



Motion Planning for Mobile Robots



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Outline



1. Introduction



2. Course Outline



3. Typical Planning Methods Overview



4. Map Representation



5. Pre-requirement



6. Homework



Introduction



About this Course

- **This course is about:**
 - Academism (old school) planning pipeline
 - Path finding algorithm
 - Trajectory generation/optimization
 - Real-time software implementation
- **This course is NOT about:**
 - Dynamics Modelling ☹
 - Robot design ☹
 - End-to-end navigation ☹
 - Learning-based method ☹
 - Mathematical/theoretical proof ☹
- **This course may also cover:**
 - Autonomy for mobile robots
 - Paper recommendations
 - Cutting-edge research direction/ethics



Basic Expectation

- **Discipline:**

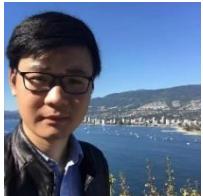
- Every researcher has his own taste/style. Since you choose this course, please follow my style.
- Q&A only at appointed office time.
- Finish your homework by yourself.

- **Project:**

- Basic algorithm validation (MATLAB)
- Sophisticated engineering implementation (ROS/C++)



Teaching Team

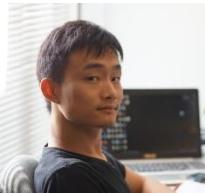


Instructor 1: **Fei Gao**

Assistant Professor, ZJU

Ph.D, HKUST

Email: fgaooa@connect.ust.hk



Instructor 2: **Chaoqun Wang**

Research Fellow, CUHK

Ph.D, CUHK

Email: zychaoqun@gmail.com



Instructor 3: **Shupeng Lai**

Research Fellow, NUS

Ph.D, NUS

Email: shupenglai@gmail.com



Instructor 4: **Delong Zhu**

Ph.D candidate, CUHK

Email: dlzhu@ee.cuhk.edu.hk



Information

- **Lecture time:**
 - Every Friday night 19:00, except October 4th
- **Course Community:**
 - www.shenlanxueyuan.com/course/188/threads/show
- **Course Website:**
 - www.shenlanxueyuan.com/course/188
- **Course Wechat Group:**
 - Connect the class teacher(Wechat: shenlancas)



Workload

- Expected Student Background:
 - Linear algebra
 - Probability
 - MATLAB programming skills
 - C++ programming skills (VERY IMPORTANT)
 - Linux
 - Love robots ☺
- Workload:
 - Attend lectures
 - Lots of project work
 - Have fun with robots ☺

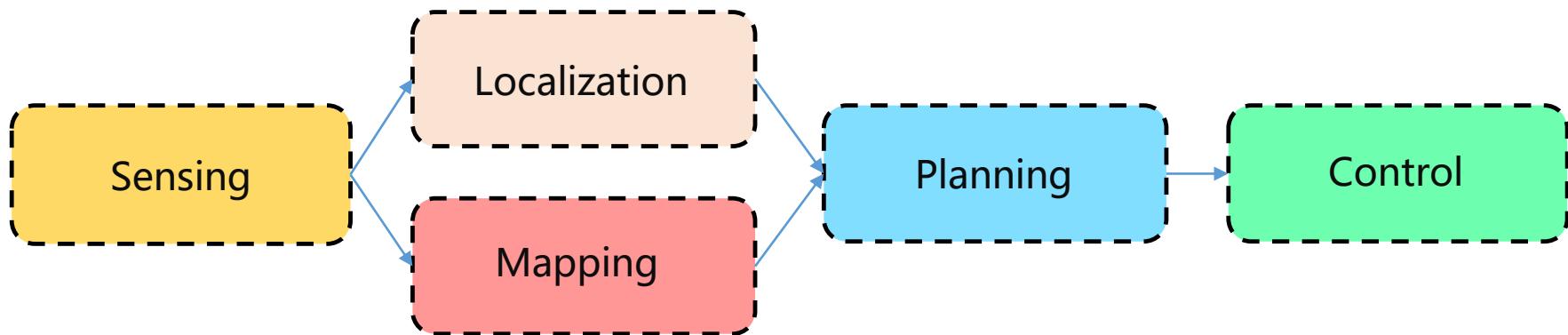


What is autonomous robot

Definition: an autonomous robot is a robot that performs behaviors or tasks with a high degree of autonomy (without external influence).

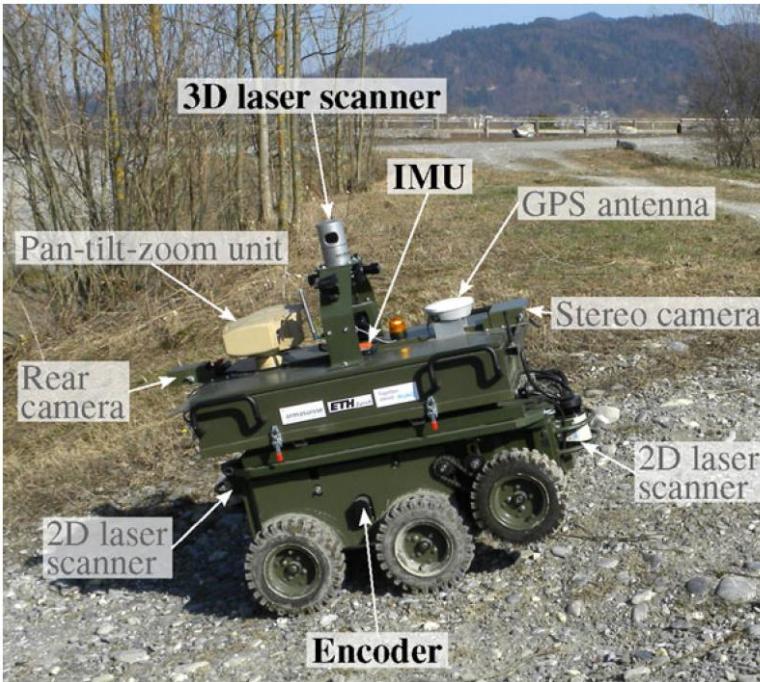
Subjects: Computer Science, Automation, Mechanism, Electronics ...

- Perception-Planning-Control action loop





Autonomous robot: applications

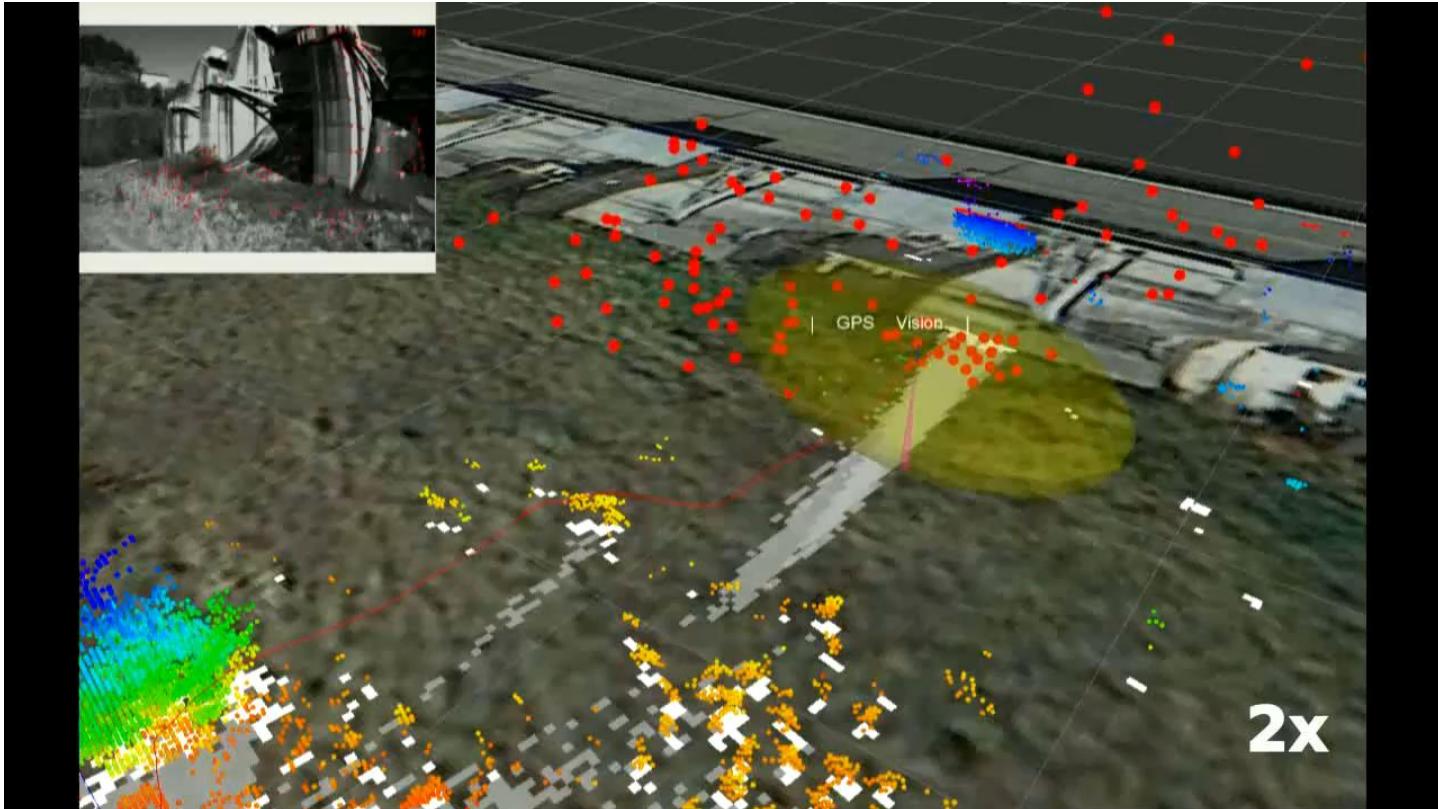




Aerial Robots



Dam Inspection



Shen, et al, 2014



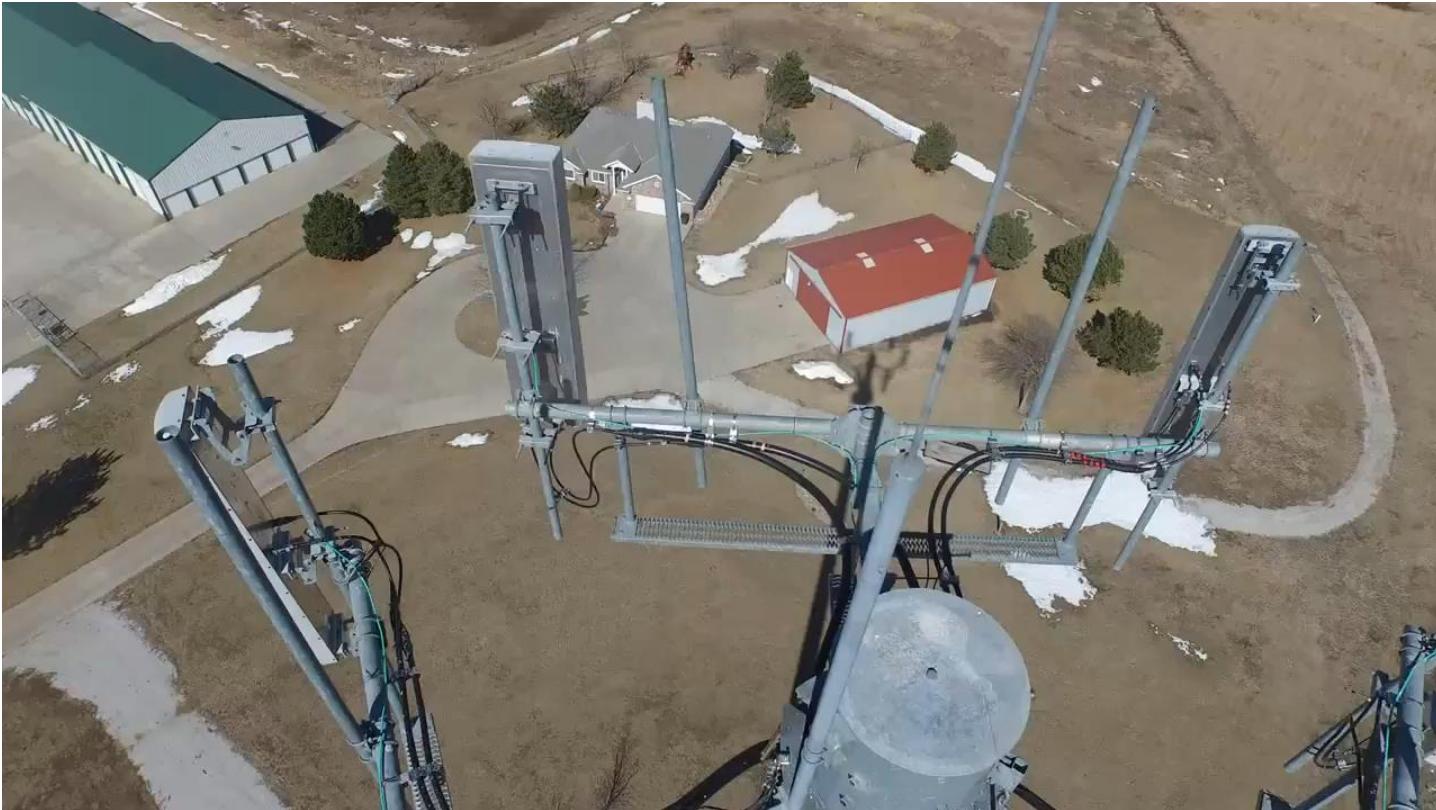
Dam Inspection



Ozaslan, et al, 2014



Cellular Tower Inspection





Precision Farming

2X



Delivery





Ground Robots



Search and Rescue



4x



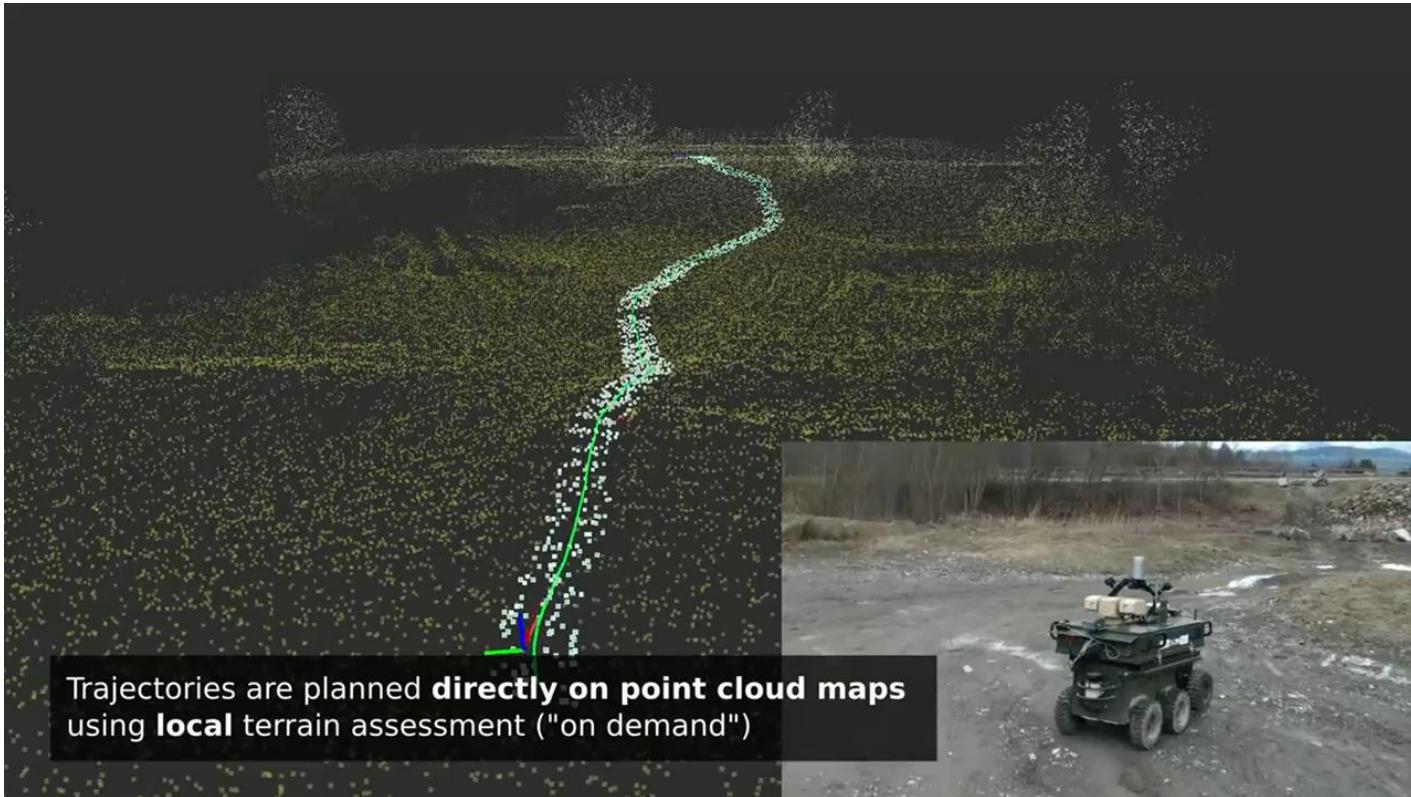
Housekeeping



iRobot®

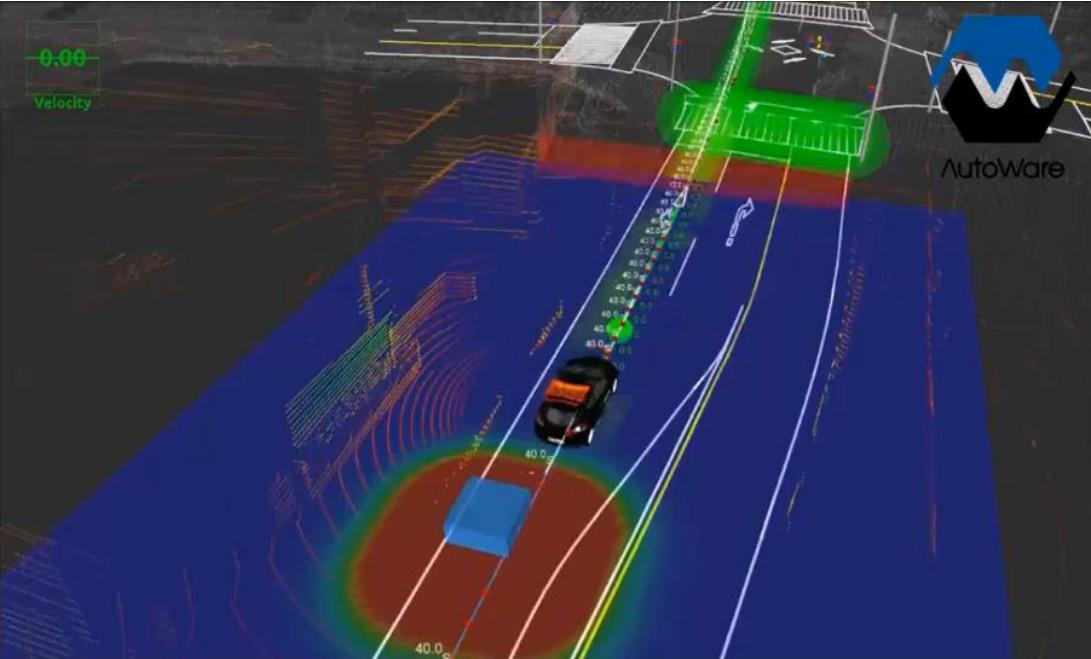


Hills Driving





Urban Driving



Tier IV
Intelligent Vehicle

アイサンテクノロジー株式会社 **AXE**



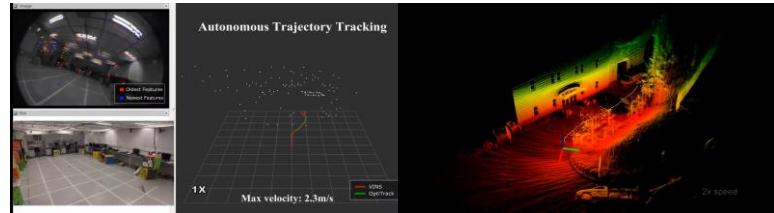
Crowd Driving



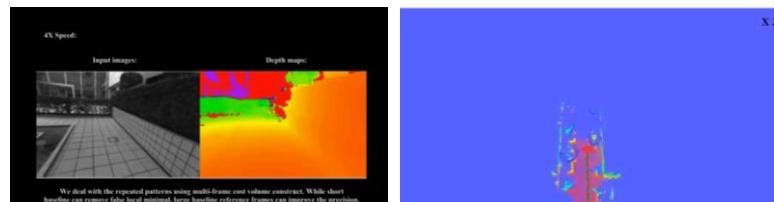


What is autonomous robot

- Estimation
 - Low latency
 - High accuracy & consistency



- Perception
 - 3D sensing & dense perception
 - Map fusion & integration for planning



- Planning
 - Complex & unknown environments
 - Safety & dynamical feasibility
 - Limited sensing & computation



- Control
 - Aggressive maneuvers
 - Smooth trajectory tracking





What is motion planning

- Basic requirements
 - Safety: collision avoidance
 - Smoothness: energy saving, comfort
 - Kinodynamic feasibility: executable, controllable
- Old-school pipeline
 - Front-end path finding
 - Search for an initial safe path
 - Low dimensional
 - Discrete space
 - Back-end trajectory generation
 - Search for an executable trajectory
 - High dimensional
 - Continuous space



How to do robotics research

- **Find a problem**

- ✓ A problem only in your imagination is not a problem at all.
- ✓ A robotician must be an engineer first.
- ✓ Hot topic is just hot.
- ✓ Be honest.

- **Solve a problem**

- ✓ Don't intentionally making things complicated.
- ✓ Simple but effective solution is always preferable.
- ✓ Simulation tells nothing, show everyone real robots.
- ✓ Solve real problems.
- ✓ Solve it 100%, or not.



How to do motion planning

- Overall knowledge of planning
 - ✓ Choose suitable methods for different scenarios.
 - ✓ Design customized strategy.
- Dirty hands
 - ✓ Don't wait, don't just read papers. Do it yourself.
 - ✓ A lot of coding work.
 - ✓ A lot of field work.
- Know the whole system well
 - ✓ Take care every component in your robot.



Groups and Researchers

University of Pennsylvania

- GRASP Lab,Vijay Kumar
Research Interests: planning, control, swarm
Homepage: www.kumarrobotics.org

Massachusetts Institute of Technology

- Jonathan How
Research Interests: modelling, control, planning
Homepage: www.mit.edu/~jhow
- Nicholas Roy
Research Interests: perception, learning
Homepage: groups.csail.mit.edu/rrg

Carnegie Mellon University

- Nathan Michael
Homepage: www.rislab.org
- Sebastian Scherer
Research Interests: perception, planning
Homepage: theairlab.org

University of California, Berkeley

- Markus Mueller
Research Interests: control, planning

ETH Zurich

- ASL Team, Roland Siegwart
Research Interests: perception, control
Homepage: asl.ethz.ch
- Raffaello D'Andrea
Research Interests : control, swarm
Homepage: raffaello.name

University of Zurich

- Davide Scaramuzza
Research Interests : perception, control
Homepage: rpg.ifi.uzh.ch

Hong Kong University of Science Technology

- Shaojie Shen
Research Interests : UAV
Homepage: uav.ust.hk
- Ming Liu
Research Interests : UGV
Homepage: ram-lab.com



Young researchers who most related to me



Helen Oleynikova

helenol.github.io

Graduate at Jan. 2019, from ASL team, ETH

Supervised by Roland Siegwart

Author of **VoxBlox**

Planning and mapping



Sikang Liu

github.com/sikang

Graduate at Aug. 2018, from GRASP Lab, UPenn

Supervised by Vijay Kumar

Planning



Course Outline



Front-end: Path finding

- SEARCH-BASED PATH FINDING

- Graph Search Basis
- Dijkstra and A*
- Jump Point Search
- Homework

- SAMPLING-BASED PATH FINDING

- Probabilistic Road Map
- Rapidly-exploring Random Tree (RRT)
- Optimal Sampling-based Methods
- Advanced Sampling-based Methods
- Homework

- KINODYNAMIC PATH FINDING

- Introduction
- State-state Boundary Value Optimal Control Problem
- State Lattice Search
- Kinodynamic RRT*
- Hybrid A*
- Homework



Back-end: Trajectory Generation

- MINIMUM SNAP TRAJECTORY GENERATION
 - Differential Flatness
 - Minimum Snap Optimization
 - Closed-form Solution to Minimum Snap
 - Time Allocation
 - Implementation in Practice
 - Homework
- SOFT AND HARD CONSTRAINED TRAJECTORY OPTIMIZATION
 - Soft Constrained Trajectory Optimization
 - Hard Constrained Trajectory Optimization
 - Homework



MDP & MPC

- MARKOV DECISION PROCESS-BASED PLANNING
 - Uncertainties in Planning and MDP
 - Minimax Cost Planning and Expected Cost Minimal Planning
 - Value Iteration and Real-Time Dynamic Programming
 - Homework
- MODEL PREDICTIVE CONTROL FOR ROBOTICS PLANNING
 - Introduction
 - Linear MPC
 - Non-linear MPC
 - Homework



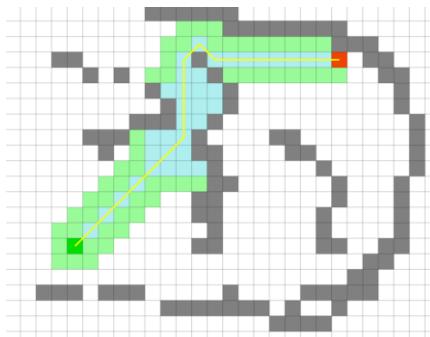
Overview



Front-end: Path Finding

- Sampling-based methods
 - Probabilistic roadmap (PRM)
 - Rapidly exploring random tree (RRT)
 - RRT*, informed RRT*
- Search-based methods
 - General graph search: DFS, BFS
 - Dijkstra and A* search
 - Jump point search

RRT example

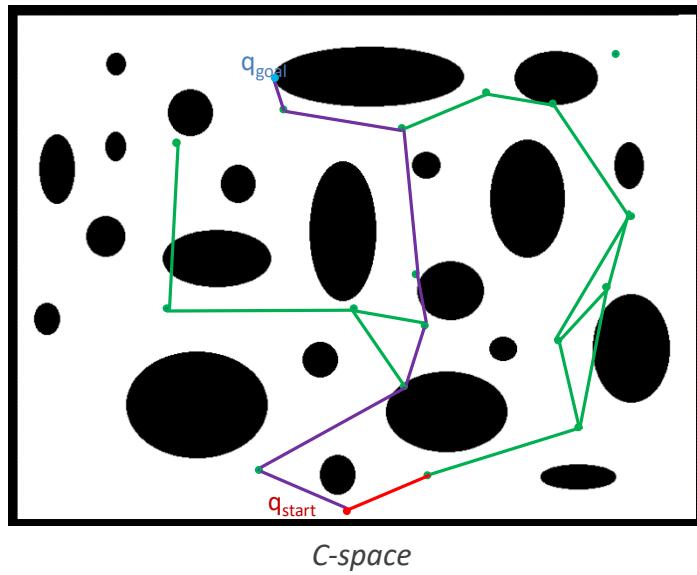


A* search example



Sampling-based Method

Probabilistic Roadmap (PRM)

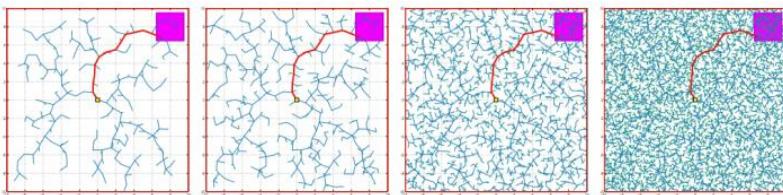




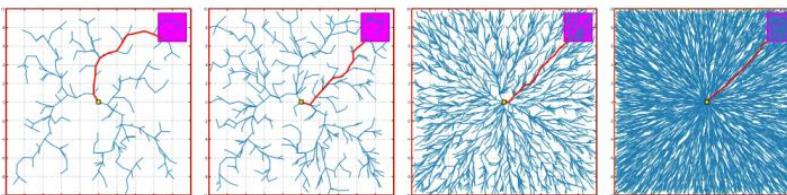
Sampling-based Method

RRT* vs RRT

RRT

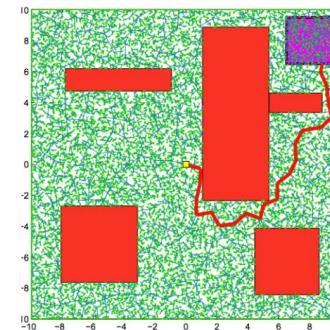


RRT*

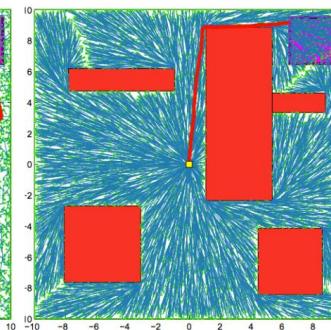


Source: Karaman and Frazzoli

RRT



RRT*

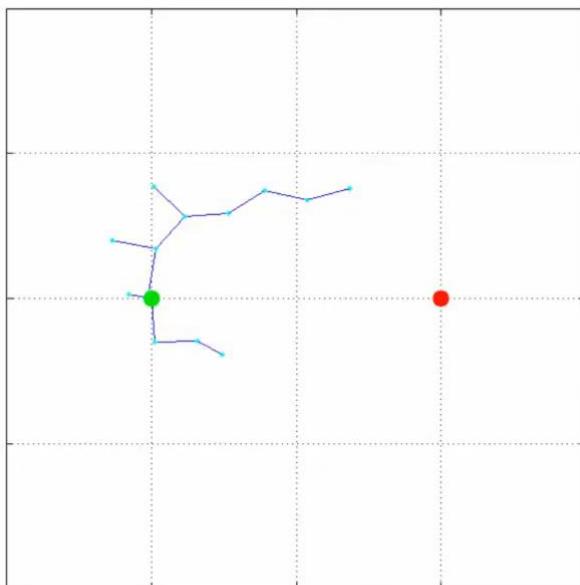




Sampling-based Method

Informed RRT*

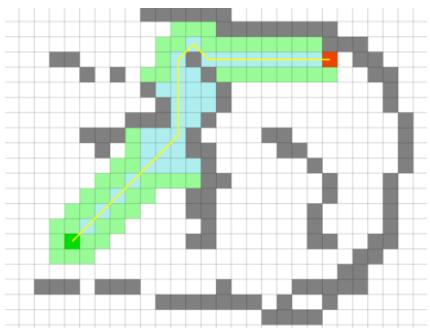
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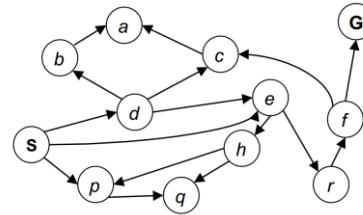


Search-based Method

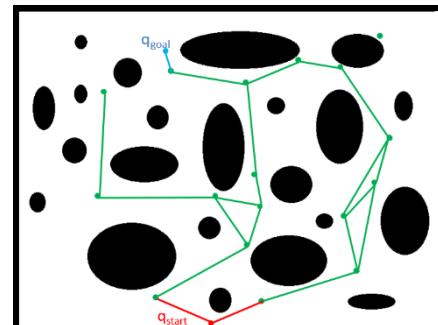
- For every search problem, there's a corresponding state space graph
- Connectivity between nodes in the graph is represented by (directed or undirected) edges



Grid-based graph: use grid as vertices and grid connections as edges



*Ridiculously tiny search graph
for a tiny search problem*



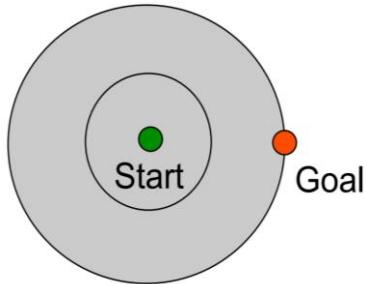
The graph generated by probabilistic roadmap (PRM)



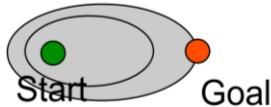
Search-based Method

Dijkstra's vs. A*

- Dijkstra's algorithm expanded in all directions



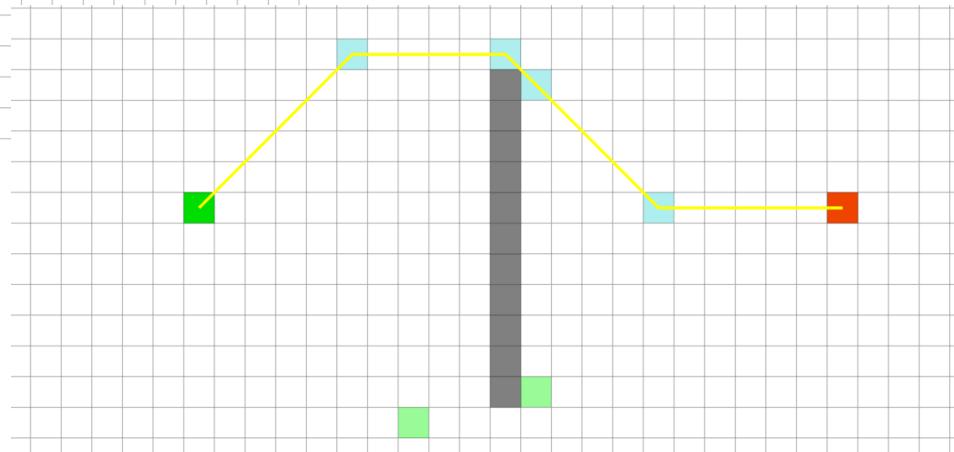
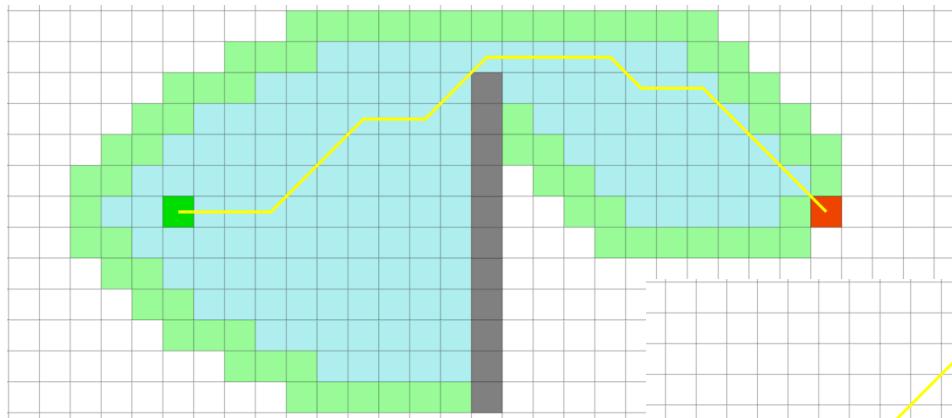
- A* expands mainly towards the goal, but does not hedge its bets to ensure optimality





Search-based Method

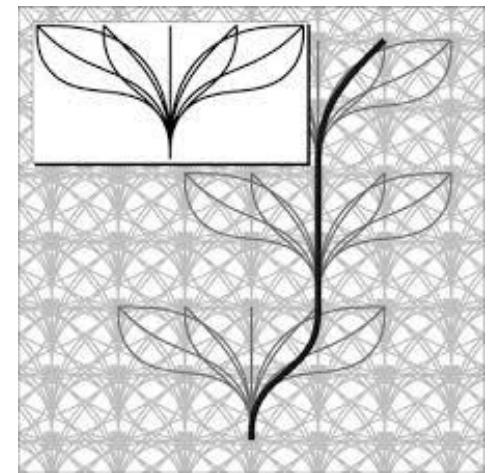
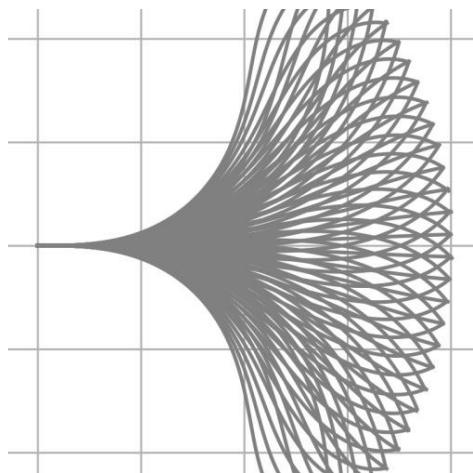
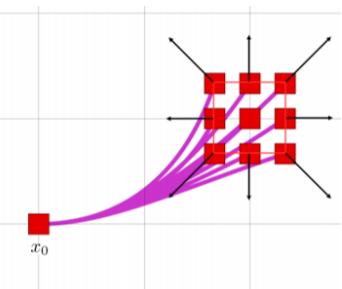
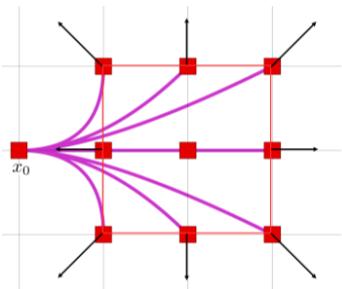
A* vs. JPS





Kinodynamic Path Finding

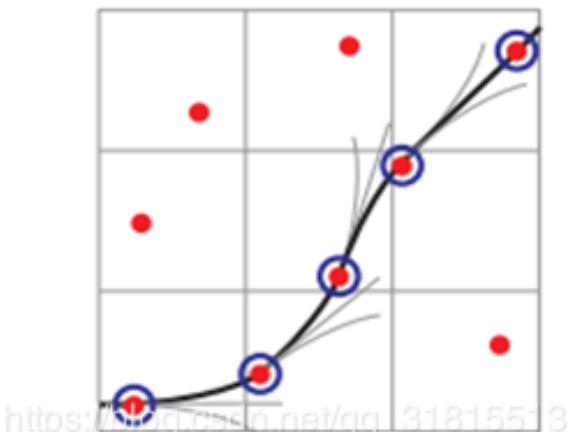
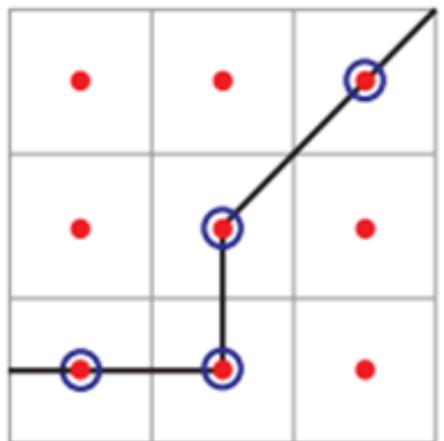
State Lattice Search





Kinodynamic Path Finding

Hybrid A*



<https://blog.csail.mit.edu/cjq/318155/> 3

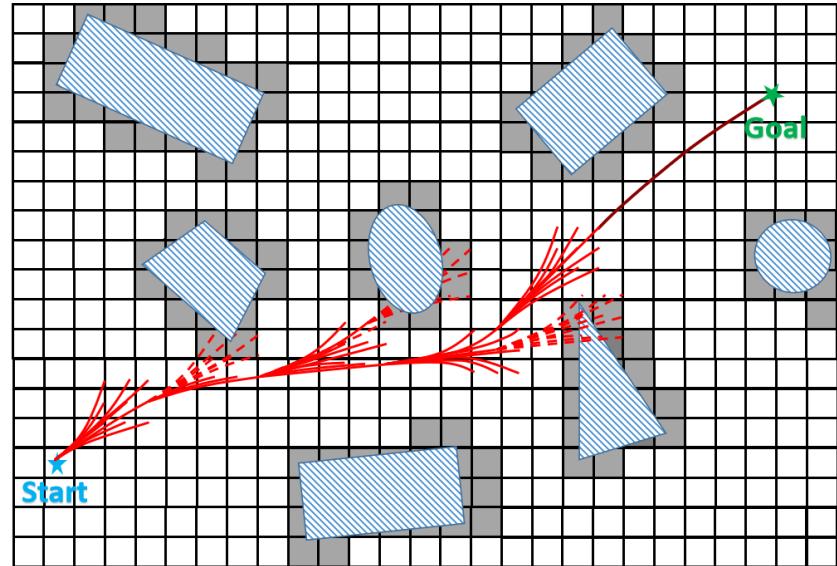
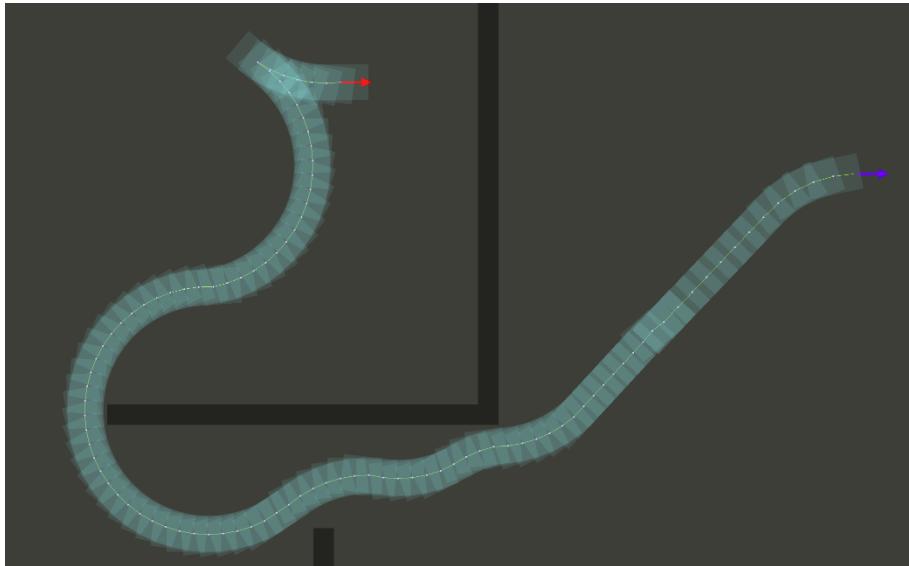
1. Follow A* algorithm
2. Forward simulate states with different discrete control inputs
3. Keep only 1 state in each grid

Discrete control



Kinodynamic Path Finding

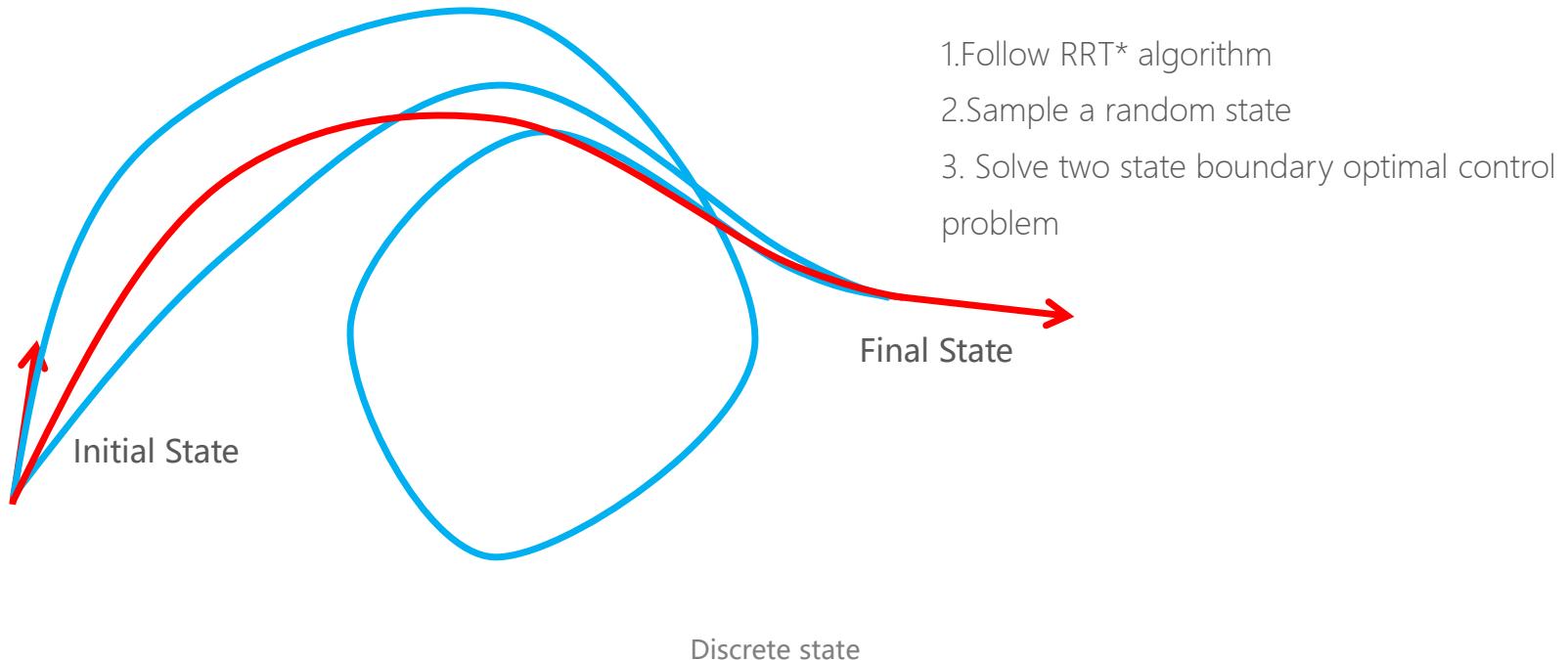
Hybrid A*





Kinodynamic Path Finding

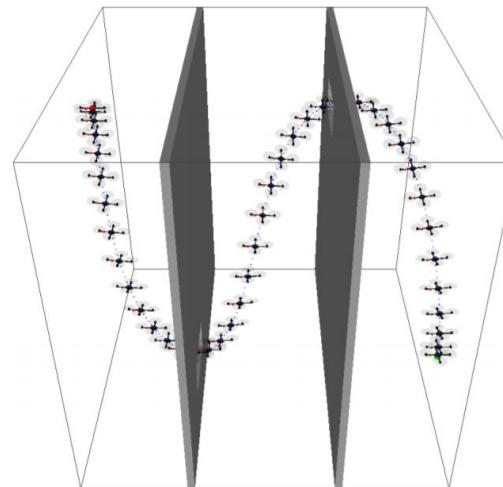
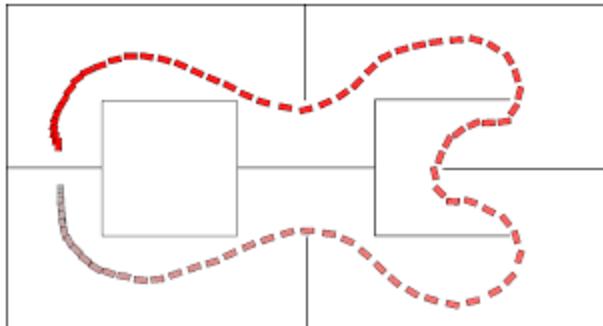
Kinodynamic RRT*





Kinodynamic Path Finding

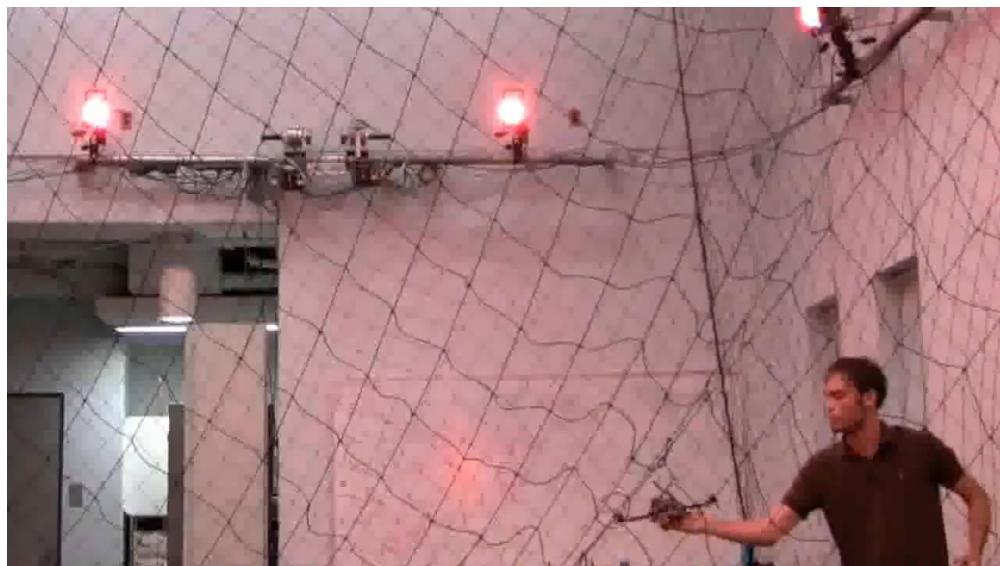
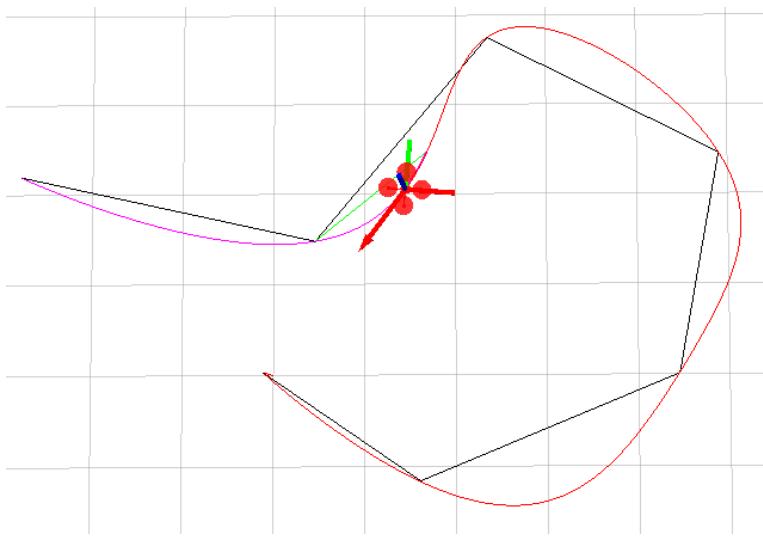
Kinodynamic RRT*





Back-end: Trajectory Optimization

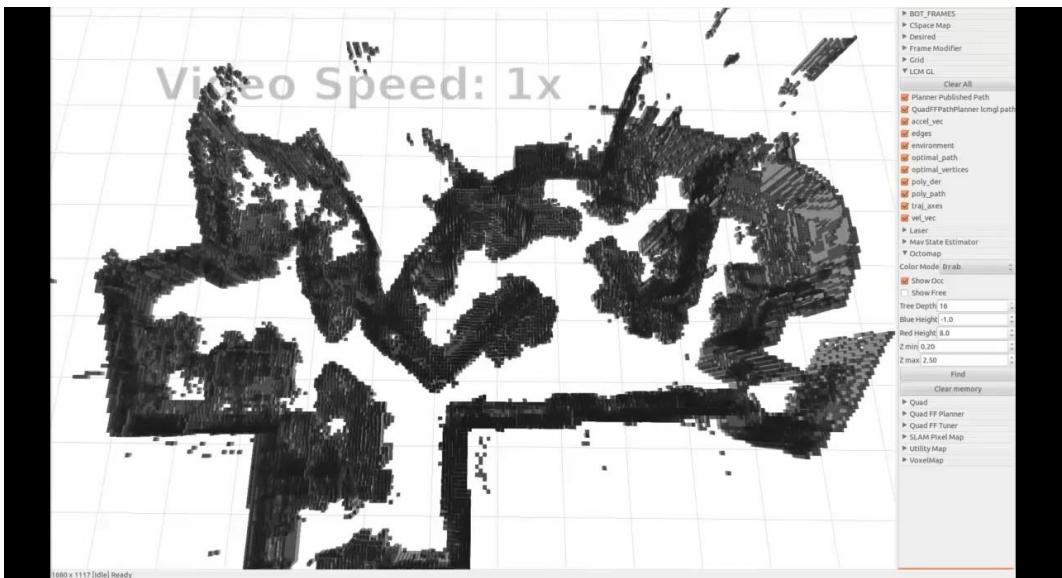
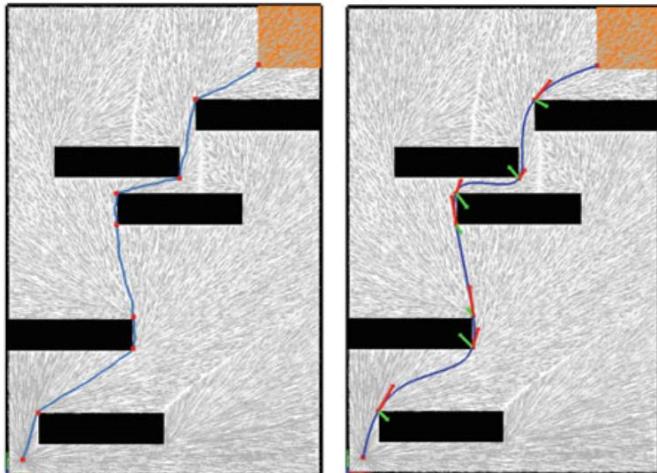
Basic Minimum-snap





Back-end: Trajectory Optimization

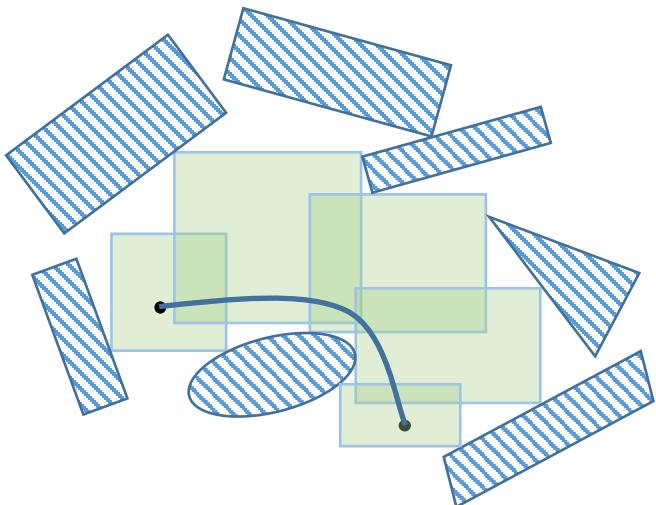
Basic Minimum-snap



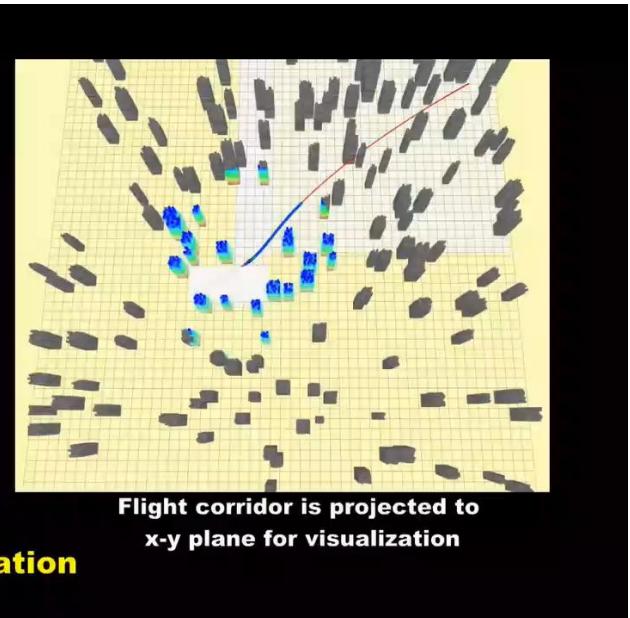


Back-end: Trajectory Optimization

Hard constrained Minimum-snap



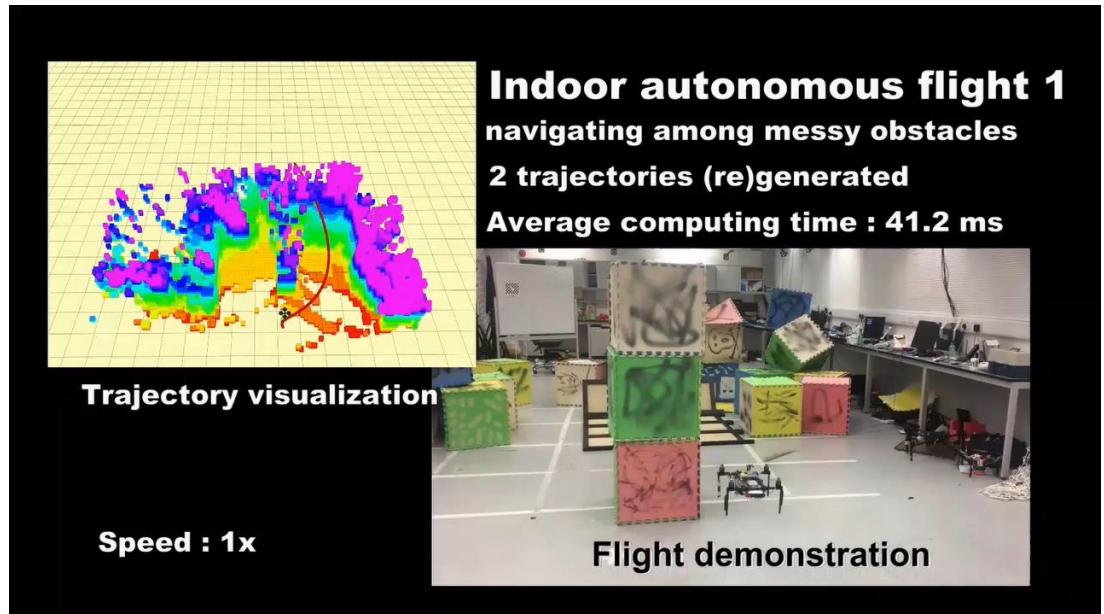
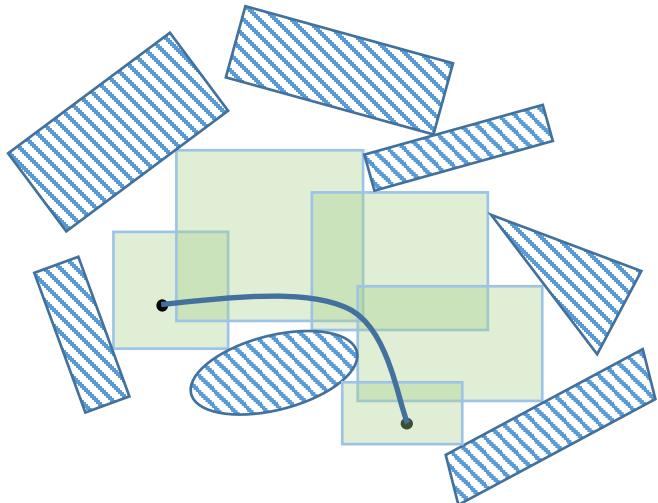
Blue curve : trajectory in execution horizon
Red curve : current trajectory
White cube : flight corridor
Colorful voxels : mapped obstacles
Grey voxels : un-mapped obstacles
Green arrow : velocity
Yellow arrow : acceleration





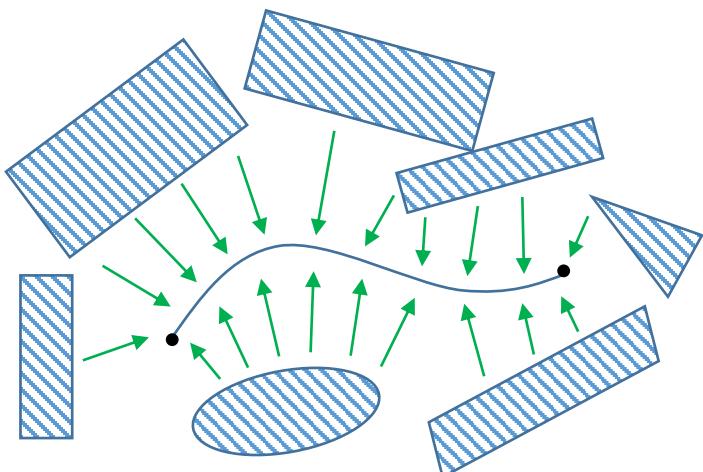
Back-end: Trajectory Optimization

Hard constrained Minimum-snap

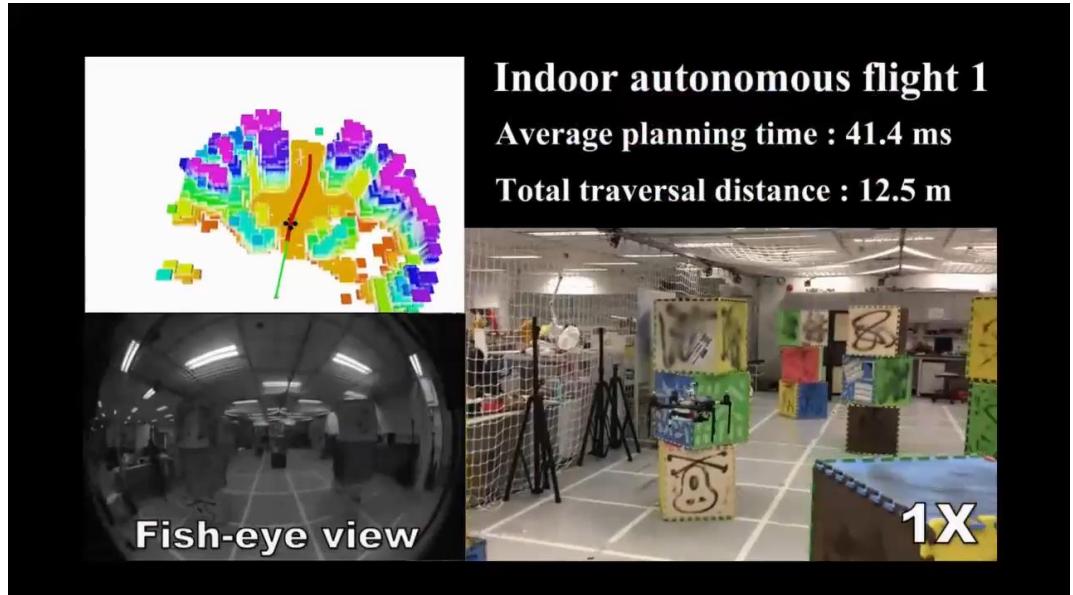




Back-end: Trajectory Optimization

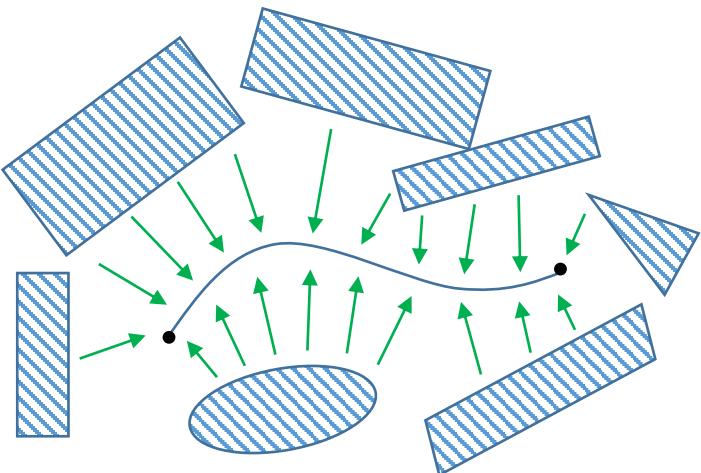


Soft constrained Minimum-snap

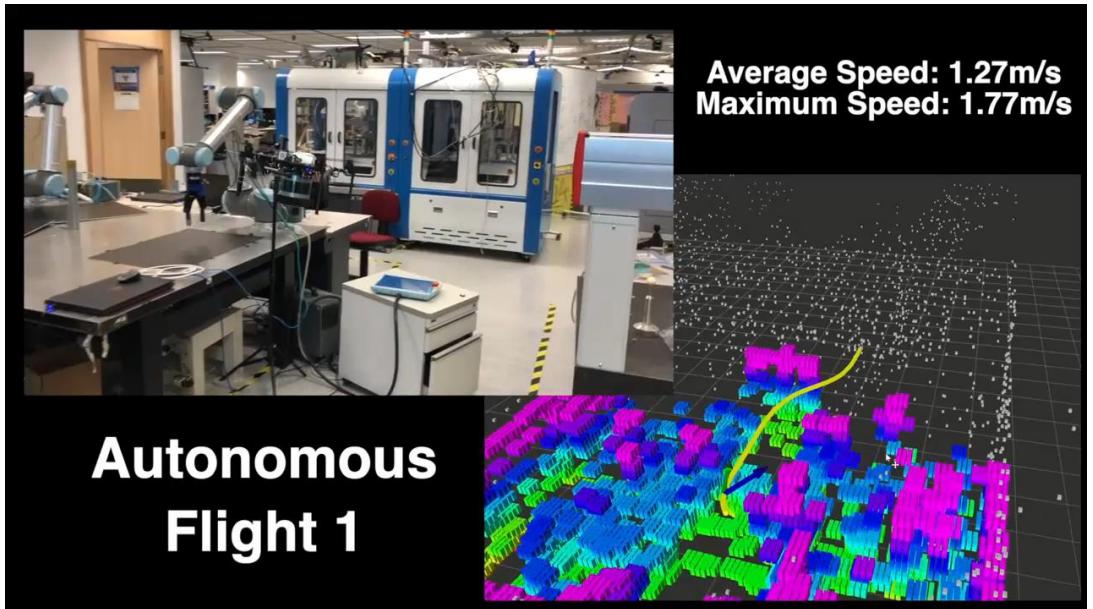




Back-end: Trajectory Optimization

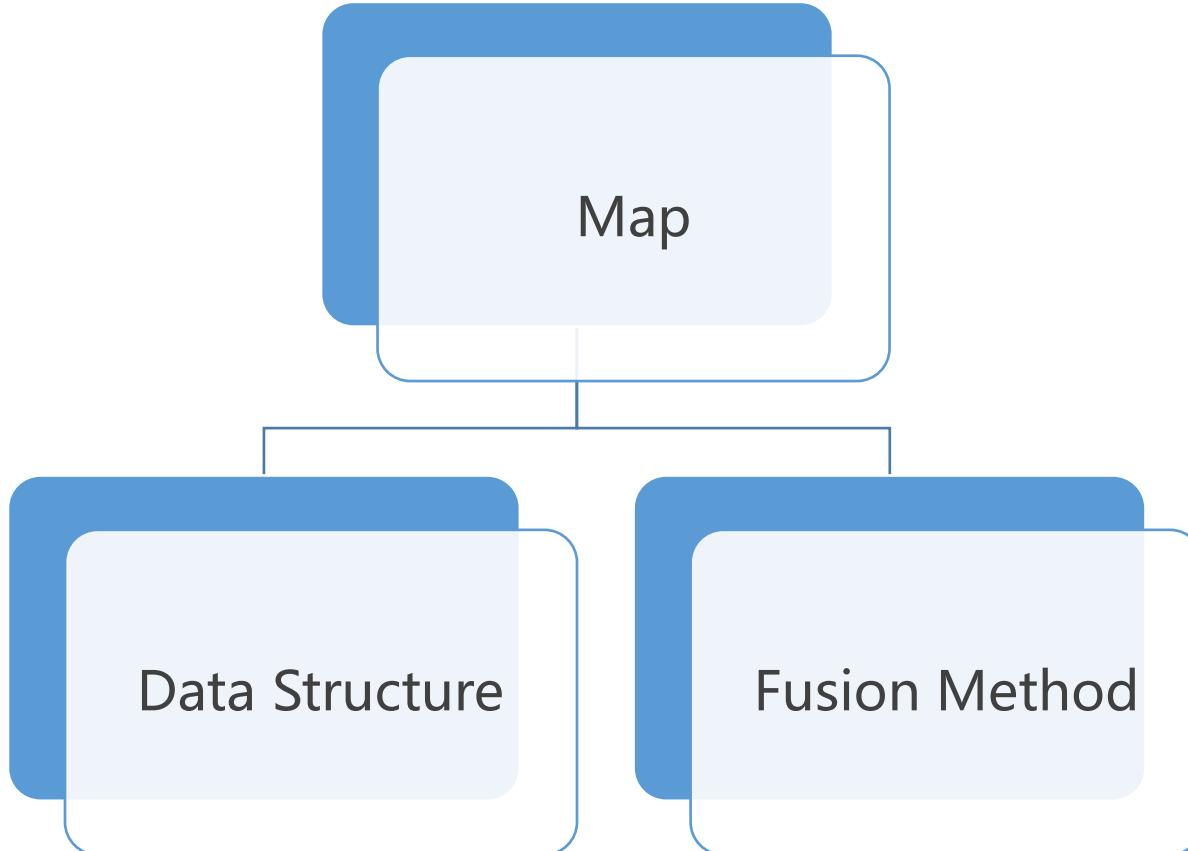


Soft constrained Minimum-snap



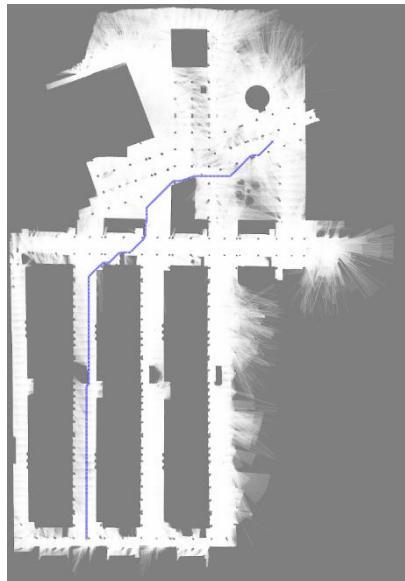
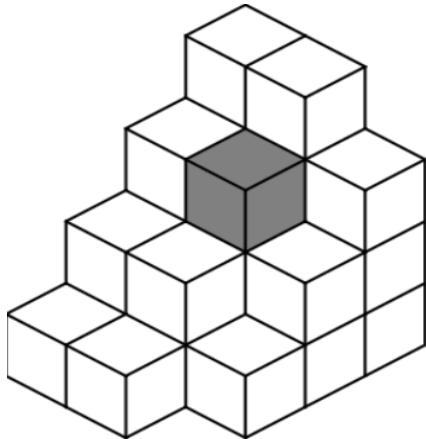


Map Representation

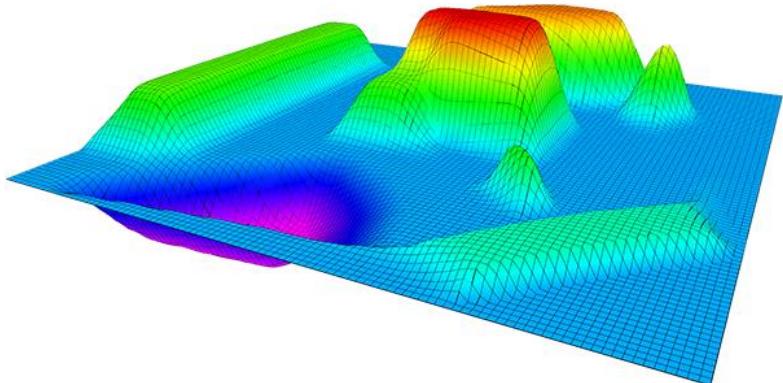




Occupancy grid map



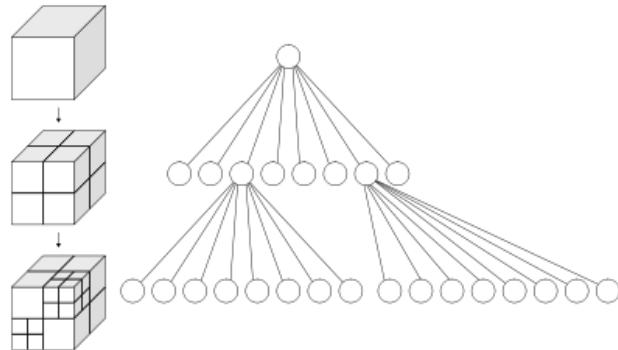
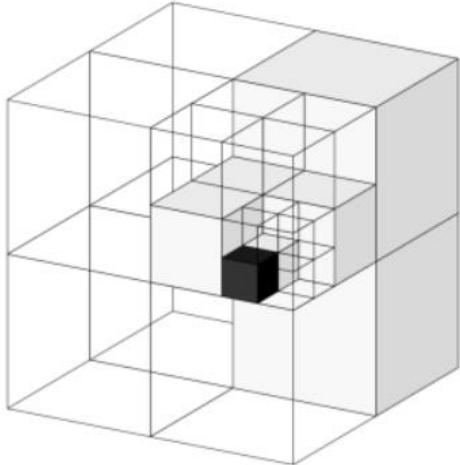
- Most Dense
- Structural
- Direct Index Query



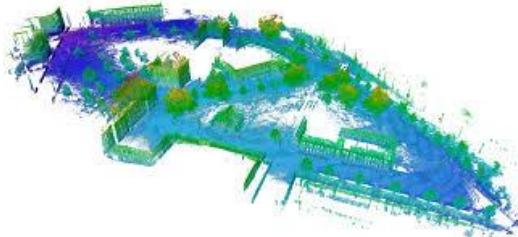
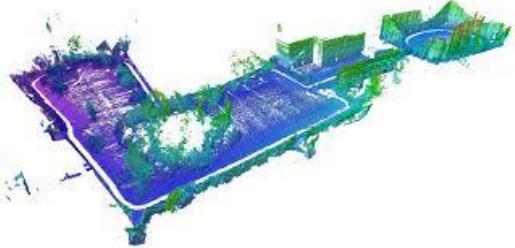
https://github.com/ANYbotics/grid_map



Octo-map



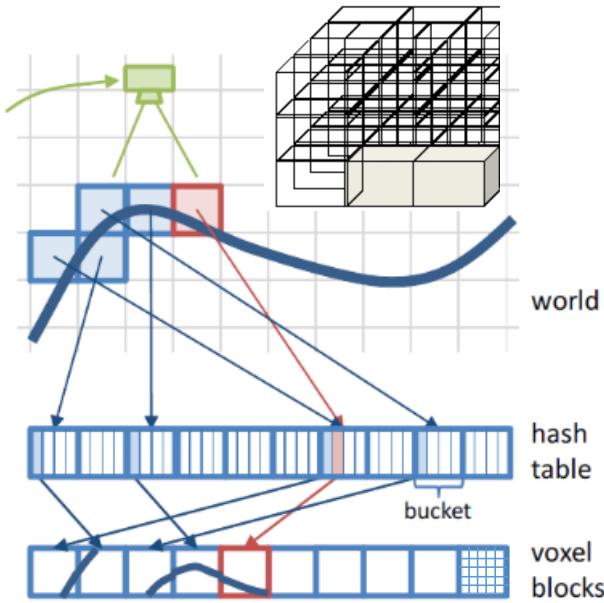
- Sparse
- Structural
- Indirect Index Query



<https://octomap.github.io/>



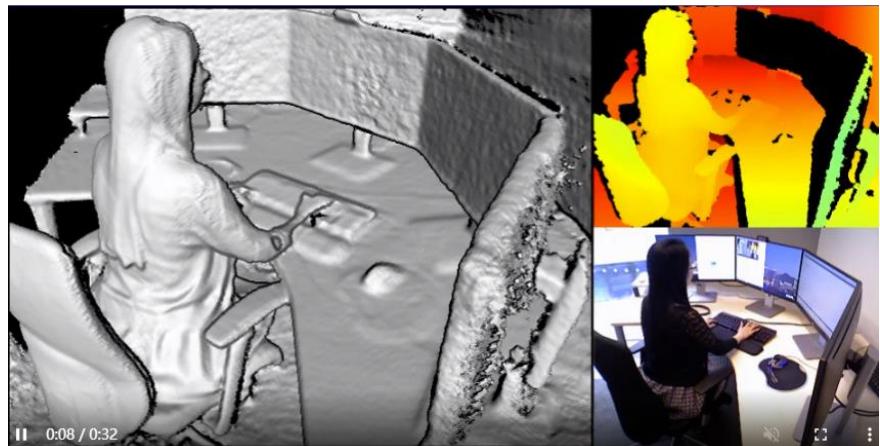
Voxel hashing



Voxel Hashing:

<https://github.com/niessner/VoxelHashing>

- Most Sparse
- Structural
- Indirect Index Query

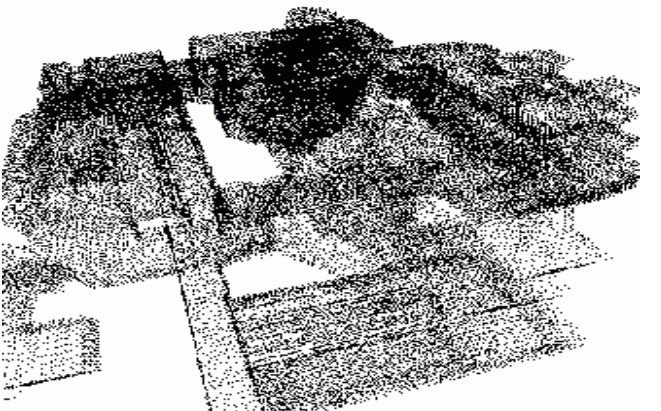


InfiniTAM:

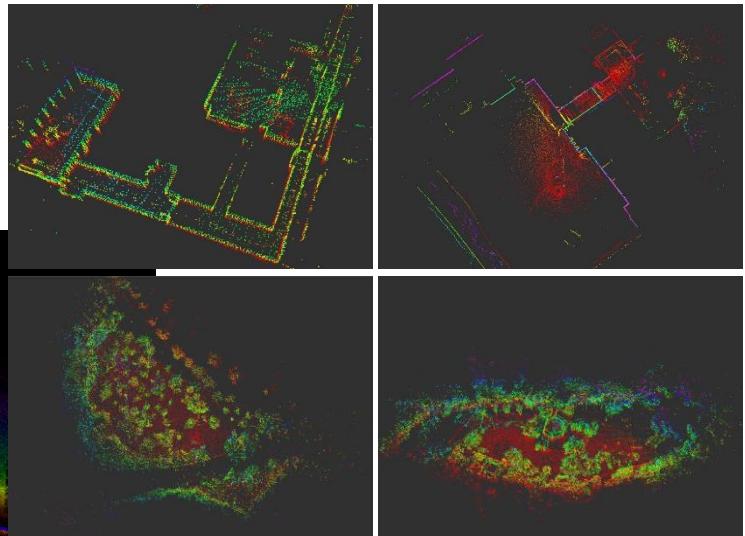
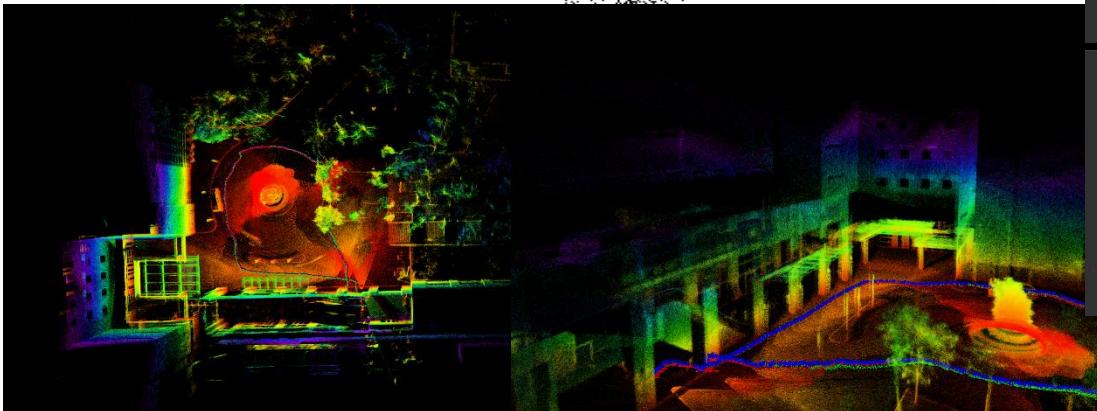
<http://www.robots.ox.ac.uk/~victor/infinitam/>



Point cloud map



- Un-ordered
- No Index Query

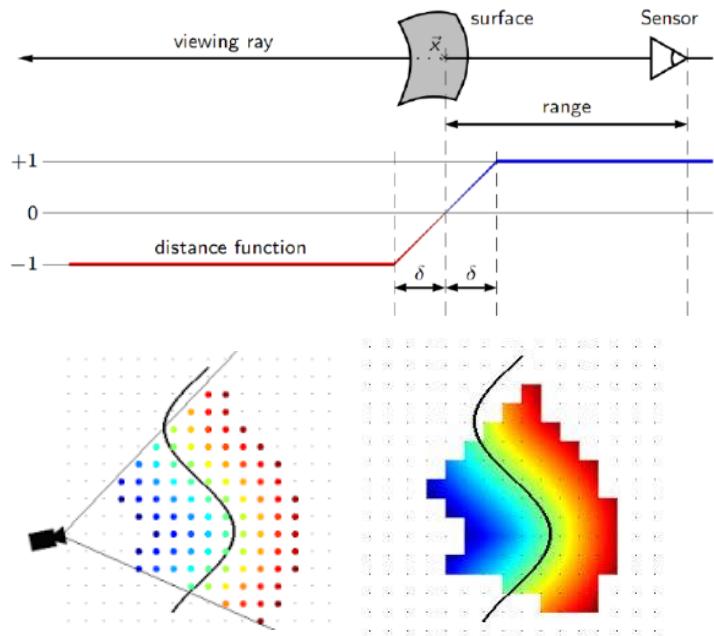


PCL
<http://pointclouds.org/>



TSDF map

Truncated Signed Distance Functions



OpenChisel

<https://github.com/personalrobotics/OpenChisel>



ESDF map

Euclidean Signed Distance Functions
Incremental Update, Global Map

Running the Cow_and_Lady Dataset[1]
Compare with Voxblox[2]

[1] <https://projects.asl.ethz.ch/datasets/doku.php?id=iros2017/>

[2] Helen Olynikova, Zachary Taylor, Marius Fehr, Juan Nieto, and Roland Siegwart, "Voxblox: Building 3D Signed Distance Fields for Planning", In IEEE Int. Conf. on Intelligent Robots and Systems (IROS), October 2017.

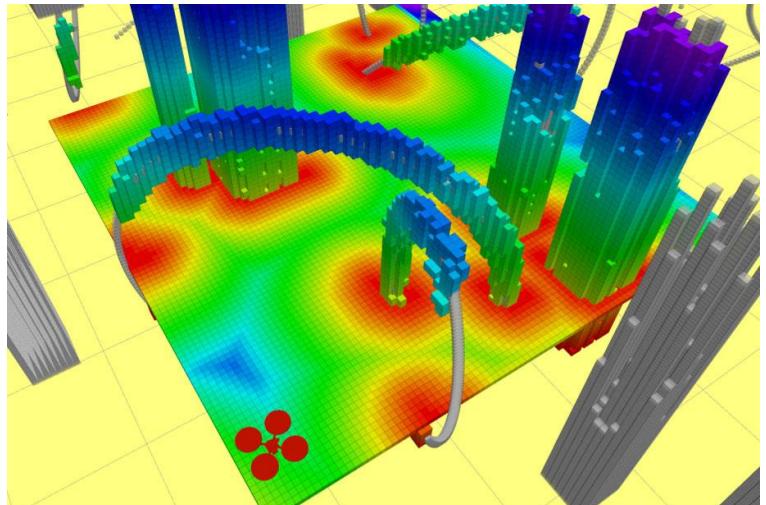
VoxBlox

<https://github.com/ethz-asl/voxblox>

FIESTA

<https://github.com/HKUST-Aerial-Robotics/FIESTA>

Batch Update, Local Map



Distance Transforms of Sampled Functions, PF Felzenswalb

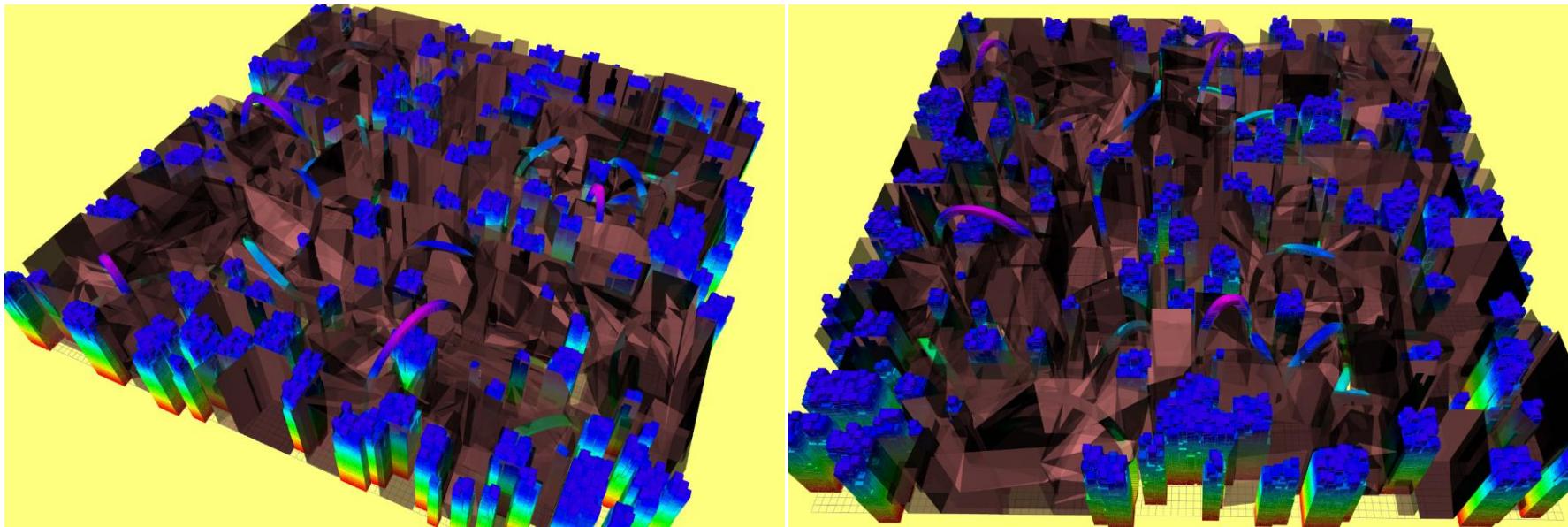
TRR's Local Map

<https://github.com/HKUST-Aerial-Robotics/Teach-Repeat-Replan>



More ?

Free-space Roadmap

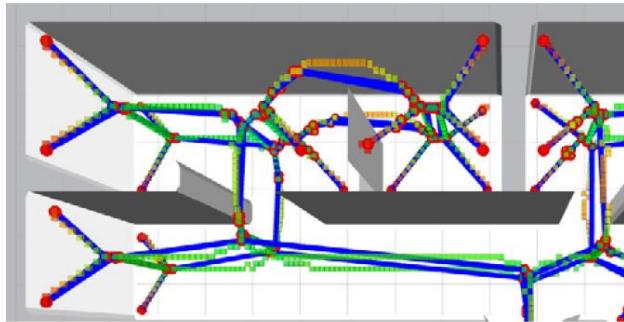


<https://github.com/HKUST-Aerial-Robotics/Teach-Repeat-Replan>

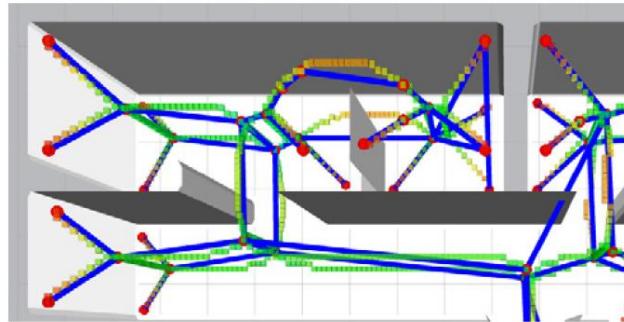


More ?

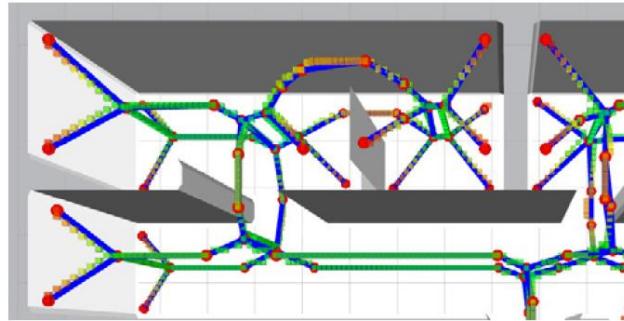
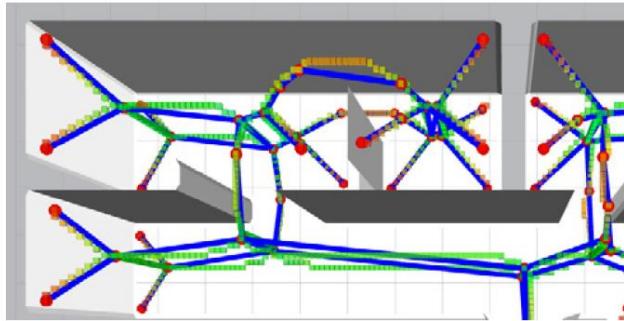
Voronoi Diagram Map



(a)



(b)



https://github.com/ethz-asl/mav_voxblox_planning



Pre-requirement



Linux

- Linux file system
- How to install software in linux
- Useful commands



C++ and GCC Toolchain

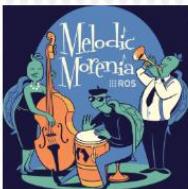
- C with class ?
- Gcc, Makefile, CMakeList
- Write CMakeList
- How to solve problems: google and document



ROS

ROS

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ROS Melodic Morenia
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- Ubuntu 16.04 + ros kinetic is recommended



Matlab

- Please install Matlab



Homework



Thanks for Listening!

