

# Documentation for the pyroll-thermal-2d Plugin

Max Weiner

January 13, 2023

## 1 Model Description

$$0 = \dot{q}_1 - \dot{q}_2 - \dot{q}_3 + \dot{q}_4 + \dot{q}_S \quad (1)$$

$$\dot{q}_1 = \varrho c_p \dot{V} T_i^n \quad (2)$$

$$\dot{q}_2 = \varrho c_p \dot{V} T_i^{n+1} \quad (3)$$

$$\dot{q}_3 = -\lambda \frac{T_{i+1}^n - T_i^n}{\Delta r} \times 2\pi \left( r_i + \frac{\Delta r}{2} \right) \Delta x \quad (4)$$

$$\dot{q}_4 = -\lambda \frac{T_i^n - T_{i-1}^n}{\Delta r} \times 2\pi \left( r_i - \frac{\Delta r}{2} \right) \Delta x \quad (5)$$

$$\dot{q}_S = \eta_S \frac{k_f}{\eta_\varphi} \dot{\varphi} \quad (6)$$

$$\dot{q}_3 = [-\alpha (T_\infty - T_S) - \epsilon_0 \epsilon_r (T_\infty^4 - T_S^4)] \times 2\pi \left( r_i + \frac{\Delta r}{2} \right) \Delta x \quad (7)$$

$$2\lambda \frac{T_S - T_i^n}{\Delta r} = \alpha (T_\infty - T_S) + \epsilon_0 \epsilon_r (T_\infty^4 - T_S^4) \quad (8)$$

for core layer  $\dot{q}_4 = 0$

$$\Delta T_0 = \frac{1}{\varrho c_p \dot{V}} [\pi \lambda \Delta x (T_1^n - T_0^n) + \dot{q}_S] \quad (9)$$

$$\Delta T_i = \frac{1}{\varrho c_p \dot{V}} \left[ \frac{2\pi \lambda \Delta x}{\Delta r} \left[ (T_{i+1}^n - T_i^n) \left( r_i + \frac{\Delta r}{2} \right) - (T_i^n - T_{i-1}^n) \left( r_i - \frac{\Delta r}{2} \right) \right] + \dot{q}_S \right] \quad (10)$$

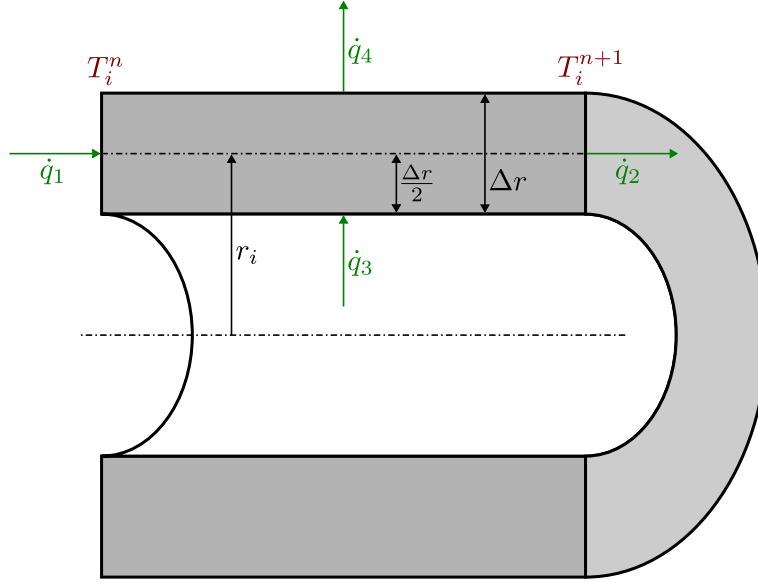


Figure 1: Heat Flows on a Disk Element Ring

$$\Delta T_i = \frac{1}{\rho c_p \dot{V}} \left[ 2\pi \Delta x \left[ \left[ -\alpha (T_\infty - T_S) - \epsilon_0 \epsilon_r (T_\infty^4 - T_S^4) \right] \left( r_i + \frac{\Delta r}{2} \right) - \lambda \frac{T_i^n - T_{i-1}^n}{\Delta r} \left( r_i - \frac{\Delta r}{2} \right) \right] + \dot{q}_S \right] \quad (11)$$

## 2 Plugin Usage

### Symbols

Symbol	Description
$\alpha$	Heat transfer coefficient
$c_p$	Thermal Capacity
$\epsilon_0$	Radiation coefficient of black radiator
$\epsilon_r$	Relative radiation coefficient
$\eta_S$	Efficiency of heat source by deformation
$\eta_\varphi$	Efficiency of deformation
$i$	Index of raster in radius

Continued on next page

Table 0: (Continued)

$\hat{i}$	Maximum index of raster in radius
$k_f$	Flow stress
$\lambda$	Thermal conductivity
$\dot{m}$	Mass flow in x-direction
$n$	Index of raster in x
$\hat{n}$	Maximum index of raster in x
$\varphi$	Equivalent strain
$\dot{\varphi}$	Equivalent strain rate
$\dot{q}$	Heat flow
$\dot{q}_S$	Heat source (generation)
$r$	Radius coordinate in polar systems
$\Delta r$	Discretization width in radius
$\varrho$	Density
$t$	Time
$\Delta t$	Discretization width in time
$T$	Absolute temperature
$\Delta T$	Increment of temperature
$T_\infty$	Environment temperature
$T_S$	Absolute surface temperature
$V$	Volume of the disk element rep. layer
$\dot{V}$	Volume flow
$x$	X Coordinate
$\Delta x$	Discretization width in x