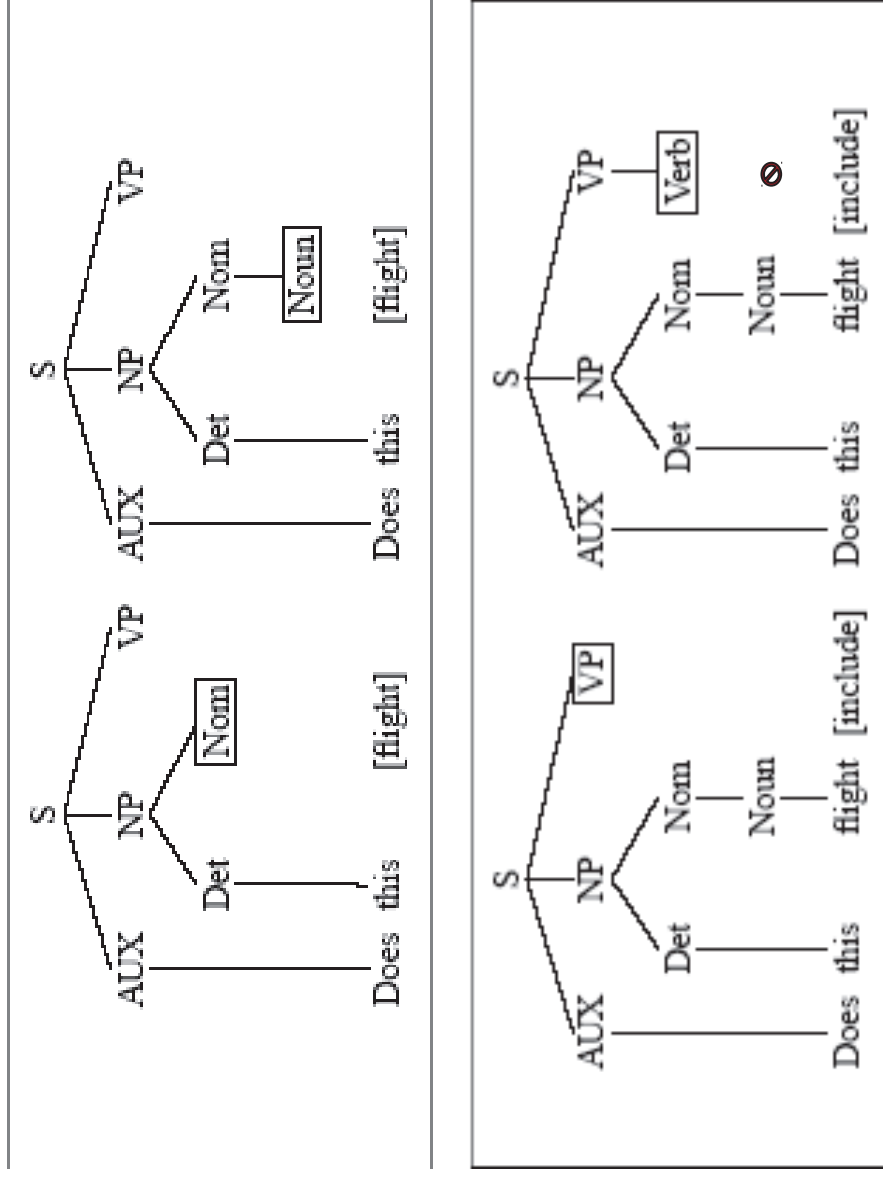
# A Basic Top-Down Parser

*Does this flight include a meal?*



A top-down, depth-first, left-right derivation

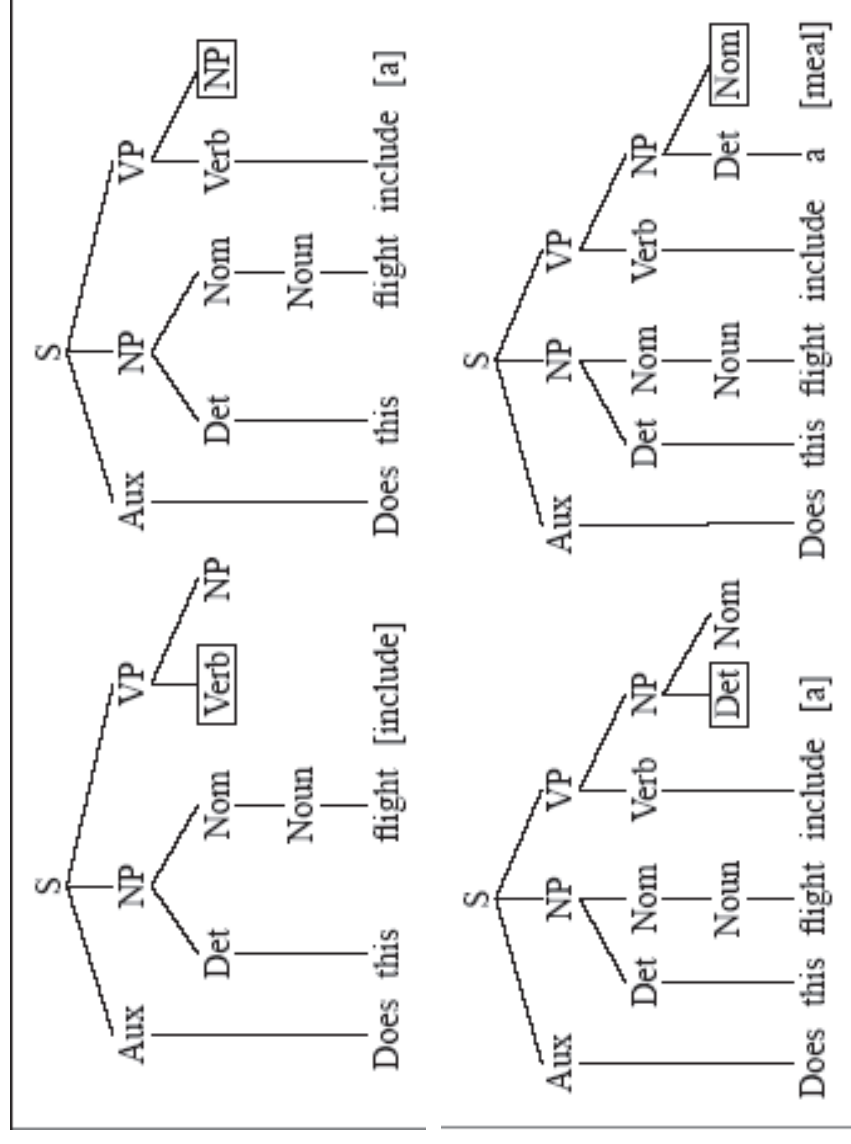
# A Basic Top-Down Parser



A top-down, depth-first, left-right derivation continued

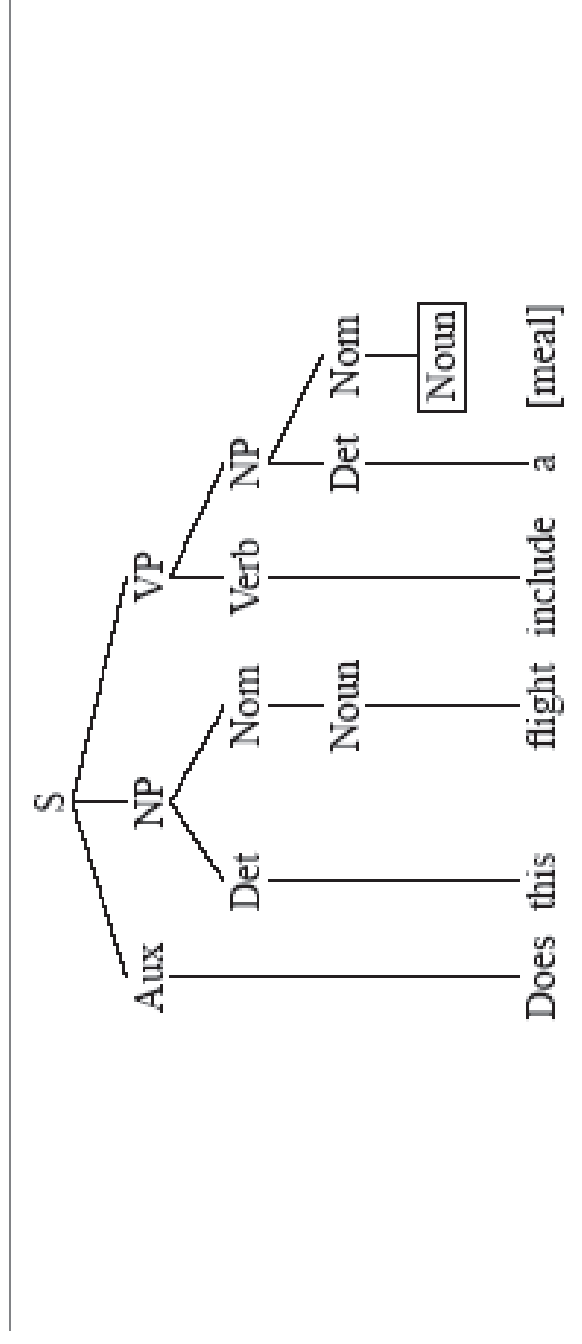


# A Basic Top-Down Parser



A top-down, depth-first, left-right derivation continued

# A Basic Top-Down Parser



A top-down, depth-first, left-right derivation continued

# A Basic Top-Down Parser

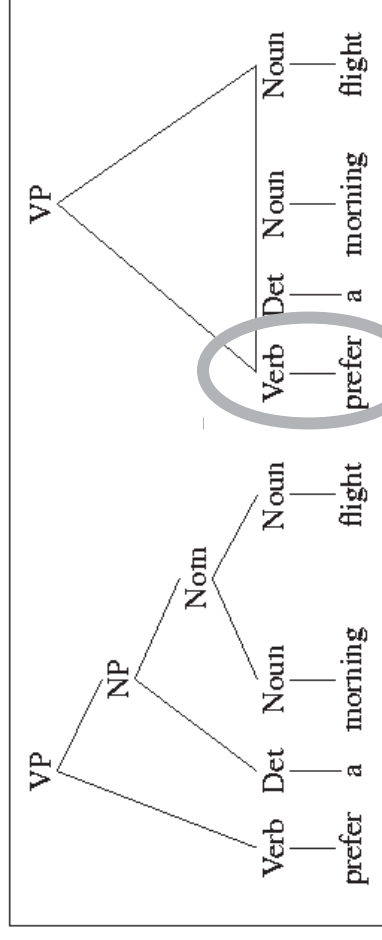
---

```
function TOP-DOWN-PARSE(input, grammar) returns a parse tree
  agenda ← (Initial S tree, Beginning of input)
  current-search-state ← POP(agenda)
  loop
    if SUCCESSFUL-PARSE?(current-search-state) then
      return TREE(current-search-state)
    else
      if CAT(NODE-TO-EXPAND(current-search-state)) is a POS then
        if CAT(node-to-expand)
          C
            POS(CURRENT-INPUT(current-search-state)) then
              PUSH(APPLY-LEXICAL-RULE(current-search-state), agenda)
            else
              return reject
          else
            PUSH(APPLY-RULES(current-search-state, grammar), agenda)
            if agenda is empty then
              return reject
            else
              current-search-state ← NEXT(agenda)
            end
```

---

# A Basic Top-Down Parser

- ◆ **Adding bottom-up filtering**
- ◆ The parser should not consider any grammar rule if the current input cannot serve as the *first word along the left edge of some derivation* from this rule
- ◆ The first word along the left edge of a derivation is called as the **left-corner** of the tree



# A Basic Top-Down Parser

- ♦ **Adding bottom-up filtering**
- ♦ Left-corner notion
  - For non-terminals  $A$  and  $B$ ,  $B$  is a left-corner of  $A$  if :  $A \xRightarrow{*} B\alpha$
- ♦ Three rules to expand  $S$  :

$S \rightarrow NP\ VP$   
 $S \rightarrow Aux\ NP\ VP$   
 $S \rightarrow VP$

*Does this flight include a meal ?*
- ♦ Using the left-corner notion, it is easy to see that only the  $S \rightarrow Aux\ NP\ VP$  rule is a viable candidate
- ♦ Since the word *Does* can not serve as the left-corner of other two  $S$ -rules

# A Basic Top-Down Parser

$S \rightarrow NP VP$	$Det \rightarrow that \mid this \mid a$
$S \rightarrow Aux NP VP$	$Noun \rightarrow book \mid flight \mid meal \mid money$
$S \rightarrow VP$	$Verb \rightarrow book \mid include \mid prefer$
$NP \rightarrow Det Nominal$	$Aux \rightarrow does$
$Nominal \rightarrow Noun$	
$Nominal \rightarrow Noun Nominal$	$Prep \rightarrow from \mid to \mid on$
$NP \rightarrow Proper-Noun$	$Proper-Noun \rightarrow Houston \mid TWA$
$VP \rightarrow Verb$	
$VP \rightarrow Verb NP$	$Nominal \rightarrow Nominal PP$

Category	Left Corners
S	Det, Proper-Noun, Aux, Verb
NP	Det, Proper-Noun
Nominal	Noun
VP	Verb

Left-corner table for the above Grammar





# Problems: Basic Top-Down Parser

- ◆ Problems with the top-down parser
  - Left-recursion
  - Ambiguity
  - Inefficient reparsing of subtrees
- ◆ Solution: Earley algorithm

# Problem: Left-recursion

- ◆ Exploring infinite search space, when **left-recursive grammars** are used
- ◆ A grammar is left-recursive if it contains at least one non-terminal  $A$ , s.t.  $A \xRightarrow{*} \alpha A \beta$ , for some  $\alpha$  and  $\beta$  and  $\alpha \xRightarrow{*} \epsilon$ .

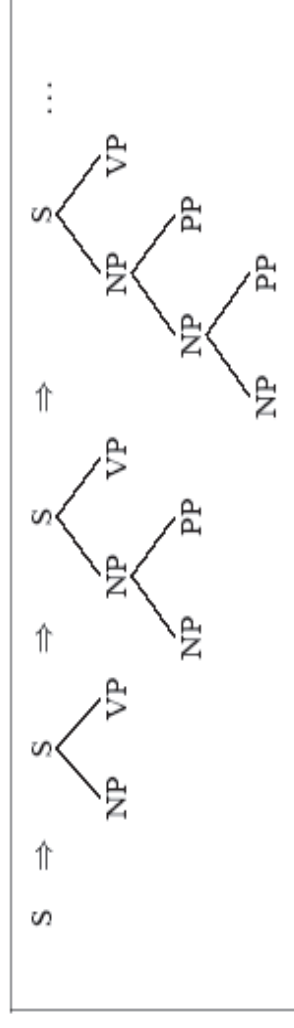
$NP \rightarrow NP PP$

$VP \rightarrow VP PP$

$S \rightarrow S \text{ and } S$

*Left-recursive rules*

$NP \rightarrow NP PP$



## Problem: Left-recursion

- ◆ Two reasonable methods for dealing with left-recursion in a backtracking top-down parser:
  - Rewriting the grammar
  - Explicitly managing the depth of the search during parsing
- ◆ Rewrite each rule of left-recursion

$$\begin{array}{lcl} A \rightarrow A\beta \mid \alpha & \Rightarrow & A \rightarrow \alpha A' \\ & & A' \rightarrow \beta A' \mid \varepsilon \end{array}$$

*left-recursive*

*Weakly equivalent non-left-recursive*

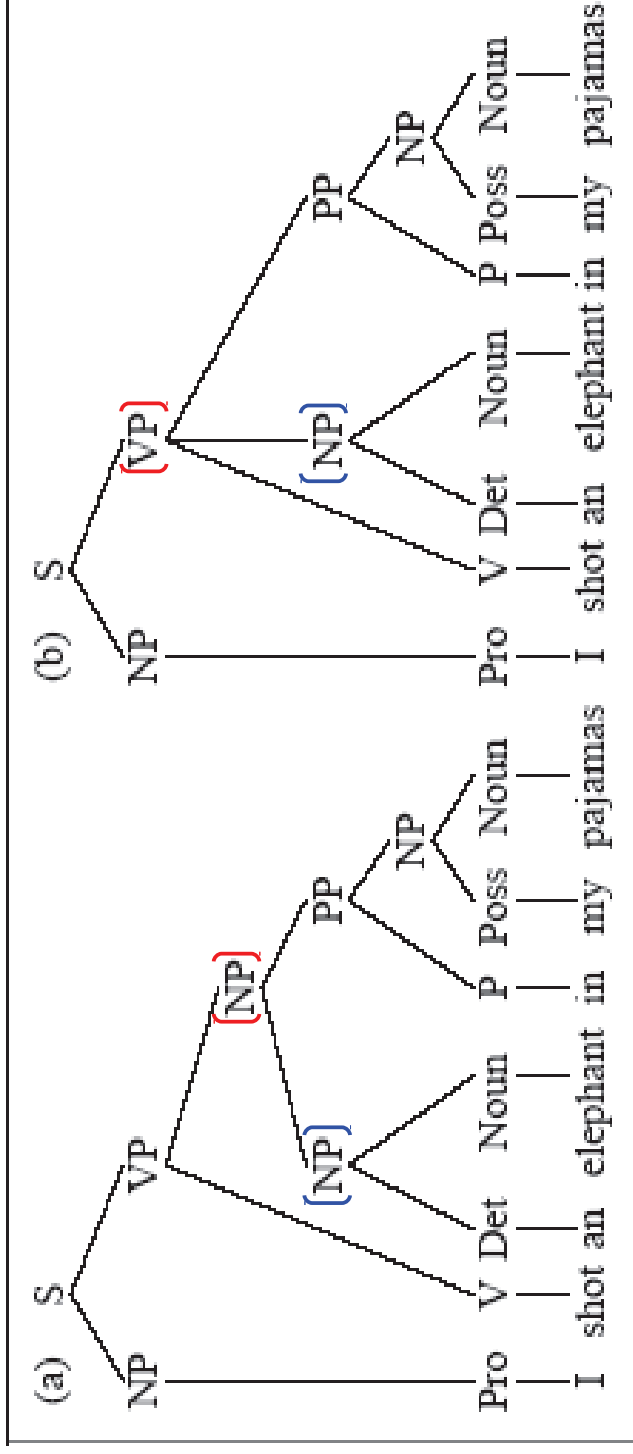
- ◆ Rewriting may make semantic interpretation quite difficult

## Problem: Ambiguity

- ◆ Lexical category ambiguity – word has more than one pos
- ◆ Disambiguation – choosing the correct pos for a word
- ◆ Structural ambiguity – grammar assigns *more than one possible parse* to a sentence
- ◆ Three kinds of structural ambiguity:
  - attachment ambiguity
  - coordination ambiguity
  - noun-phrase bracketing ambiguity

# Problem: Ambiguity

- ◆ Attachment ambiguity
  - A particular constituent can be attached to the parse tree at *more than one place*

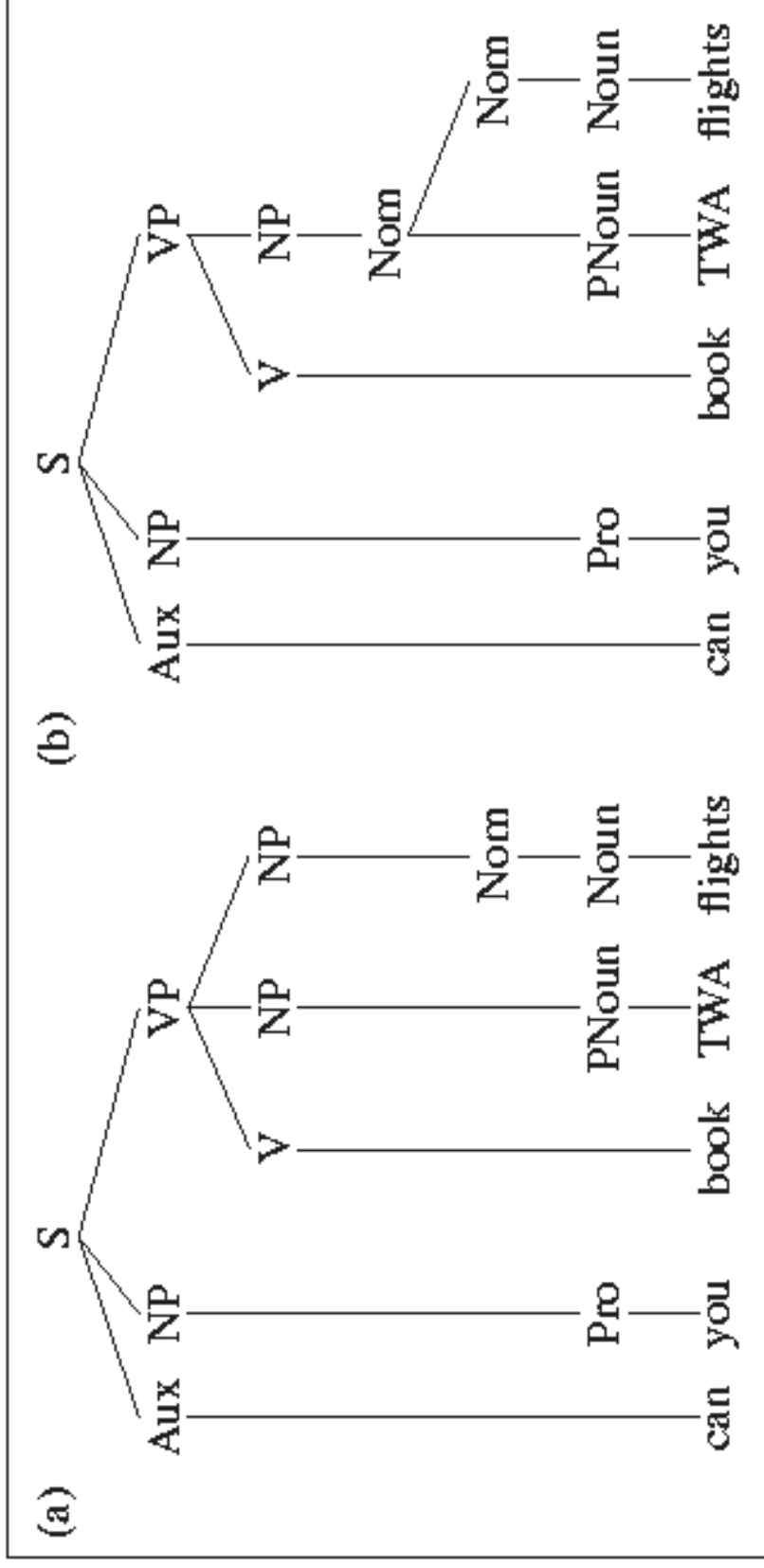


a) *elephant is in the pajamas*

b) *Captain did the shooting in his pajamas*

# Problem: Ambiguity

- ◆ The sentence “Can you book TWA flights” is ambiguous:



*a) Can you book flights on behalf of TWA*

*b) Can you book flights run by TWA*



## Problem: Ambiguity

- ◆ *Coordination ambiguity* – different sets of phrases can be conjoined by conjunction like *and*  
*old men and women*  
*[old [men and women]]*  $\Rightarrow$  *old men and old women*  
*[old men] and [women]*  $\Rightarrow$  *only the men who are old*
- ◆ Parsing sentence thus requires disambiguation:
  - Choosing the correct parse from a multitude of possible parser
  - Requiring both statistical and semantic knowledge

## Problem: Ambiguity

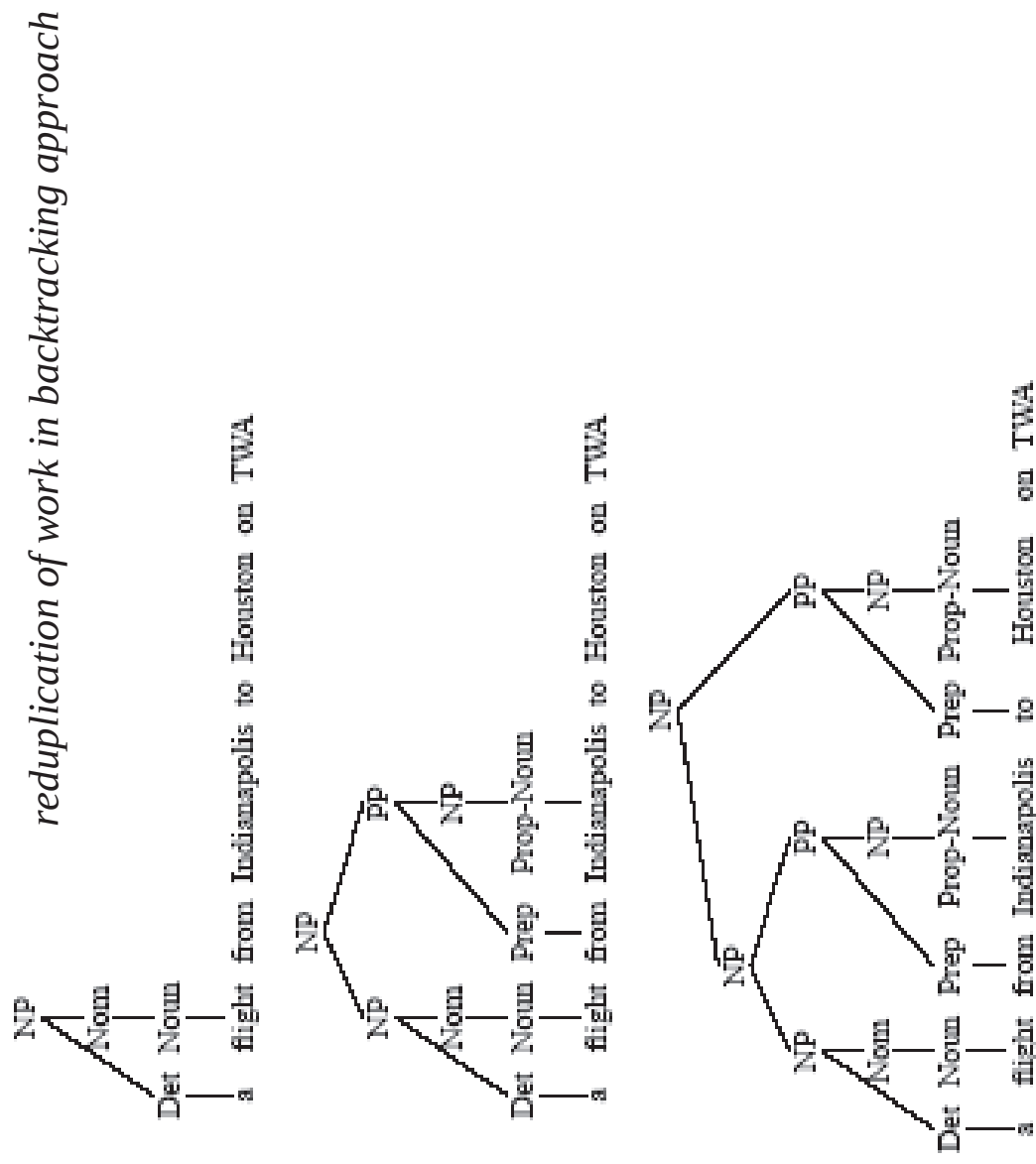
- ◆ Parsers which do not incorporate disambiguators may simply return all the possible parse trees for a given input.
- ◆ Potentially exponential number of parses that are possible for certain inputs
  - Show me the meal **on** Flight UA 386 **from** San Francisco **to** Denver.
  - The three PP's at the end of this sentence yield a total of 14 parse trees for this sentence.
  - Solution: use dynamic programming

## Problem: Repeated Parsing Subtrees

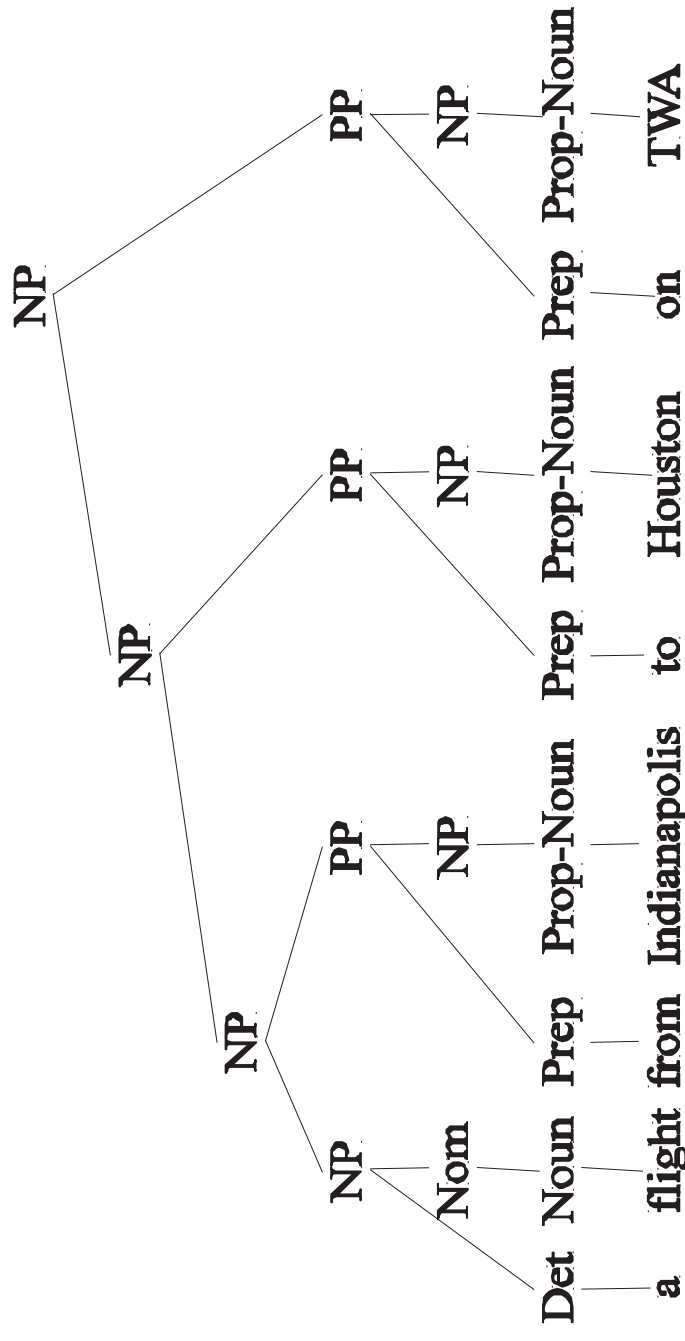
- ♦ The parser often builds valid trees for portions of the input, *then discards them during backtracking, only to find that it has to rebuild them again.*

a flight 4  
From Indianapolis 3  
To Houston 2  
On TWA 1  
A flight from Indianapolis 3  
A flight from Indianapolis to Houston 2  
A flight from Indianapolis to Houston on TWA 1

# Problem: Repeated Parsing Subtrees



# Problem: Repeated Parsing Subtrees



*reduplication of work in backtracking approach*

# Dynamic Programming

- ◆ Dynamic programming provides framework for solving the three kinds of problems afflicting top-down or bottom-up parsers
- ◆ Dynamic programming approaches systematically fill in tables of solutions to sub-problems
- ◆ When complete, the tables contain the solution to all the sub-problems needed to solve the problem
- ◆ Using tables to store the sub-trees for each constituents in the input solves reparsing and the ambiguity problem
- ◆ Also solves left-recursion problem



# Dynamic Programming

- ◆ Three well-known dynamic parsers:
  - Cocke-Younger-Kasami (CYK) algorithm
  - Graham-Harrison-Ruzzo (GHR) algorithm
  - Earley algorithm

# References

- ◆ Speech and Language Processing, *Jurafsky and H.Martin*  
[Chapter 10. Parsing with Context-Free Grammars]

---

Thank you