# 0.1 Markov Model

# 0.1.1 NCX Channel Inactivation Model

$$\begin{array}{c|c} E_2 3N_o \longleftrightarrow E_2 \longleftrightarrow E_2 C_o \\ k_1 \parallel k_2 & k_4 \parallel k_3 \\ E_0 3N & E_0 C \\ k_7 \parallel k_8 & k_6 \parallel k_5 \\ E_1 3N_1 & & & & & & & & & & & \\ E_1 3N_1 & & & & & & & & & & \\ E_1 3N_1 & & & & & & & & & & \\ \end{array}$$

Figure 1: NCX Ion Channel Model

## Notations

- $\bullet$   $E_1$ : States with binding sites oriented to the cytoplasmic sides
- $\bullet$   $E_2$ : States with binding sites oriented to the extra-cellular sides
- $E_13N_i$ : States with binding sites oriented to the cytoplasmic sides containing 3 Na+ions
- $E_03N$ : States with binding sites occluded with 3 Na+ ions
- $E_23N_0$ : States with binding sites oriented to the extra cellular sides with 3 Na+ ions
- $E_1C_1$ : States with binding sites oriented to the cytoplasmic sides containing 1 Ca++
  ion
- $E_0C$ : States with binding sites occluded with 1 Ca++ ion
- $E_2C_0$ : States with binding sites oriented to the extra cellular sides with 1 Ca++ ion

# Simultaneous Diff Equation

$$\begin{split} &\frac{d(E_23N_o)}{dt} = k_1(E_03N) - k_2(E_23N_o) \\ &\frac{d(E_03N)}{dt} = k_7(E_13N_i) + k_2(E_23N_o) - (k_1 + k_8)(E_03N) \\ &\frac{d(E_13N_i)}{dt} = k_{bak}(E_i3N_i) + k_8(E_o3N) - (k_{inact} + k_7)(E_13N_i) \\ &\frac{d(E_i3N_i)}{dt} = k_{inact}(E_13N_i) - k_{bak}(E_i3N_i) \\ &\frac{d(E_23N_i)}{dt} = k_4(E_oC) - k_3(E_2C_o) \\ &\frac{d(E_2C_o)}{dt} = k_3(E_2C_o) + k_6(E_1C_i) - (k_4 + k_5)(E_oC) \\ &\frac{d(E_1C_i)}{dt} = k_5(E_oC) - k_6(E_1C_i) \end{split}$$

#### **Summed Version**

$$\frac{d(E_1)}{dt} = k_{bak}(E_i 3N_i) + k_8(E_o 3N) + k_5(E_o C) - (k_{inact} + k_7 + k_6)(E_1)$$

$$\frac{d(E_0 3N)}{dt} = k_7(E_1) + k_2(E_2) - (k_1 + k_8)(E_o 3N)$$

$$\frac{d(E_0 C)}{dt} = k_3(E_2) + k_6(E_1) - (k_4 + k_5)(E_o C)$$

$$\frac{d(E_2)}{dt} = k_1(E_o 3N) + k_4(E_o C) - (k_2 + k_3)E_2$$

$$\frac{d(E_i 3N_i)}{dt} = k_{inact}(E_1) - k_{bak}E_i 3N_i$$

$$E_i 3N_i = 1 - E_1 - E_2 - E_o C - E_o 3N$$

## Reduced Equation

$$\frac{d(E_1)}{dt} = k_{bak} - k_{bak}E_2 + (k_8 - k_{bak})(E_o3N) + (k_5 - k_{bak})(E_oC) 
- (k_{bak} + k_{inact} + k_7 + k_6)(E_1)$$

$$\frac{d(E_03N)}{dt} = k_7(E_1) + k_2(E_2) - (k_1 + k_8)(E_o3N)$$

$$\frac{d(E_oC)}{dt} = k_3(E_2) + k_6(E_1) - (k_4 + k_5)(E_oC)$$

$$\frac{d(E_2)}{dt} = k_1(E_o3N) + k_4(E_oC) - (k_2 + k_3)E_2$$

#### Constants

- Membrane Potential : Em = ...
- Kem :  $Kem = exp(0.5 \times (1 \gamma) \times Em \times \frac{F}{RT}) = ....$
- Rate Constan :  $k_1 = 10^4 \times Kem$
- Rate Constan :  $k_2 = F_{3no} \times \frac{10^4}{Kem}$
- Rate Constan :  $k_3 = F_{co} \times 5.17 \times 10^4 \times Kem$
- Rate Constan :  $k_4 = 5.17 \times 10^4$
- Rate Constan :  $k_5 = 5.17 \times 10^4$
- Rate Constan :  $k_6 = F_{ci} \times 5.17 \times 10^4$
- Rate Constan :  $k_7 = F_{3ni} \times 1.84 \times 10^4$
- Rate Constan :  $k_8 = 1.84 \times 10^4 \times$
- Rate Constan :  $k_{bak} = 0.12$
- Rate Constan:  $k_{in} = 0.8$

# 0.2 Quantum Algorithms

## 0.2.1 Stoicheometric Correction in NCX channel

Trapped ion Quantum Computer is already in practice. There are interesting application of Quantum Physics phenomena in Quantum Biology (e.g., Photosynthesis and Mutation). In case of trapped ion, the spin of ion can be considered as a quantum qubit. In this article we want to study the interaction of three Na ions and Ca ion during the exchange process in NCX channel.