



# Universalizing Approximate Query Processing

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Joseph Sorenson

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Junhao Wang

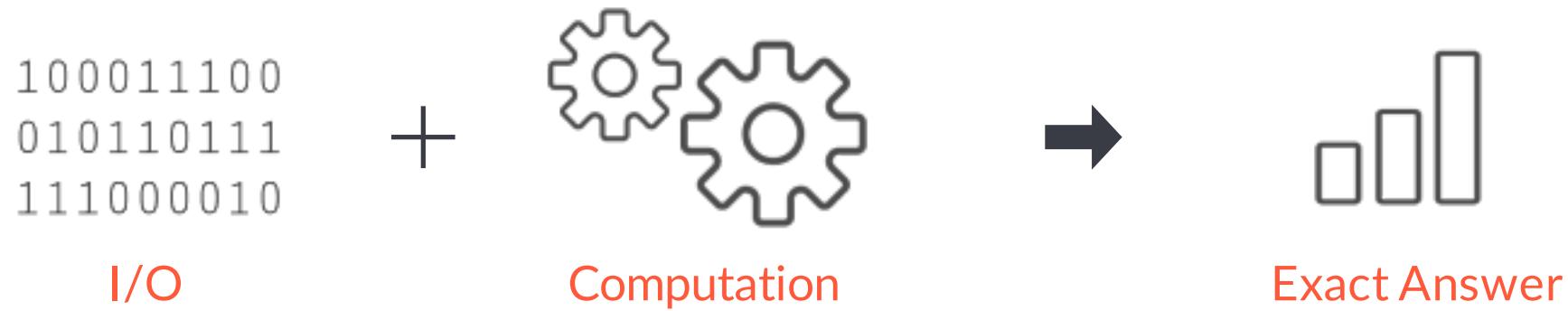


# Universal Approximate Query Processing

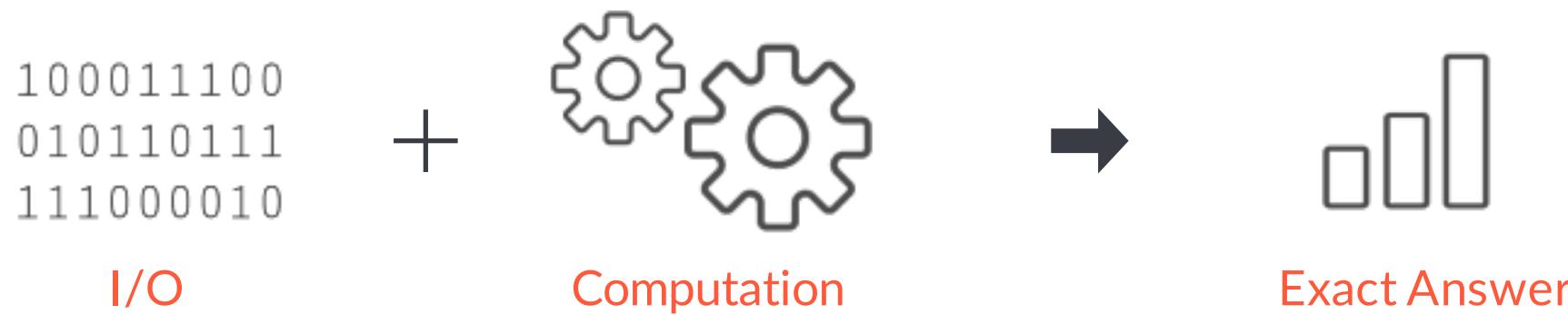


Universal  
Approximate Query Processing

# What is Approximate Query Processing (AQP)?



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Numerous studies:

*A latency > 2 seconds* is no longer interactive and negatively affects creativity!

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Human time: Money

Machine time: No one loves their EC2 bill!

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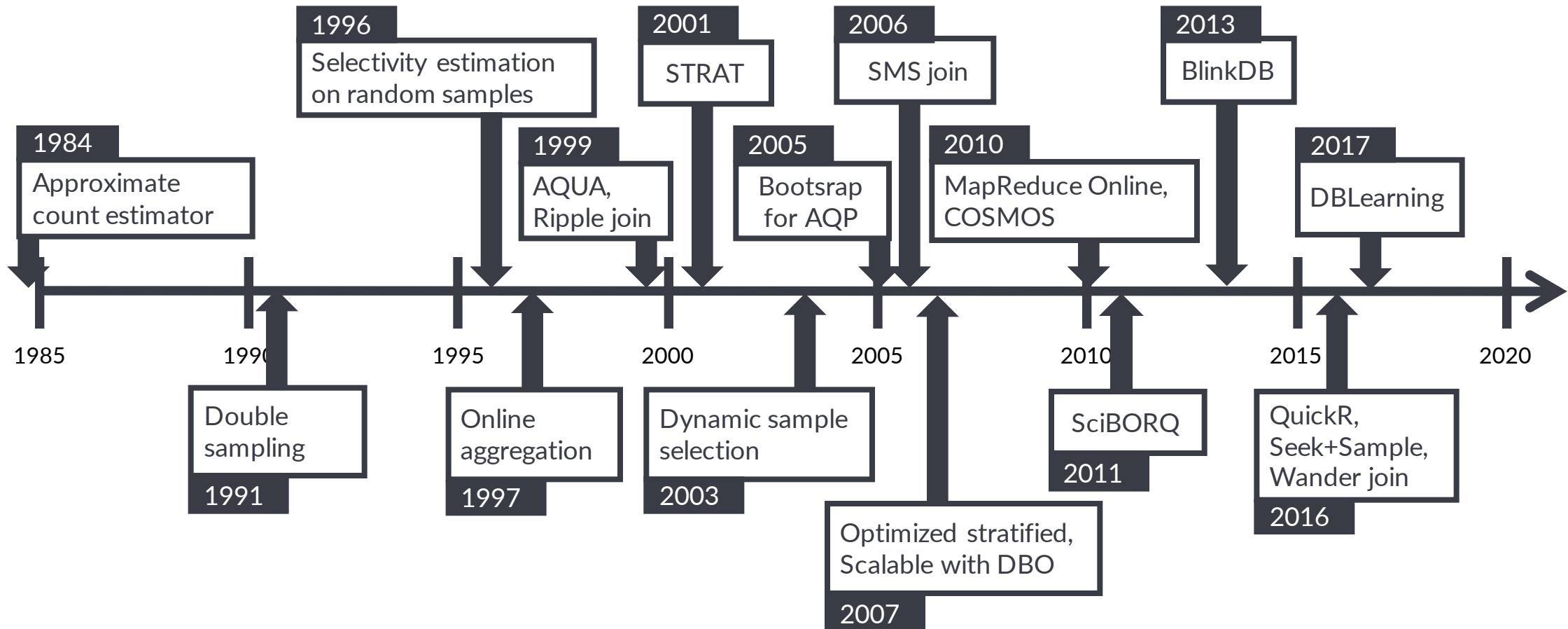
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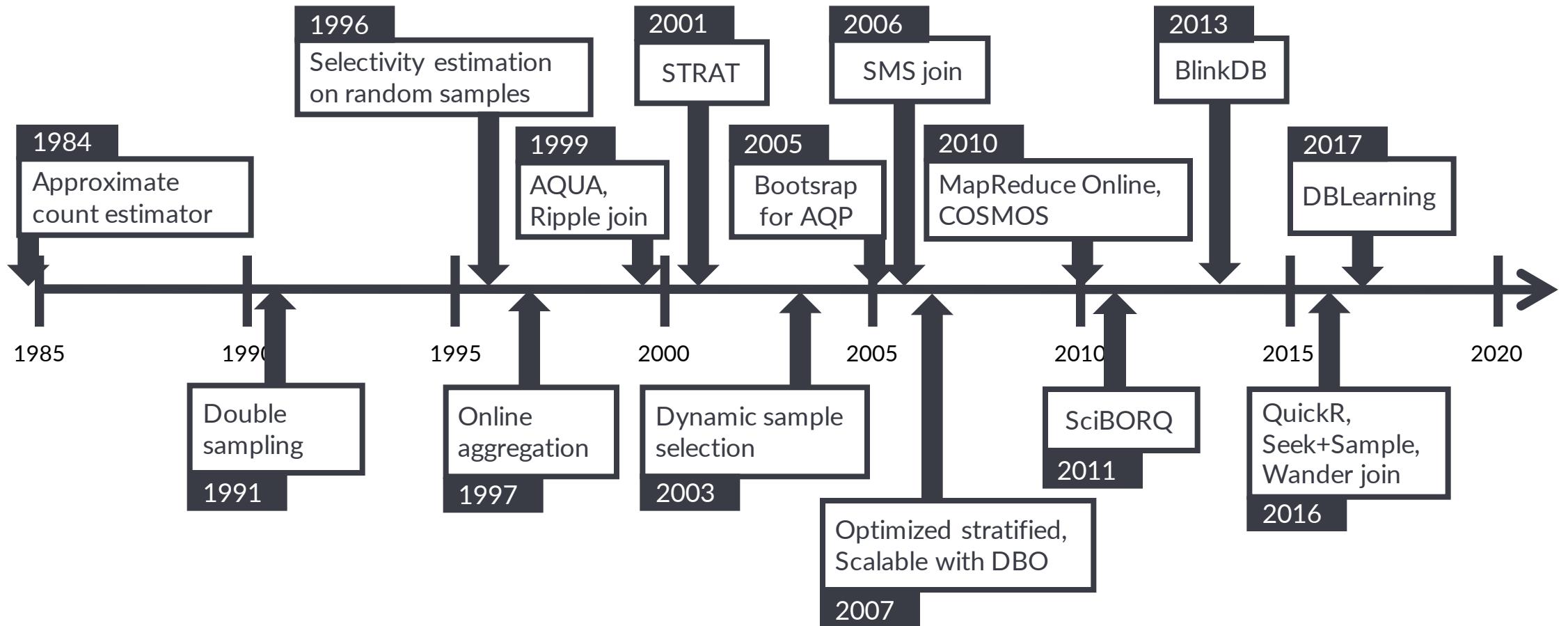


Jeff Bezos

# AQP research in academia



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*35 years of research, little industry adoption*

# AQP is hard to adopt

AQP typically requires **significant** modifications of DBMS internals

- Error estimation: [BlinkDB '13], [G-OLA '15], ...
- Query evaluation: [Online '97], [Join Synopses '99], ...
- Relational operators: [ABM '14], ...

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## Newer SQL-on-Hadoop systems: implementing standard features

*Users won't abandon their existing DBMS just to use AQP.*



# Built-in AQP functions in OLAP engines



APPROXIMATE  
PERCENTILE\_DISC



approx\_count\_distinct  
approx\_percentile



approxCountDistinct  
approxQuantile



NDV  
APX\_MEDIAN

count-distinct    or    quantile

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But, too little, too slow*

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## Limitations

1. Good **only when** the data does not fit in memory
2. Good **only for** flat queries: no error propagation
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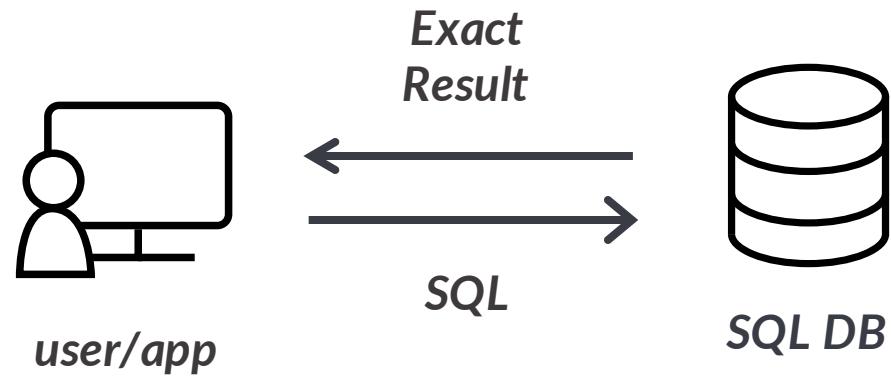
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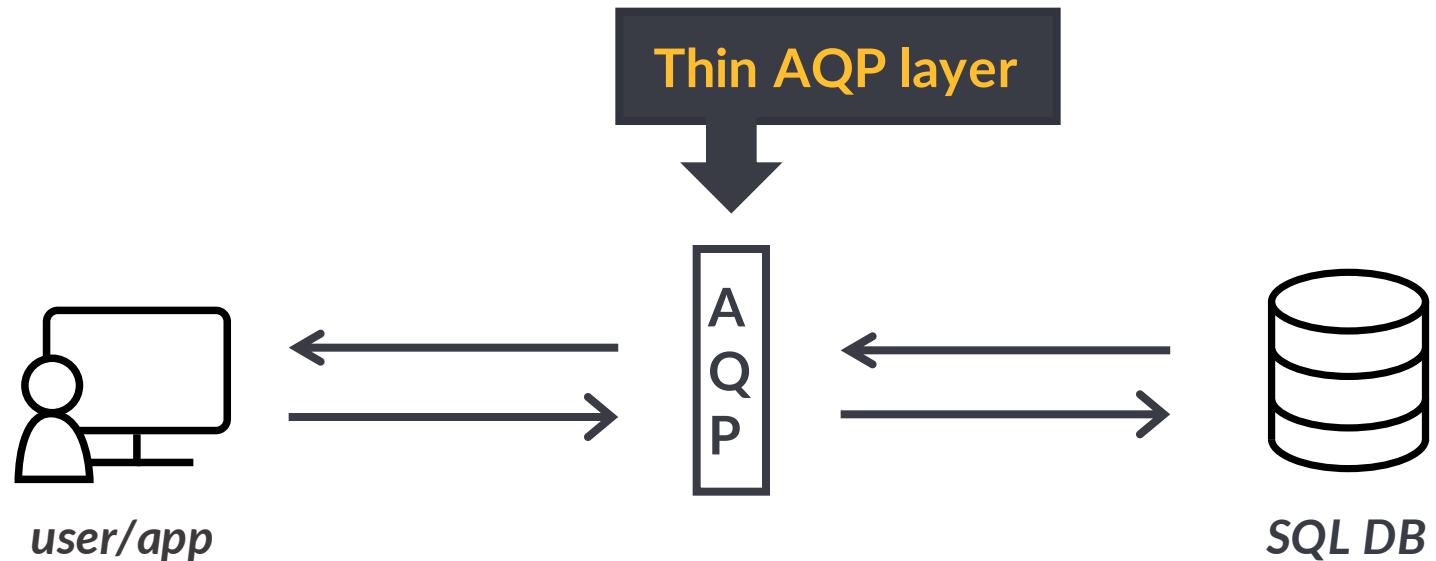
*Good progress!  
But, too little, too slow*

*Need for complete AQP solutions that are easy to adopt*

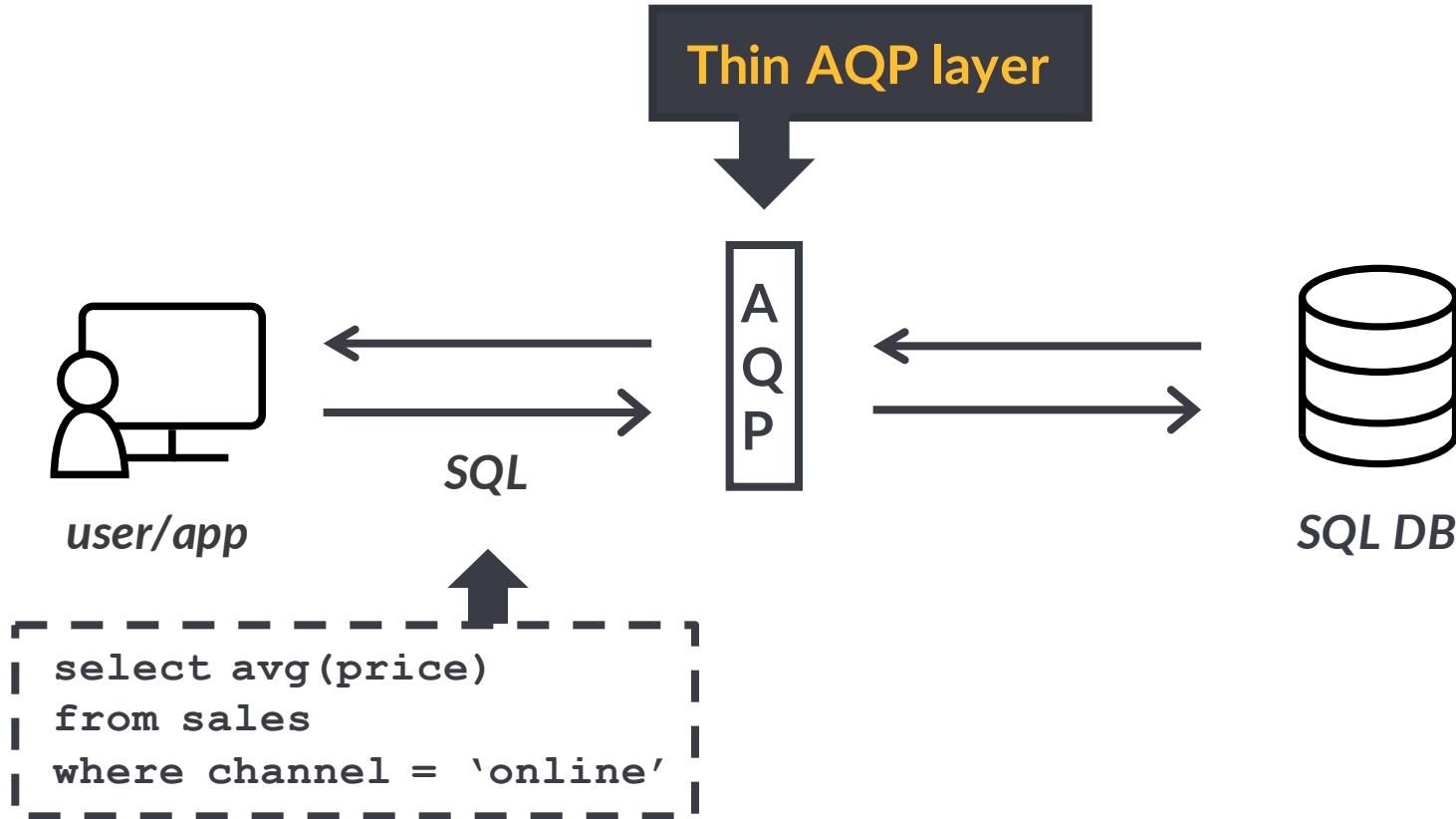
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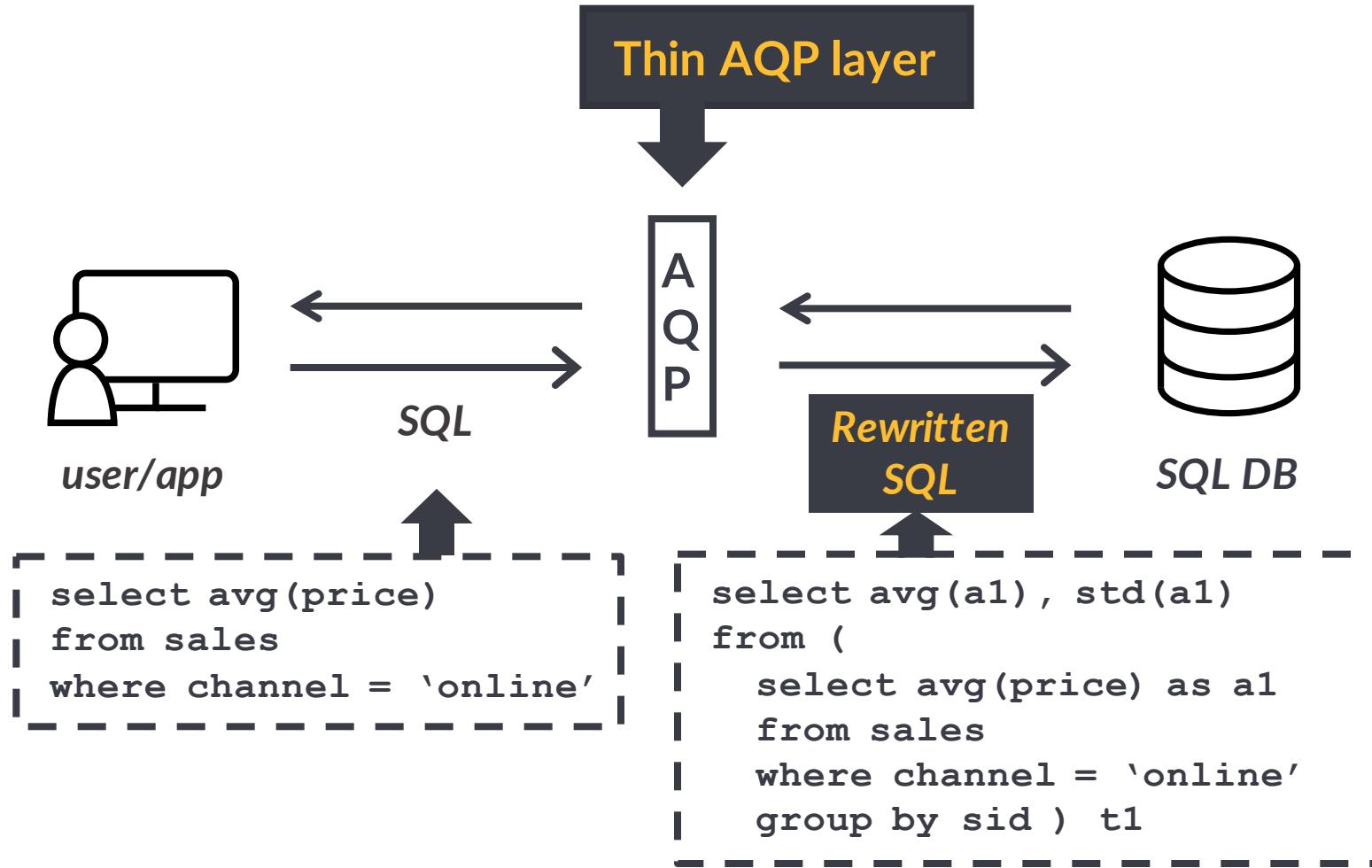
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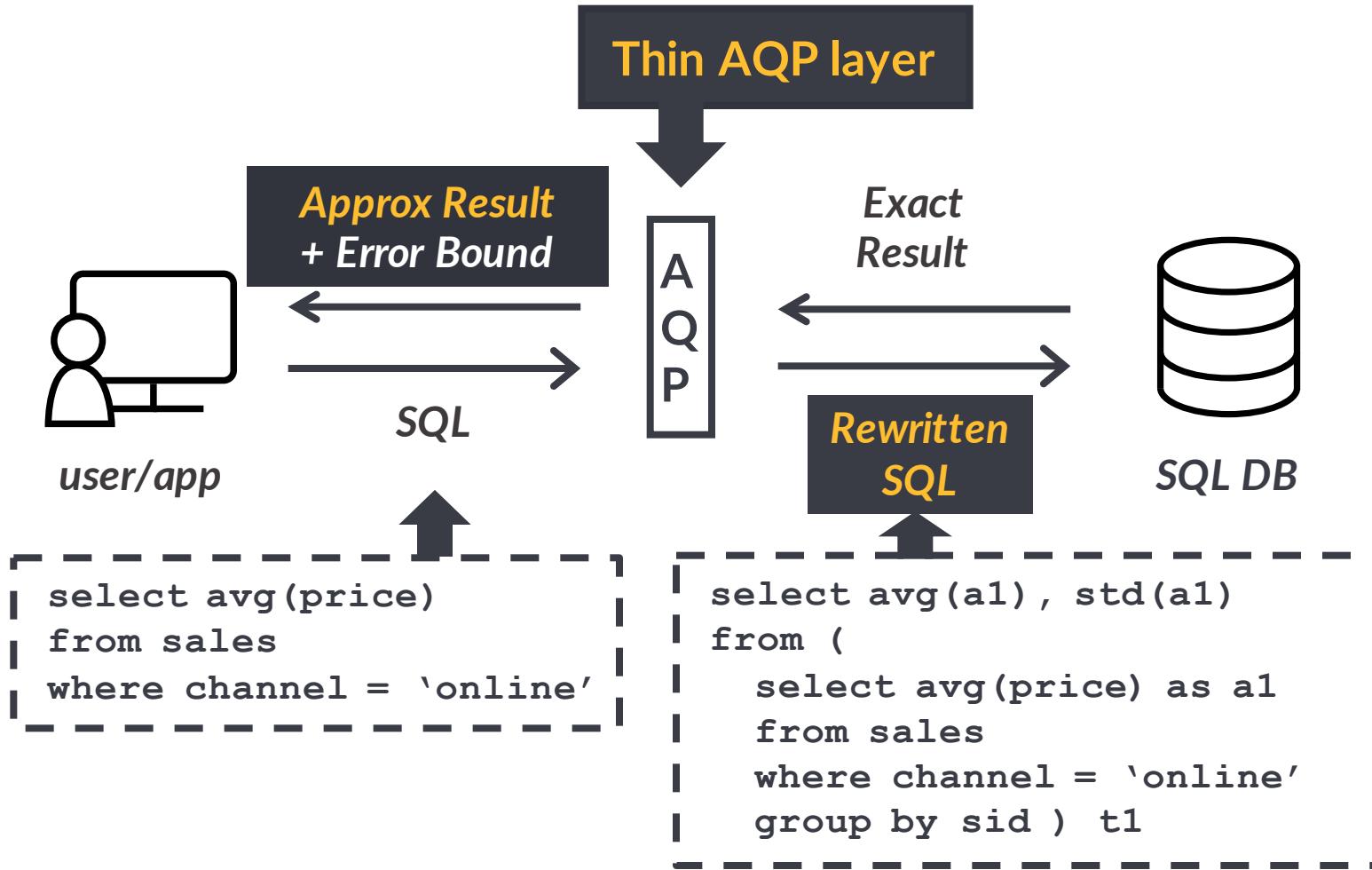
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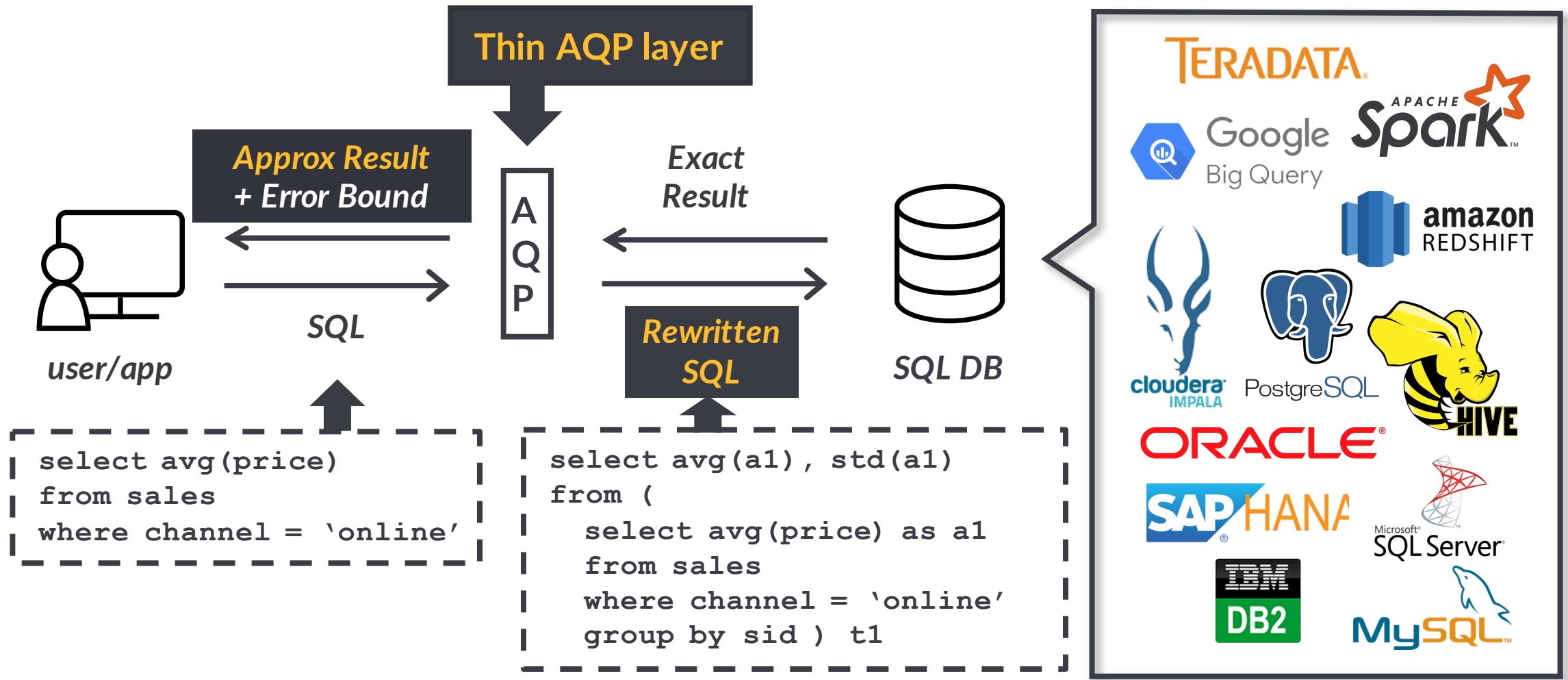
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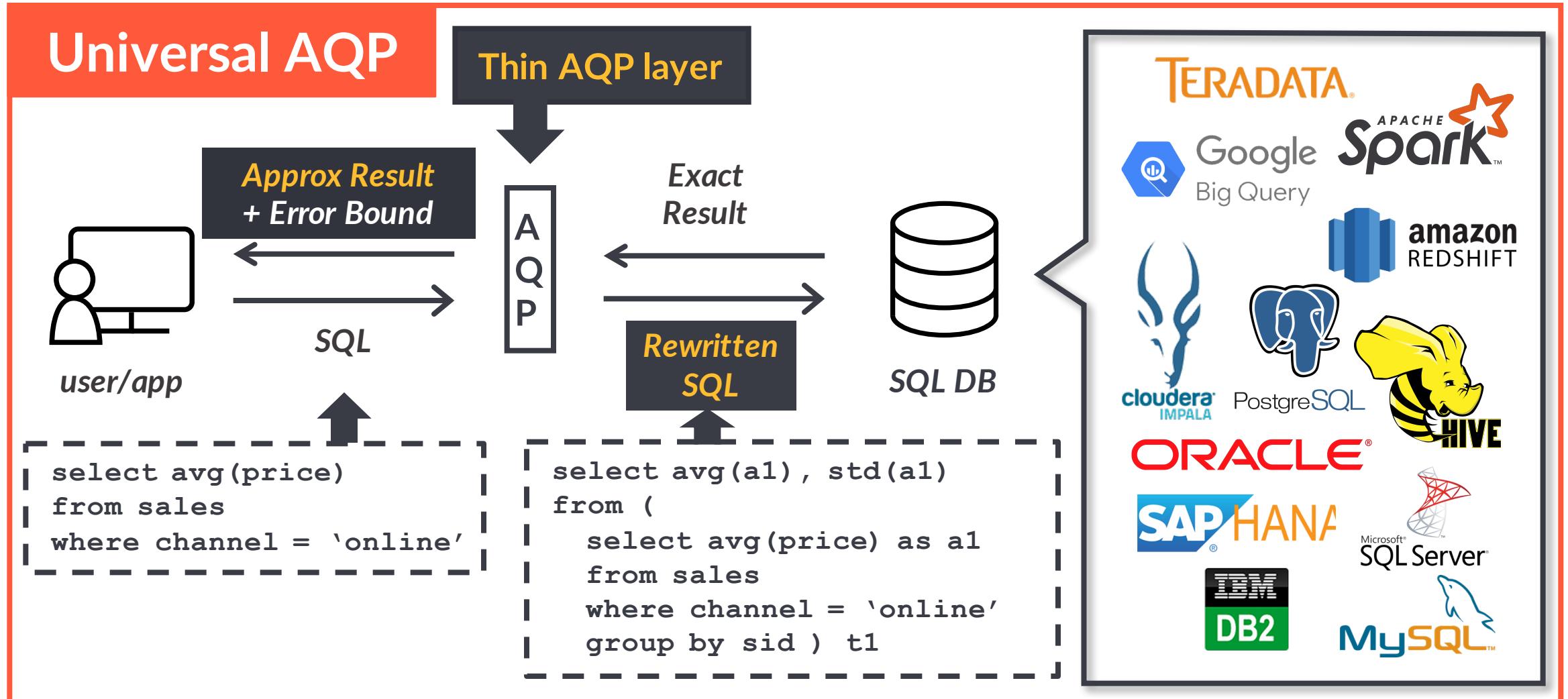
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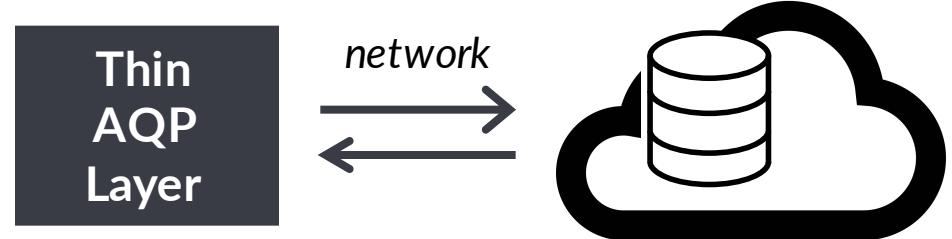
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## 2. Middleware efficiency

- Lack of access to DBMS machinery



## 3. Server efficiency

- Resampling-based techniques [Pol and Jermaine '05, BlinkDB '14]
- Intimate integration of err est. logic into scan operators [Quickr '16, SnappyData]
- Overriding the relational operators altogether [ABM '14]

# VerdictDB Overview

First Universal AQP system

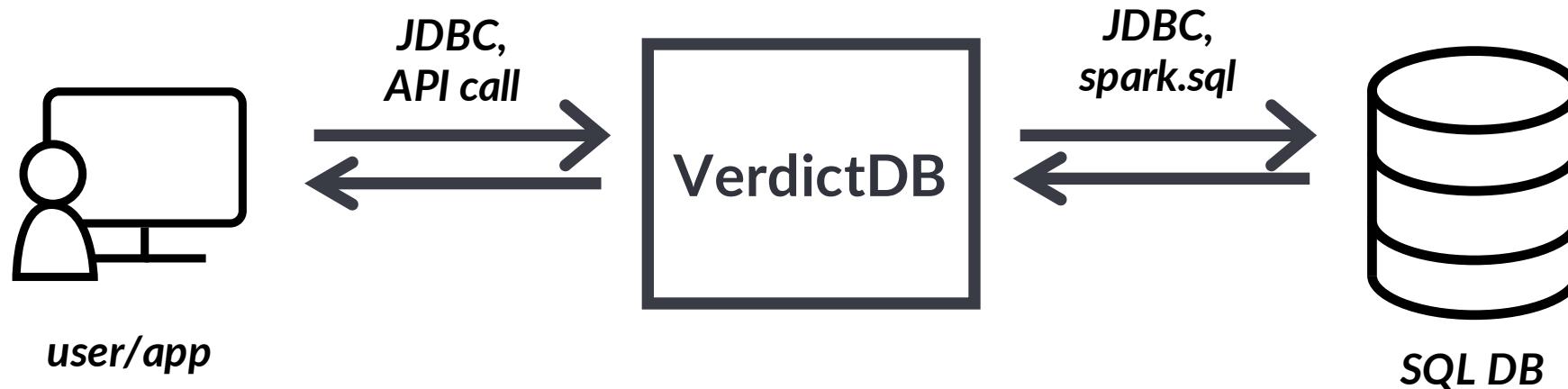
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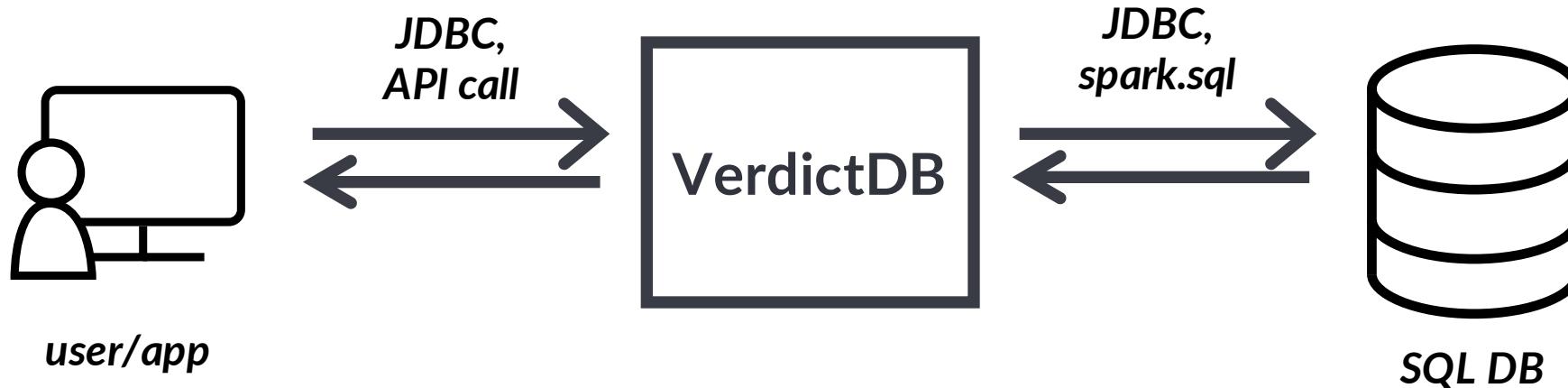


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Stores (1) offline-created samples, and (2) VerdictDB-managed metadata

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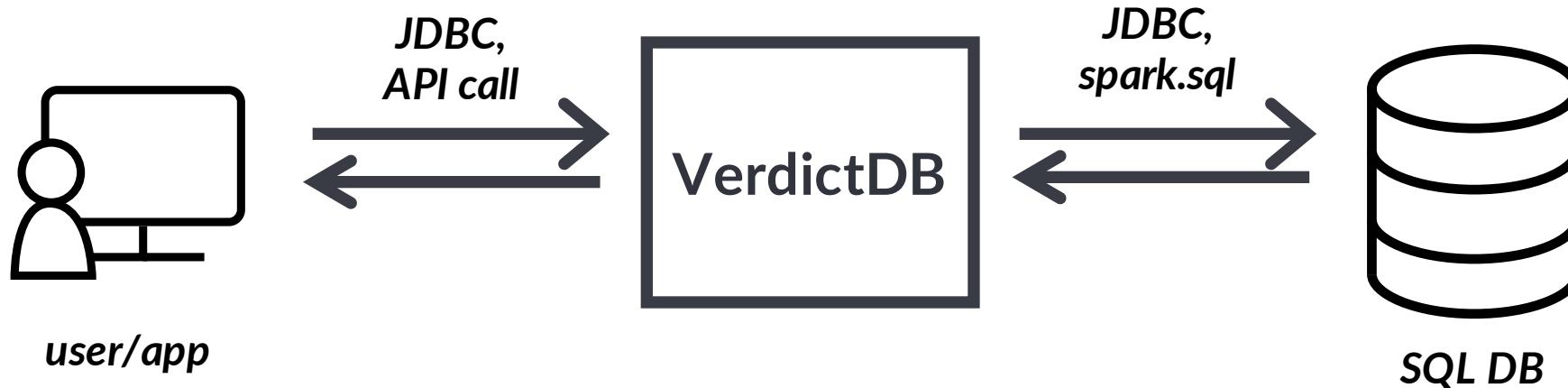


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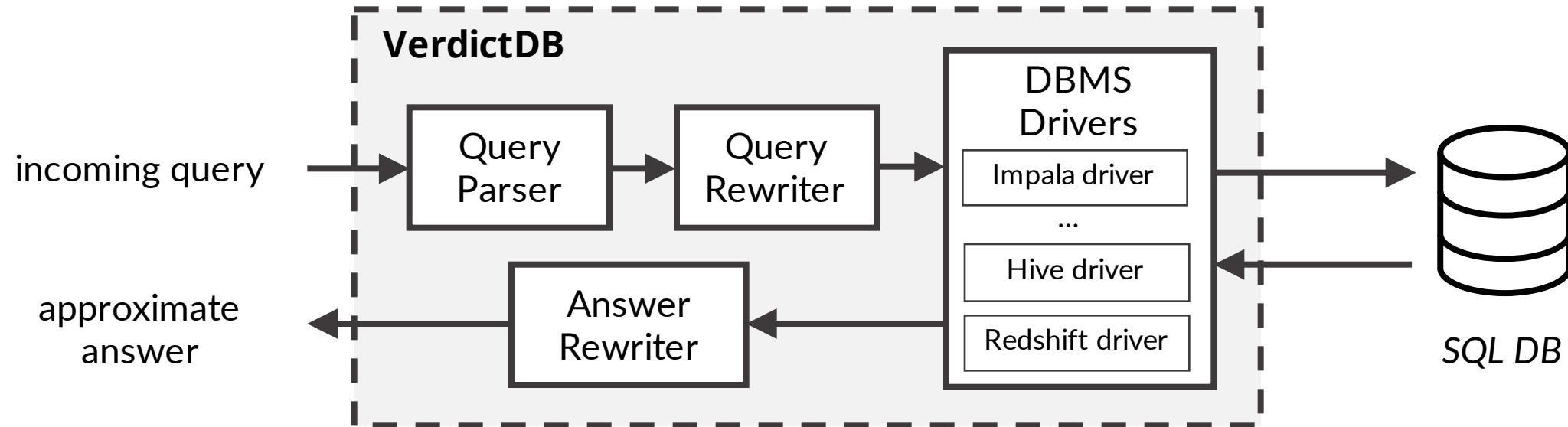
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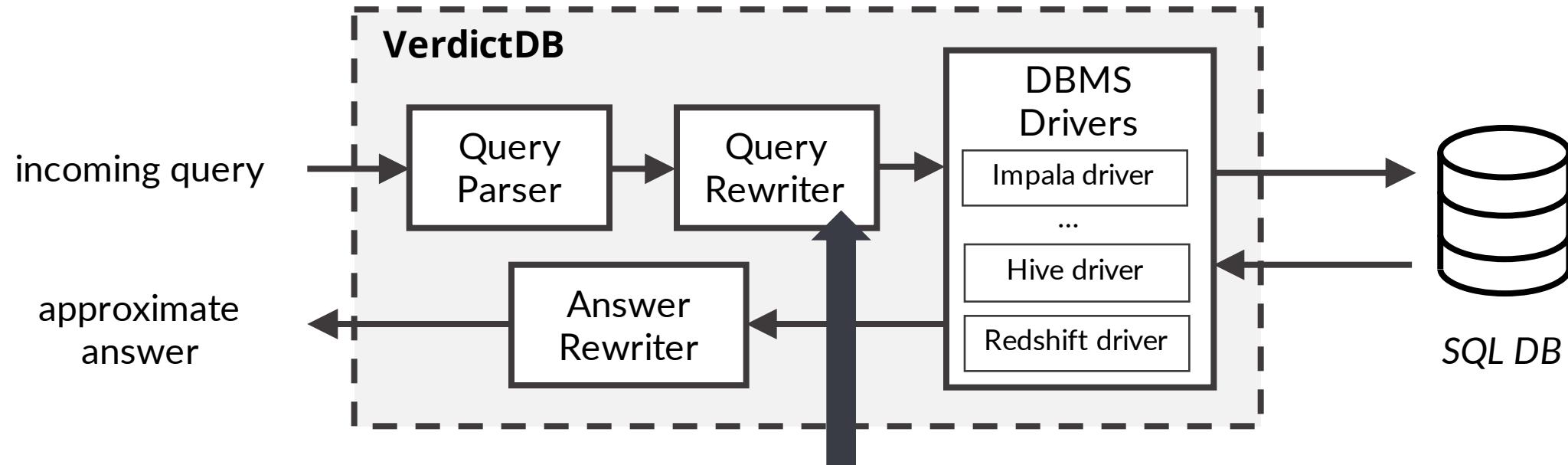
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*supported by  
almost any SQL engines*

# Architecture



# Architecture



## Crucial component

1. Chooses an optimal set of samples
2. Scales values appropriately
3. **Inserts an error estimation logic**

# Error estimation in VerdictDB

# Error estimation in general

User interested in  $Q(T)$

We compute  $Q(S)$  where  $S$  is a sample of  $T$

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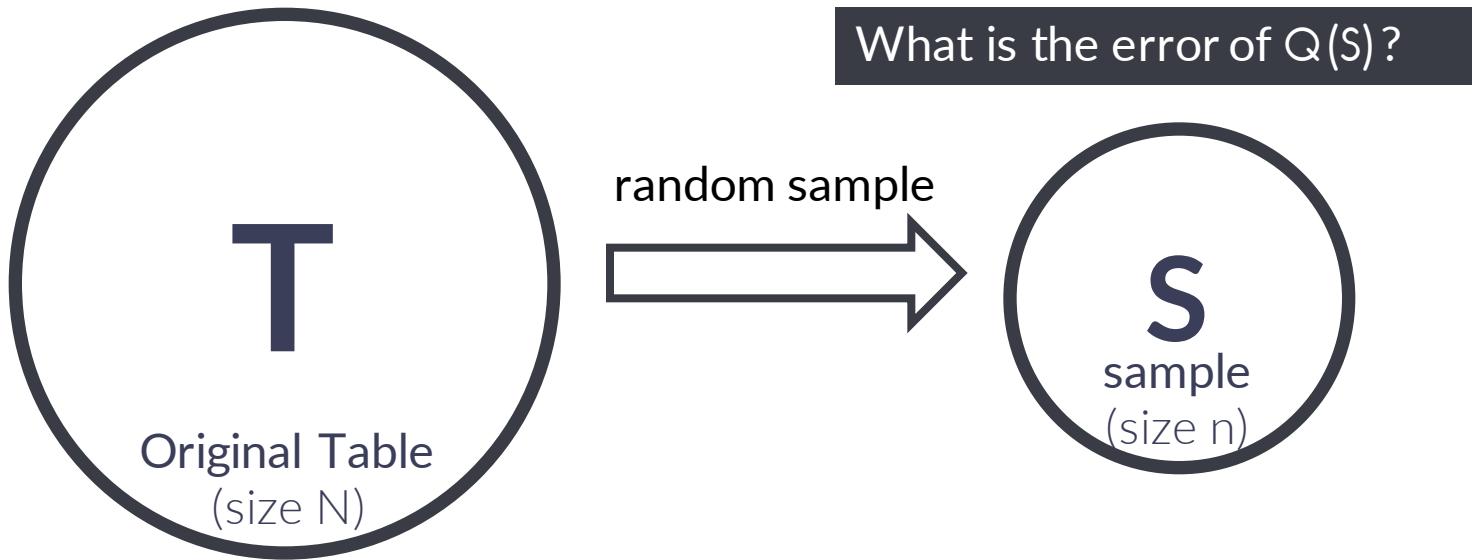
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# Recap: traditional subsampling

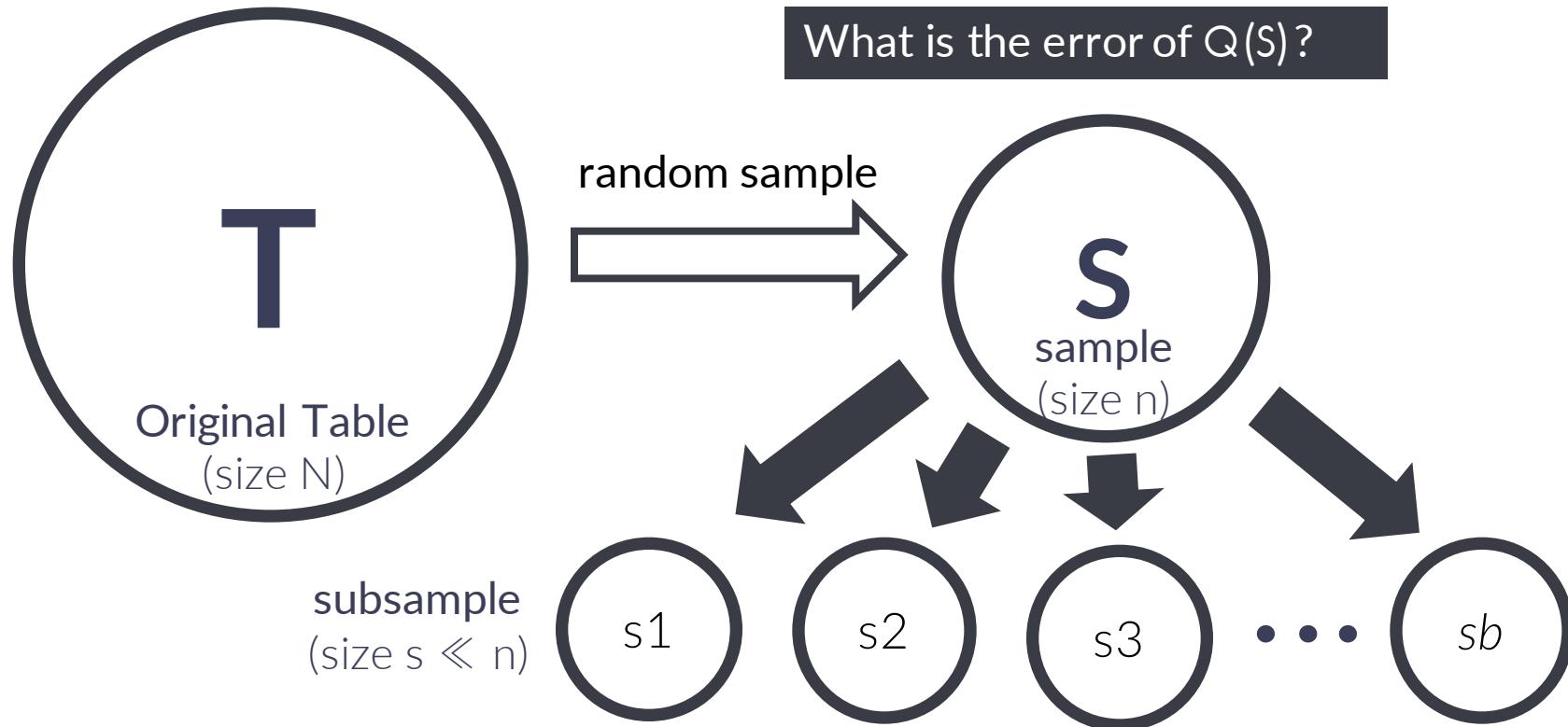


$Q(T)$  is slow / expensive

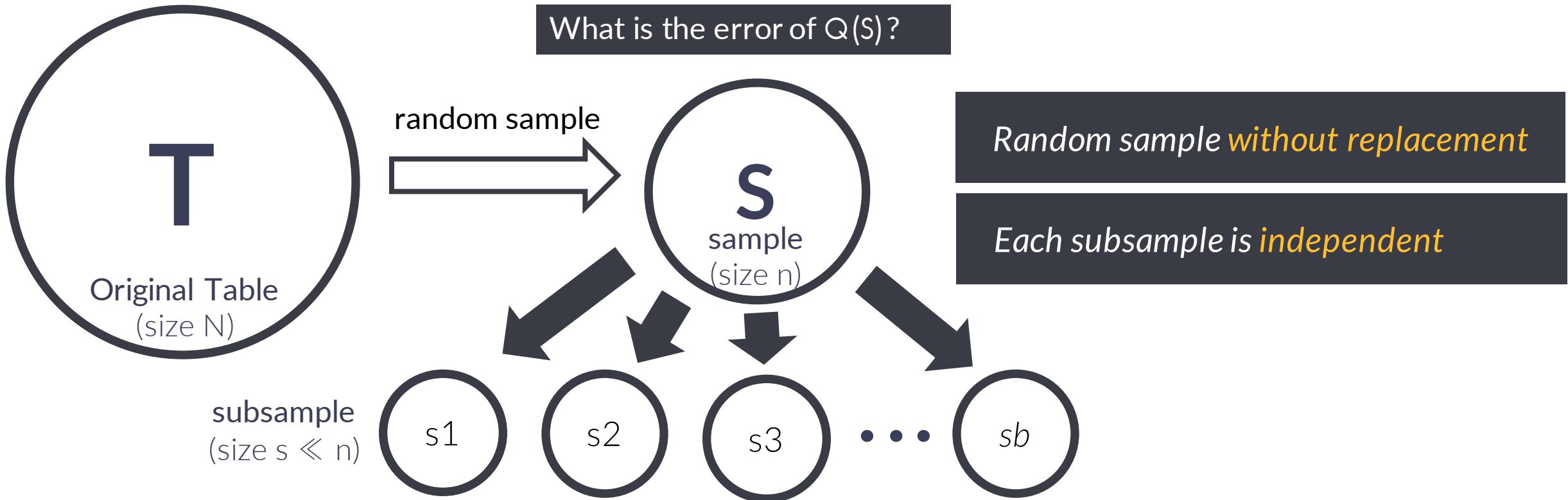
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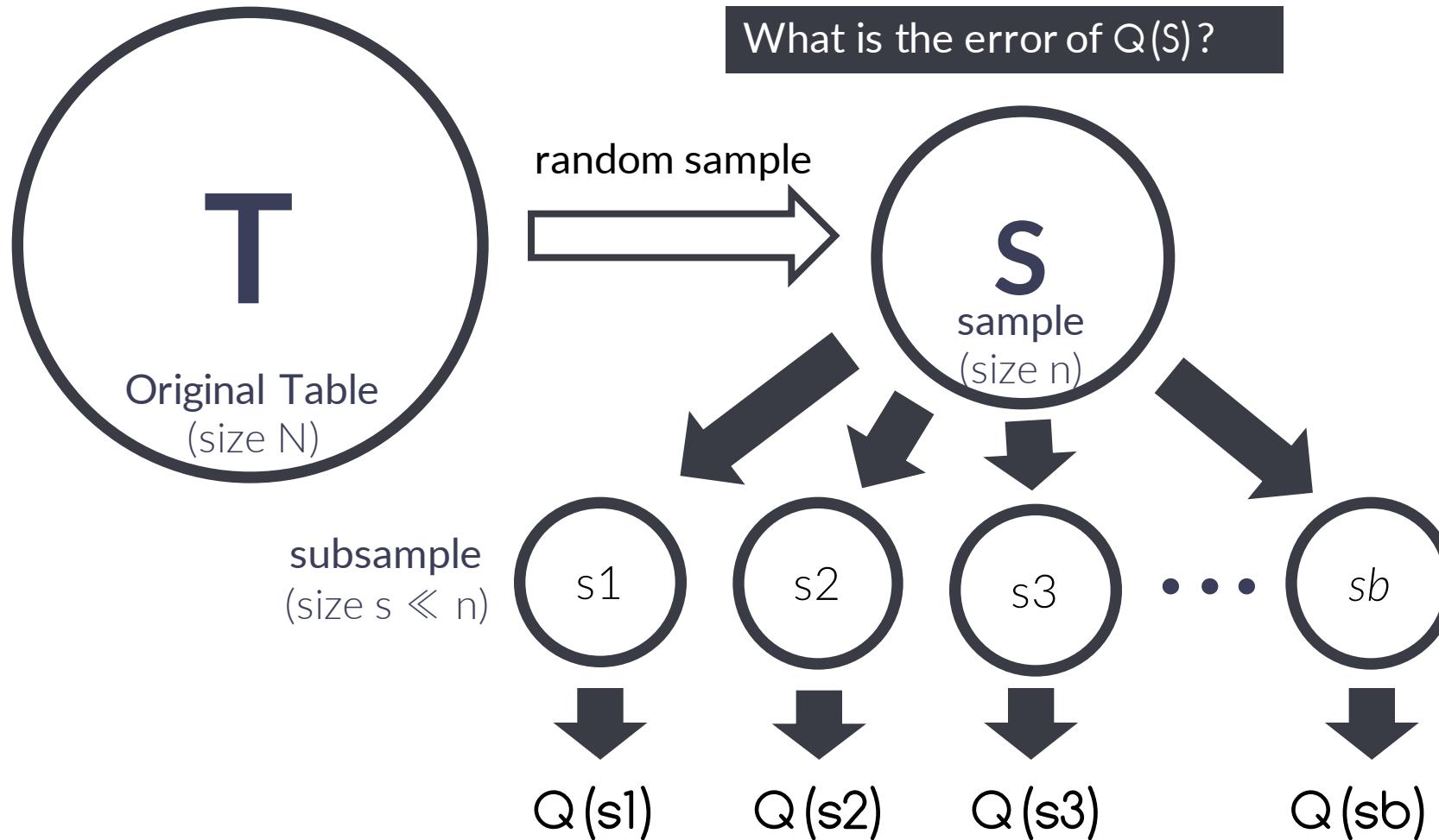
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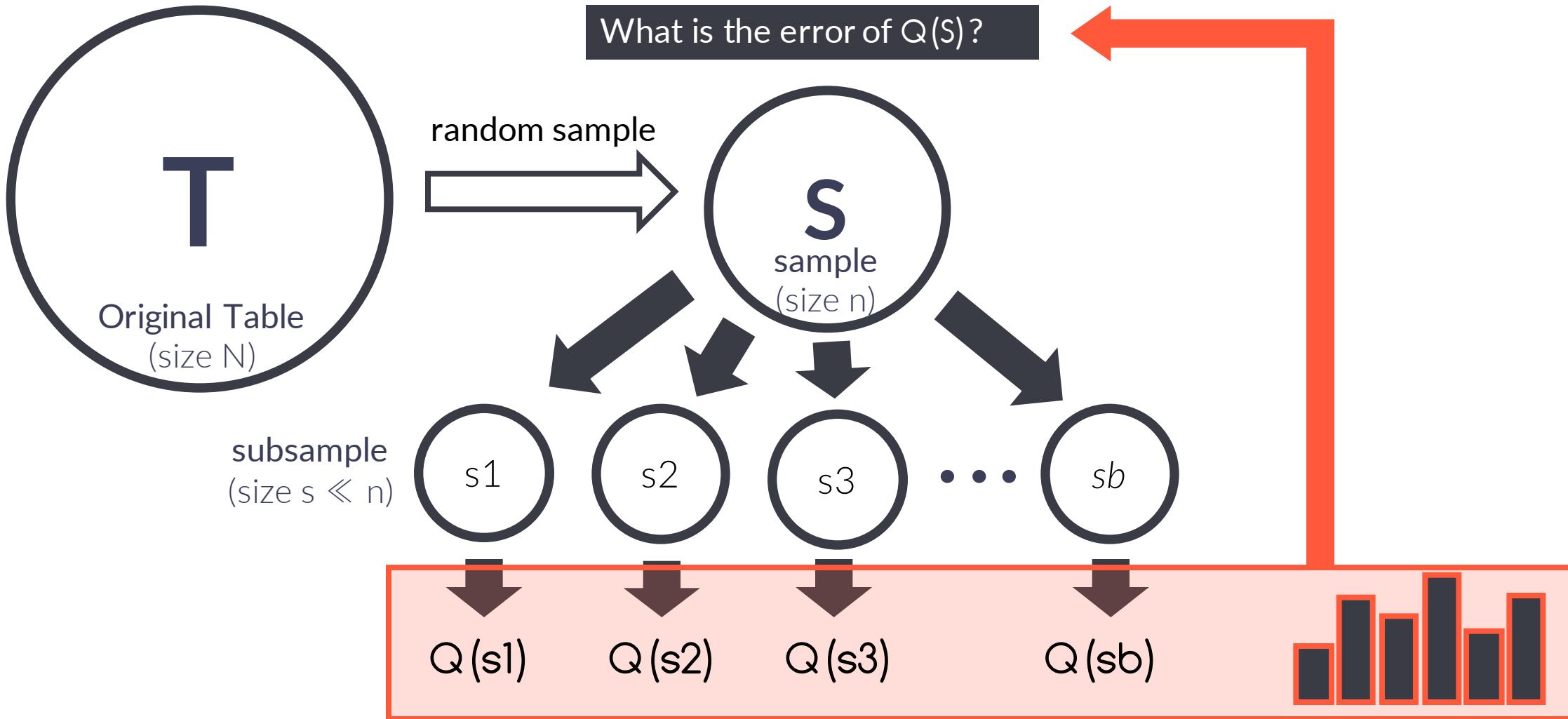
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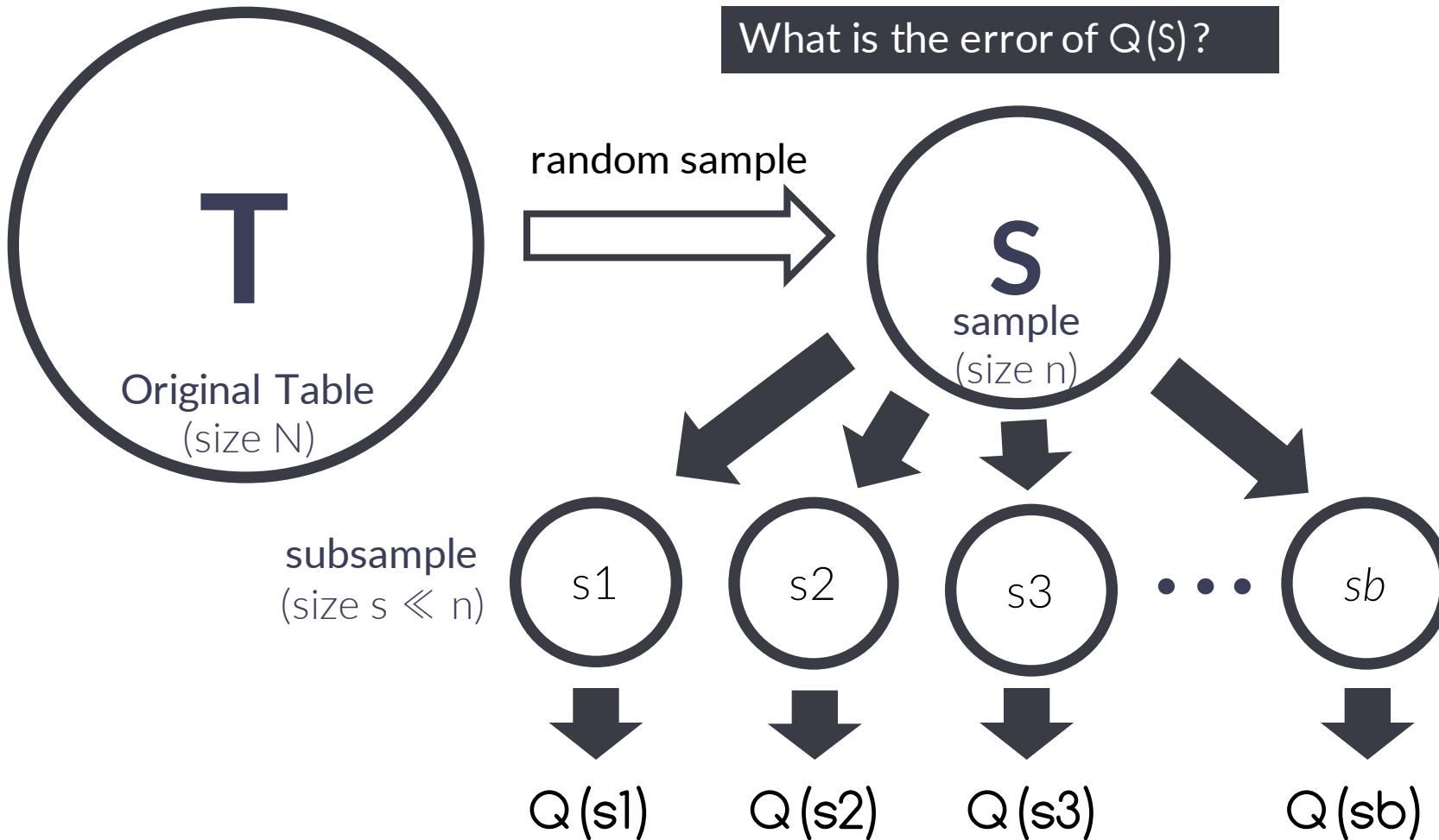
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## Important properties

1. A tuple may belong to multiple subsamples.
2. The size of every subsample is  $s$ .

# Traditional subsampling in SQL is slow

subsample ID

CITY	PRODUCT	PRICE	1	2	...	b
n tuples	AA	egg	\$3.00	1	0	1
	AA	milk	\$5.00	0	1	0
	AA	egg	\$3.00	0	0	1
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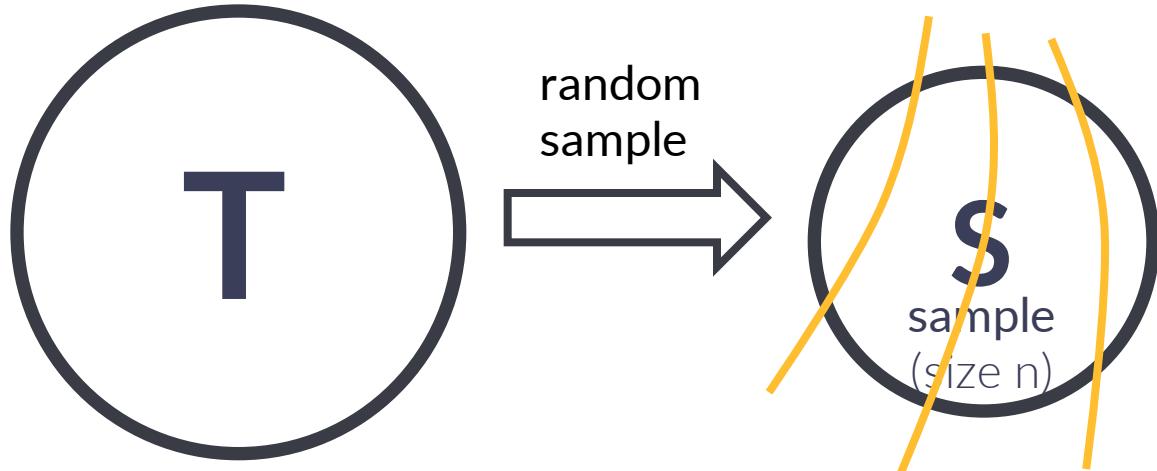
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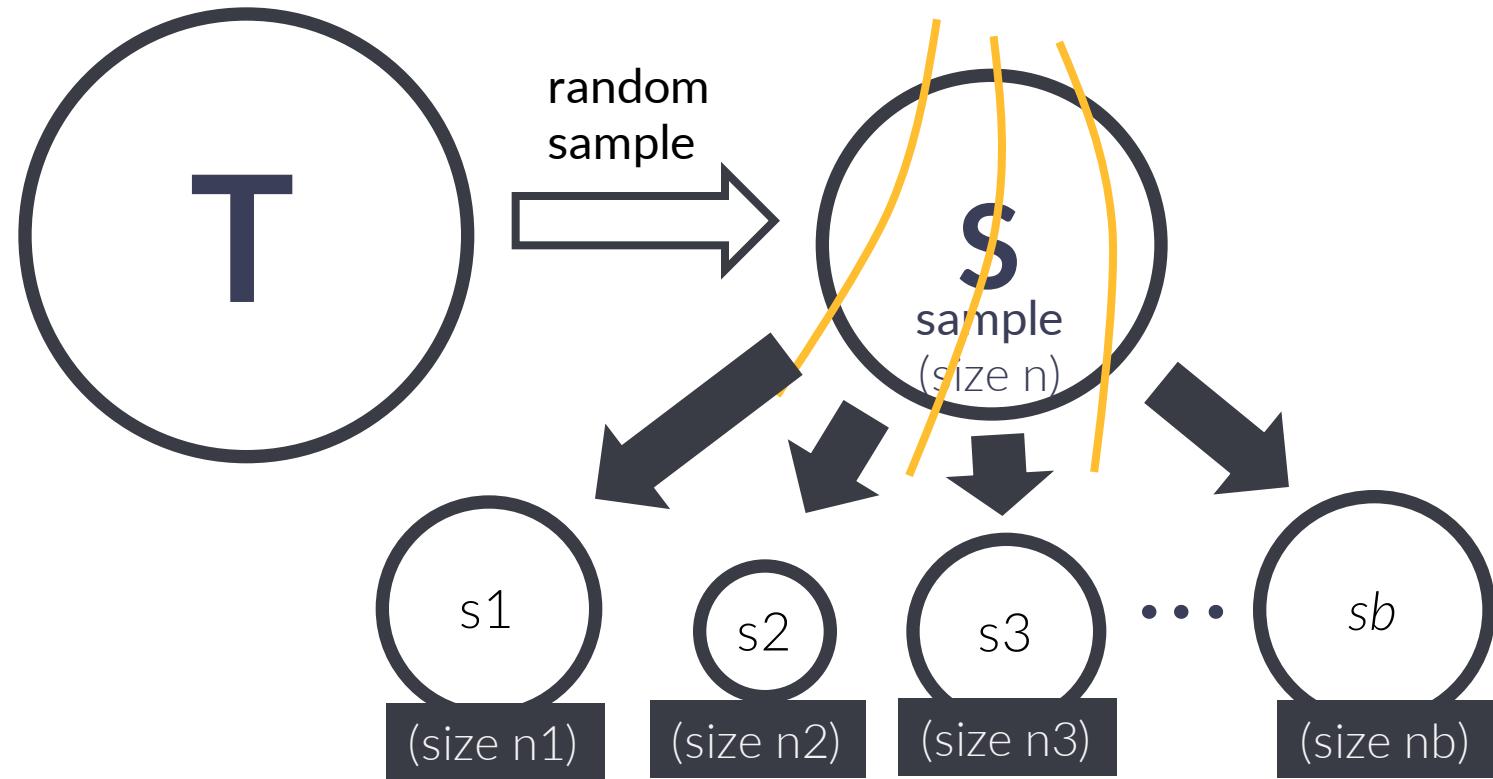
No error est: 0.35 sec  
Trad. subsampling: 118 sec  
**337x slower**

(based on 1G sample, Impala)

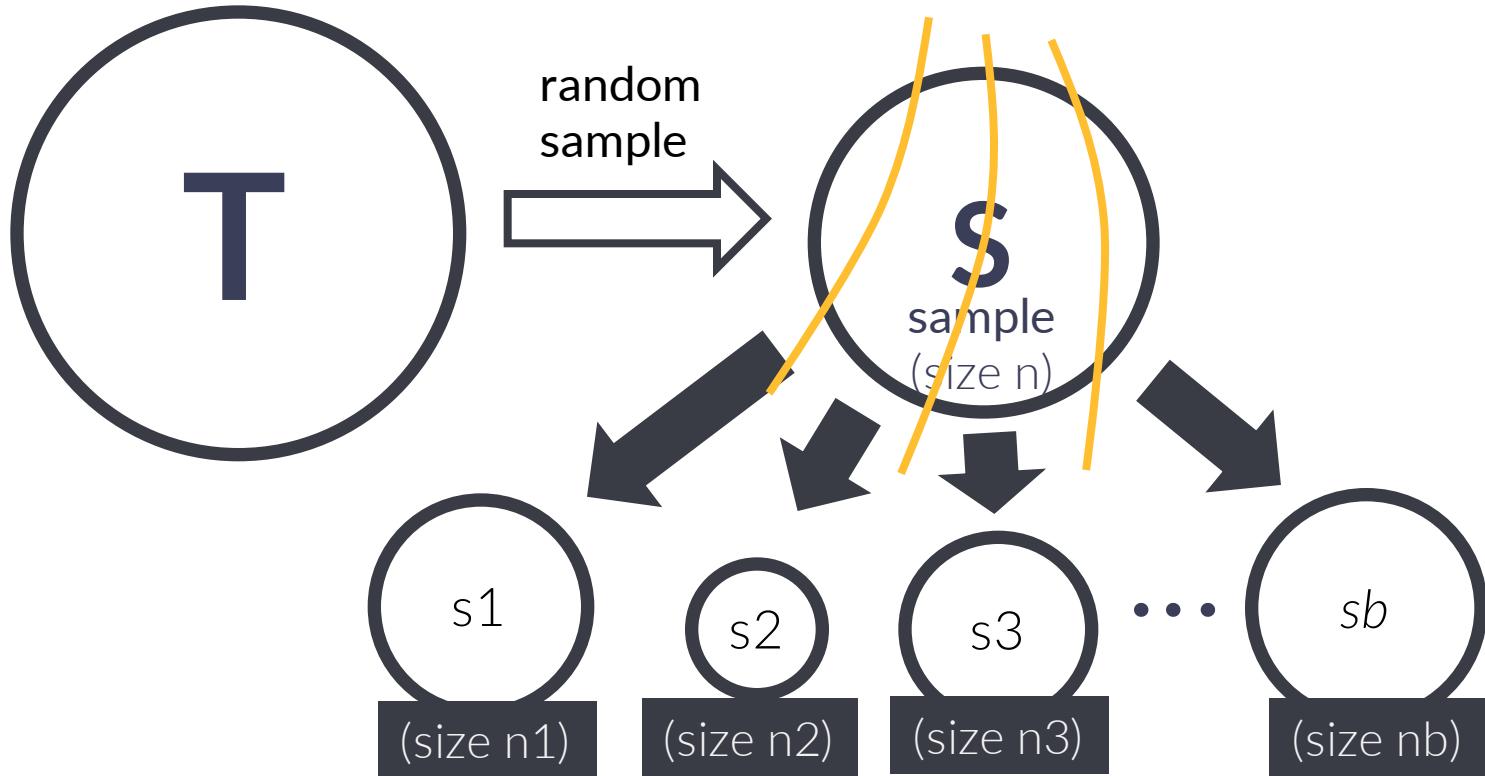
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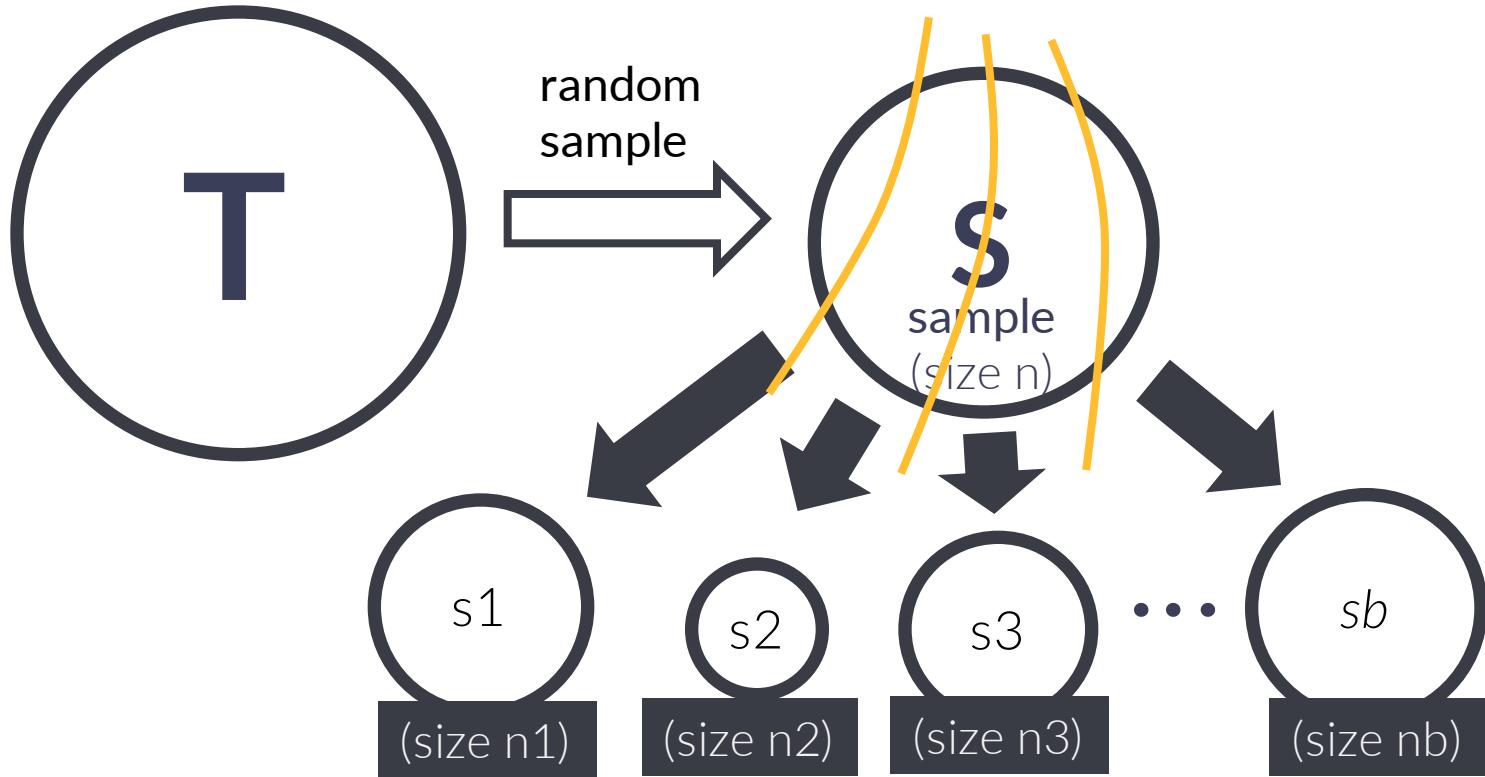
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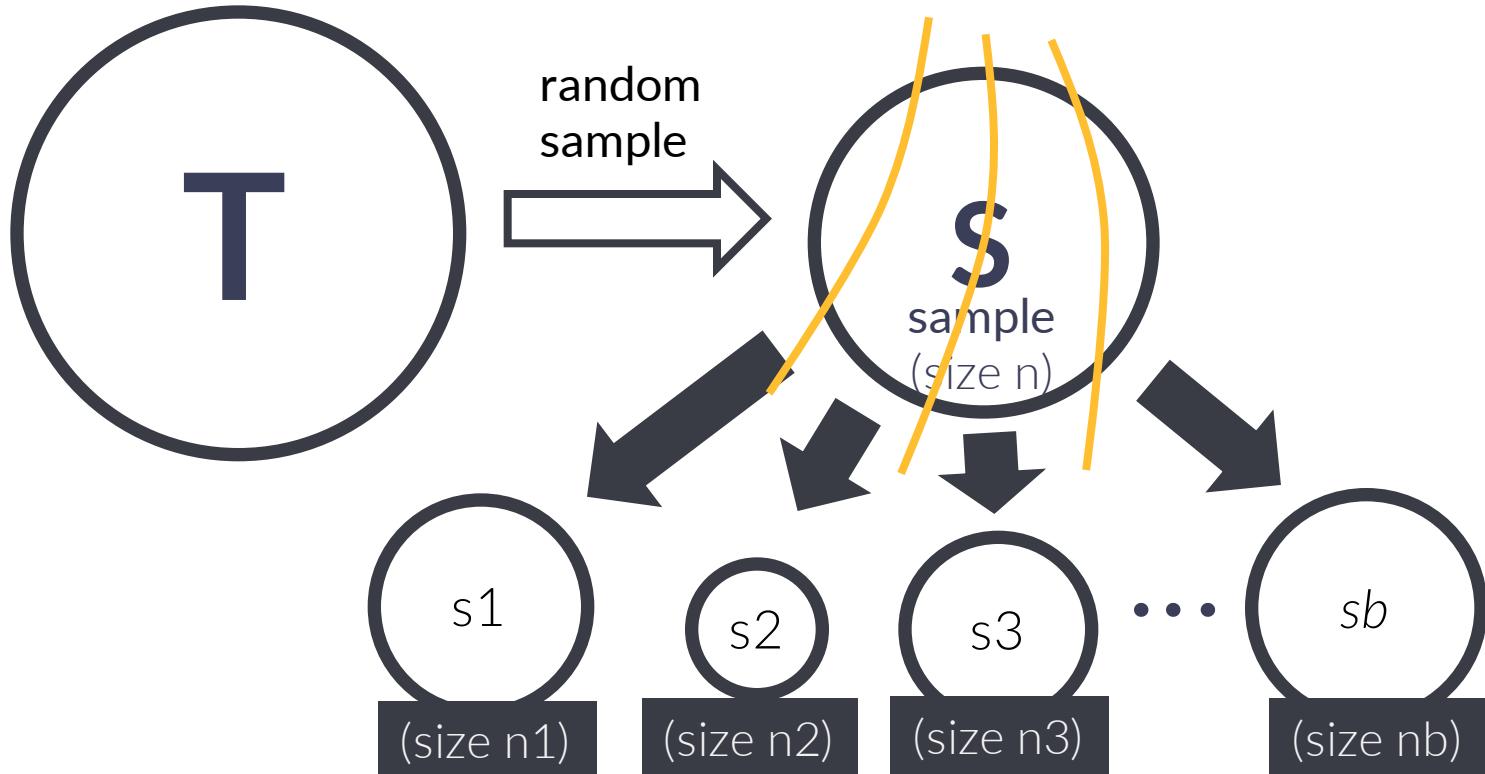
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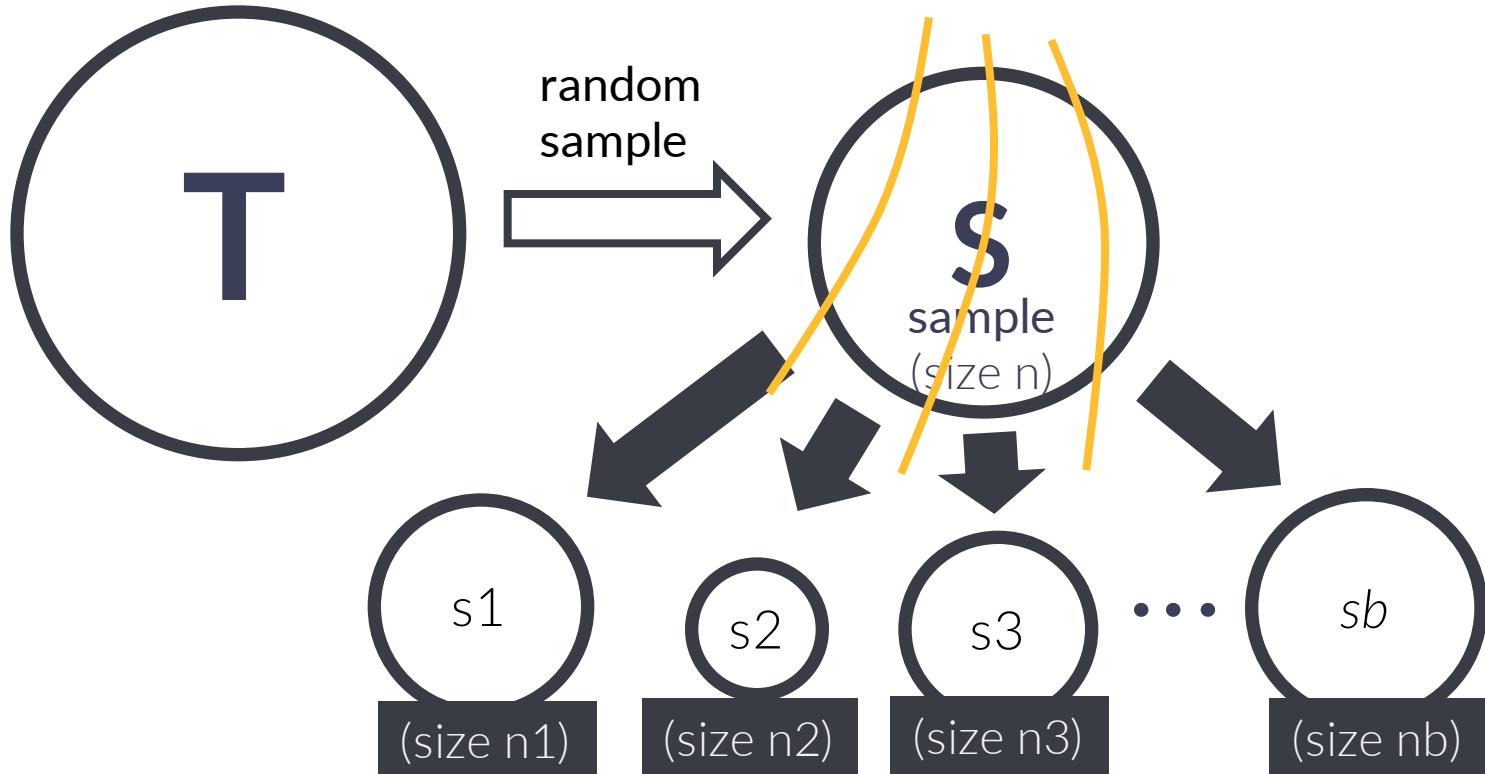
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*Each sampled tuple can belong to at most one subsample*
2. ~~The size of every subsample is s.~~  
*Allow subsamples to differ in size.*

*Can be implemented in SQL as a single group-by query!*

# Variational subsampling in SQL is fast

*n tuples*

CITY	PRODUCT	PRICE	subsample ID	
AA	egg	\$3.00	1	randint(1,b)
AA	milk	\$5.00	3	
AA	egg	\$3.00	2	
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Trad. subsampling: 118 sec

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**$162 \times$  faster than traditional**

(based on 1G sample, Impala)

# Main results

Theorem 1 (Consistency) ***The distribution*** of the aggregates of ***variational subsamples***, after appropriate scaling, ***converges to the true distribution*** of the aggregate of a sample as  $n \rightarrow \infty$ .

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Theorem 2 (Convergence Rate) *The convergence rate of variational subsampling is equal to that of traditional subsampling ***when b is finite.****

$$O\left(n_s^{-1/2} + \frac{n_s}{n} + \underline{b^{-1/2}}\right)$$



The error term from the finite b  
(The Dvoretzky–Kiefer–Wolfowitz inequality)

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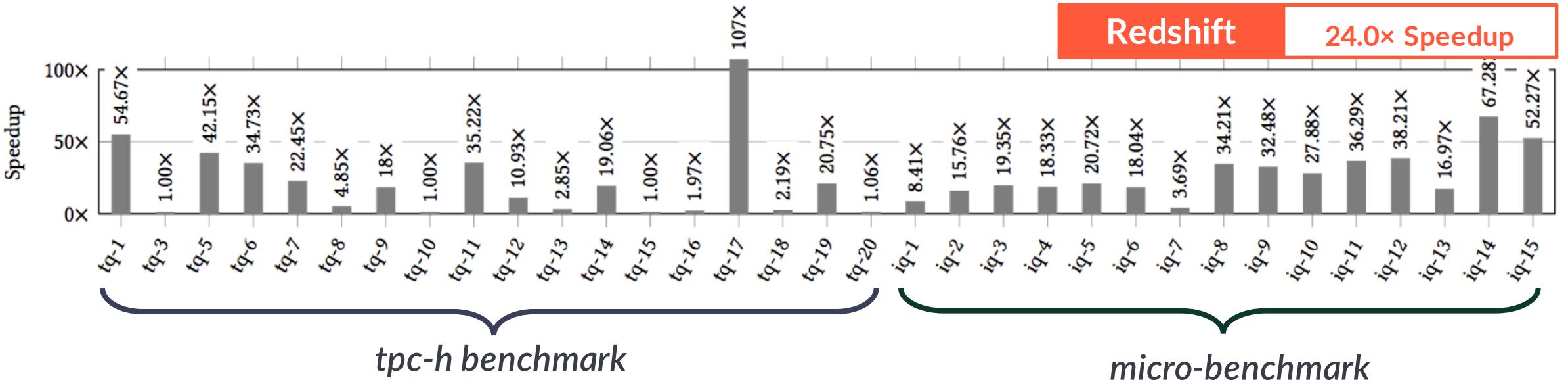
## Datasets:

- 500GB TPC-H benchmark / 200GB Instacart dataset / synthetic datasets

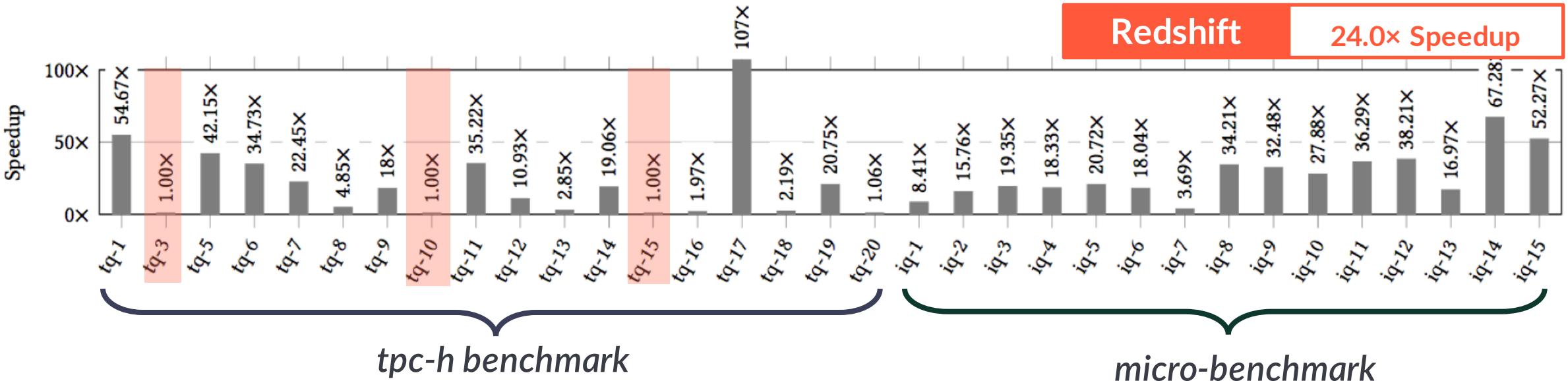
## Underlying databases

- Amazon Redshift, Apache Spark SQL, Apache Impala on 10+1 r4.xlarge cluster

# Speedup for Redshift

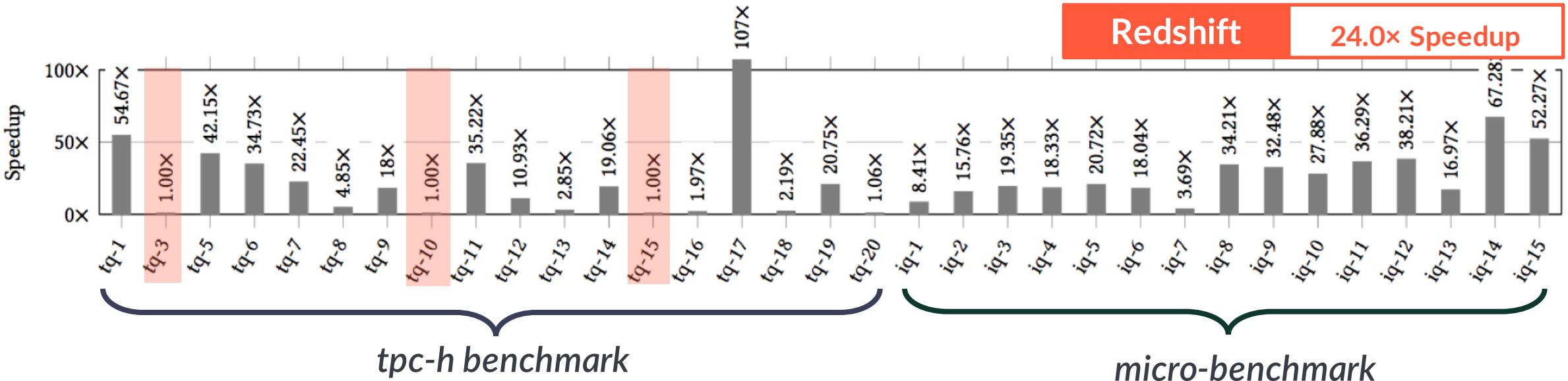


# Speedup for Redshift



t3, t10, t15: no speedup (i.e., 1x) due to high-cardinality grouping attributes

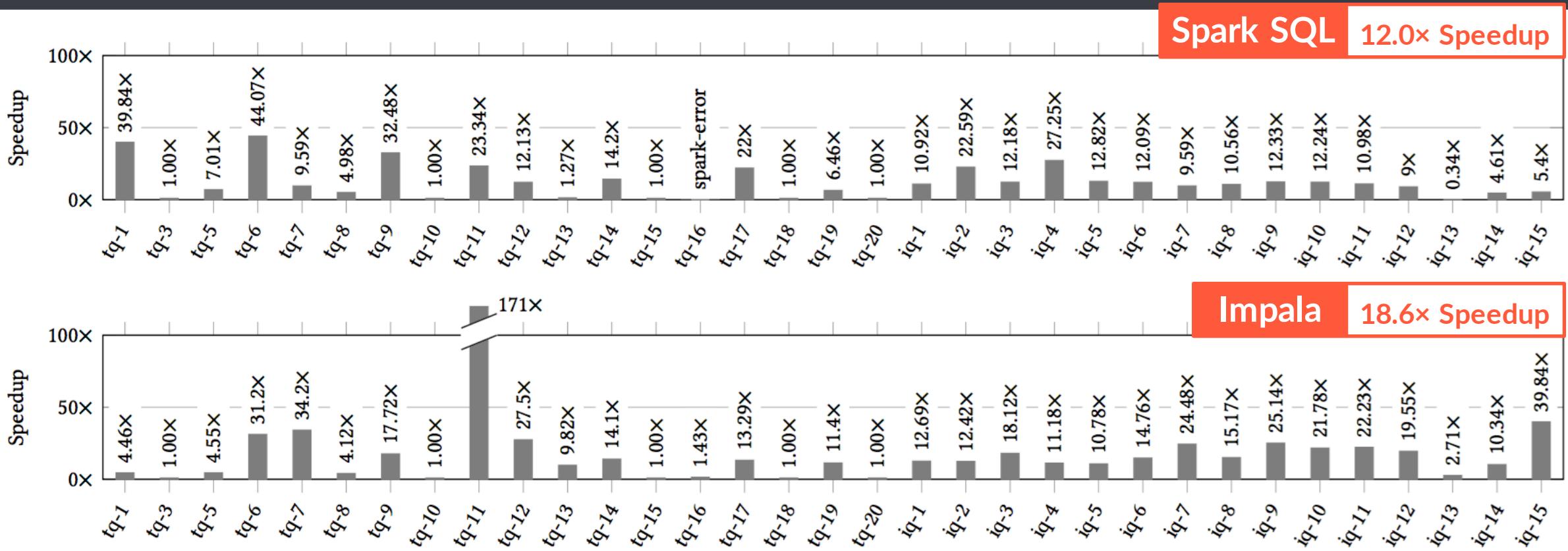
# Speedup for Redshift



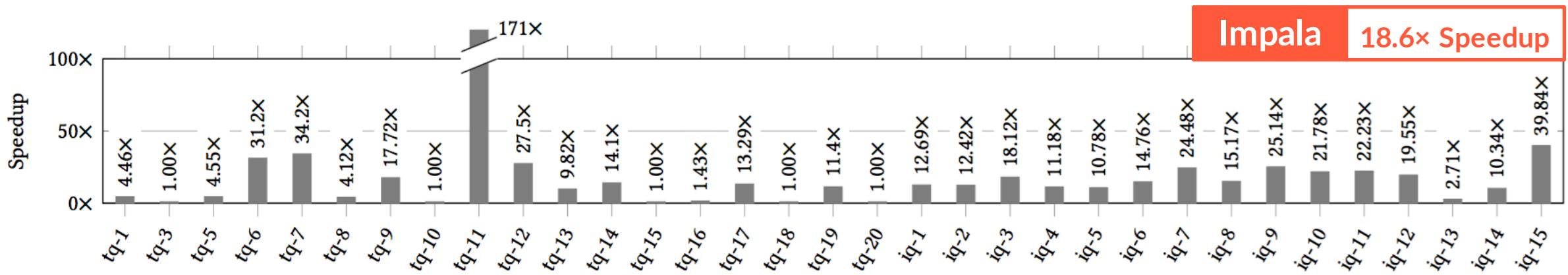
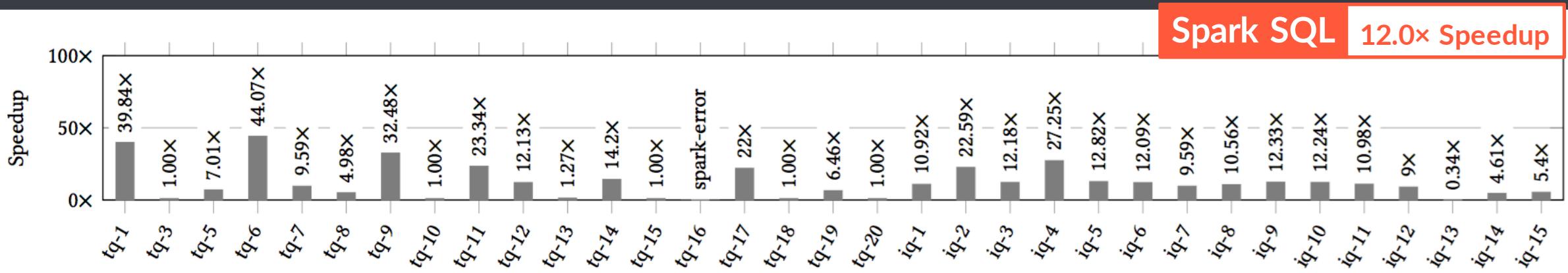
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Other queries: **26.3x speedups** (relative errors were 2%)

# Speedup for Apache Spark & Impala



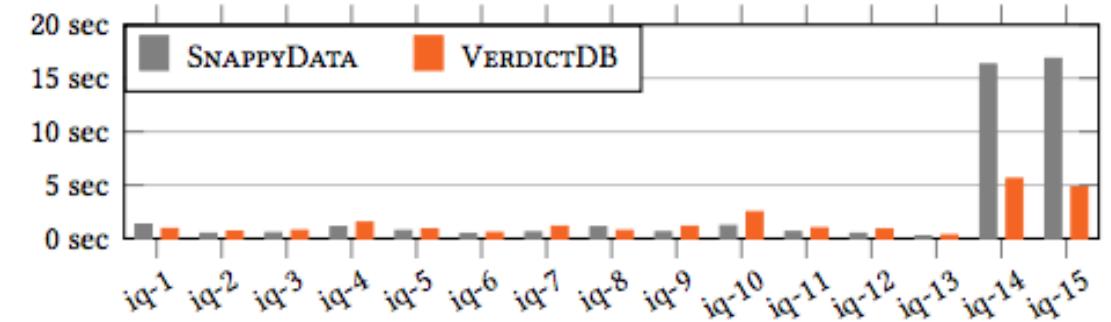
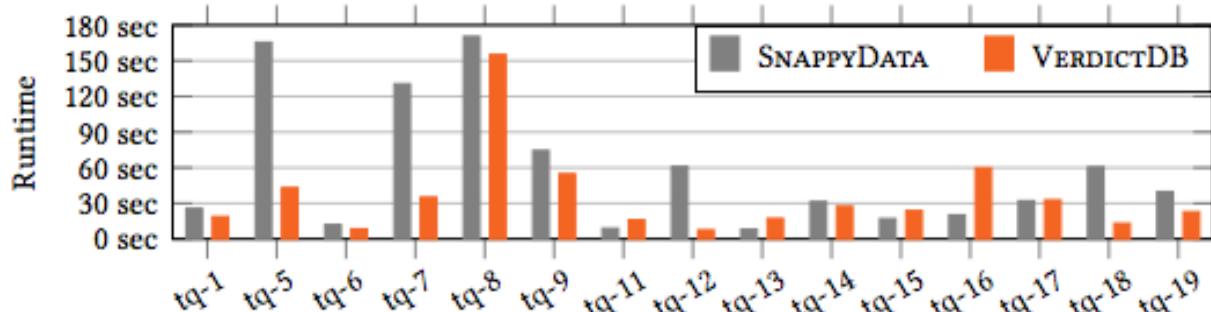
# Speedup for Apache Spark & Impala



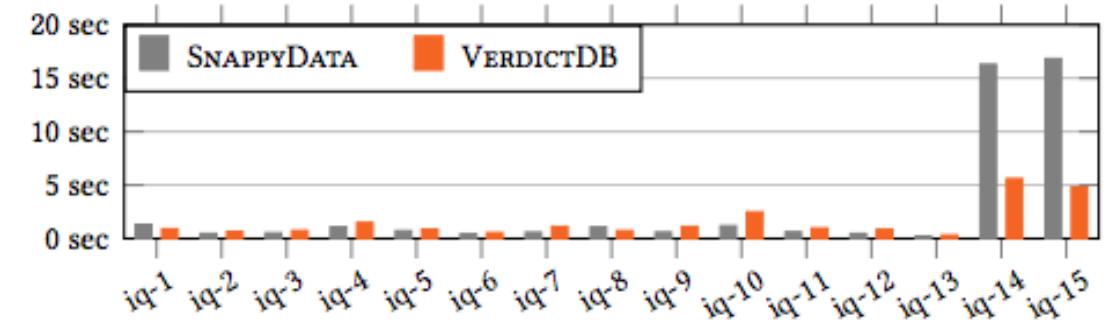
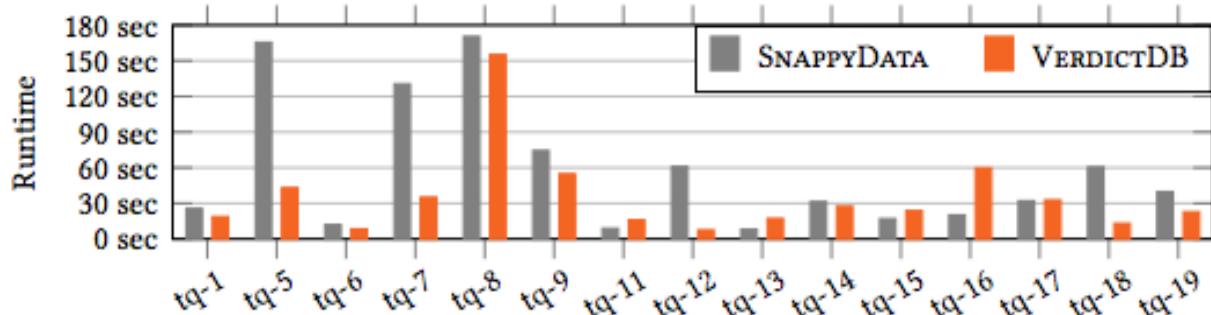
$$speedup = \frac{overhead + processing}{overhead + (sample\ processing)}$$

*Lower overhead → Larger speedup*

# UAQP vs. Tightly-integrated AQP

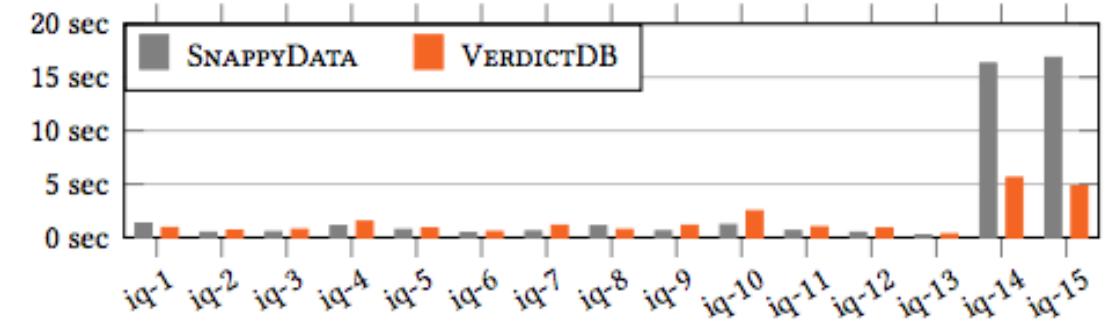
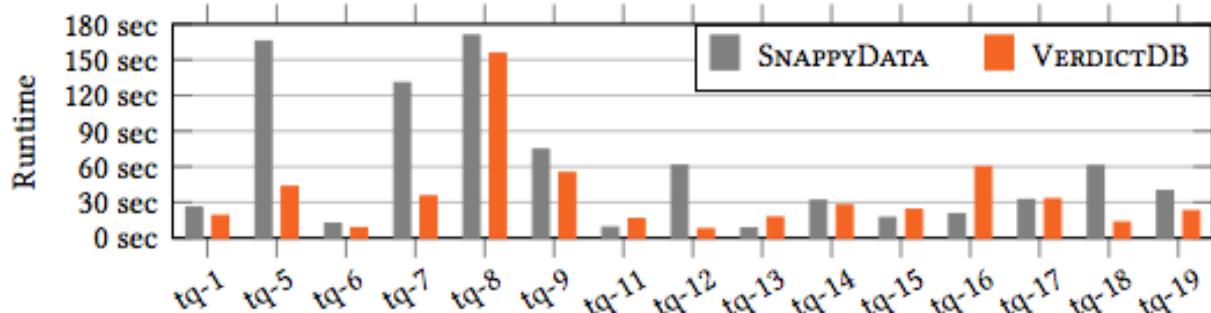


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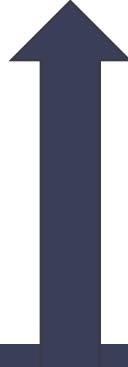
*VerdictDB was comparable to SnappyData.*

# UAQP vs. Tightly-integrated AQP



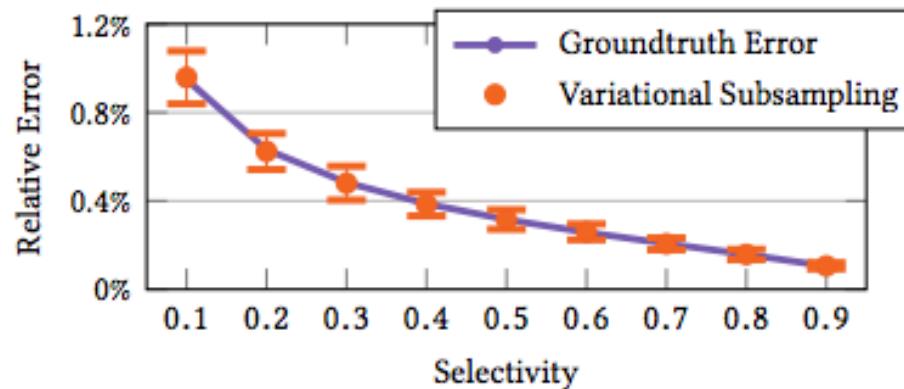
*VerdictDB was comparable to SnappyData.*

*SnappyData ver 0.8 didn't support the join of two sample tables.*



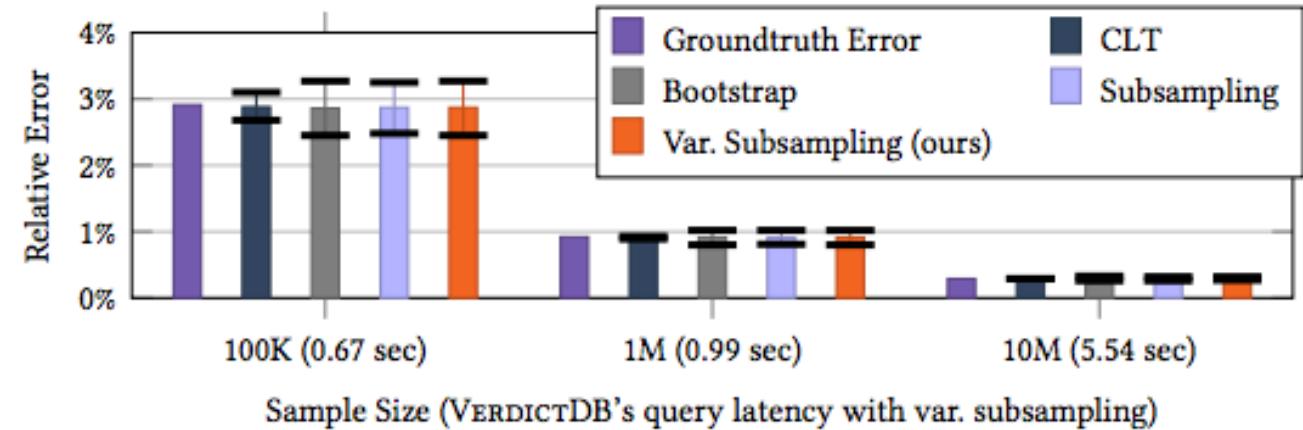
# Variational subsampling: correctness

Rel. err. naturally become smaller for higher selectivity.



(a) Estimated error for different selectivity

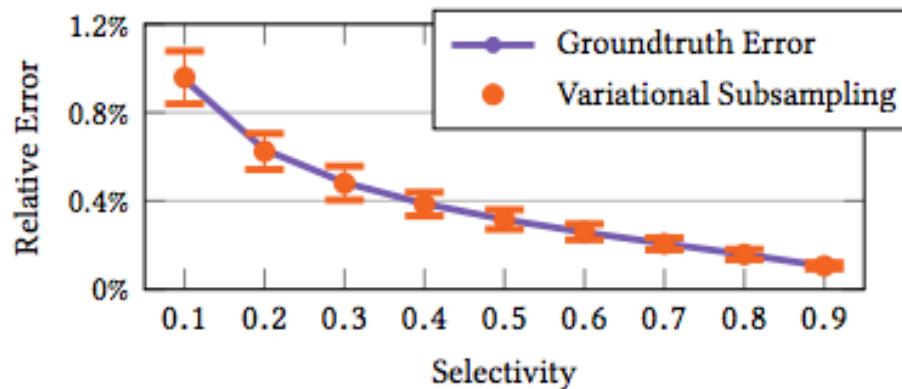
The bars are 5<sup>th</sup> and 95<sup>th</sup> percentiles.



(b) Estimated error for different sample sizes

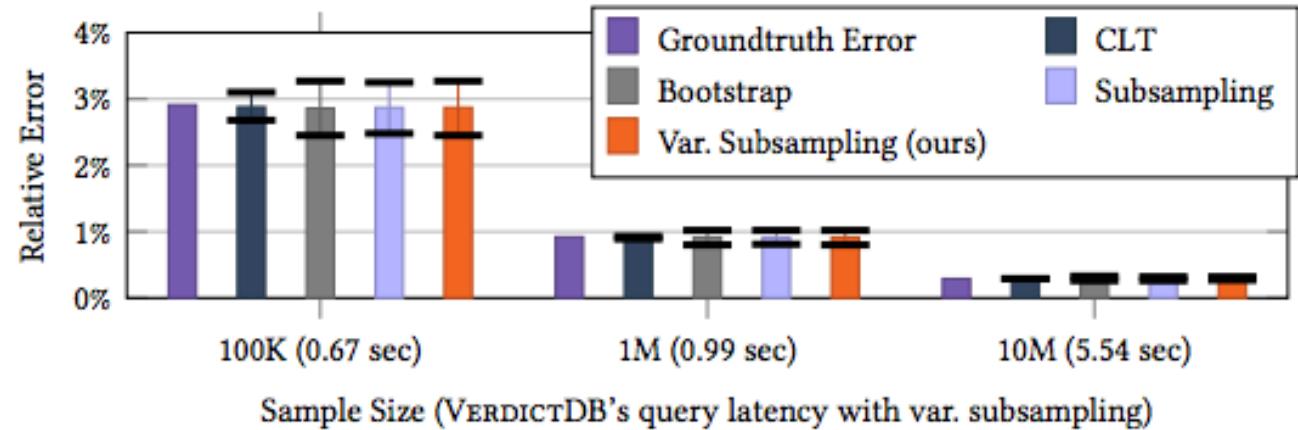
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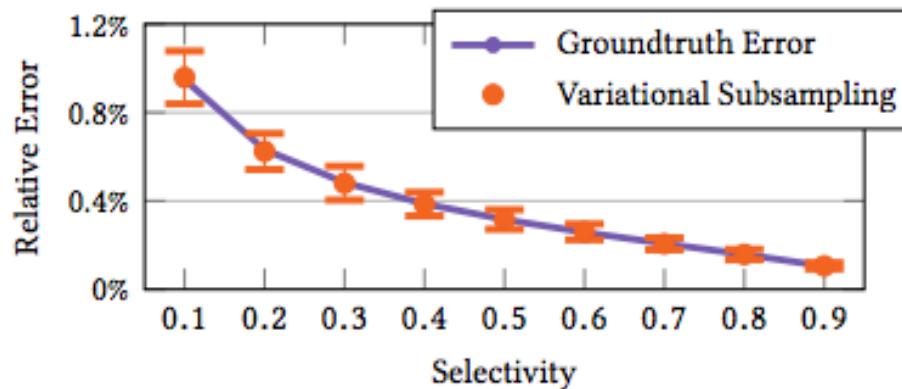


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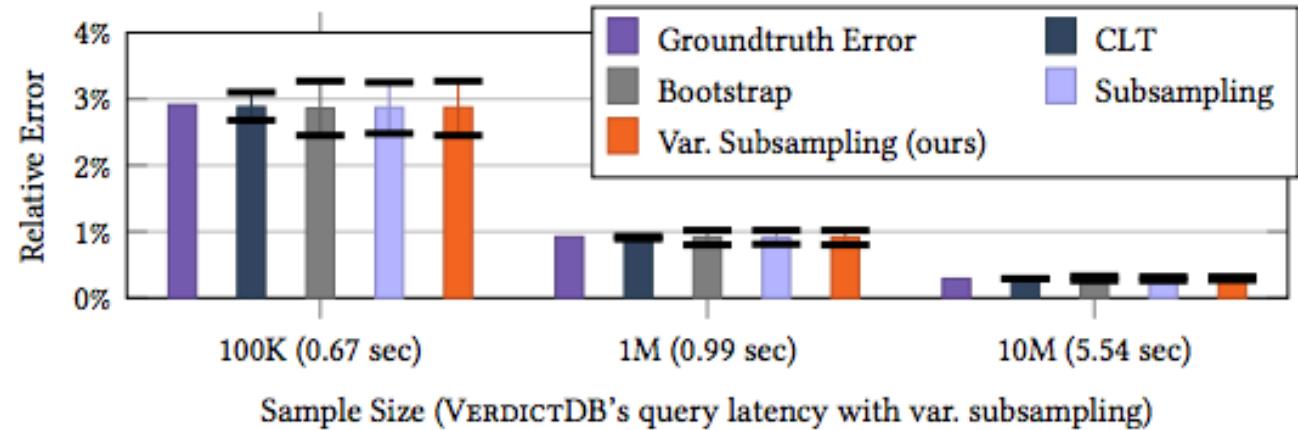
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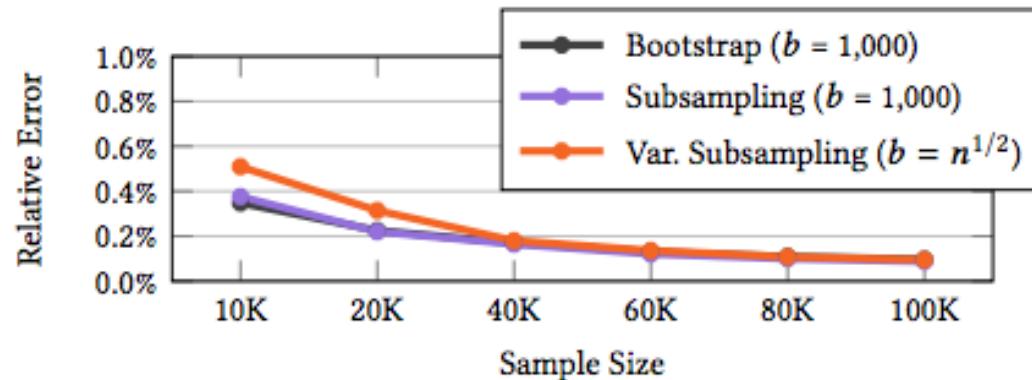


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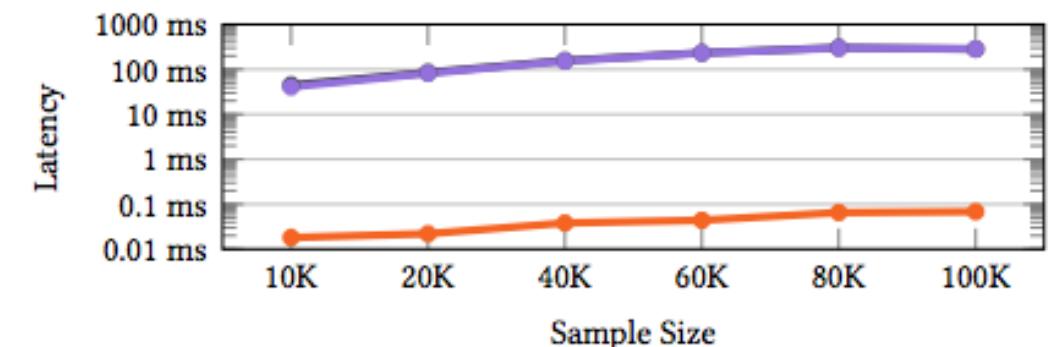
The estimated errors close to true errors.

The accuracy of var. subsampling  $\approx$  (a) bootstrap and (b) trad. subsampling

# Variational subsampling: convergence rate

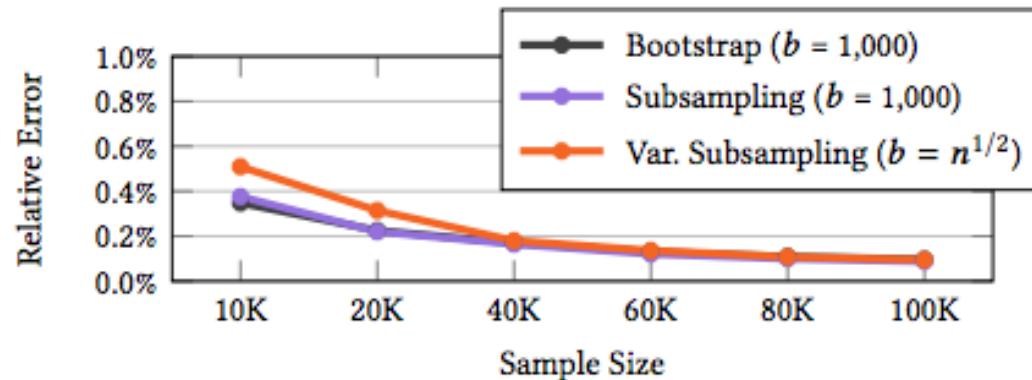


(a) Accuracy of error bound estimation

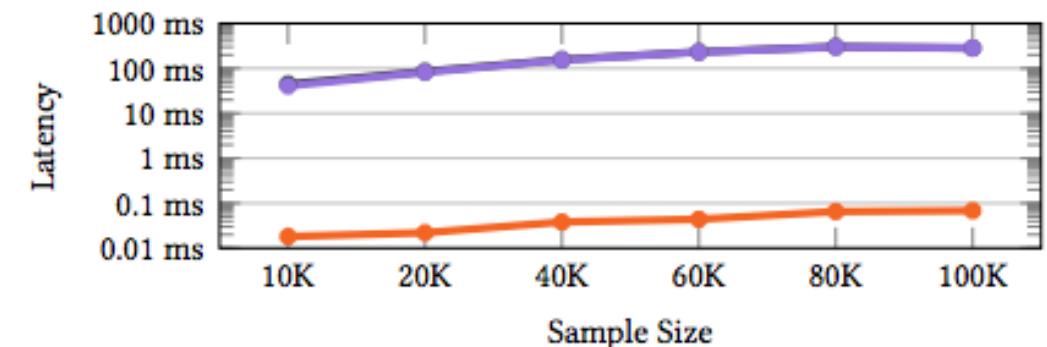


(b) Latency of error bound estimation

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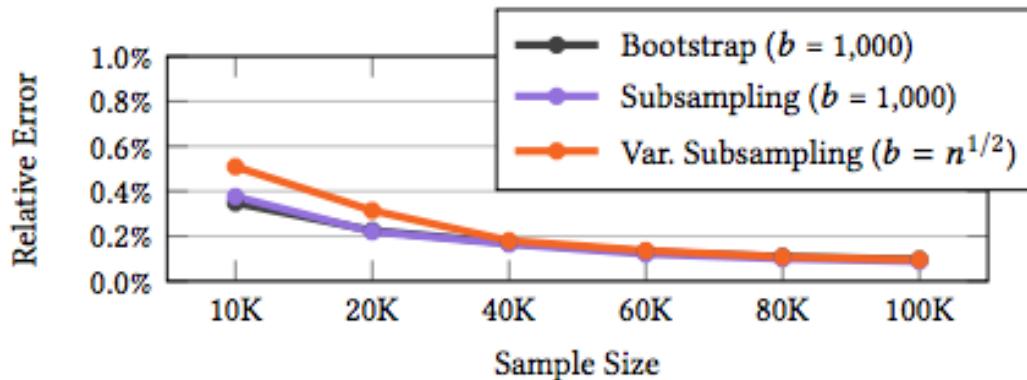


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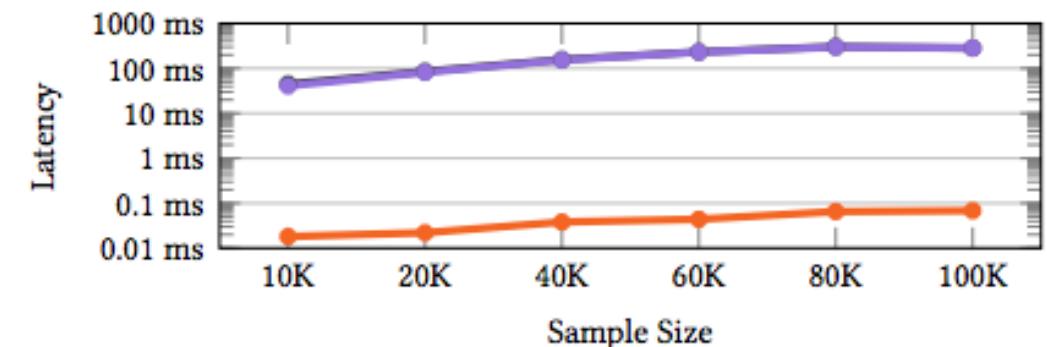
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# Variational subsampling: convergence rate



(a) Accuracy of error bound estimation



(b) Latency of error bound estimation

The accuracy was *almost the same* for relatively large samples.

Variational subsampling was *significantly faster*.

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Open-sourced (Apache v2.0): <http://verdictdb.org>

# Future Work

Development

Research

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- Adding more **drivers** (Presto, Teradata, Oracle, SQL Server, ...)

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- Adding more **drivers** (Presto, Teradata, Oracle, SQL Server, ...)

## Research

- Support for **online sampling**
- Robust **physical designer** (see CliffGuard @ SIGMOD 15)
- Integration with **ML libraries** (sampling-based model tuning)



# Thank You

# VerdictDB: current status

- We support
  - aggregates: sum, count, avg, count-distinct, quantiles, UDAs
  - sources: base table, derived table, equi-join
  - filters: comparison, some subquery
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- Upcoming features
  - Online sampling, automated physical designer

# Example of query rewriting

**original**

```
select l_returnflag , count (*) as cc  
from lineitem  
group by l_returnflag ;
```

**rewritten**

```
select vt1 .`l_returnflag ` AS `l_returnflag `,  
       round ( sum (( vt1 .`cc ` * vt1 .`sub_size `)) / sum ( vt1 .`sub_size `)) AS `cc `,  
       (stddev ( vt1 .`count_order `) * sqrt ( avg ( vt1 .`sub_size `)))  
         / sqrt ( sum ( vt1 .`sub_size `)) AS `cc_err `  
  from (select vt0 .`l_returnflag ` AS `l_returnflag `,  
           (( sum ((1.0 / vt0 .`sampling_prob `)) / count (*))  
             * sum ( count (*)) OVER ( partition BY vt0 .`l_returnflag `)) AS `cc `,  
           vt0 .`sid ` AS `sid `, count (*) AS `sub_size `  
        from lineitem_sample vt0  
        GROUP BY vt0 .`l_returnflag ` , vt0 .`sid `) AS vt1  
  GROUP BY vt1 .`l_returnflag `;
```

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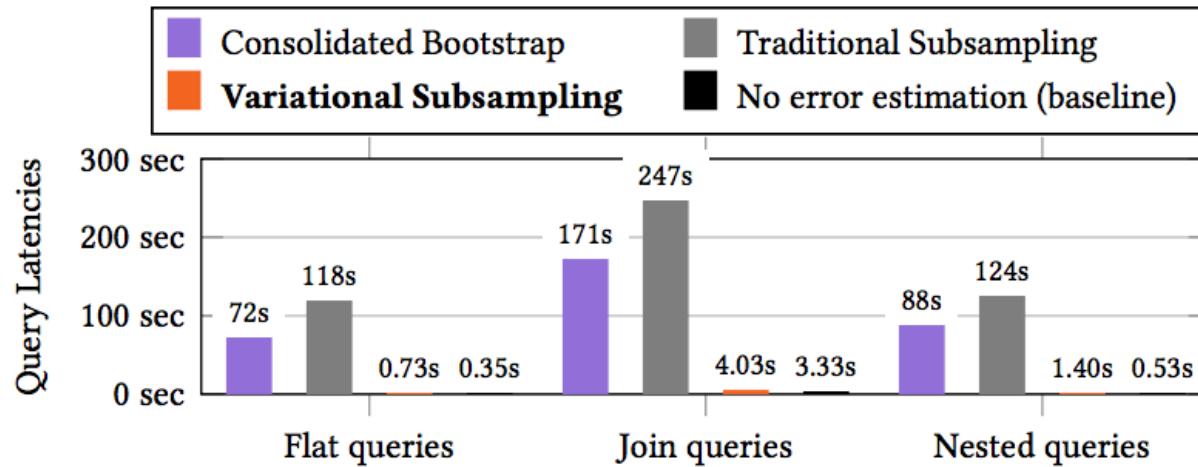
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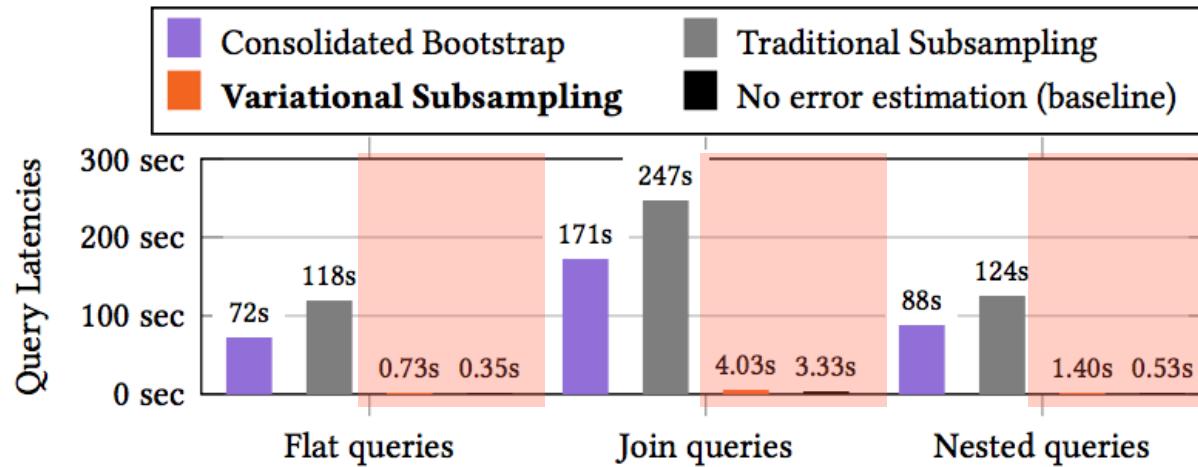
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**[Politis '94]** Politis, Dimitris N., and Joseph P. Romano. "Large sample confidence regions based on subsamples under minimal assumptions." *The Annals of Statistics*, 1994

# Variational subsampling: overhead

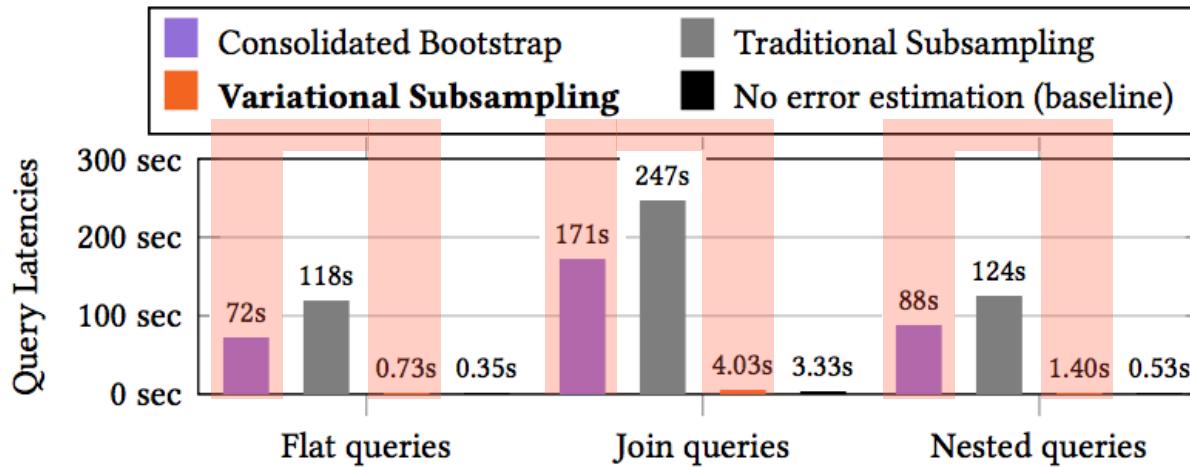


# Variational subsampling: overhead



Overhead of *variational subsampling*: 0.38–0.87 seconds

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*Variational subsampling was 100×–237× faster compared to Consolidated Bootstrap.*