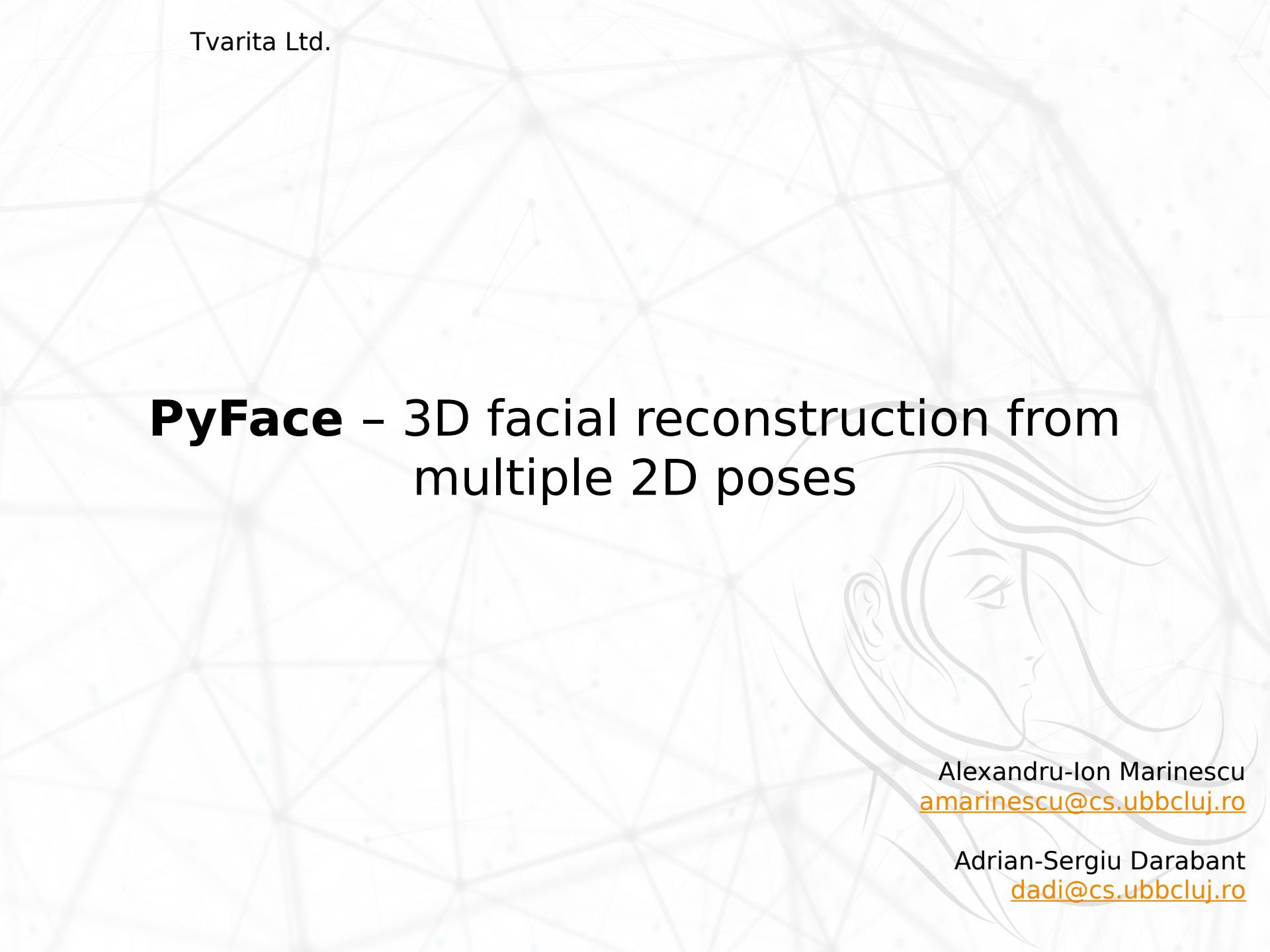


# **PyFace** – 3D facial reconstruction from multiple 2D poses



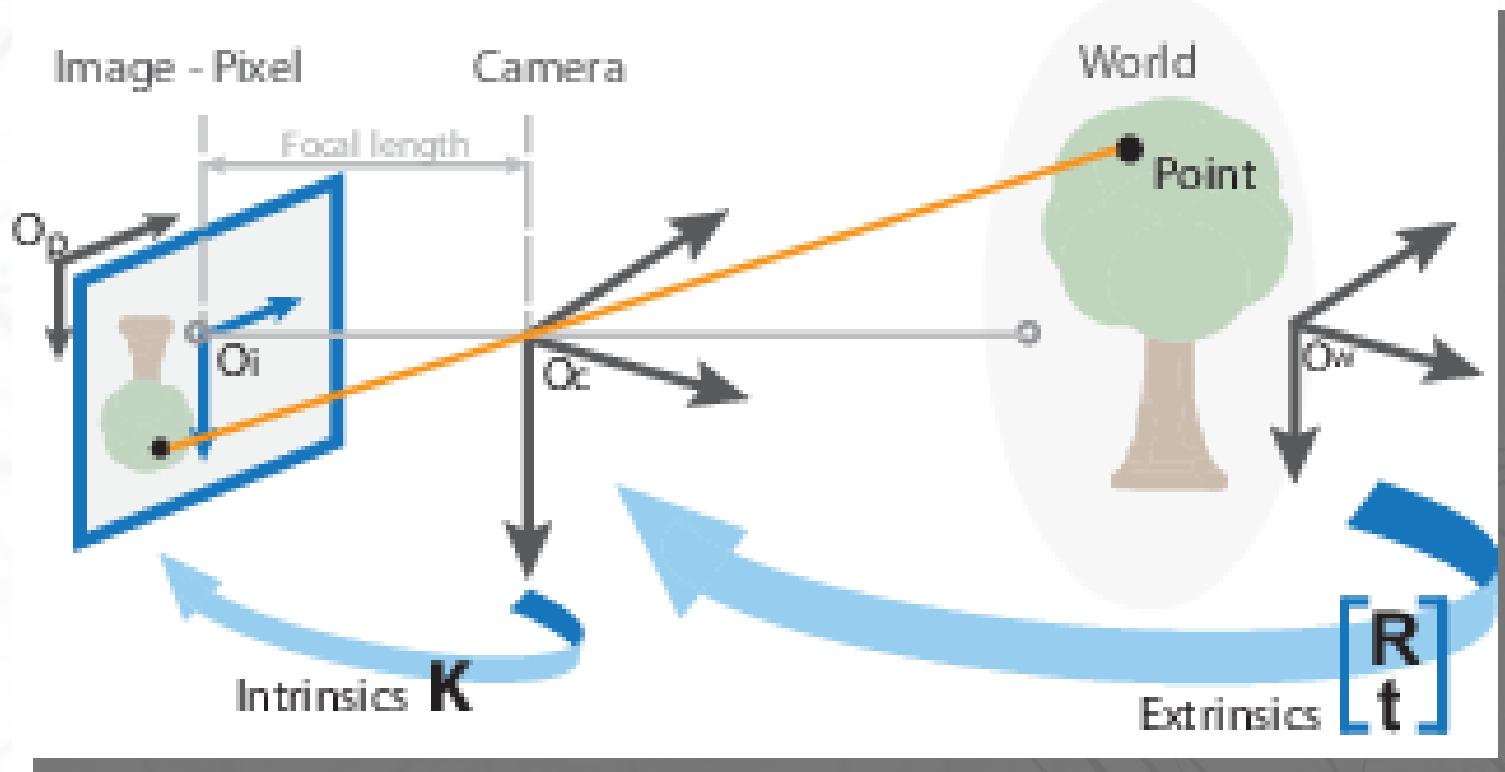
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# Problem presentation



# Intrinsic and extrinsic params



Intrinsic:  $k\_mat$  and  $d\_vec$   
Constant for each **camera**...

Extrinsic:  $r\_vec$  and  $t\_vec$   
Constant for each **image**...

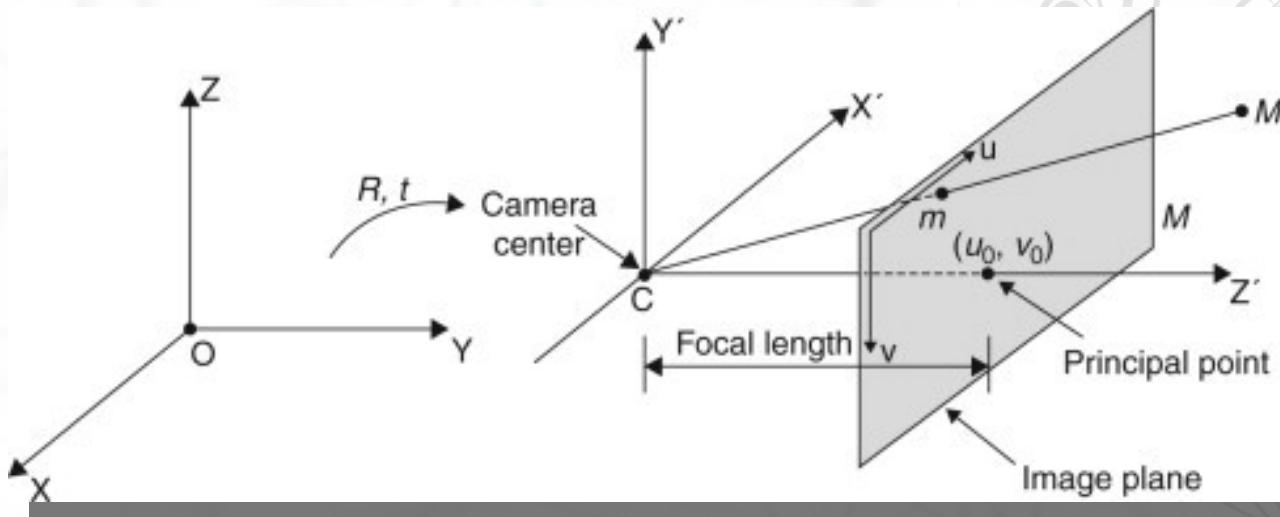
# Intrinsic and extrinsic params

Either perform a camera calibration or use an approximation:

$$k_{mat} = \begin{pmatrix} W & 0 & \frac{W}{2} \\ 0 & W & \frac{H}{2} \\ 0 & 0 & 1 \end{pmatrix}$$

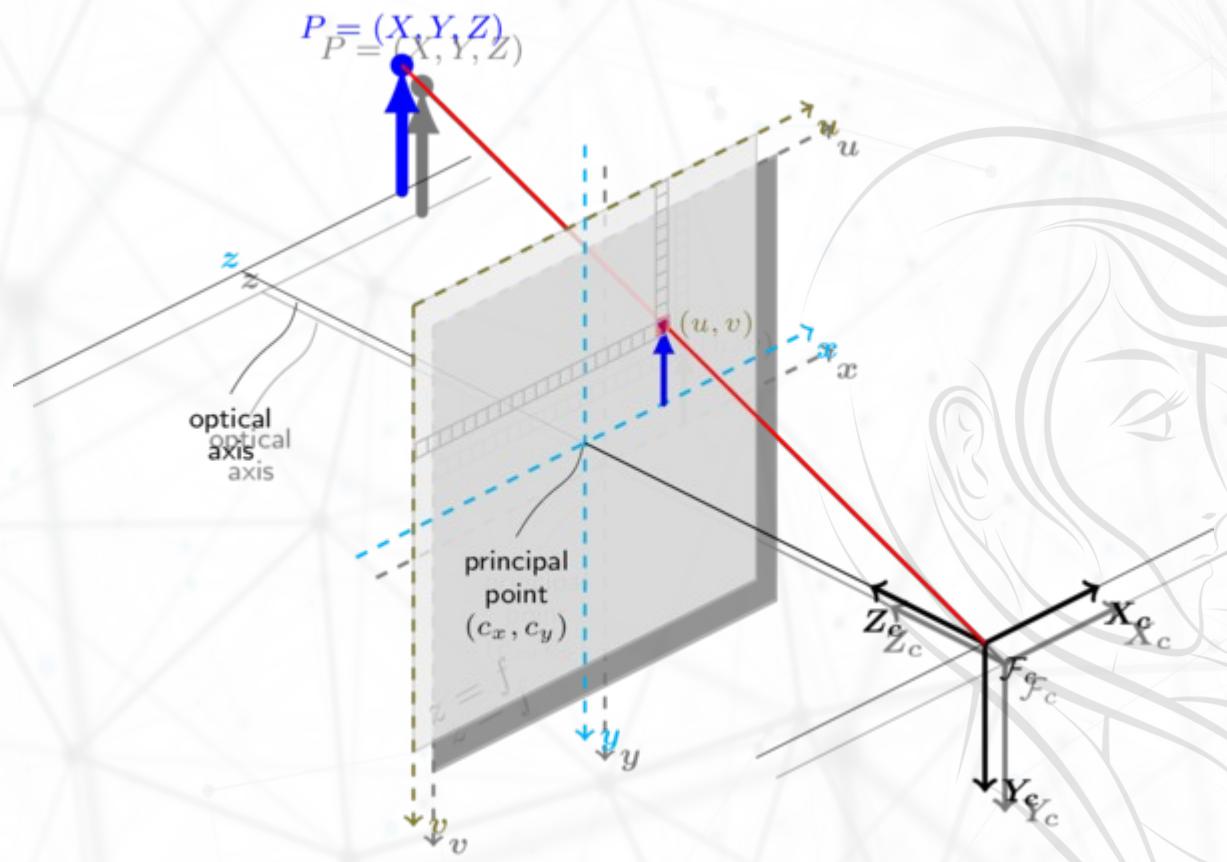
$$d_{vec} = [0, 0, 0, 0, 0]$$

$r_{vec}, t_{vec} = \text{solvePnP}(\text{Ransac}(pts_{obj}, pts_{img}, k_{mat}, d_{vec}))$

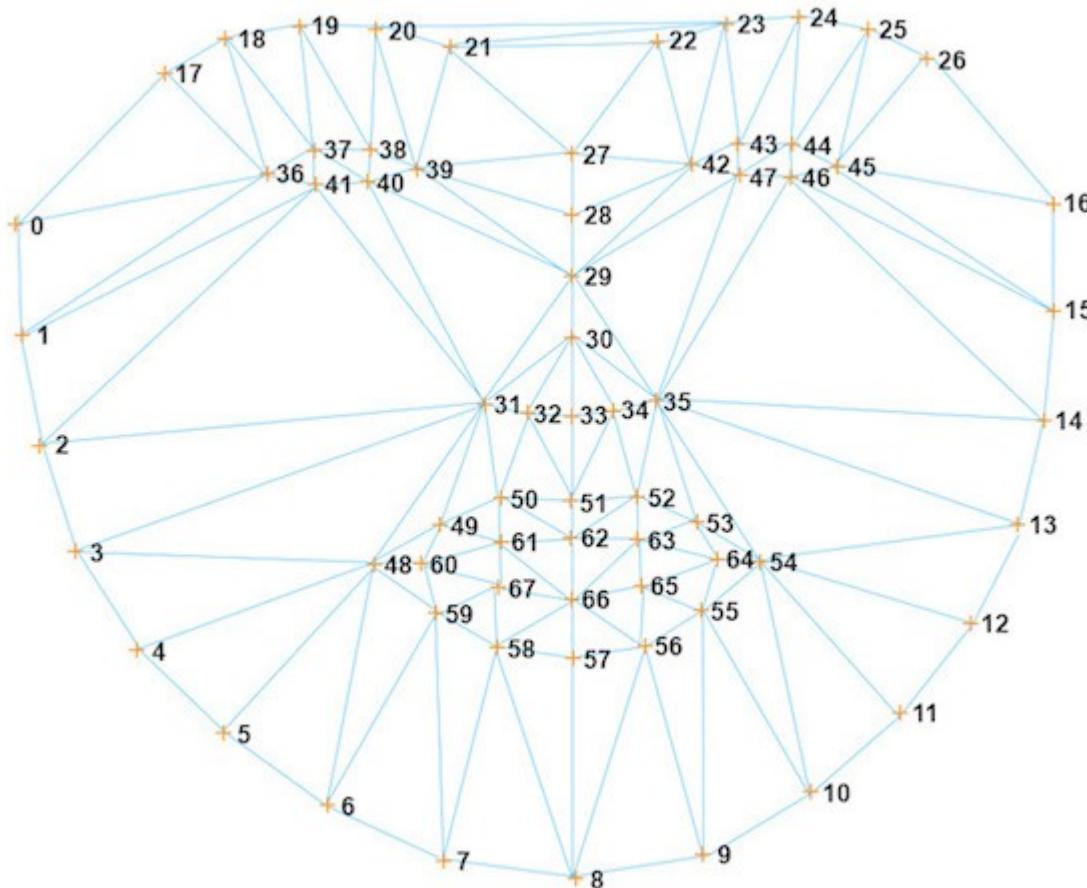


# Pinhole camera model

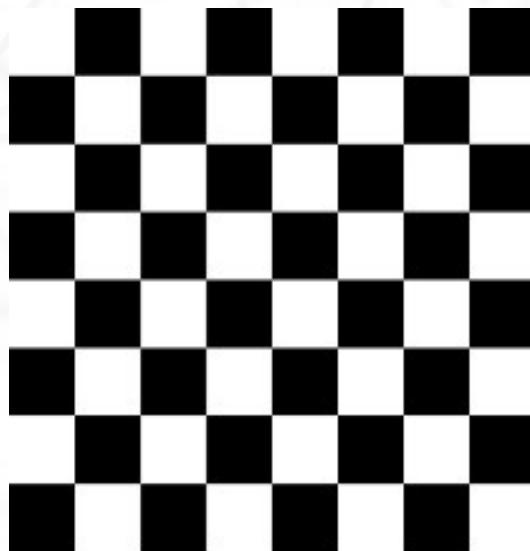
Assumes **zero** distortion...



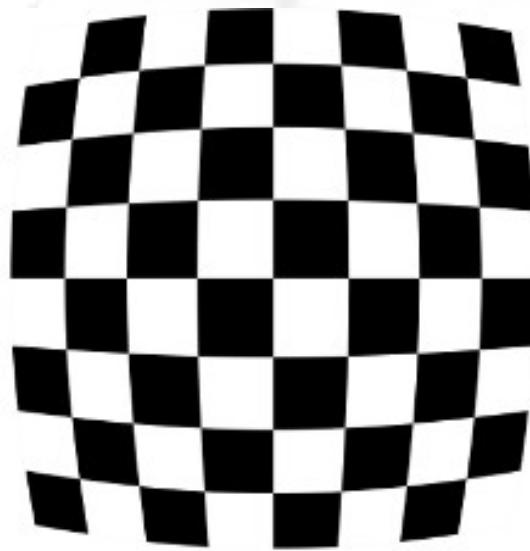
# Landmark detection



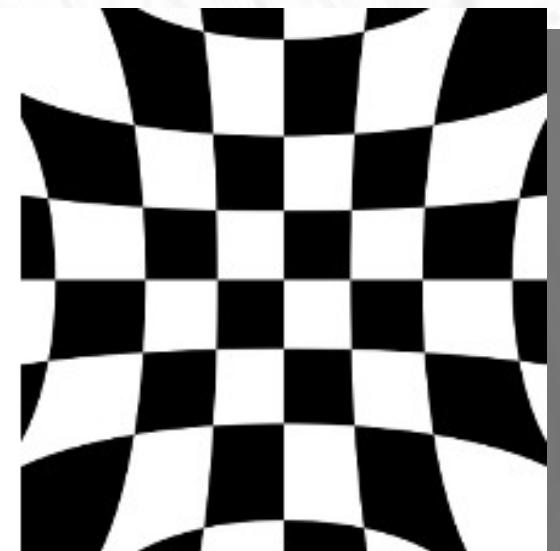
# Examples of lens distortion



No distortion



Positive radial distortion  
(Barrel distortion)



Negative radial distortion  
(Pincushion distortion)

## solvePnP(...) Ransac(...)

$$s p_c = K [R | T] p_w$$

$$s \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} f_x & \gamma & u_0 \\ 0 & f_y & v_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_1 \\ r_{21} & r_{22} & r_{23} & t_2 \\ r_{31} & r_{32} & r_{33} & t_3 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

**Perspective-n-Point** is the problem of estimating the pose of a calibrated camera given a set of n 3D points in the world and their corresponding 2D projections in the image.

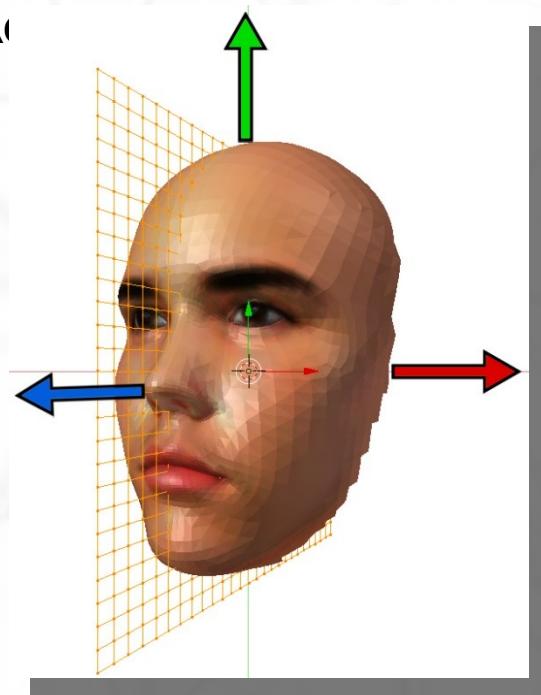
The camera pose consists of 6 degrees-of-freedom...

PnP is prone to errors if there are **outliers** in the set of point correspondences. **RANSAC** can be used with existing approaches to make the solution for the camera pose more *robust to outliers*...

# Image pre-processing

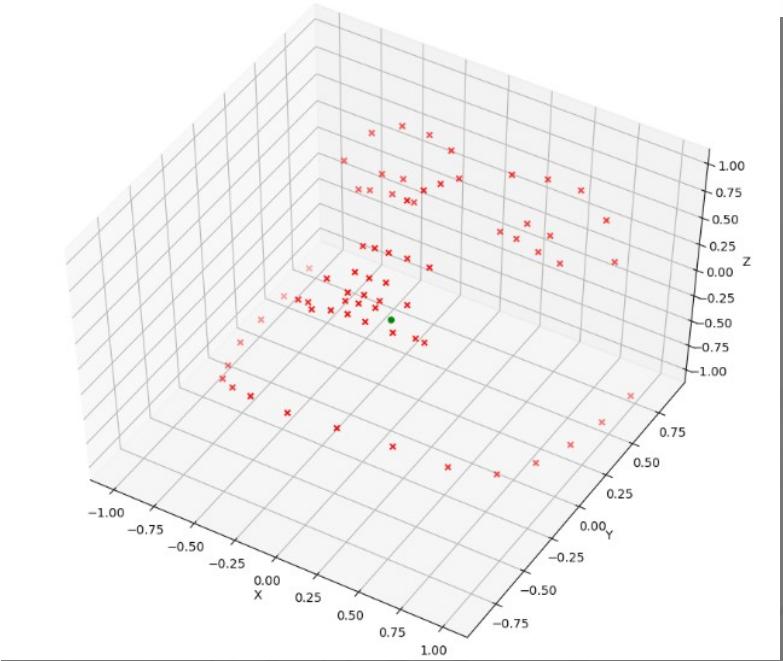
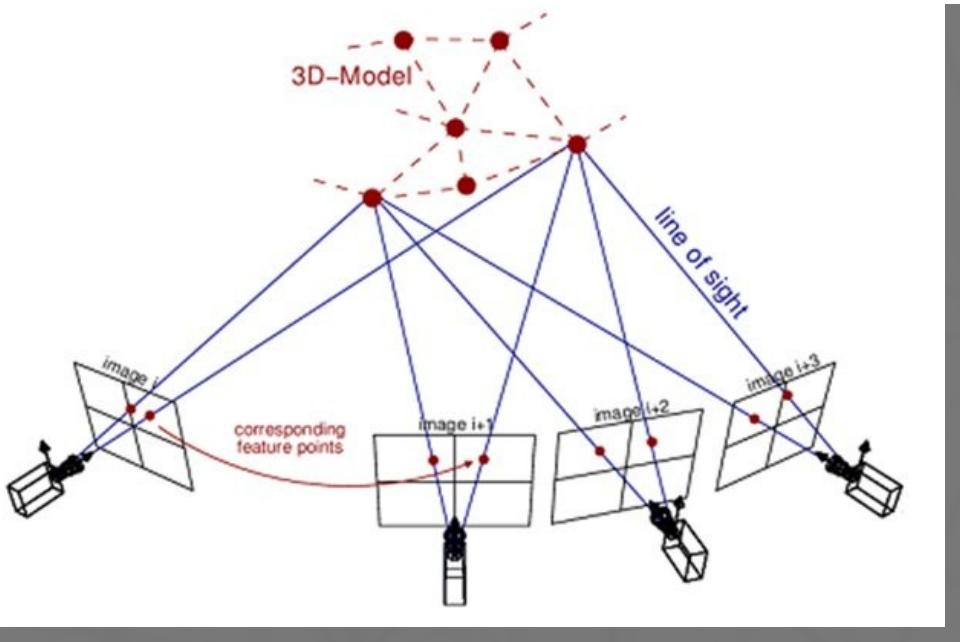
Crop square **center** to  
face...

Re



# Bundle adjustment

Optimize **3D** point cloud with **minimal reprojection error**...



# Bundle adjustment

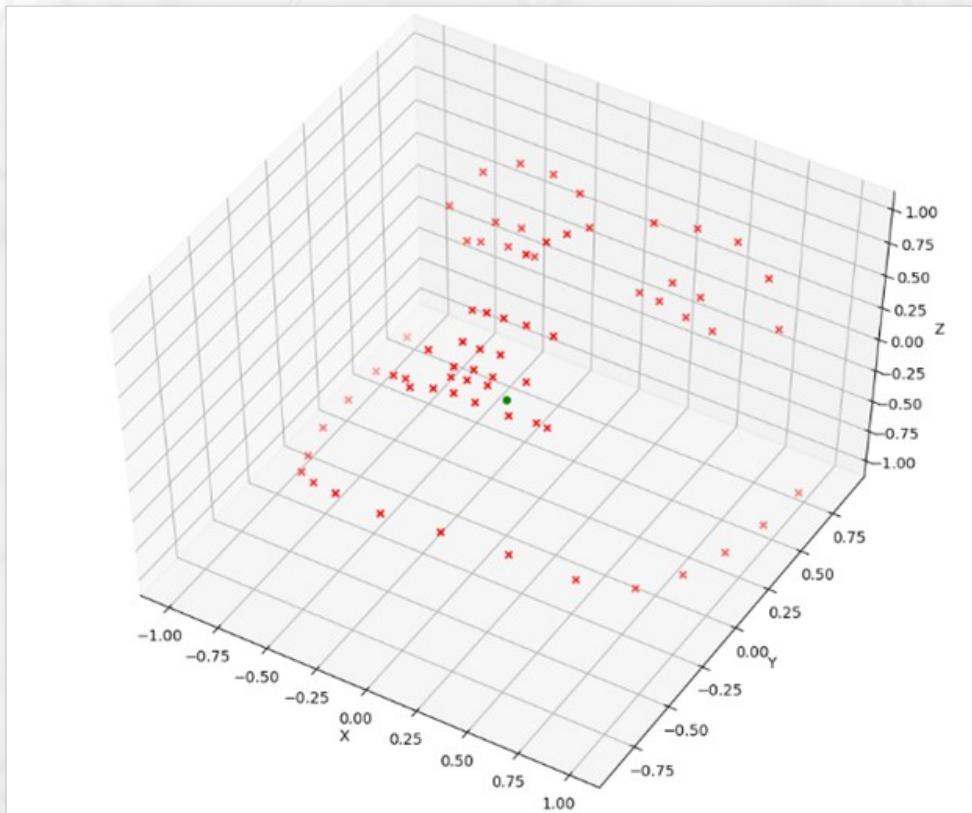
Least Squares and algorithm is Levenberg-Marquardt...

Mathematically, the function to minimize is:

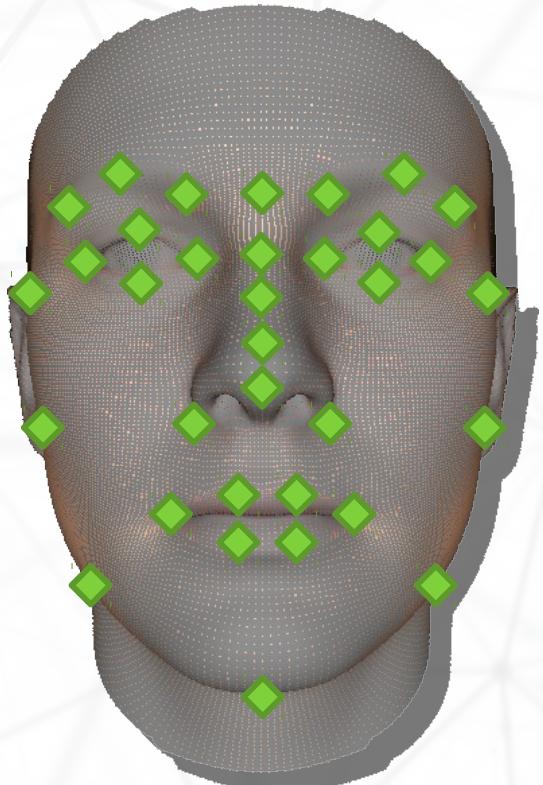
$$\min_{a_j b_i} \sum_{i=1}^n \sum_{j=1}^m \|Q(a_j, b_i) - x_{ij}\|^2$$

- 3D points to optimize
- cameras/images
- is the projection of the  $i^{th}$  point on the  $j^{th}$  image
- Camera  $j$  is parameterized by a vector  $a_j$ , and points by a vector  $b_i$  ( $b_1, b_3$ )
- is the predicted projection of point  $i$  in image  $j$

# Face specific - 3D point cloud

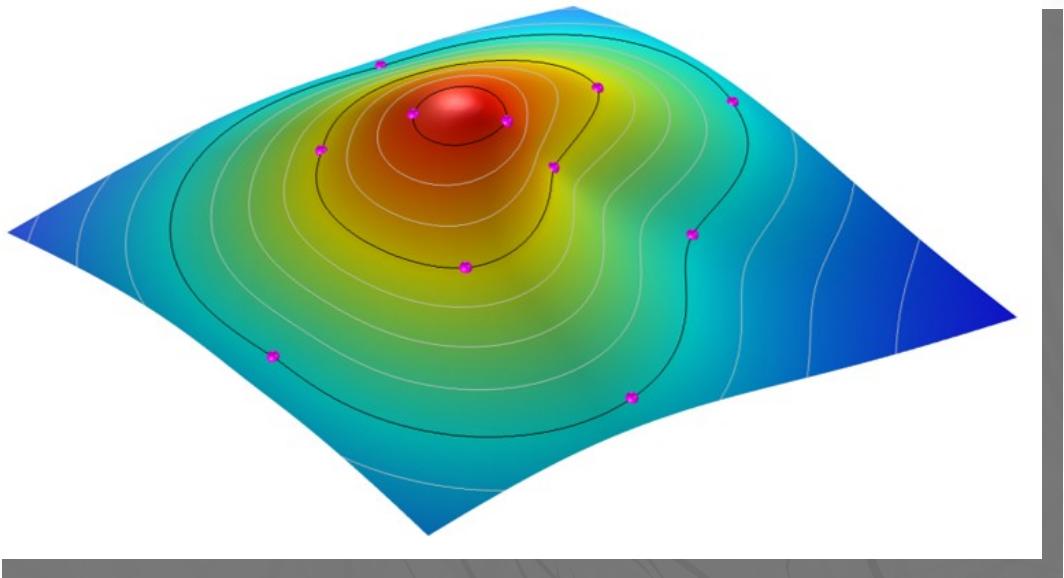


# Generic deformable models



**Basel 2009**

53,490 vertices  
106,466  
triangles



RBF interpolation using multiquadric  
 $\phi(r) = \sqrt{1 + (\varepsilon r)^2}$

# Forehead extraction

Is needed for complete facial reconstruction and performed by a separate pipeline...

A CNN takes 5 landmarks along the hair line

