# CIND123 Summer 2018 - Assignment #2

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Use RStudio for this assignment. Edit the file assignment-2.Rmd and insert your R code where wherever you see the string "INSERT YOUR ANSWER HERE"

When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document.

When your are done with your answers and before submitting, save the file with the following naming convention: your Lastname\_firstname

Submit **both** the rmd and the pdf output(or word or html) files, failing to submit **both** will be subject to mark deduction.

This assignment may make use of data provided by the ISWR package.

#library(ISwR)

#### Sample Question and Solution

Use seq() to create the vector (1, 2, 3, ..., 10).

seq(1,10)

## [1] 1 2 3 4 5 6 7 8 9 10

Consider the probability distribution associated with rolling 3 fair dice. We can label the faces of a single die using the numbers from 1 to 6. We can therefore label the simple events in this distribution by triples of numbers from 1 to 6. Let d1, d2, and d3 represent the labels on each of the dice.

a) Set d1 to the sequence  $(1,2,\ldots,6)$  repeated 36 times.

```
d1<-rep(c(1:6),times=36)
```

b) Set d2 to the sequence consisting of 6 repetitions of the sequence in which each of the numbers  $(1,2,\ldots,6)$  is repeated 6 times.

```
d2<-rep(c(1:6),each=6)
```

c) Set d3 to the sequence in which each of the numbers  $(1,2,\ldots,6)$  is repeated 36 times.

```
d3<-rep(c(1:6),each=36)
```

d) Create a new data frame three.dice from d1, d2, and d3. Write a script to confirm that there are  $6 \times 6 \times 6 = 216$  rows and each row contains a unique combination of dice labels.

```
three.dice<-data.frame(d1,d2,d3)
```

e) Since the dice are fair and independent, each simple event has the same probability, namely  $\frac{1}{216}$ . Add the column P to the data frame with this value.

#### cbind(three.dice,p=1/216)

```
##
       d1 d2 d3
            1
               1 0.00462963
## 1
        1
               1 0.00462963
        2
            1
##
   3
        3
               1 0.00462963
            1
##
        4
            1
               1 0.00462963
## 5
        5
            1
               1 0.00462963
##
  6
        6
            1
               1 0.00462963
            2
##
        1
               1 0.00462963
            2
##
   8
        2
               1 0.00462963
##
        3
            2
               1 0.00462963
##
   10
        4
            2
               1 0.00462963
        5
            2
##
               1 0.00462963
        6
            2
##
   12
               1 0.00462963
  13
        1
            3
               1 0.00462963
##
   14
        2
            3
               1 0.00462963
##
   15
        3
            3
               1 0.00462963
##
   16
        4
            3
               1 0.00462963
        5
            3
               1 0.00462963
   17
##
   18
        6
            3
               1 0.00462963
               1 0.00462963
##
   19
        1
##
   20
        2
               1 0.00462963
##
  21
        3
            4
               1 0.00462963
## 22
            4
        4
               1 0.00462963
##
        5
            4
               1 0.00462963
   23
##
   24
        6
            4
               1 0.00462963
##
   25
        1
            5
               1 0.00462963
##
   26
        2
            5
               1 0.00462963
##
   27
        3
            5
               1 0.00462963
           5
## 28
        4
               1 0.00462963
```

```
## 29
        5 5
              1 0.00462963
##
   30
        6
           5
               1 0.00462963
##
   31
            6
               1 0.00462963
##
  32
            6
        2
               1 0.00462963
##
   33
        3
            6
               1 0.00462963
##
   34
        4
            6
               1 0.00462963
##
   35
        5
            6
               1 0.00462963
               1 0.00462963
##
   36
        6
            6
##
   37
        1
            1
               2 0.00462963
   38
        2
##
            1
               2 0.00462963
##
   39
        3
           1
               2 0.00462963
##
   40
               2 0.00462963
        4
            1
        5
##
   41
            1
               2 0.00462963
               2 0.00462963
## 42
            1
        6
## 43
            2
               2 0.00462963
        1
            2
## 44
        2
               2 0.00462963
##
        3
            2
               2 0.00462963
   45
##
   46
               2 0.00462963
##
   47
        5
            2
               2 0.00462963
##
   48
        6
            2
               2 0.00462963
##
   49
        1
            3
               2 0.00462963
##
  50
            3
               2 0.00462963
            3
## 51
        3
               2 0.00462963
##
   52
        4
            3
               2 0.00462963
        5
            3
##
  53
               2 0.00462963
##
   54
        6
            3
               2 0.00462963
##
   55
            4
               2 0.00462963
        1
##
   56
        2
            4
               2 0.00462963
            4
##
   57
        3
               2 0.00462963
               2 0.00462963
##
  58
        4
            4
               2 0.00462963
## 59
        5
            4
##
   60
        6
            4
               2 0.00462963
            5
##
   61
        1
               2 0.00462963
##
   62
        2
            5
               2 0.00462963
##
   63
        3
            5
               2 0.00462963
##
   64
        4
           5
               2 0.00462963
##
   65
        5
            5
               2 0.00462963
##
  66
        6
            5
               2 0.00462963
##
   67
        1
            6
               2 0.00462963
   68
            6
        2
               2 0.00462963
##
##
   69
            6
               2 0.00462963
##
   70
        4
            6
               2 0.00462963
##
        5
            6
               2 0.00462963
   71
##
        6
            6
   72
               2 0.00462963
##
   73
            1
               3 0.00462963
        1
  74
        2
               3 0.00462963
##
            1
               3 0.00462963
        3
            1
##
   75
##
   76
            1
               3 0.00462963
##
   77
        5
            1
               3 0.00462963
##
   78
        6
            1
               3 0.00462963
##
  79
            2
               3 0.00462963
        1
        2
           2
## 80
               3 0.00462963
## 81
        3
           2
               3 0.00462963
        4 2
## 82
               3 0.00462963
```

```
## 83
        5
           2
             3 0.00462963
              3 0.00462963
##
  84
        6
           2
##
   85
           3
               3 0.00462963
           3
##
   86
        2
              3 0.00462963
##
   87
        3
           3
               3 0.00462963
  88
        4
           3
               3 0.00462963
##
##
   89
        5
           3
               3 0.00462963
           3
               3 0.00462963
## 90
        6
##
  91
        1
           4
               3 0.00462963
        2
           4
               3 0.00462963
##
  92
##
   93
        3
               3 0.00462963
##
   94
        4
           4
               3 0.00462963
        5
           4
##
   95
               3 0.00462963
               3 0.00462963
        6
           4
## 96
## 97
           5
               3 0.00462963
        1
## 98
        2
           5
               3 0.00462963
##
        3
           5
               3 0.00462963
  99
##
   100
        4
           5
               3 0.00462963
  101
##
        5
           5
               3 0.00462963
        6
##
  102
           5
               3 0.00462963
##
  103
        1
           6
               3 0.00462963
## 104
        2
           6
               3 0.00462963
        3
           6
## 105
              3 0.00462963
## 106
        4
           6
               3 0.00462963
              3 0.00462963
        5
           6
## 107
  108
        6
           6
               3 0.00462963
##
  109
               4 0.00462963
        1
           1
  110
        2
           1
               4 0.00462963
##
        3
## 111
           1
               4 0.00462963
## 112
        4
           1
               4 0.00462963
               4 0.00462963
## 113
        5
           1
## 114
        6
           1
               4 0.00462963
           2
  115
        1
               4 0.00462963
## 116
        2
           2
               4 0.00462963
           2
## 117
        3
               4 0.00462963
## 118
        4
           2
               4 0.00462963
## 119
        5
           2
               4 0.00462963
## 120
        6
           2
               4 0.00462963
           3
## 121
        1
               4 0.00462963
        2
           3
              4 0.00462963
## 122
## 123
        3
           3
               4 0.00462963
## 124
        4
           3
               4 0.00462963
##
  125
        5
           3
               4 0.00462963
## 126
        6
           3
               4 0.00462963
## 127
        1
           4
               4 0.00462963
## 128
        2
           4
               4 0.00462963
        3
           4
               4 0.00462963
## 129
  130
        4
           4
##
               4 0.00462963
##
  131
        5
           4
               4 0.00462963
        6
           4
##
   132
               4 0.00462963
               4 0.00462963
##
  133
        1
           5
        2
           5
## 134
               4 0.00462963
## 135
        3
          5
              4 0.00462963
       4 5 4 0.00462963
## 136
```

```
## 137
        5 5
             4 0.00462963
## 138
        6
           5
              4 0.00462963
               4 0.00462963
  139
        1
           6
  140
        2
           6
##
               4 0.00462963
##
   141
        3
           6
               4 0.00462963
## 142
        4
           6
               4 0.00462963
## 143
        5
           6
               4 0.00462963
               4 0.00462963
        6
           6
## 144
## 145
        1
           1
               5 0.00462963
        2
               5 0.00462963
##
  146
           1
   147
        3
           1
               5 0.00462963
   148
        4
           1
               5 0.00462963
##
        5
##
   149
           1
               5 0.00462963
               5 0.00462963
  150
        6
           1
##
## 151
        1
           2
               5 0.00462963
        2
           2
##
  152
               5 0.00462963
##
  153
        3
           2
               5 0.00462963
   154
        4
           2
               5 0.00462963
  155
        5
           2
              5 0.00462963
##
##
   156
        6
           2
               5 0.00462963
##
  157
        1
           3
               5 0.00462963
## 158
        2
           3
               5 0.00462963
        3
           3
              5 0.00462963
## 159
##
  160
        4
           3
               5 0.00462963
              5 0.00462963
        5
           3
## 161
  162
        6
           3
               5 0.00462963
##
  163
        1
           4
               5 0.00462963
   164
        2
           4
               5 0.00462963
##
        3
           4
               5 0.00462963
##
  165
        4
           4
               5 0.00462963
## 166
               5 0.00462963
## 167
        5
           4
##
   168
        6
           4
               5 0.00462963
           5
##
   169
        1
               5 0.00462963
  170
        2
           5
               5 0.00462963
##
           5
##
   171
        3
               5 0.00462963
## 172
        4
           5
              5 0.00462963
## 173
        5
           5
               5 0.00462963
## 174
        6
           5
              5 0.00462963
##
   175
        1
           6
               5 0.00462963
        2
           6
## 176
               5 0.00462963
  177
        3
           6
               5 0.00462963
## 178
        4
           6
               5 0.00462963
        5
           6
               5 0.00462963
##
  179
  180
        6
           6
               5 0.00462963
##
## 181
           1
               6 0.00462963
        1
        2
               6 0.00462963
## 182
           1
               6 0.00462963
        3
           1
##
  183
   184
        4
##
           1
               6 0.00462963
##
   185
        5
           1
               6 0.00462963
        6
##
   186
           1
               6 0.00462963
               6 0.00462963
##
   187
        1
           2
        2
           2
## 188
               6 0.00462963
## 189
        3
           2
              6 0.00462963
        4 2 6 0.00462963
## 190
```

```
## 191
        5
           2
               6 0.00462963
  192
        6
           2
               6 0.00462963
               6 0.00462963
  193
        1
           3
  194
        2
           3
##
               6 0.00462963
##
   195
        3
           3
               6 0.00462963
  196
        4
           3
##
               6 0.00462963
               6 0.00462963
  197
        5
           3
## 198
        6
           3
               6 0.00462963
##
  199
        1
           4
               6 0.00462963
        2
           4
##
  200
               6 0.00462963
##
  201
        3
           4
               6 0.00462963
   202
        4
##
           4
               6 0.00462963
        5
##
   203
           4
               6 0.00462963
   204
        6
               6 0.00462963
##
           4
  205
           5
##
        1
               6 0.00462963
##
   206
        2
           5
               6 0.00462963
  207
        3
           5
               6 0.00462963
##
   208
           5
               6 0.00462963
  209
        5
##
           5
               6 0.00462963
##
  210
        6
           5
               6 0.00462963
## 211
        1
           6
               6 0.00462963
## 212
        2
           6
               6 0.00462963
## 213
        3
           6
               6 0.00462963
## 214
        4
           6
               6 0.00462963
## 215
        5
           6
               6 0.00462963
## 216
        6
           6
               6 0.00462963
```

f) Add a new column sum equal to the sum of the dice labels. Add another new column mean equal to the average of the dice labels.

 $\label{line:cond} three.dice \ensuremath{$^{\circ}$} d1 + three.dice \ensuremath{$^{\circ}$} d2 + three.dice \ensuremath{$^{\circ}$} d3) \ensuremath{,mean=(three.dice \ensuremath{$^{\circ}$} d1 + three.dice \ensuremath{$^{\circ}$} d2 + three.dice \ensuremath{$^{\circ}$} d3) \ensuremath{,mean=(three.dice \ensuremath{$^{\circ}$} d1 + three.dice \ensuremath{$^{\circ}$} d2 + three.dice \ensuremath{$^{\circ}$} d3) \ensuremath{,mean=(three.dice \ensuremath{$^{\circ}$} d1 + three.dice \ensuremath{$^{\circ}$} d2 + three.dice \ensuremath{$^{\circ}$} d3) \ensuremath{,mean=(three.dice \ensuremath{$^{\circ}$} d1 + three.dice \ensuremath{$^{\circ}$} d2 + three.dice \ensuremath{$^{\circ}$} d3) \ensuremath{,mean=(three.dice \ensuremath{$^{\circ}$} d1 + three.dice \ensuremath{$^{\circ}$} d2 + three.dice \ensuremath{$^{\circ}$} d3) \ensuremath{,mean=(three.dice \ensuremath{$^{\circ}$} d1 + three.dice \ensuremath{$^{\circ}$} d2 + three.dice \ensuremath{$^{\circ}$} d3) \ensuremath{,mean=(three.dice \ensuremath{$^{\circ}$} d1 + three.dice \ensuremath{$^{\circ}$} d2 + three.dice \ensuremath{$^{\circ}$} d3) \ensuremath{,mean=(three.dice \ensuremath{$^{\circ}$} d1 + three.dice \ensuremath{$^{\circ}$} d2 + three.dice \ensuremath{$^{\circ}$} d3) \ensuremath{,mean=(three.dice \ensuremath{$^{\circ}$ 

```
##
       d1 d2 d3
                           p sum
                                      mean
## 1
           1
               1 0.00462963
                               3 1.000000
        1
##
        2
           1
               1 0.00462963
                               4 1.333333
##
  3
        3
           1
               1 0.00462963
                               5 1.666667
##
           1
               1 0.00462963
                               6 2.000000
##
   5
        5
           1
               1 0.00462963
                               7 2.333333
##
   6
        6
           1
               1 0.00462963
                               8 2.666667
  7
           2
##
        1
               1 0.00462963
                               4 1.333333
               1 0.00462963
## 8
           2
        2
                               5 1.666667
## 9
        3
           2
               1 0.00462963
                               6 2.000000
## 10
        4
           2
               1 0.00462963
                               7 2.333333
##
  11
        5
           2
               1 0.00462963
                               8 2.666667
##
  12
        6
           2
               1 0.00462963
                               9 3.000000
##
   13
        1
           3
               1 0.00462963
                               5 1.666667
               1 0.00462963
##
  14
        2
           3
                               6 2.000000
##
  15
        3
           3
               1 0.00462963
                               7 2.333333
##
  16
        4
           3
               1 0.00462963
                               8 2.666667
##
   17
        5
           3
               1 0.00462963
                               9
                                 3.000000
        6
           3
##
   18
               1 0.00462963
                              10 3.333333
   19
               1 0.00462963
                               6 2.000000
        1
        2
##
   20
           4
               1 0.00462963
                               7 2.333333
## 21
           4
               1 0.00462963
                               8 2.666667
```

```
## 22
               1 0.00462963
                               9 3.000000
##
        5
           4
  23
               1 0.00462963
                             10 3.333333
                              11 3.666667
##
   24
               1 0.00462963
##
   25
           5
                               7 2.333333
        1
               1 0.00462963
##
   26
        2
           5
               1 0.00462963
                               8 2.666667
  27
           5
##
        3
               1 0.00462963
                               9 3.000000
##
  28
           5
               1 0.00462963
                              10 3.333333
##
  29
        5
           5
               1 0.00462963
                              11 3.666667
##
   30
        6
           5
               1 0.00462963
                              12 4.000000
##
   31
        1
           6
               1 0.00462963
                               8 2.666667
##
   32
        2
           6
               1 0.00462963
                               9 3.000000
   33
##
        3
           6
               1 0.00462963
                              10 3.333333
##
   34
        4
           6
               1 0.00462963
                              11 3.666667
##
   35
        5
           6
               1 0.00462963
                              12 4.000000
##
   36
           6
                              13 4.333333
        6
               1 0.00462963
##
   37
        1
           1
               2 0.00462963
                               4 1.333333
               2 0.00462963
##
   38
        2
           1
                               5 1.666667
##
   39
               2 0.00462963
                                6 2.000000
                               7 2.333333
##
   40
        4
               2 0.00462963
           1
##
   41
        5
               2 0.00462963
                               8 2.666667
               2 0.00462963
##
  42
        6
           1
                               9 3.000000
##
  43
               2 0.00462963
                               5 1.666667
        1
           2
               2 0.00462963
##
  44
        2
                                6 2.000000
           2
                               7 2.333333
##
   45
        3
               2 0.00462963
##
   46
        4
           2
               2 0.00462963
                                8 2.666667
##
   47
        5
           2
               2 0.00462963
                               9 3.000000
        6
           2
               2 0.00462963
##
   48
                              10 3.333333
##
   49
        1
           3
               2 0.00462963
                                6 2.000000
        2
##
   50
           3
                               7 2.333333
               2 0.00462963
##
  51
        3
           3
               2 0.00462963
                               8 2.666667
## 52
        4
           3
               2 0.00462963
                               9 3.000000
##
   53
        5
           3
               2 0.00462963
                              10 3.333333
##
   54
           3
               2 0.00462963
                              11 3.666667
##
   55
           4
               2 0.00462963
                               7 2.333333
        1
##
   56
        2
           4
               2 0.00462963
                               8 2.666667
##
           4
  57
        3
               2 0.00462963
                               9 3.000000
##
  58
               2 0.00462963
                              10 3.333333
##
  59
        5
           4
               2 0.00462963
                              11 3.666667
        6
           4
               2 0.00462963
                              12 4.000000
##
   60
           5
                               8 2.666667
##
   61
        1
               2 0.00462963
                               9 3.000000
##
   62
        2
           5
               2 0.00462963
        3
           5
               2 0.00462963
                              10 3.333333
##
   63
##
   64
        4
           5
               2 0.00462963
                              11 3.666667
##
   65
        5
           5
               2 0.00462963
                              12 4.000000
##
   66
        6
           5
               2 0.00462963
                              13 4.333333
  67
           6
               2 0.00462963
##
        1
                               9 3.000000
##
   68
        2
           6
               2 0.00462963
                              10 3.333333
##
   69
        3
           6
               2 0.00462963
                              11 3.666667
##
   70
        4
           6
               2 0.00462963
                              12 4.000000
##
   71
        5
           6
               2 0.00462963
                              13 4.333333
##
           6
  72
        6
               2 0.00462963
                              14 4.666667
## 73
        1
           1
               3 0.00462963
                               5 1.666667
## 74
        2
           1
               3 0.00462963
                                6 2.000000
## 75
           1
              3 0.00462963
                               7 2.333333
```

```
## 76
               3 0.00462963
                               8 2.666667
##
        5
                               9 3.000000
  77
           1
              3 0.00462963
##
   78
               3 0.00462963
                             10 3.333333
##
  79
           2
               3 0.00462963
                               6 2.000000
        1
##
   80
           2
               3 0.00462963
                               7 2.333333
##
           2
  81
        3
               3 0.00462963
                               8 2.666667
           2
##
  82
               3 0.00462963
                               9 3.000000
## 83
        5
           2
               3 0.00462963
                              10 3.333333
##
   84
        6
           2
               3 0.00462963
                              11 3.666667
##
   85
        1
           3
               3 0.00462963
                               7 2.333333
##
   86
        2
           3
               3 0.00462963
                               8 2.666667
           3
##
   87
        3
               3 0.00462963
                               9 3.000000
##
   88
        4
           3
               3 0.00462963
                              10 3.333333
           3
                              11 3.666667
##
  89
        5
               3 0.00462963
## 90
           3
               3 0.00462963
                              12 4.000000
        6
##
  91
        1
           4
               3 0.00462963
                               8 2.666667
        2
           4
##
  92
               3 0.00462963
                               9 3.000000
##
   93
               3 0.00462963
                              10 3.333333
##
  94
        4
           4
               3 0.00462963
                              11 3.666667
##
   95
        5
           4
               3 0.00462963
                              12 4.000000
##
  96
        6
           4
               3 0.00462963
                              13 4.333333
  97
           5
               3 0.00462963
                               9 3.000000
##
        1
## 98
        2
           5
               3 0.00462963
                             10 3.333333
        3
           5
               3 0.00462963
##
  99
                              11 3.666667
                              12 4.000000
##
  100
        4
           5
               3 0.00462963
  101
        5
           5
               3 0.00462963
                              13 4.333333
   102
        6
           5
               3 0.00462963
                              14 4.666667
##
##
   103
        1
           6
               3 0.00462963
                              10 3.333333
        2
           6
               3 0.00462963
##
  104
                              11 3.666667
## 105
        3
           6
               3 0.00462963
                              12 4.000000
##
  106
        4
           6
               3 0.00462963
                              13 4.333333
##
  107
        5
           6
               3 0.00462963
                              14 4.666667
##
   108
           6
               3 0.00462963
                              15 5.000000
  109
##
               4 0.00462963
                               6 2.000000
        1
           1
   110
        2
           1
               4 0.00462963
                               7 2.333333
        3
           1
## 111
               4 0.00462963
                               8 2.666667
## 112
        4
               4 0.00462963
                               9 3.000000
## 113
        5
           1
               4 0.00462963
                              10 3.333333
        6
           1
               4 0.00462963
                              11 3.666667
## 114
           2
## 115
        1
               4 0.00462963
                               7 2.333333
        2
  116
               4 0.00462963
                               8 2.666667
## 117
        3
           2
               4 0.00462963
                               9 3.000000
##
  118
        4
           2
               4 0.00462963
                             10 3.333333
        5
##
  119
           2
               4 0.00462963
                              11 3.666667
        6
           2
## 120
               4 0.00462963
                              12 4.000000
## 121
           3
               4 0.00462963
                               8 2.666667
        1
        2
##
  122
           3
               4 0.00462963
                               9 3.000000
  123
        3
##
           3
               4 0.00462963
                              10 3.333333
##
  124
        4
           3
               4 0.00462963
                              11 3.666667
##
   125
        5
           3
               4 0.00462963
                              12 4.000000
   126
        6
           3
##
               4 0.00462963
                              13 4.333333
## 127
        1
           4
               4 0.00462963
                               9 3.000000
## 128
        2
           4
              4 0.00462963
                             10 3.333333
        3
## 129
           4 4 0.00462963 11 3.666667
```

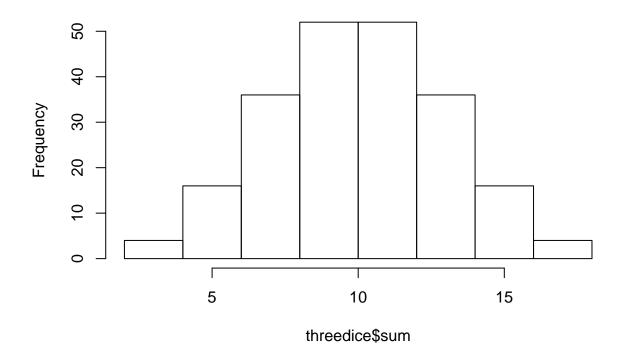
```
## 130
           4
              4 0.00462963
                             12 4.000000
## 131
        5
           4
              4 0.00462963
                             13 4.333333
  132
        6
               4 0.00462963
                              14 4.666667
  133
           5
               4 0.00462963
                              10 3.333333
##
        1
##
   134
        2
           5
               4 0.00462963
                              11 3.666667
        3
           5
## 135
               4 0.00462963
                              12 4.000000
           5
               4 0.00462963
## 136
                             13 4.333333
## 137
        5
           5
               4 0.00462963
                              14 4.666667
##
  138
        6
           5
               4 0.00462963
                              15 5.000000
##
  139
        1
           6
               4 0.00462963
                              11 3.666667
   140
        2
           6
               4 0.00462963
                              12 4.000000
        3
               4 0.00462963
##
   141
           6
                              13 4.333333
##
   142
        4
           6
               4 0.00462963
                              14 4.666667
        5
               4 0.00462963
##
  143
           6
                              15 5.000000
## 144
        6
           6
               4 0.00462963
                              16 5.333333
##
  145
        1
           1
               5 0.00462963
                               7 2.333333
        2
##
   146
           1
               5 0.00462963
                               8 2.666667
   147
               5 0.00462963
                               9 3.000000
               5 0.00462963
                             10 3.333333
##
  148
        4
           1
##
   149
        5
               5 0.00462963
                              11 3.666667
##
  150
        6
           1
               5 0.00462963
                              12 4.000000
               5 0.00462963
                               8 2.666667
  151
        2
           2
               5 0.00462963
                               9 3.000000
## 152
        3
           2
               5 0.00462963
##
  153
                             10 3.333333
           2
## 154
        4
               5 0.00462963
                              11 3.666667
  155
        5
           2
               5 0.00462963
                              12 4.000000
   156
        6
           2
               5 0.00462963
                              13 4.333333
##
##
   157
        1
           3
               5 0.00462963
                               9 3.000000
        2
   158
           3
               5 0.00462963
##
                              10 3.333333
## 159
        3
           3
               5 0.00462963
                              11 3.666667
## 160
        4
           3
               5 0.00462963
                              12 4.000000
##
   161
        5
           3
               5 0.00462963
                              13 4.333333
##
   162
        6
           3
               5 0.00462963
                              14 4.666667
               5 0.00462963
##
   163
                              10 3.333333
        1
   164
           4
               5 0.00462963
                              11 3.666667
##
        3
           4
               5 0.00462963
##
   165
                              12 4.000000
##
  166
        4
               5 0.00462963
                              13 4.333333
## 167
        5
           4
               5 0.00462963
                              14 4.666667
        6
           4
               5 0.00462963
                              15 5.000000
##
   168
           5
               5 0.00462963
##
  169
        1
                              11 3.666667
        2
  170
               5 0.00462963
                              12 4.000000
  171
        3
           5
               5 0.00462963
                             13 4.333333
##
##
  172
           5
               5 0.00462963
                              14 4.666667
##
        5
           5
  173
               5 0.00462963
                              15 5.000000
        6
           5
               5 0.00462963
## 174
                              16 5.333333
## 175
           6
               5 0.00462963
                              12 4.000000
        1
        2
##
  176
           6
               5 0.00462963
                              13 4.333333
        3
##
  177
           6
               5 0.00462963
                              14 4.666667
  178
           6
               5 0.00462963
                              15 5.000000
##
   179
        5
           6
               5 0.00462963
                              16 5.333333
##
   180
        6
           6
               5 0.00462963
                              17 5.666667
## 181
        1
           1
               6 0.00462963
                               8 2.666667
## 182
        2
           1
               6 0.00462963
                               9 3.000000
        3 1 6 0.00462963 10 3.333333
## 183
```

```
## 184
        4 1 6 0.00462963 11 3.666667
## 185
        5
           1
             6 0.00462963 12 4.000000
              6 0.00462963
## 186
                            13 4.333333
  187
##
           2
              6 0.00462963
                              9 3.000000
        1
##
  188
              6 0.00462963
                            10 3.333333
## 189
        3
           2
             6 0.00462963
                            11 3.666667
## 190
              6 0.00462963
                            12 4.000000
           2
## 191
        5
              6 0.00462963
                            13 4.333333
## 192
        6
           2
              6 0.00462963
                             14 4.666667
## 193
           3
        1
              6 0.00462963
                            10 3.333333
  194
        2
              6 0.00462963
                            11 3.666667
  195
        3
           3
              6 0.00462963
                            12 4.000000
##
           3
##
   196
        4
              6 0.00462963
                            13 4.333333
        5
           3
              6 0.00462963
##
  197
                             14 4.666667
## 198
        6
           3
              6 0.00462963
                            15 5.000000
## 199
        1
           4
              6 0.00462963
                             11 3.666667
## 200
        2
           4
              6 0.00462963
                            12 4.000000
##
  201
              6 0.00462963
                            13 4.333333
## 202
        4
              6 0.00462963
                            14 4.666667
## 203
        5
              6 0.00462963
                             15 5.000000
              6 0.00462963
##
  204
        6
                             16 5.333333
## 205
        1
              6 0.00462963
                             12 4.000000
## 206
        2
           5
              6 0.00462963
                            13 4.333333
## 207
        3
           5
              6 0.00462963
                            14 4.666667
              6 0.00462963
        4
           5
## 208
                            15 5.000000
                            16 5.333333
## 209
        5
           5
              6 0.00462963
## 210
        6
           5
              6 0.00462963
                            17 5.666667
           6
              6 0.00462963
                             13 4.333333
## 211
        1
           6
## 212
             6 0.00462963
                            14 4.666667
        3
## 213
           6
              6 0.00462963
                            15 5.000000
## 214
        4
           6
              6 0.00462963
                             16 5.333333
## 215
        5 6
             6 0.00462963
                             17 5.666667
          6 6 0.00462963
## 216
                            18 6.000000
```

g) Plot a probability histogram of three.dice\$sum.

hist(threedice\$sum)

# Histogram of threedice\$sum



h) Compute the probability that the sum of the dice is greater than 12 and less than 18.

HINT: Use subset() to select the events and sum P.

```
h<-subset(threedice,sum>12&sum<18)
h2<-length(h\$sum)
print(h2/216)
```

#### ## [1] 0.2546296

i) Compute the probability that the sum is even.

```
i<-subset(threedice,sum%2==0)
i2<-length(i$sum)
print(i2/216)</pre>
```

#### ## [1] 0.5

j) Compute the probability that the mean is exactly 4.

```
j<-subset(threedice,mean==4)
j2<-length(j$mean)
print(j2/216)</pre>
```

## [1] 0.1157407

a) You have two groups of distinctly different items, 10 in the first group and 8 in the second. If you select one item from each group, how many different pairs can you form? q2a<-10\*8 q2a ## [1] 80 b) Evaluate the following permutation  $P_3^5$ factorial(5)/factorial(2) ## [1] 60 c) Evaluate the following combinations  $C_3^5 + C_2^5$ (factorial(5)/(factorial(2)\*factorial(3)))+(factorial(5)/(factorial(3)\*factorial(2))) ## [1] 20 d)In how many ways can you select five people from a group of eight if the order of selection is important? factorial(8)/factorial(3) ## [1] 6720 e)In how many ways can you select two people from a group of 20 if the order of selection is not important? (factorial(20)/(factorial(18)\*factorial(2))) ## [1] 190

a) Use simulation to estimate the mean and variance of a binomial random variable with size = 45 and p = 0.32. One time use 100 samples and the other time use 10000 samples.

```
q3a<-rbinom(100,45,0.32)
mean(q3a)

## [1] 14.41

var(q3a)

## [1] 9.840303

q3b<-rbinom(10000,45,0.32)
mean(q3b)

## [1] 14.393

var(q3b)
```

## [1] 9.98855

b) Calculate the values using the theroy (state the value and the equation in your answer), compare the values you get with the values you got in (a), wirte one sentence sumurizing the comparision. Explain the difference between 100 samples and 10000 samples and which one seems to be more accurate and why?

 $\#For\ the\ 100\ samples$ , the mean was 14.62 and the variance was 8.6218. For the 10000 samples, the mean w

a) If there are twelve customers entering a mall per minute on average, find the probability of having seventeen or more customers entering the mall in a particular minute.

```
ppois(16, lambda=12, lower=FALSE) # upper tail
```

## [1] 0.101291

b) Estimate the mean and variance of a Poisson random variable in the previuos question by simulating 100 and 10,000 Poisson random numbers.

```
q4b1<-rpois(100,12)
mean(q4b1)

## [1] 11.98

var(q4b1)

## [1] 11.75717

q4b2<-rpois(10000,12)
mean(q4b2)

## [1] 12.0096

var(q4b2)</pre>
```

## [1] 12.00711

c) Compare the mean value you got in (b), with the one stated in the question. wirte one sentence summarizing the comparision. Explain the difference between 100 samples and 10000 samples and which one seems to be more accurate and why?

#In the question, the mean value was 12 and the one generated by R produced 11.69 by the 100 samples an

END of Assignment #2.