

# CSC 449/549 Advanced Topics in Artificial Intelligence

## Deep Reinforcement Learning

### Final Exam

Fall, 2022

Name: \_\_\_\_\_ ID#: \_\_\_\_\_ Score: \_\_\_\_\_

1. (10 pts) Monte Carlo methods for learning value functions require episodic tasks. Why, specifically? How is it that  $n$ -step TD methods avoid this limitation and can work with continuing tasks?

2. (20 pts) Your Monte-Carlo algorithm generates the following episode using policy  $\pi$  when interacting with its environment. This is the first episode that has been generated.

Timestep	Reward	State	Action
0		$s_1$	$a_1$
1	13	$s_1$	$a_2$
2	7	$s_1$	$a_1$
3	13	$s_1$	$a_2$
4	14	$s_2$	

Assume the discount factor,  $\gamma$ , is 1, and  $s_2$  is a terminal state.

- a) What are the estimates of:  $q_\pi(s_1, a_1)$  and  $q_\pi(s_1, a_2)$  if using first-visit?

- b) What are the estimates of:  $q_\pi(s_1, a_1)$  and  $q_\pi(s_1, a_2)$  if using every-visit?

3. (4 pts) True or False?

- a) \_\_\_\_\_ Q-learning can learn the optimal Q-function  $Q^*$  without ever executing the optimal policy.
- b) \_\_\_\_\_ If an MDP has a transition model  $T$  that assigns non-zero probability for all triples  $T(s, a, s')$  then Q-learning will fail.

4. (16 pts) What is the formal definition of a Partially Observable Markov Decision Process (POMDP), and why is it so much more difficult to find an optimal policy for a POMDP compared to a Completely Observable Markov Decision process?

5. (50 pts) A rat is involved in an experiment. It experiences one episode. At the first step it hears a bell. At the second step it sees a light. At the third step it both hears a bell and sees a light. It then receives some food, worth  $+1$  reward, and the episode terminates on the fourth step. All other rewards were zero. The experiment is undiscounted.
- a) (7 pts) Represent the rat's state  $s$  by a vector of two binary features,  $bell(s) \in \{0, 1\}$  and  $light(s) \in \{0, 1\}$ . Write down the sequence of feature vectors corresponding to this episode.
- b) (7 pts) Approximate the state-value function by a linear combination of these features with two parameters:  $b \cdot bell(s) + l \cdot light(s)$ . If  $b = 2$  and  $l = -2$  then write down the sequence of approximate values corresponding to this episode.
- c) (4 pts) Define the  $\lambda$ -return  $v_t^\lambda$ .
- d) (7 pts) Write down the sequence of  $\lambda$ -returns  $v_t^\lambda$  corresponding to this episode, for  $\lambda = 0.5$  and  $b = 2, l = -2$ .

- e) (7 pts) Using the forward-view  $TD(\lambda)$  algorithm and your linear function approximator, what are the sequence of updates to weight  $b$ ? What is the total update to weight  $b$ ? Use  $\lambda = 0.5$ ,  $\gamma = 1$ ,  $\alpha = 0.5$  and start with  $b = 2$ ,  $l = -2$ .
- f) (4 pts) Define the  $TD(\lambda)$  accumulating eligibility trace  $\mathbf{e}_t$  when using linear value function approximation.
- g) (7 pts) Write down the sequence of eligibility traces  $\mathbf{e}_t$  corresponding to the bell, using  $\lambda = 0.5$  and  $\gamma = 1$ ,
- h) (7 pts) Using the backward-view  $TD(\lambda)$  algorithm and your linear function approximator, what are the sequence of updates to weight  $b$ ? (Use offline updates, i.e. do not actually change your weights, just accumulate your updates). What is the total update to weight  $b$ ? Use  $\lambda = 0.5$ ,  $\gamma = 1$ ,  $\alpha = 0.5$  and start with  $b = 2$ ,  $l = -2$ .