# Package 'Metrics'

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<b>Description</b> An implementation of evaluation metrics in R that are commonly used in supervised machine learning. It implements metrics for regression, time series, binary classification, classification, and information retrieval problems. It has zero dependencies and a consistent, simple interface for all functions.
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# Description

accuracy is defined as the proportion of elements in actual that are equal to the corresponding element in predicted

# Usage

```
accuracy(actual, predicted)
```

# Arguments

actual The ground truth vector, where elements of the vector can be any variable type.

predicted The predicted vector, where elements of the vector represent a prediction for the corresponding value in actual.

# See Also

ae 3

#### **Examples**

```
actual <- c('a', 'a', 'c', 'b', 'c')
predicted <- c('a', 'b', 'c', 'b', 'a')
accuracy(actual, predicted)</pre>
```

ae

Absolute Error

# Description

ae computes the elementwise absolute difference between two numeric vectors.

# Usage

```
ae(actual, predicted)
```

# Arguments

actual

The ground truth numeric vector.

predicted

The predicted numeric vector, where each element in the vector is a prediction for the corresponding element in actual.

# See Also

mae mdae mape

# **Examples**

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6) predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2) ae(actual, predicted)
```

ape

Absolute Percent Error

#### **Description**

ape computes the elementwise absolute percent difference between two numeric vectors

```
ape(actual, predicted)
```

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#### **Arguments**

actual The ground truth numeric vector.

predicted The predicted numeric vector, where each element in the vector is a prediction

for the corresponding element in actual.

#### **Details**

ape is calculated as (actual - predicted) / actual. This means that the function will return -Inf, Inf, or NaN if actual is zero.

#### See Also

```
mape smape
```

#### **Examples**

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6)
predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2)
ape(actual, predicted)
```

apk

Average Precision at k

#### **Description**

apk computes the average precision at k, in the context of information retrieval problems.

#### Usage

```
apk(k, actual, predicted)
```

# Arguments

k The number of elements of predicted to consider in the calculation.

actual The ground truth vector of relevant documents. The vector can contain any

numeric or character values, order does not matter, and the vector does not need

to be the same length as predicted.

predicted The predicted vector of retrieved documents. The vector can contain any nu-

meric of character values. However, unlike actual, order does matter, with the

most documents deemed most likely to be relevant at the beginning.

#### **Details**

apk loops over the first k values of predicted. For each value, if the value is contained within actual and has not been predicted before, we increment the number of sucesses by one and increment our score by the number of successes divided by k. Then, we return our final score divided by the number of relevant documents (i.e. the length of actual).

apk will return NaN if length(actual) equals 0.

auc 5

#### See Also

```
apk f1
```

#### **Examples**

```
actual <- c('a', 'b', 'd')
predicted <- c('b', 'c', 'a', 'e', 'f')
apk(3, actual, predicted)</pre>
```

auc

Area under the ROC curve (AUC)

# Description

auc computes the area under the receiver-operator characteristic curve (AUC).

#### **Usage**

```
auc(actual, predicted)
```

# **Arguments**

actual The ground truth binary numeric vector containing 1 for the positive class and 0

for the negative class.

predicted A numeric vector of predicted values, where the smallest values correspond to

the observations most believed to be in the negative class and the largest values indicate the observations most believed to be in the positive class. Each element

represents the prediction for the corresponding element in actual.

#### **Details**

auc uses the fact that the area under the ROC curve is equal to the probability that a randomly chosen positive observation has a higher predicted value than a randomly chosen negative value. In order to compute this probability, we can calculate the Mann-Whitney U statistic. This method is very fast, since we do not need to compute the ROC curve first.

```
actual <- c(1, 1, 1, 0, 0, 0)
predicted <- c(0.9, 0.8, 0.4, 0.5, 0.3, 0.2)
auc(actual, predicted)
```

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bias Bias

# Description

bias computes the average amount by which actual is greater than predicted.

#### Usage

```
bias(actual, predicted)
```

#### **Arguments**

actual The ground truth numeric vector.

predicted The predicted numeric vector, where each element in the vector is a prediction

for the corresponding element in actual.

#### **Details**

If a model is unbiased bias(actual, predicted) should be close to zero. Bias is calculated by taking the average of (actual - predicted).

# See Also

```
percent_bias
```

# **Examples**

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6) predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2) bias(actual, predicted)
```

ce

Classification Error

# Description

ce is defined as the proportion of elements in actual that are not equal to the corresponding element in predicted.

```
ce(actual, predicted)
```

*f*1 7

#### **Arguments**

actual The ground truth vector, where elements of the vector can be any variable type.

The predicted vector, where elements of the vector represent a prediction for the

corresponding value in actual.

#### See Also

accuracy

predicted

# **Examples**

```
actual <- c('a', 'a', 'c', 'b', 'c')
predicted <- c('a', 'b', 'c', 'b', 'a')
ce(actual, predicted)</pre>
```

f1

F1 Score

#### Description

f1 computes the F1 Score in the context of information retrieval problems.

#### Usage

```
f1(actual, predicted)
```

#### **Arguments**

actual The ground truth vector of relevant documents. The vector can contain any

numeric or character values, order does not matter, and the vector does not need

to be the same length as predicted.

predicted The predicted vector of retrieved documents. The vector can contain any nu-

meric or character values, order does not matter, and the vector does not need to

be the same length as actual.

#### **Details**

f1 is defined as 2\*precision\*recall/(precision+recall). In the context of information retrieval problems, precision is the proportion of retrieved documents that are relevant to a query and recall is the proportion of relevant documents that are successfully retrieved by a query. If there are zero relevant documents that are retrieved, zero relevant documents, or zero predicted documents, f1 is defined as  $\emptyset$ .

#### See Also

apk mapk

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# **Examples**

```
actual <- c('a', 'c', 'd')
predicted <- c('d', 'e')
f1(actual, predicted)</pre>
```

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Log Loss

# Description

11 computes the elementwise log loss between two numeric vectors.

# Usage

```
ll(actual, predicted)
```

# Arguments

actual

The ground truth binary numeric vector containing 1 for the positive class and 0

for the negative class.

predicted

A numeric vector of predicted values, where the values correspond to the prob-

abilities that each observation in actual belongs to the positive class

#### See Also

logLoss

# **Examples**

```
actual <- c(1, 1, 1, 0, 0, 0)
predicted <- c(0.9, 0.8, 0.4, 0.5, 0.3, 0.2)
ll(actual, predicted)
```

logLoss

Mean Log Loss

# **Description**

logLoss computes the average log loss between two numeric vectors.

```
logLoss(actual, predicted)
```

mae 9

# Arguments

actual The ground truth binary numeric vector containing 1 for the positive class and 0

for the negative class.

predicted A numeric vector of predicted values, where the values correspond to the prob-

abilities that each observation in actual belongs to the positive class

#### See Also

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#### **Examples**

```
actual <- c(1, 1, 1, 0, 0, 0)
predicted <- c(0.9, 0.8, 0.4, 0.5, 0.3, 0.2)
logLoss(actual, predicted)
```

mae

Mean Absolute Error

#### **Description**

mae computes the average absolute difference between two numeric vectors.

#### Usage

```
mae(actual, predicted)
```

#### **Arguments**

actual The ground truth numeric vector.

predicted The predicted numeric vector, where each element in the vector is a prediction

for the corresponding element in actual.

#### See Also

mdae mape

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6)
predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2)
mae(actual, predicted)
```

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mape

Mean Absolute Percent Error

#### **Description**

mape computes the average absolute percent difference between two numeric vectors.

#### Usage

```
mape(actual, predicted)
```

# Arguments

actual The ground truth numeric vector.

predicted The predicted numeric vector, where each element in the vector is a prediction

for the corresponding element in actual.

#### **Details**

mape is calculated as the average of (actual - predicted) / actual. This means that the function will return -Inf, Inf, or NaN if actual is zero. Due to the instability at or near zero, smape or mase are often used as alternatives.

#### See Also

```
\  \, \text{mae smape mase} \,
```

# Examples

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6)
predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2)
mape(actual, predicted)
```

mapk

Mean Average Precision at k

#### **Description**

mapk computes the mean average precision at k for a set of predictions, in the context of information retrieval problems.

```
mapk(k, actual, predicted)
```

mase 11

#### **Arguments**

k The number of elements of predicted to consider in the calculation.

actual A list of vectors, where each vector represents a ground truth vector of relevant

documents. In each vector, the elements can be numeric or character values, and

the order of the elements does not matter.

predicted A list of vectors, where each vector represents the predicted vector of retrieved

documents for the corresponding element of actual. In each vector, the order of the elements does matter, with the elements believed most likely to be relevant

at the beginning.

#### **Details**

mapk evaluates apk for each pair of elements from actual and predicted.

#### See Also

```
apk f1
```

#### **Examples**

```
actual <- list(c('a', 'b'), c('a'), c('x', 'y', 'b'))
predicted <- list(c('a', 'c', 'd'), c('x', 'b', 'a', 'b'), c('y'))
mapk(2, actual, predicted)

actual <- list(c(1, 5, 7, 9), c(2, 3), c(2, 5, 6))
predicted <- list(c(5, 6, 7, 8, 9), c(1, 2, 3), c(2, 4, 6, 8))
mapk(3, actual, predicted)</pre>
```

mase

Mean Absolute Scaled Error

# **Description**

mase computes the mean absolute scaled error between two numeric vectors. This function is only intended for time series data, where actual and numeric are numeric vectors ordered by time.

# Usage

```
mase(actual, predicted, step_size = 1)
```

#### **Arguments**

actual The ground truth numeric vector ordered in time, with most recent observation

at the end of the vector.

predicted The predicted numeric vector ordered in time, where each element of the vector

represents a prediction for the corresponding element of actual.

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step\_size

A positive integer that specifies how many observations to look back in time in order to compute the naive forecast. The default is 1, which means that the naive forecast for the current time period is the actual value of the previous period.

However, if actual and predictions were quarterly predictions over many years, letting step\_size = 4, would mean that the naive forecast for the current time period would be the actual value from the same quarter last year. In this way, mase can account for seasonality.

#### See Also

smape mape

#### **Examples**

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6)
predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2)
step_size <- 1
mase(actual, predicted, step_size)
```

mdae

Median Absolute Error

#### **Description**

mdae computes the median absolute difference between two numeric vectors.

# Usage

```
mdae(actual, predicted)
```

# **Arguments**

actual The ground truth numeric vector.

predicted The predicted numeric vector, where each element in the vector is a prediction

for the corresponding element in actual.

#### See Also

mae mape

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6)
predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2)
mdae(actual, predicted)
```

 ${\tt MeanQuadraticWeightedKappa}$ 

Mean Quadratic Weighted Kappa

# Description

MeanQuadraticWeightedKappa computes the mean quadratic weighted kappa, which can optionally be weighted

#### Usage

```
MeanQuadraticWeightedKappa(kappas, weights = rep(1, length(kappas)))
```

#### **Arguments**

kappas A numeric vector of possible kappas.

weights An optional numeric vector of ratings.

#### See Also

ScoreQuadraticWeightedKappa

# Examples

```
kappas <- c(0.3, 0.2, 0.2, 0.5, 0.1, 0.2)
weights <- c(1.0, 2.5, 1.0, 1.0, 2.0, 3.0)
MeanQuadraticWeightedKappa(kappas, weights)
```

mse

Mean Squared Error

# **Description**

mse computes the average squared difference between two numeric vectors.

#### Usage

```
mse(actual, predicted)
```

#### **Arguments**

actual The ground truth numeric vector.

predicted The predicted numeric vector, where each element in the vector is a prediction

for the corresponding element in actual.

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#### See Also

rmse mae

#### **Examples**

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6) predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2) mse(actual, predicted)
```

msle

Mean Squared Log Error

# **Description**

msle computes the average of squared log error between two numeric vectors.

#### Usage

```
msle(actual, predicted)
```

#### **Arguments**

actual The ground truth non-negative vector

predicted The predicted non-negative vector, where each element in the vector is a predic-

tion for the corresponding element in actual.

# **Details**

msle adds one to both actual and predicted before taking the natural logarithm to avoid taking the natural log of zero. As a result, the function can be used if actual or predicted have zero-valued elements. But this function is not appropriate if either are negative valued.

# See Also

```
rmsle sle
```

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6)
predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2)
msle(actual, predicted)
```

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params_binary	Inherit Documentation for Binary Classification Metrics	
params_binary	Inherit Documentation for Binary Classification Metrics	

#### **Description**

This object provides the documentation for the parameters of functions that provide binary classification metrics

#### **Arguments**

actual The ground truth binary numeric vector containing 1 for the positive class and 0

for the negative class.

predicted The predicted binary numeric vector containing 1 for the positive class and 0 for

the negative class. Each element represents the prediction for the corresponding

element in actual.

 ${\tt params\_classification} \ \ \textit{Inherit Documentation for Classification Metrics}$ 

# Description

This object provides the documentation for the parameters of functions that provide classification metrics

# **Arguments**

actual The ground truth vector, where elements of the vector can be any variable type.

predicted The predicted vector, where elements of the vector represent a prediction for the

corresponding value in actual.

#### **Description**

This object provides the documentation for the parameters of functions that provide regression metrics

# **Arguments**

actual The ground truth numeric vector.

predicted The predicted numeric vector, where each element in the vector is a prediction

for the corresponding element in actual.

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percent\_bias

Percent Bias

# **Description**

percent\_bias computes the average amount that actual is greater than predicted as a percentage of actual.

#### Usage

```
percent_bias(actual, predicted)
```

# **Arguments**

actual

The ground truth numeric vector.

predicted

The predicted numeric vector, where each element in the vector is a prediction

for the corresponding element in actual.

#### **Details**

If a model is unbiased percent\_bias(actual, predicted) should be close to zero. Percent Bias is calculated by taking the average of (actual - predicted) / actual.

percent\_bias will give -Inf, Inf, or NaN, if any elements of actual are 0.

# See Also

bias

#### **Examples**

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6)
predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2)
percent_bias(actual, predicted)
```

rae

Relative Absolute Error

#### **Description**

rae computes the relative absolute error between two numeric vectors.

```
rae(actual, predicted)
```

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#### **Arguments**

actual The ground truth numeric vector.

predicted The predicted numeric vector, where each element in the vector is a prediction

for the corresponding element in actual.

#### **Details**

rae divides sum(ae(actual, predicted)) by sum(ae(actual, mean(actual))), meaning that it provides the absolute error of the predictions relative to a naive model that predicted the mean for every data point.

#### See Also

```
rse rrse
```

# Examples

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6)
predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2)
rrse(actual, predicted)
```

rmse

Root Mean Squared Error

#### **Description**

rmse computes the root mean squared error between two numeric vectors

#### Usage

```
rmse(actual, predicted)
```

# **Arguments**

actual The ground truth numeric vector.

predicted The predicted numeric vector, where each element in the vector is a prediction

for the corresponding element in actual.

#### See Also

mse

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6)
predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2)
rmse(actual, predicted)
```

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rmsle

Root Mean Squared Log Error

#### **Description**

rmsle computes the root mean squared log error between two numeric vectors.

#### Usage

```
rmsle(actual, predicted)
```

#### **Arguments**

actual The ground truth non-negative vector

predicted The predicted non-negative vector, where each element in the vector is a predic-

tion for the corresponding element in actual.

#### **Details**

rmsle adds one to both actual and predicted before taking the natural logarithm to avoid taking the natural log of zero. As a result, the function can be used if actual or predicted have zero-valued elements. But this function is not appropriate if either are negative valued.

#### See Also

```
msle sle
```

# **Examples**

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6)
predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2)
rmsle(actual, predicted)
```

rrse

Root Relative Squared Error

# Description

rrse computes the root relative squared error between two numeric vectors.

```
rrse(actual, predicted)
```

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# **Arguments**

actual The ground truth numeric vector.

predicted The predicted numeric vector, where each element in the vector is a prediction

for the corresponding element in actual.

#### **Details**

rrse takes the square root of sse(actual, predicted) divided by sse(actual, mean(actual)), meaning that it provides the squared error of the predictions relative to a naive model that predicted the mean for every data point.

#### See Also

rse rae

# **Examples**

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6) predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2) rrse(actual, predicted)
```

rse

Relative Squared Error

# Description

rse computes the relative squared error between two numeric vectors.

#### Usage

```
rse(actual, predicted)
```

# **Arguments**

actual The ground truth numeric vector.

predicted The predicted numeric vector, where each element in the vector is a prediction

for the corresponding element in actual.

#### **Details**

rse divides sse(actual, predicted) by sse(actual, mean(actual)), meaning that it provides the squared error of the predictions relative to a naive model that predicted the mean for every data point.

#### See Also

rrse rae

# **Examples**

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6)
predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2)
rse(actual, predicted)
```

 ${\tt ScoreQuadraticWeightedKappa}$ 

Quadratic Weighted Kappa

#### **Description**

 ${\tt ScoreQuadraticWeightedKappa\ computes\ the\ quadratic\ weighted\ kappa\ between\ two\ vectors\ of\ integers}$ 

#### Usage

```
ScoreQuadraticWeightedKappa(rater.a, rater.b, min.rating = min(c(rater.a, rater.b)), max.rating = max(c(rater.a, rater.b)))
```

#### **Arguments**

rater.a	An integer vector of the first rater's ratings.
rater.b	An integer vector of the second rater's ratings.
min.rating	The minimum possible rating.
max.rating	The maximum possible rating.

#### See Also

MeanQuadraticWeightedKappa

```
rater.a <- c(1, 4, 5, 5, 2, 1)
rater.b <- c(2, 2, 4, 5, 3, 3)
ScoreQuadraticWeightedKappa(rater.a, rater.b, 1, 5)</pre>
```

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se

Squared Error

# Description

se computes the elementwise squared difference between two numeric vectors.

#### Usage

```
se(actual, predicted)
```

#### **Arguments**

actual The ground truth numeric vector.

predicted The predicted numeric vector, where each element in the vector is a prediction

for the corresponding element in actual.

#### See Also

mse rmse

#### **Examples**

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6) predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2) se(actual, predicted)
```

sle

Squared Log Error

#### Description

sle computes the elementwise squares of the differences in the logs of two numeric vectors.

# Usage

```
sle(actual, predicted)
```

# **Arguments**

actual The ground truth non-negative vector

predicted The predicted non-negative vector, where each element in the vector is a predic-

tion for the corresponding element in actual.

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#### **Details**

sle adds one to both actual and predicted before taking the natural logarithm of each to avoid taking the natural log of zero. As a result, the function can be used if actual or predicted have zero-valued elements. But this function is not appropriate if either are negative valued.

#### See Also

```
msle rmsle
```

#### **Examples**

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6)
predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2)
sle(actual, predicted)
```

smape

Symmetric Mean Absolute Percentage Error

#### **Description**

smape computes the symmetric mean absolute percentage error between two numeric vectors.

#### Usage

```
smape(actual, predicted)
```

# **Arguments**

actual The ground truth numeric vector.

predicted The predicted numeric vector, where each element in the vector is a prediction

for the corresponding element in actual.

#### **Details**

smape is defined as two times the average of abs(actual - predicted) / (abs(actual) + abs(predicted)). Therefore, at the elementwise level, it will provide NaN only if actual and predicted are both zero. It has an upper bound of 2, when either actual or predicted are zero or when actual and predicted are opposite signs.

```
smape is symmetric in the sense that smape(x, y) = smape(y, x).
```

#### See Also

```
mape mase
```

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6)
predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2)
smape(actual, predicted)
```

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sse

Sum of Squared Errors

# Description

sse computes the sum of the squared differences between two numeric vectors.

# Usage

```
sse(actual, predicted)
```

# Arguments

actual The ground truth numeric vector.

predicted The predicted numeric vector, where each element in the vector is a prediction

for the corresponding element in actual.

# See Also

mse

```
actual <- c(1.1, 1.9, 3.0, 4.4, 5.0, 5.6)
predicted <- c(0.9, 1.8, 2.5, 4.5, 5.0, 6.2)
sse(actual, predicted)
```

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