

#### PyData Cluj-Napoca

27<sup>th</sup> of July, 2024

# PREDICTING ROMANIAN STOCK MOVEMENT TRENDS: A COMPLEX NETWORK APPROACH COMBINED WITH MACHINE LEARNING

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### About me



Orsolya Holgyes (Orsi)



Bachelor's degree: Business Computer Science @ FSEGA

Master's degree: Data Science for Industry & Society @ CS, UBB

Intern in Financial Audit @ EY Jan 2021 – Jun 2022



Intern » Junior » Mid Data Engineer @ Endava finance (stock market) & insurance projects
Jun 2022 – May 2024

Mid Data Engineer @ Vertiv
Device data for Condition Based Maintenance
Jun 2024 - Present



Until now: Learning + Friends & Family

From now on: Friends & Family + Adulthood + Traveling + Cycling & Hiking

### From ideas to a dissertation thesis



A desire to have a single topic for all my university projects (including Social Network Analysis), forming in the end my dissertation thesis regarding stock markets.



How to define a stock network?

<u>nodes</u>: different assets on the stock exchanges

(stocks, bonds, etc.)

<u>links</u>: linked if these appear in similar portfolios? if purchased by similar users? If in same index or industry?

available data is only about stock prices and details of the issuers



Research topic #1.1: How to model the Romanian stock market as a network?



Research topic #1.2: analysis of the structure and behavior of the stock network

Source: Janosov (2021)

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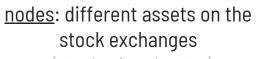


Include somehow machine learning; if potential investors would have a fair assumption on the future market outlook, the invested capital could remain in the Romanian industry.



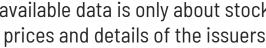


How to define a stock network?



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Research topic #1.2: analysis of the structure and behavior of the stock network

Besides the diverse machine learning and deep learning methods applied on the prices or other raw data, lately another research direction is to have as input data properties extracted from the stock network » basically, train algorithms which learn based on network interactions pl. Milan Janosov (2021). "Network science predicts who dies next in Game of Thrones".

Research topic #2: predict the next day movement of the stock prices based on features extracted from the stock network

Source: Janosov (2021)

#### OBJECTIVES & ORIGINAL CONTRIBUTIONS

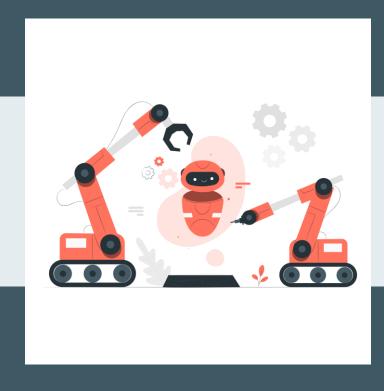
# 1. MODELLING THE STOCK NETWORK



2. ANALYZING THE STOCK NETWORK



# 3. TRAINING A PREDICTION ALGORITHM



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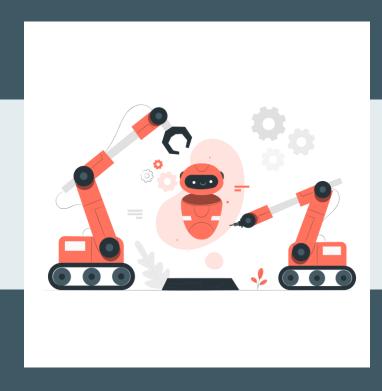
# 1. MODELLING THE STOCK NETWORK



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### How others modelled the stock market

**Step 0**: choose time range (T) and stocks to include

**Step 1**: calculate between each stock-pair the Pearson correlation coefficient

$$c_{ij} = \frac{\sum_{t} [(x_i(t) - \overline{x_i}) * (x_j(t) - \overline{x_j})]}{\sqrt{\sum_{t} (x_i(t) - \overline{x_i})^2} * \sqrt{\sum_{t} (x_j(t) - \overline{x_j})^2}}$$

 $x_i(t)$  = the close price  $(p_{c,i}(t))$  of stock i on day t OR the trading volumes of stock i ron day t OR the most frequently:  $x_i(t)$  = return =  $ln[\frac{p_{c,i}(t)}{p_{c,i}(t-1)}]$ 

 $\overline{X_i}$  = the average of  $X_i$  for the whole analyzed period

**Step 2**: define a threshold value based on that the links of the stock network can be defined:

if the correlation coefficient  $c_{ij}$  between two stocks is greater than the threshold, an undirected link is placed between the two nodes of the stocks

				_	
paper	data	modeling approach	link creation	N	L
[29]	daily U.S. stock data between July 2007-2008	cross-correlation on the logarithmic daily price return; no lag considered; undirected network	threshold of 0.6	465	n/m
[6]	daily U.S. stock data between July 2005-August 2007 and June 2007 - May 2009	cross-correlation on the daily logarithmic price return, close price and trading volume; no lag considered; undirected network	multiple thresholds: 0.7, 0.8, 0.85, 0.9, 0.95	19,807	2,359 at thd = 0.9
[9]	daily Tehran stock data between 26 March 2011 and 8 April 2017	cross-correlation on the daily logarithmic price return; no lag considered; undirected network	threshold of 0.1	142	3,457
[10]	daily stock data from Shanghai and Shenzhen between 2003 and 2007	cross-correlation on the logarithmic daily price return; no lag considered; undirected network	experimented with multiple thresholds	1,080	n/m
[18]	daily Tehran stock data between 2014 and 2017	cross-correlation on the logarithmic daily price return; no lag considered; undirected network	threshold of 0.4 selected with an objective function	246	n/m
П	daily stock indices data from 70 countries between 2017-2019 and 2020-2022	novel methodology open-high-low-close data; undirected network	based on no lag considered;	70	n/m
[3]	S&P500, NASDAQ, DJIA stock data from 2000-2014	price volatility patter cross-correlation; 5-day directed and weighted netwo	lag considered;	47	n/m

Table 3.1: Summary of other researchers' stock network modeling approaches. N refers to the number of nodes and L to the number of edges in the stock network which was modeled in the specific papers.

What value should the threshold take? How can we determine this threshold?

arbitrary value

based on

experiments

# The approach in this thesis



Data: ethically sourced close prices of stocks from the Bucharest Stock Exchange between 2022-2023



Nodes of the stock network: the 328 stocks on the Romanian stock market, from those 18 had constant close prices and are isolated nodes Links of the stock network: based on the cross-correlation of the stocks' returns between 2022-2023



Threshold: for each value between 0,00 and 1,00 a different stock network was modelled. The optimal threshold was chosen based on network-level metrics which reflect the structure of the network

The threshold must be in the interval of [0, 0.20] so that valuable data and insights can be retrieved from the network, based on that algorithms can truly learn the stock interactions.

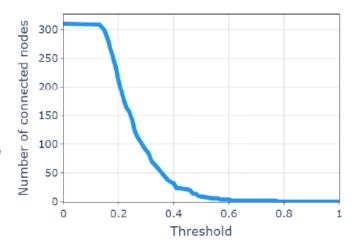
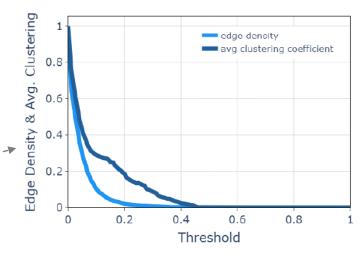


Figure 4.1

Number of non-isolated nodes based on the threshold » as the threshold increases, the number of non-isolated nodes decreases

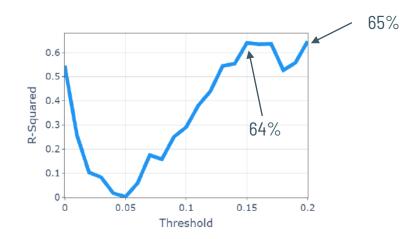


The density and the average clustering coefficient of the network » after the threshold value 0.25, the number of edges are only 1% of all possible edges; the average clustering coefficient is higher than density, therefore the dense relations in the network were expected

# The approach in this thesis

Depending on the extent of the scale-free property: for each network built based on thresholds in the [0, 0.20] interval, a linear regression model was fitted on the degree distribution of each network and the power-law distribution, both on log-log scale» we should choose the threshold with the highest R<sup>2</sup>

$$P(k) = \alpha * k^{-\gamma} \stackrel{\log}{\Longleftrightarrow} log P(k) = log \alpha + (-\gamma) * log k$$



Threshold = 0.20

Number of connected nodes = 211 Number of edges = 1005 Threshold = 0.15

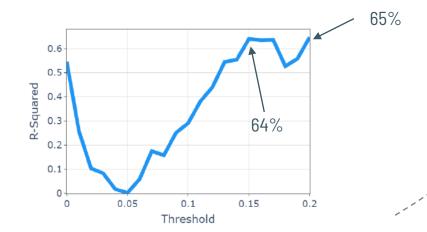
Number of connected nodes = 298 Number of edges = 2089

Source: Pósfai és Barabási (2016)

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#### Threshold = 0.20

Number of connected nodes = 211 Number of edges = 1005

#### Threshold = 0.15

Number of connected nodes = 298 Number of edges = 2089

#### Average the node-level centralities avg degree centrality ava betweenness centrality Centrality 0.8 avg closeness centrality avg eigenvector centrality 0.6 Average 0.4 0.2 0.05 0.1 0.15 0.2 Threshold Centralities are higher for threshold 0.15, especially the closeness centrality which means that information flows are

more efficient in this network.

Source: Pósfai és Barabási (2016)

### The modelled network

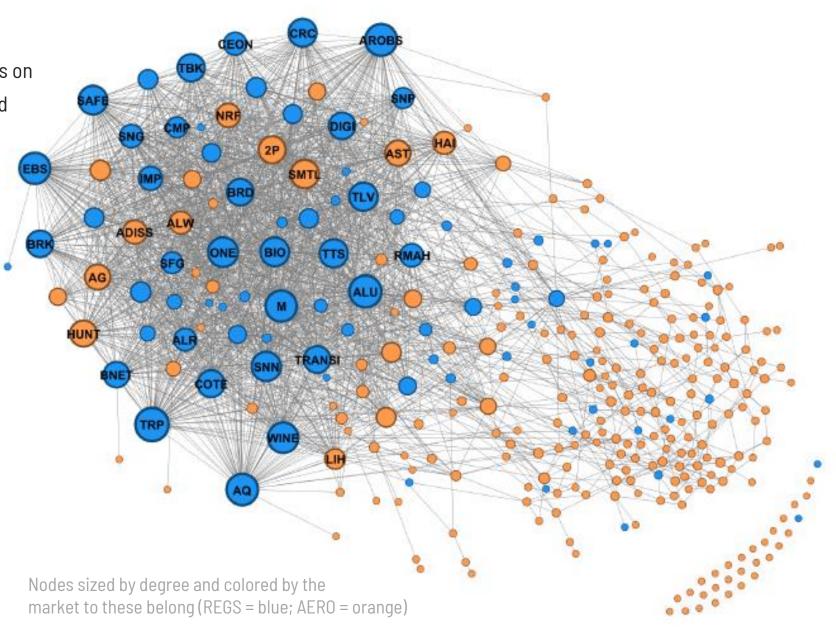
Nodes of the stock network: the 328 stocks on the Romanian stock market, from those 18 had constant close prices and are isolated nodes

Links of the stock network: based on the cross-correlation of the stocks' returns between 2022-2023; if it is higher than 0.15

N = 360

L = 2089

Nr of isolated nodes = 20



#### **OBJECTIVES & ORIGINAL CONTRIBUTIONS**

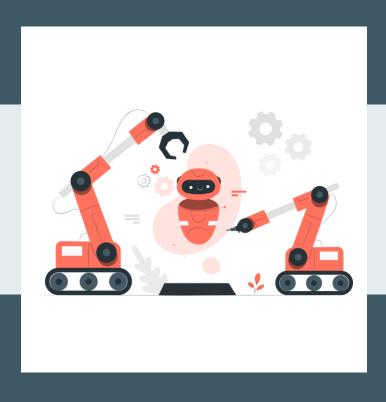
# 1. MODELLING THE STOCK NETWORK

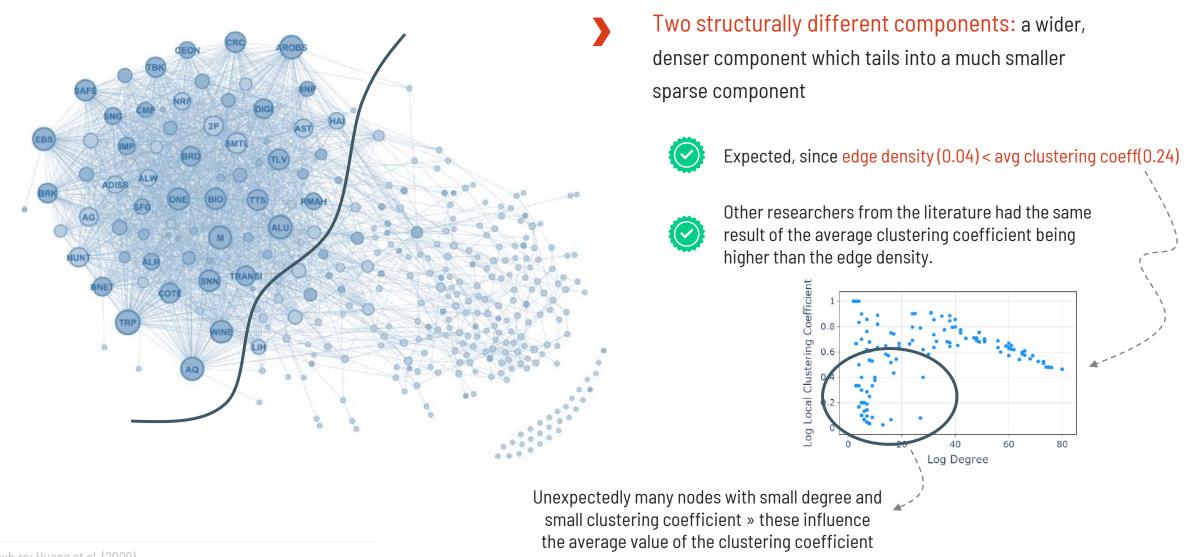
- » based on the cross-correlation between the stock returns
- » the nodes are the 328 stocks from the Romanian stock market
- » the value of the threshold used at edge construction was defined to be 0.15, based on experiments
  - » the threshold significantly influences the structure of the stock network

# 2. ANALYZING THE STOCK NETWORK

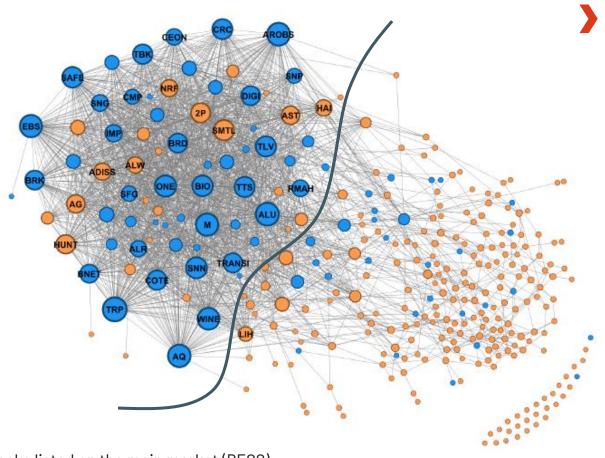


# 3. TRAINING A PREDICTION ALGORITHM





Source: bvb.ro; Huang et al. (2009)



- stocks listed on the main market (REGS)
- stocks listed on the secondary market (AERO)

Two structurally different components: visually looked like the dense component mainly consists of stocks listed on REGS and the other component is dominated by AERO stocks



The network is actually homogeneous regarding the distribution of nodes based on market:

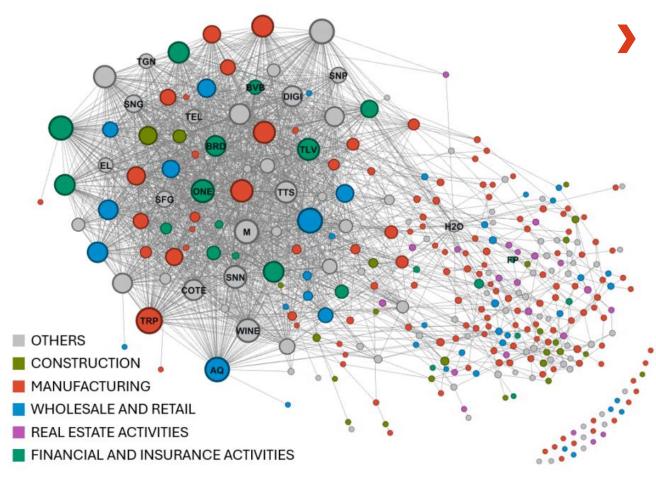
» 41% of edges are linking together REGS and AERO nodes
» the cumulative degree of AERO-nodes is 1719 (41%), while the REGS nodes have in total 2459 degrees, even though there are fewer REGS nodes than AERO





Can be explained through the investing behavior on the Romanian market: investors balance out the riskier AERO stocks with the mature and secure REGS stocks in their portfolios. Secondary market driven by the Primary market.

Source: bvb.ro



The nodes of the network are labeled if the stock that these represent belongs to the BET index. There are also low-degree nodes belonging to BET.

The nodes are not clustered by industry, even though this was the expectation: the prices of assets in the same industry tend to move together, hence the correlation should be higher.



The network is homogeneous also based on the clustering on industry, the nodes connecting also with nodes from other industries: 

» 40% of stocks activate in the manufacturing industry but this does not represent the industry with the highest cumulative degrees 

» the industry with the highest cumulative degrees is finance and insurance services to that belong only 21 nodes





The number of shares belonging to an industry doesn't mean consequently that the industry drives the stock market. This does not depend on the index either, even though indices represent benchmark portfolios, and it was expected that these are popular among investors.

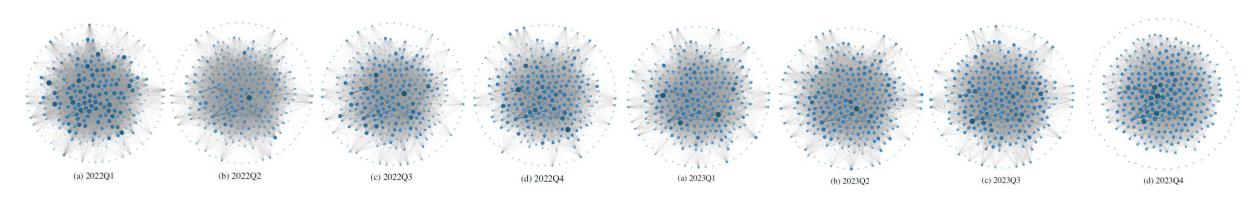
Fast information-flows: all price changes are quickly incorporated and reflected by all nodes » dynamic system, free economy

diameter = 9
average shortest path = 3.44
60% of nodes achieve in 4-5 steps (i.e.
connections) other nodes
small-world property

temporal networks: aggregating the data from the 2022-2023 time-period on subperiods » the smaller the period, the more connections there were » stock prices and returns closer in time have higher correlation

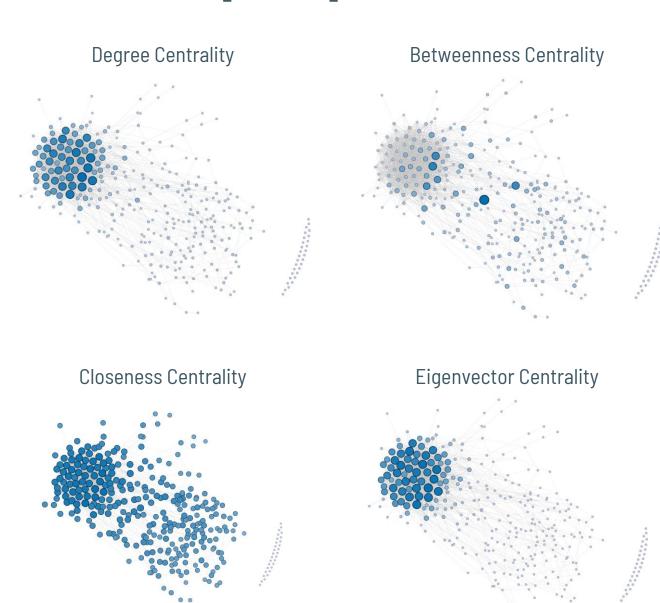
		N	N_isolated	L	edge_density	avg_clust_coeff	k_min	k_max	k_avg
type	metric								
year	mean	328.0	28.500000	3321.500000	0.061936	0.214279	0.0	73.000000	20.253049
halfyear	mean	328.0	43.500000	5264.250000	0.098162	0.220671	0.0	83.000000	32.099085
trimester	mean	328.0	56.000000	6645.000000	0.123909	0.246695	0.0	105.166667	40.518293
quarter	mean	328.0	67.500000	7508.750000	0.140015	0.267713	0.0	104.250000	45.785061
month	mean	328.0	110.166667	9917.958333	0.184940	0.353211	0.0	140.750000	60.475356
					ì	<u> </u>			·

The network dynamics as captured by quarterly aggregated temporal networks



The most important nodes: based on the four centralities. The price of the most stocks are linked to TRP (TERAPLAST SA; AERO), ALU (ALUMIL ROM INDUSTRY S.A.; REGS), AROBS (AROBS TRANSILVANIA SOFTWARE)

rank	degree	betweenness	closeness	eigenvector
	centrality	centrality	centrality	centrality
1	TRP (0.24)	H2O (0.06)	TRP (0.4)	TRP (0.17)
2	ALU (0.23)	AROBS (0.05)	ALU (0.39)	EBS (0.16)
3	AROBS (0.23)	ALU (0.05)	M (0.39)	ALU (0.16)
4	AQ (0.23)	MIB (0.05)	AQ (0.39)	M (0.16)
5	EBS (0.22)	WINE (0.04)	AROBS (0.39)	ONE (0.16)
6	M (0.22)	AQ (0.04)	WINE (0.39)	AROBS (0.16)
7	WINE (0.22)	TBM (0.03)	EBS (0.38)	WINE (0.16)
8	ONE (0.21)	TBK (0.03)	ONE (0.38)	SAFE (0.16)
9	SNN (0.21)	COKJ (0.03)	CRC (0.38)	AQ (0.16)
10	SAFE (0.2)	MEOR (0.03)	SMTL (0.38)	SNN (0.15)



#### **OBJECTIVES & ORIGINAL CONTRIBUTIONS**

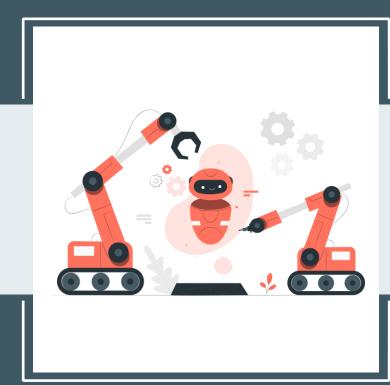
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- » visually there are two components outlined, but the network is homogeneous by market, index or industry
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# 3. TRAINING A PREDICTION ALGORITHM

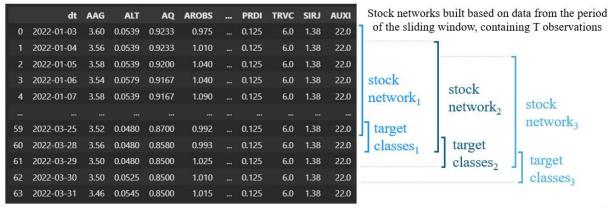


### From close prices to prediction

Methodology: quarterly close prices » networks »

5 extracted properties = features of the prediction algorithm

#### Extract of raw close prices



0.492248 0.663239 0.004778 0.078745 0.500000 0.666667 0.008708 0.074586 0.577519 0.002290 0.684020 0.702997 0.099315 0.616003 0.600775 0.714681 0.005485 0.098044 0.575313 0.426357 0.635468 0.005369 0.066308 0.670513 0.154440 0.541841 0.000499 0.025700 IPRO stagnate 0.596703 0.494208 0.004947 0.080254 0.422222 0.138996 0.537344 0.000722 0.016172 0.386100 0.619617 0.001080 0.070019 0.004415 0.642715 0.444015 0.074595

T = 60 trading days ~ a quarter

input variables of the prediction model

target variable of the prediction model

Extract from each

network five metrics on

node-level and associate

each observation-set

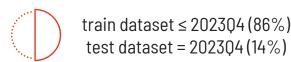
with the target class of

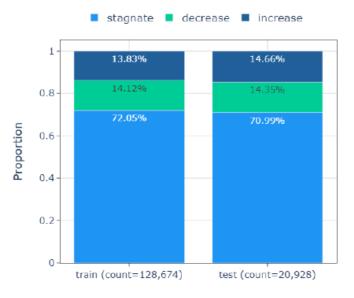
the node



460 stock networks 149,602 observations

Target class distribution: stagnate = 72%, increase = 14%, decrease = 14%





multi-class classification problem; unbalanced classes, but this is the natural distribution. 30% of the stagnate class because of isolated nodes.

### The multi-class classification problem



Models



Performance metrics:



Goal

Classify in increase, decrease or stagnate classes the movement of the next-day close prices of the stocks on the Bucharest Stock Exchange

Multinomial logistic regression » for each class there is a two-class logistic regression built: one class vs. all the others. The results are combined based on the SoftMax function.

LogisticRegression(multi\_class='ovr')

Decision Tree » at each level there is a split made based on the feature that best divides the data into two different classes.

DecisionTreeClassifier()

SVM » searching for the optimal hyperplane which best divides the data on the basis of one class vs others.

LinearSVC(dual=False)

accuracy » the ratio of the correctly predicted classes from all observations



unbalanced classes, accuracy can be biased, therefore precision, recall and F1 score are equally important



precision » how many predictions were correct from all the cases when a certain class was predicted

recall » measures how many of the observations in a certain class were predicted correctly

F1 score » the harmonic mean of precision and recall

Source: Pedregosa et al. (2011)

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F1 score » the harmonic mean of precision and recall

metrics on class level

model-level metrics = the simple mean of the class-level metrics

Source: Pedregosa et al. (2011)

# The learning algorithms

Baseline model: predict for each observation the stagnate class

$$f_{baseline}(x) = "stagnate"$$

dataset	indicator	increase	decrease	stagnate	model
train	accuracy		0.7	205	
	precision	0	0	0.7205	0.2402
	recall	0	0	1.000	0.3333
	F1 score	0	0	0.8375	0.2792
test	accuracy		0.7	099	
	precision	0	0	0.7099	0.2366
	recall	0	0	1.000	0.3333
	F1 score	0	0	0.8303	0.2767

Machine learning models: from each algorithm-family a single model was trained using the sklearn library

train	0.9996 0.9992 0.9993	0.7310 0.4800 0.3984
recall 0.4151 F1-score 0.4053	0.9993	
recall 0.4151 F1-score 0.4053		0.3984
	0.000	
accuracy 0.7127	0.9992	0.3788
0.7127	0.6236	0.7149
test precision 0.4835	0.4414	0.4430
recall 0.4257	0.4519	0.3945
F1-score 0.4251	0.4450	0.3719

» even though the Decision Tree had the smallest accuracy, even lower than the baseline model (because of the overfit on train dataset), this had the highest recall and F1-score.

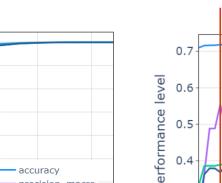


fine tune this model to reduce the overfitting

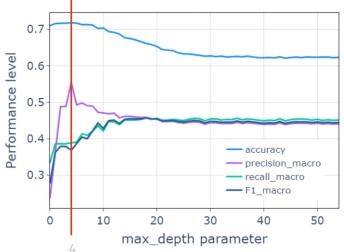
Forrás: Pedregosa et al. (2011)

### Choosing the best decision tree

The decision tree had a depth of 55: training decision trees with different depths from 1 up to 55, searching for a balance among the 4 performance metrics» decision tree with depth 4



50



(a) train dataset

max\_depth parameter

30

20

F1 macro

1

0.9

0.8

0.7

0.5

0.3

0.2

10

Performance level

(b) test dataset

indicator	Baseline	$DecisionTree_{55}$	$DecisionTree_4$
accuracy	0.7205	0.6236	0.7184
precision	0.2402	0.4414	0.3686
recall	0.3333	0.4519	0.5544
F1-score	0.2792	0.4450	0.3894

» tried to increase the performance by taking the different combination of features, but it did not help.



### The model corresponds to the goal of this thesis



#### Validation on data from 2024Q1



1308 observations 85% stagnate, 8%

increase, 7% decrease



accuracy = 0.8257 precision = 0.3917

recall = 0.3628

F1 score = 0.3584

<sup>»</sup> after 10 splits the overfit is evidenced: increasing performance on the train dataset while these decrease on the test dataset

<sup>»</sup> the precision is the highest at the decision tree with depth of 4 splits

#### CONCLUSIONS

# 1. MODELLING THE STOCK NETWORK

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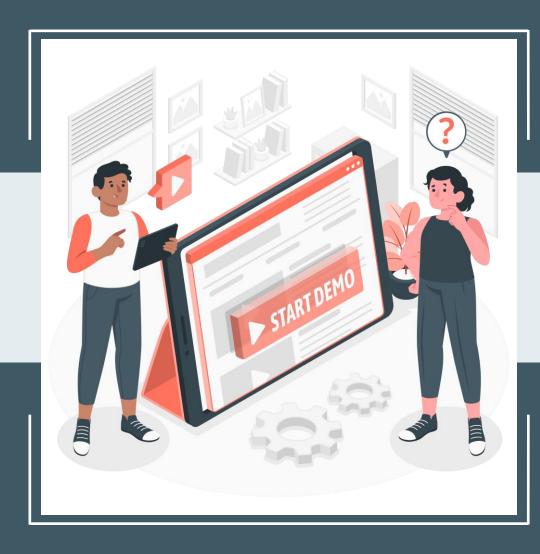
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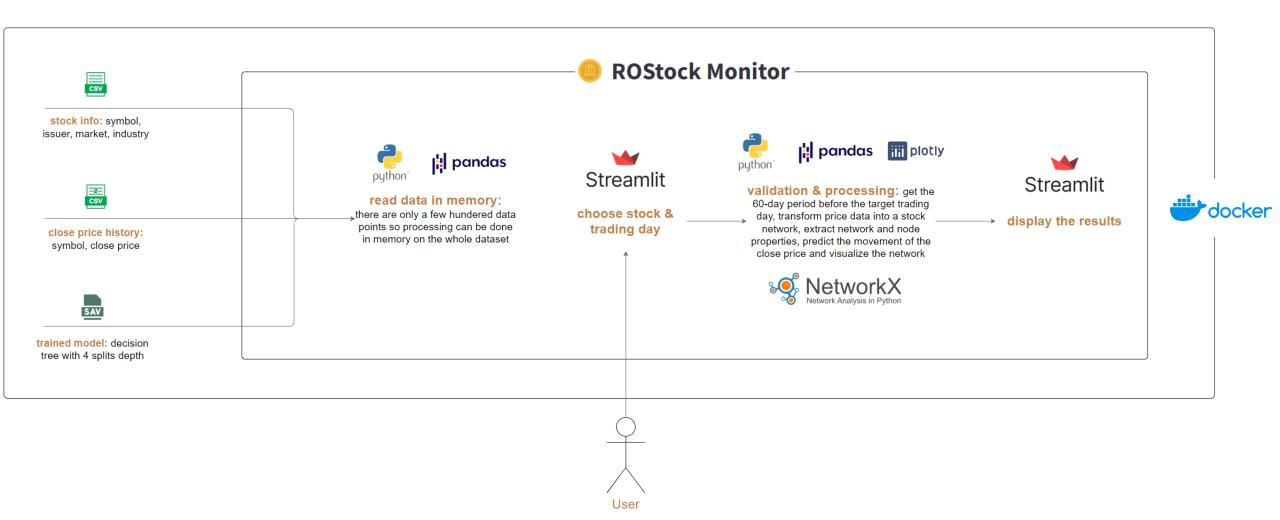
- » multi-class supervised classification problem
- » the features are 5 metrics extracted from 460 stock network
  - » unbalanced classes
- » logistic regression, decision trees, SVM. Final model: decision tree with 4 splits depth, having accuracy of 72% and F1 score of 39%.

#### APPLICATION

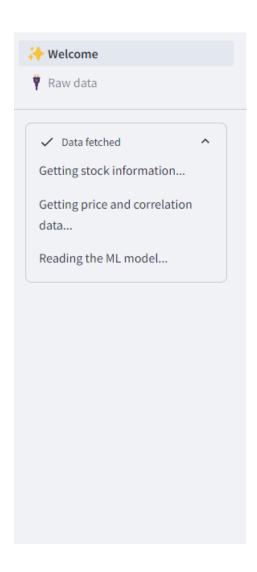


**APPLICATION: ROSTOCK MONITOR** 

# Architecture & Technologies used



# User Interface - landing page



#### Welcome to ROStock! \*



#### About this project

What? ROStock offers an overview on the Romanian stocks listed on the Bucharest Stock Exchange and enables users to inspect the stock network and the prediction of the next-day close price movements.

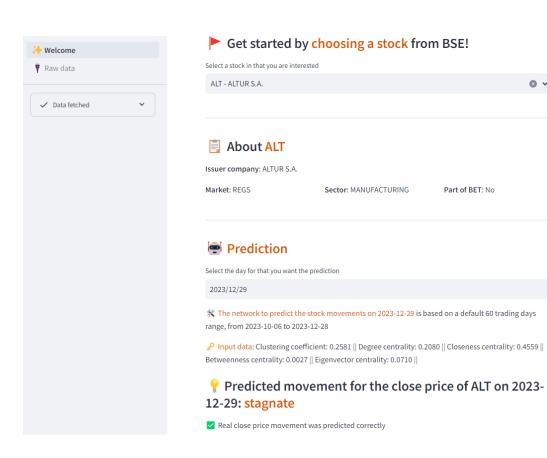
How? Behind the scenes, the platform uses a network science approach to model the Bucharest Stock Exchange as a complex network based on which the movement of the next-day close prices can be predicted. The decision tree model underlying the prediction was trained on 5 features (clustering coefficient, degree centrality, closeness centrality, betweenness centrality, eigenvector centrality) extracted from each of the 328 nodes of 460 networks built for 2022-2023. The model has 72% accuracy, 55% precision, 39% recall, and 37% F1-score.

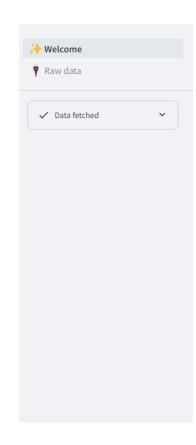
#### Get started by choosing a stock from BSE!

Select a stock in that you are interested



# User Interface - prediction and network





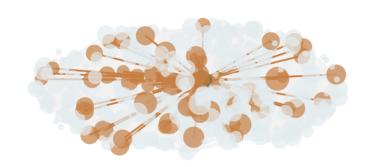
#### The network underlying the prediction

➡ Network properties: Number of nodes (N): 328.00 || Number of isolated nodes: 68.00 || Number of edges (L): 7408.00 || Edge density: 0.14 || Average Clustering Coefficient: 0.24 || Minimum degree: 0.00 || Maximum degree: 94.00 || Average degree: 45.17 || Average degree centrality: 0.14 || Average betweenness centrality: 0.00 || Average closeness centrality: 0.35 || Average eigenvector centrality: 0.05 ||

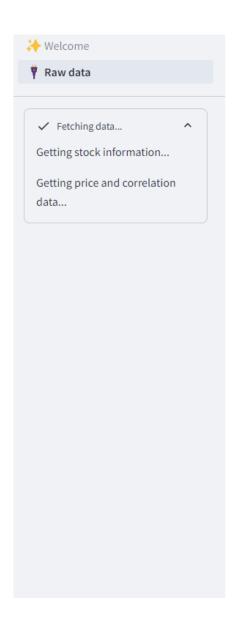
Please expand the visualization for better visibility.

Legend: Nodes are sized by degree. The node in green is ALT and the nodes highlighted with brown are the stocks which had a correlation higher than 0.15 with ALT.





# User Interface - data behind the app



#### The data behind ROStock! 🌣



#### Information about the stocks:

symbol	share_name	company_name	market	sector
AAG	AAGES S.A.	S.C AAGES S.A.	REGS	MANUFACTURING
ALR	ALRO S.A.	ALRO S.A.	REGS	MANUFACTURING
ALT	ALTUR S.A.	ALTUR S.A.	REGS	MANUFACTURING
ALU	ALUMIL ROM INDUSTRY S.A.	ALUMIL ROM INDUSTRY S.A.	REGS	WHOLESALE AND RETAIL
AQ	AQUILA PART PROD COM	AQUILA PART PROD COM	REGS	WHOLESALE AND RETAIL
ARM	ARMATURA S.A.	ARMATURA S.A.	REGS	MANUFACTURING
AROBS	AROBS TRANSILVANIA SOFTWARE	AROBS TRANSILVANIA SOFTWARE	REGS	INFORMATION AND COMM
ARS	AEROSTAR S.A.	AEROSTAR S.A.	REGS	MANUFACTURING
ARTE	ARTEGO SA	ARTEGO SA	REGS	MANUFACTURING
ATB	ANTIBIOTICE S.A.	ANTIBIOTICE S.A.	REGS	MANUFACTURING

#### Historical stock prices:

	dt	AAG	ALT	AQ	AROBS	ARTE	ВСМ	BNET	BRK	BVB	CBC	CMCN
0	2022-01-03	3.6	0.0539	0.9233	0.975	11.9	0.098	0.3177	0.283	25.4	17.1	0.2
1	2022-01-04	3.56	0.0539	0.9233	1.01	11.5	0.095	0.3255	0.292	25.2	17.1	0.2
2	2022-01-05	3.58	0.0539	0.92	1.04	11.5	0.095	0.3445	0.3	25.4	19.2	0.2
3	2022-01-06	3.54	0.0579	0.9167	1.04	11.5	0.095	0.3491	0.293	25.2	22	0.2

### **Future work**



#### THE INPUT DATA EXTRACTION

Different periods could be used for the sliding window to optimize the prediction. When modelling the stock networks, different thresholds can be used for each network. It could be also an option to start from a basenetwork and each day add the new information to this.



#### THE PREDICTION ALGORITHMS

Extract more input features from the network, even on the macro- and meso-level. Compare different algorithms and parameters. Try ensemble models, for example stagnate vs. others layer and increase vs decrease layer.



#### THE ANALYSIS OF STOCK NETWORKS

Comparing networks modelled based on different thresholds to uncover more insights e.g. constant connections independent of the threshold



#### PyData Cluj-Napoca

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# PREDICTING ROMANIAN STOCK MOVEMENT TRENDS: A COMPLEX NETWORK APPROACH COMBINED WITH MACHINE LEARNING

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