

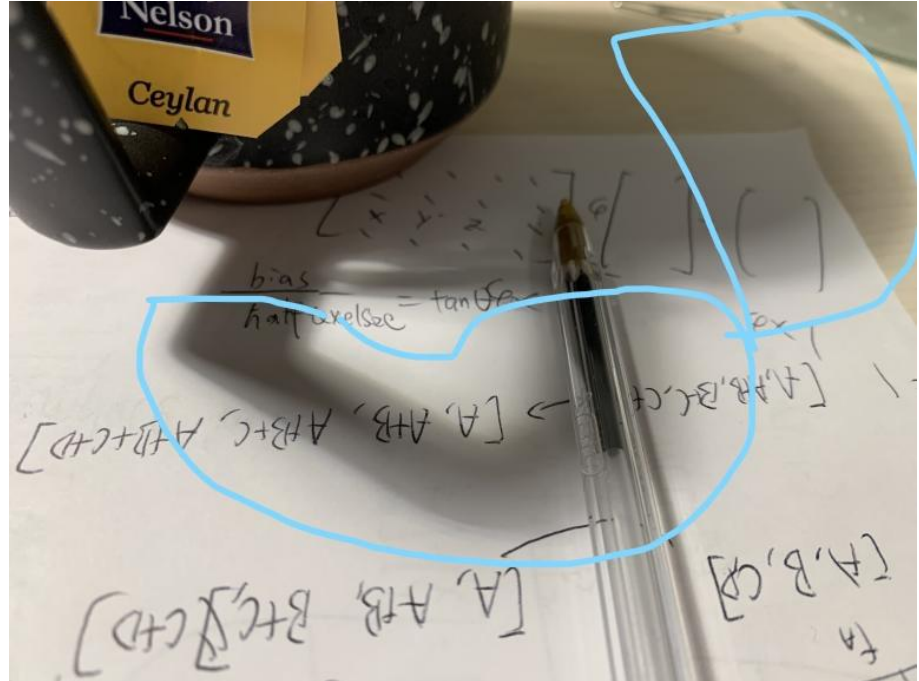
# IG3DA-Project: Variance Soft Shadow Mapping

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# What Variance Soft Shadow Mapping(VSSM) does?

To render soft shadow(e.g. penumbra)



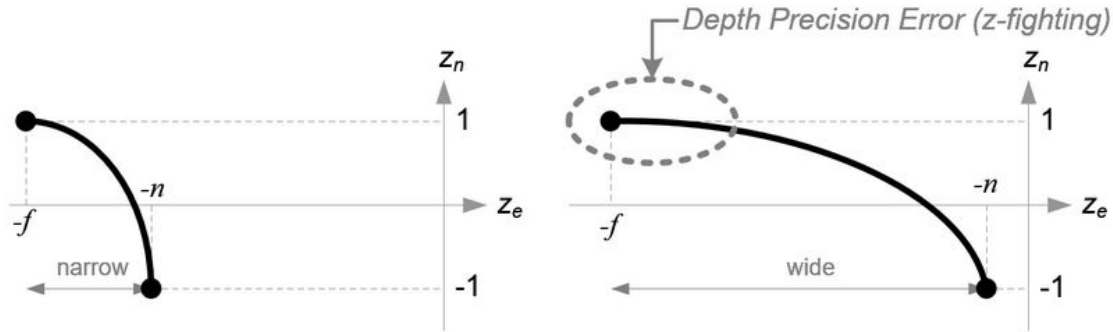


## Related work

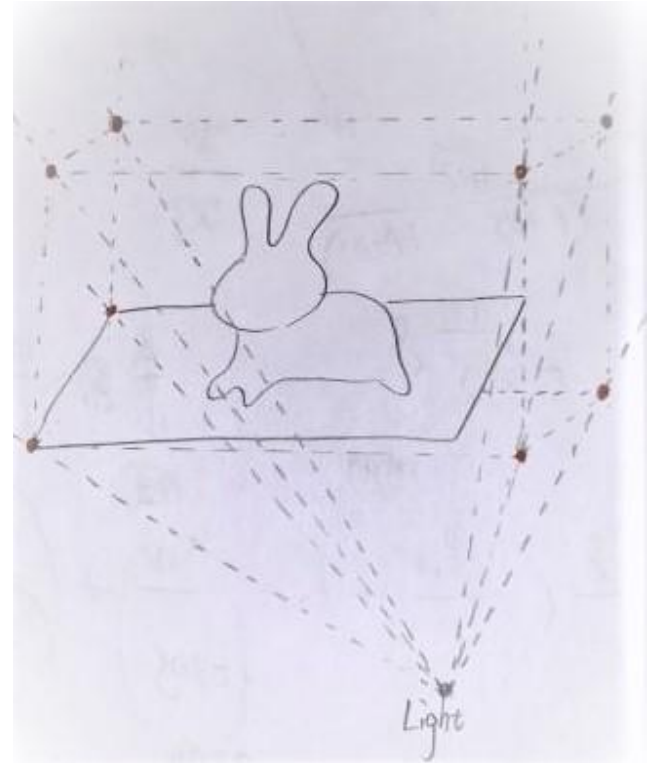
- Shadow Maps
- Percentage-Closer Filtering(PCF)
- Percentage-Closer Soft Shadow(PCSS)
- Variance Shadow Maps(VSM)
- Summed-Area Table(SAT)
- Summed-Area Table Variance Shadow Maps(SAT-VSM)

# Implementation

# Shadow Maps



Comparison of Depth Buffer Precisions





# PCF

0	0	0	1
0	0	1	1
1	1	1	1
1	1	1	1

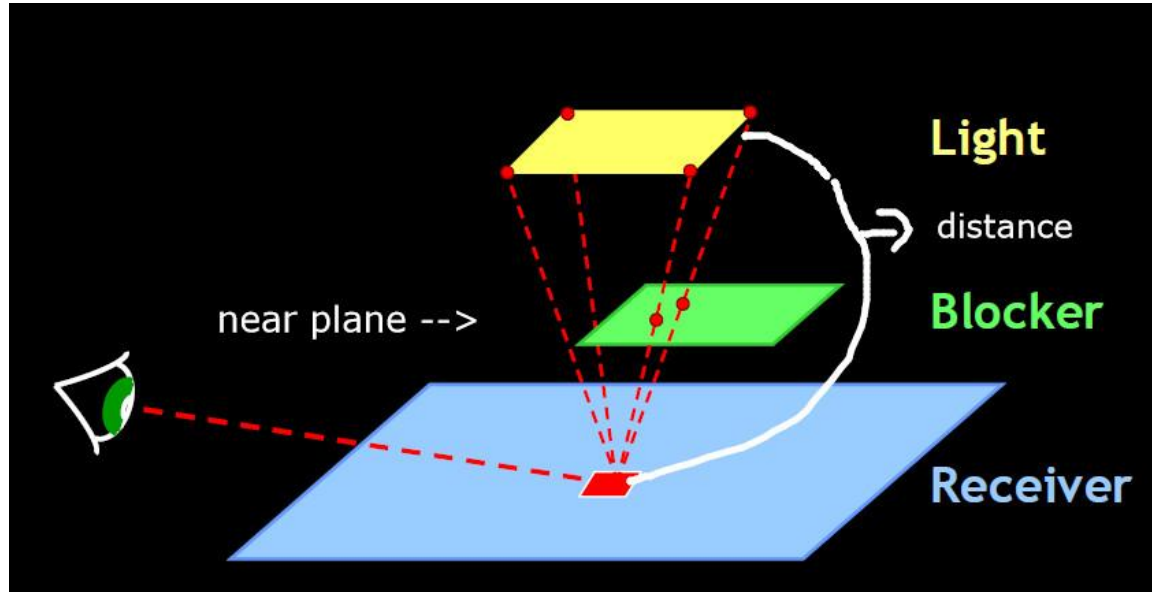
Averaged result =  $(0+1+1+1)/4 = 0.75$

2\*2 kernel



## PCSS

- Compute averaged blocker depth
- Penumbra size estimation
- Use PCF with penumbra size to filter depth-test results



$$\begin{aligned} \text{Blocker Search Size} &= (\text{distance} - \text{near}) / \text{distance} * \text{LightSize} \\ &= (\text{distance} - \text{near}) / \text{distance} * \text{MaxSearchSize} \end{aligned}$$



$$\omega_{penumbra} = \frac{\omega_{light}(d_{receiver} - d_{blocker})}{d_{blocker}}$$
$$= \omega_{light} \left( \frac{d_{receiver}}{d_{blocker}} - 1 \right)$$

Clamp the penumbra size into user-defined range [min, max]



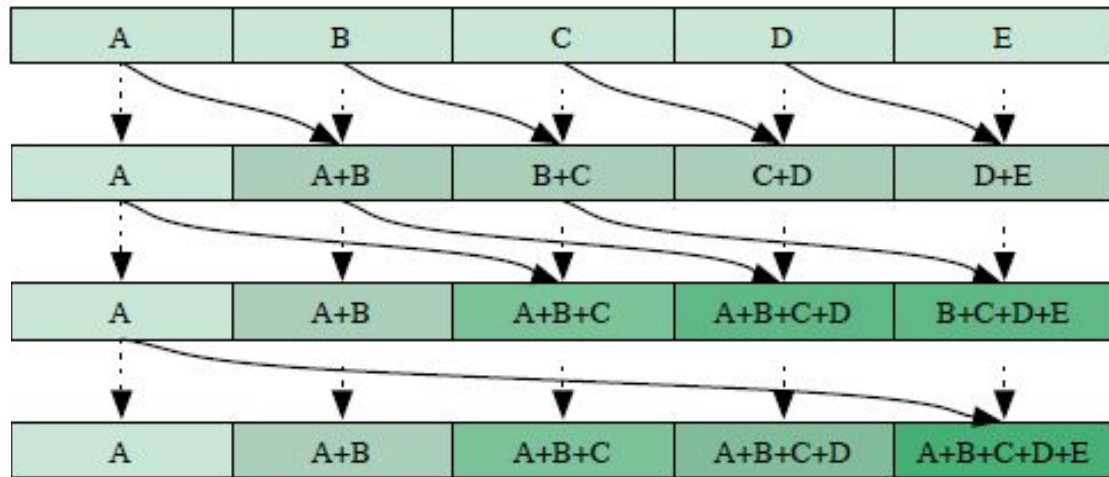
# SAT

1	1	1
1	1	1
1	1	1

Input image

1	2	3
2	4	6
3	6	9

Integral image



**Origin(0,0) is at left-top**

**recursive doubling algorithm**

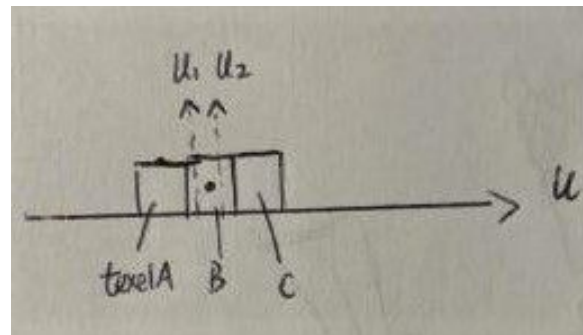
- 32-bits Texture for storage
- Reading 8 texels at the same time
- Minus 0.5 for each texel before generating SAT



# VSM

$$M_2 = \mu^2 + \frac{1}{4} \left( \left[ \frac{\partial f}{\partial x} \right]^2 + \left[ \frac{\partial f}{\partial y} \right]^2 \right). \quad \text{Instead of} \quad M_2 = E(x^2) = \int_{-\infty}^{\infty} x^2 p(x) dx$$



- Linear depth scaled into [0,1] not projected depth(no z-fighting)
- Minimum variance to eliminate shadow acne
- Minimum pMin to reduce light bleeding
- 32-bits floating-point RG-color texture(mipmap, linear interpolation)
- Four neighbor texels for bilinear interpolation





## An attempt of separating lighting and shadowing

$$colorResponse = ambient + lightRatio * (diffuse + specular)$$


- Can we use two separate passes: one for light ratio computation (shadowing), one for lighting (diffuse, specular), then use any filter function to filter the light ratio (shadow)?
- Light ratio texture (32-bits floating point) → crack issue
- Not every decimal has a terminating representation in binary format. (0.25 or 0.5 ) (0.3  → be truncated)
- Possible solution: Floating-value represented by two integers can solve.





## **VSSM $\approx$ (SAT-VSM+PCSS)**

- Novel formula for averaged blocker depth  $Z_{Occ} = \frac{Z_{Avg} - P_{max}Z_{unocc}}{1 - P_{max}}$
- Subdivision scheme to solve “non-planarity” issue



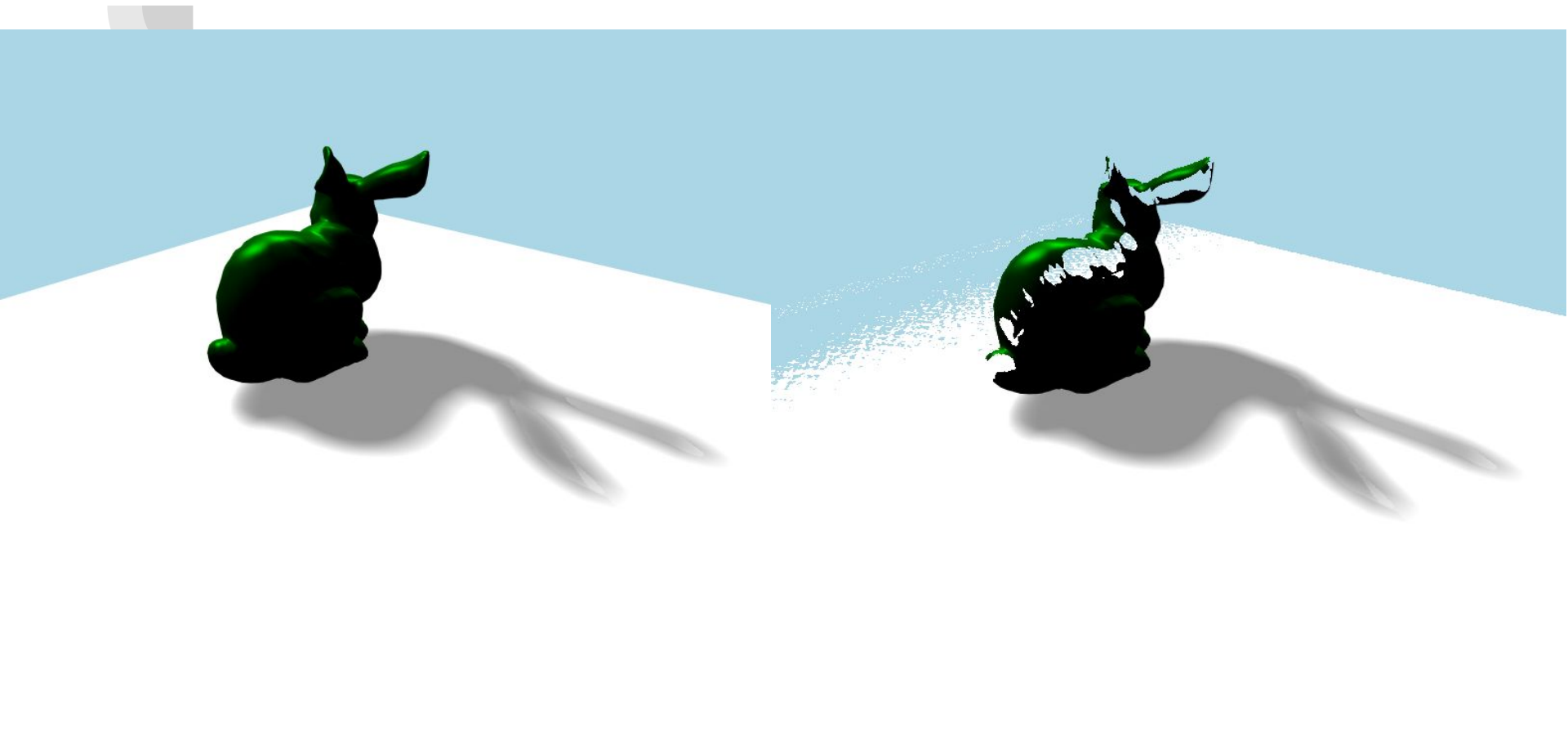
$$Z_{Avg} \geq d \quad \text{"Non-planarity" condition}$$

when  $Z_{Avg} < d$  (they call it as planar case)

they use 
$$Z_{Occ} = \frac{Z_{Avg} - P_{max}Z_{unocc}}{1 - P_{max}} \quad \text{and assume} \quad Z_{unocc} = d$$

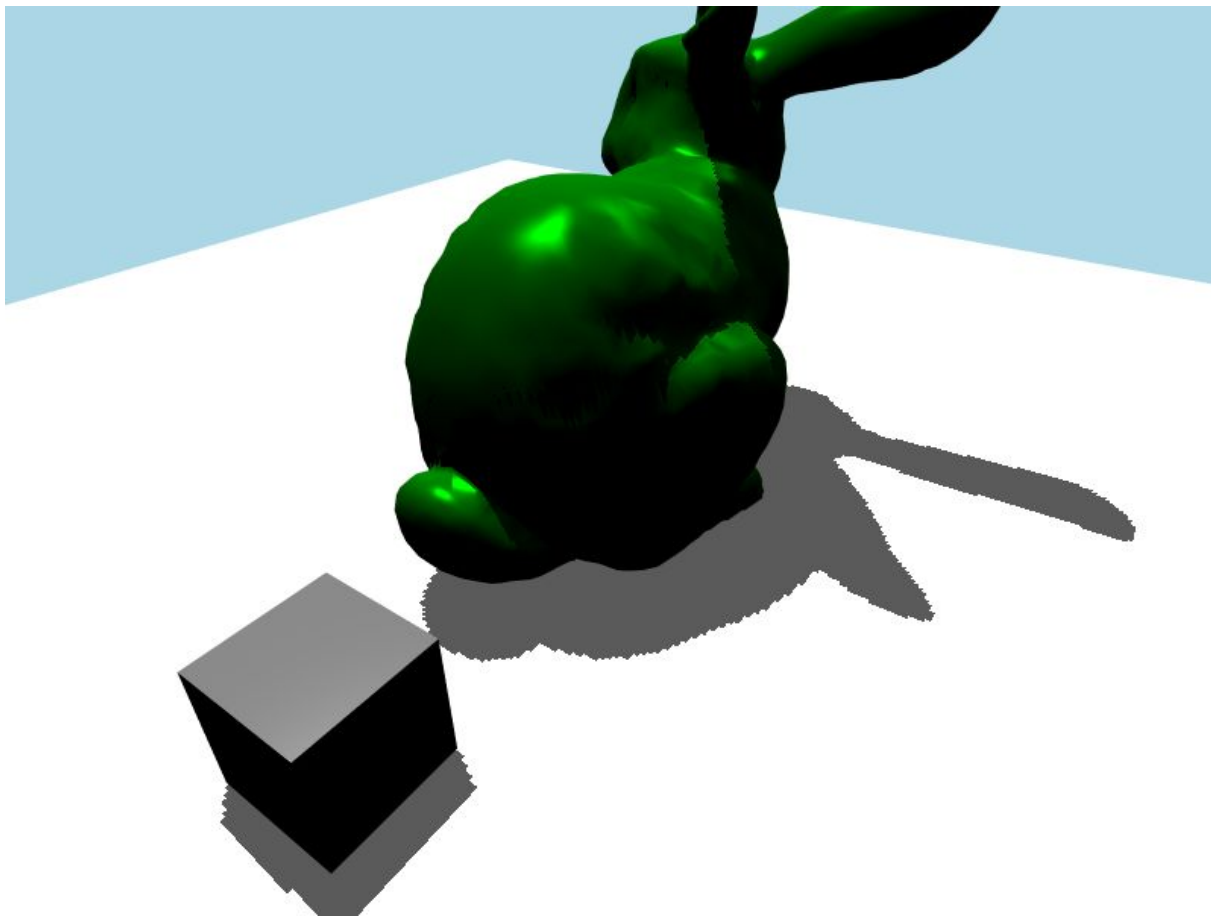
·  $Z_{Avg} < d$ , we can let  $Z_{Avg} = P_0d$ , and  $P_0$  must be less than 1.

$$Z_{Occ} = (P_0 - P_{max})\left(\frac{d}{1 - P_{max}}\right) \quad \rightarrow \quad Z_{Occ} \text{ can be negative!!!}$$

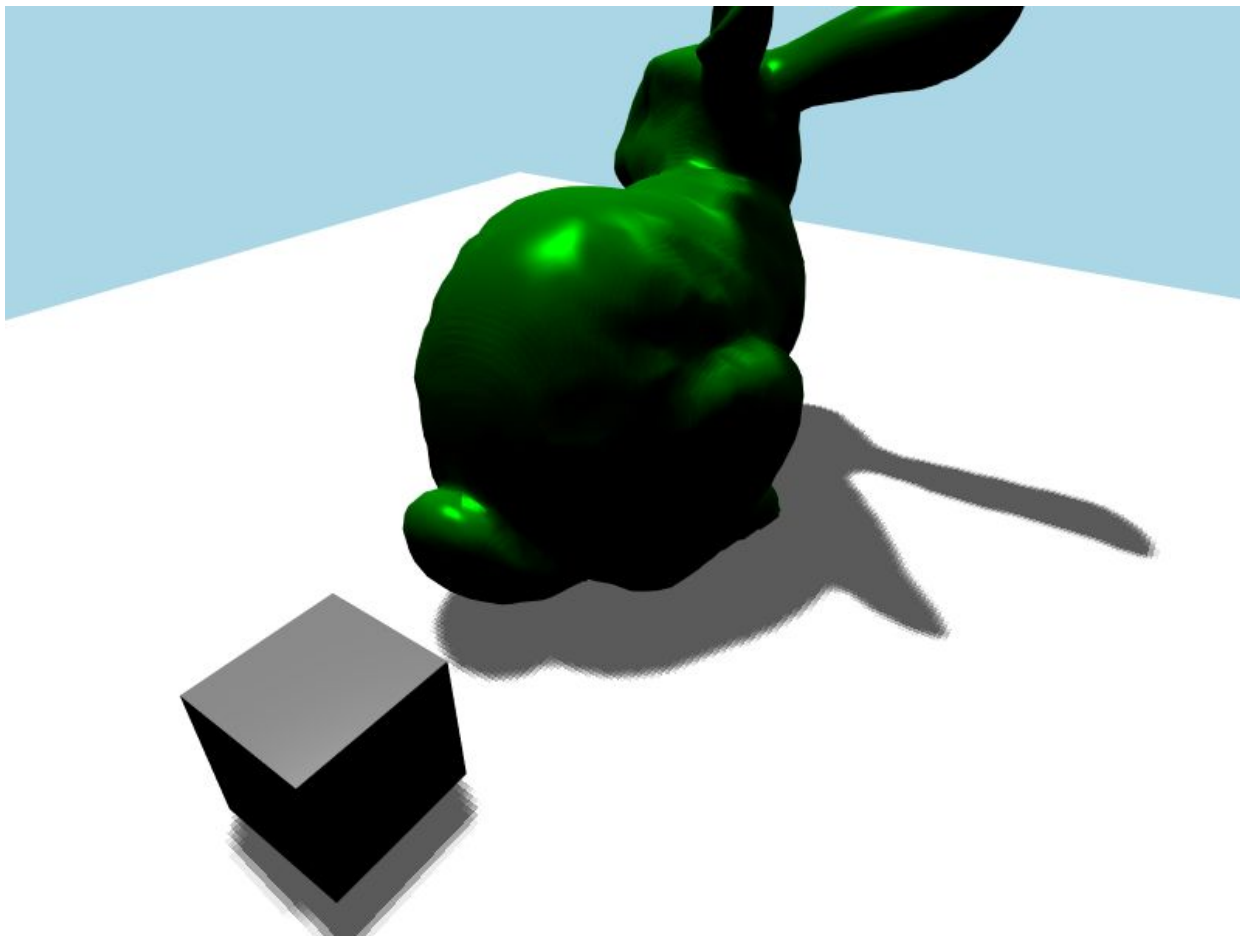




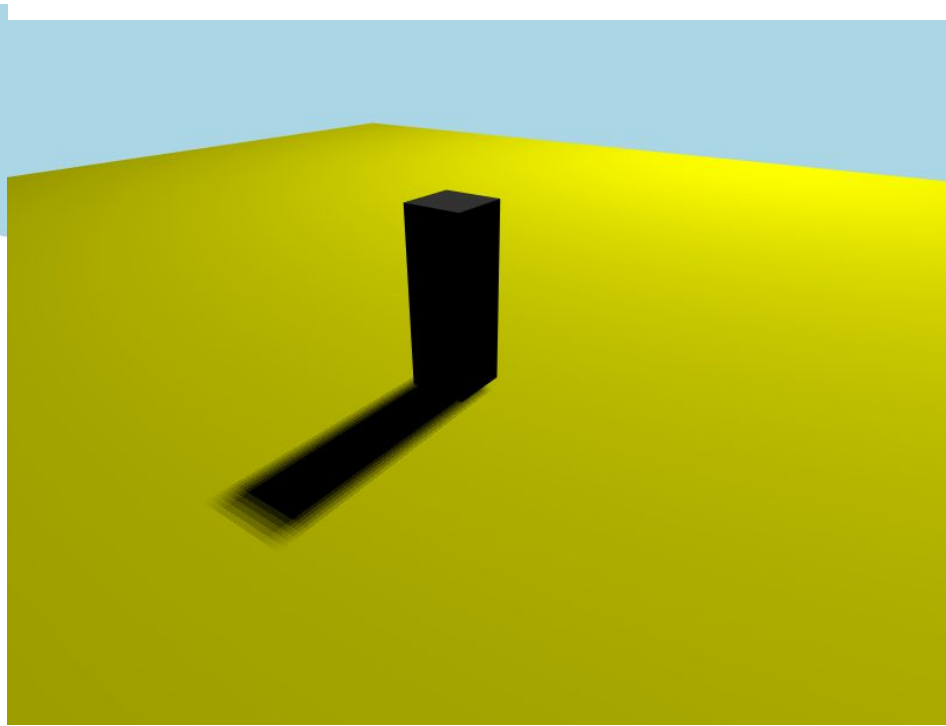
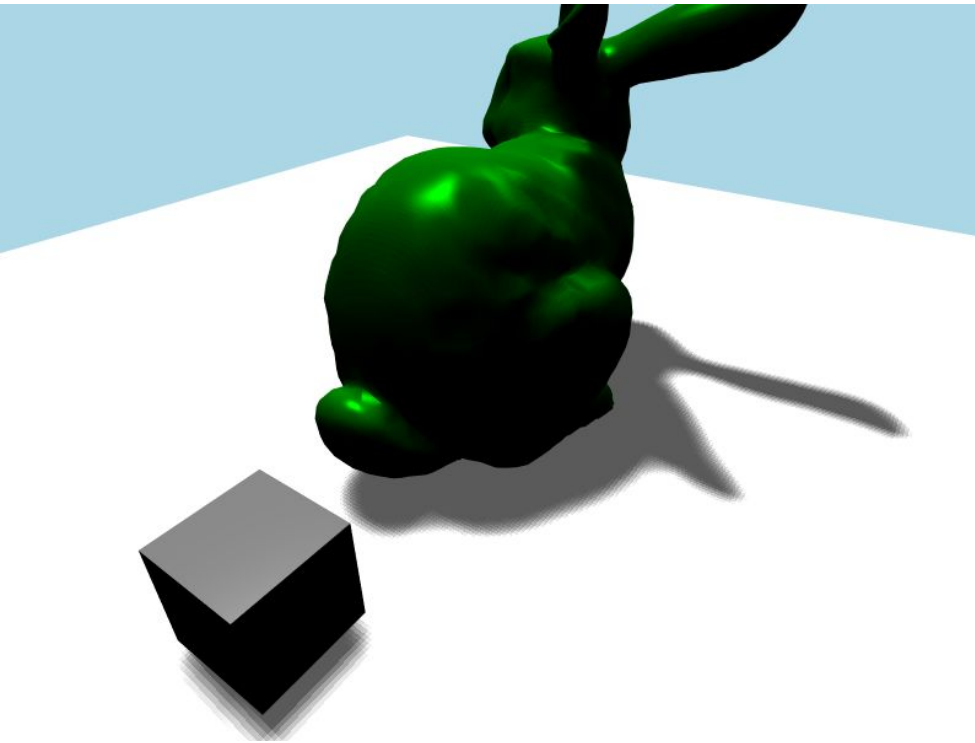
# Results



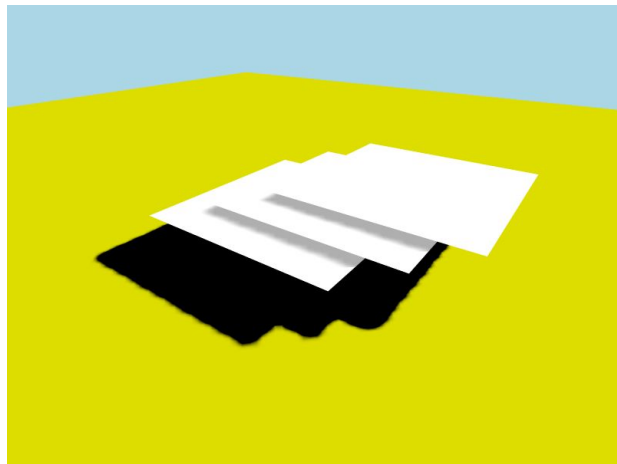
Basic Shadow Maps



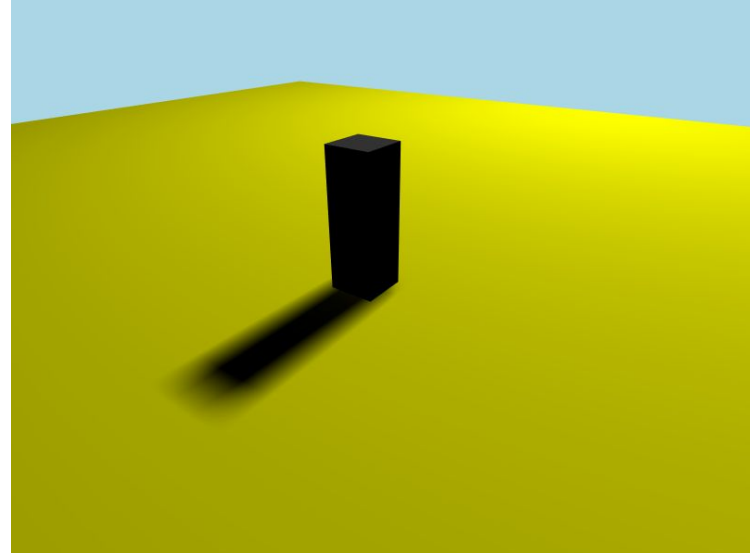
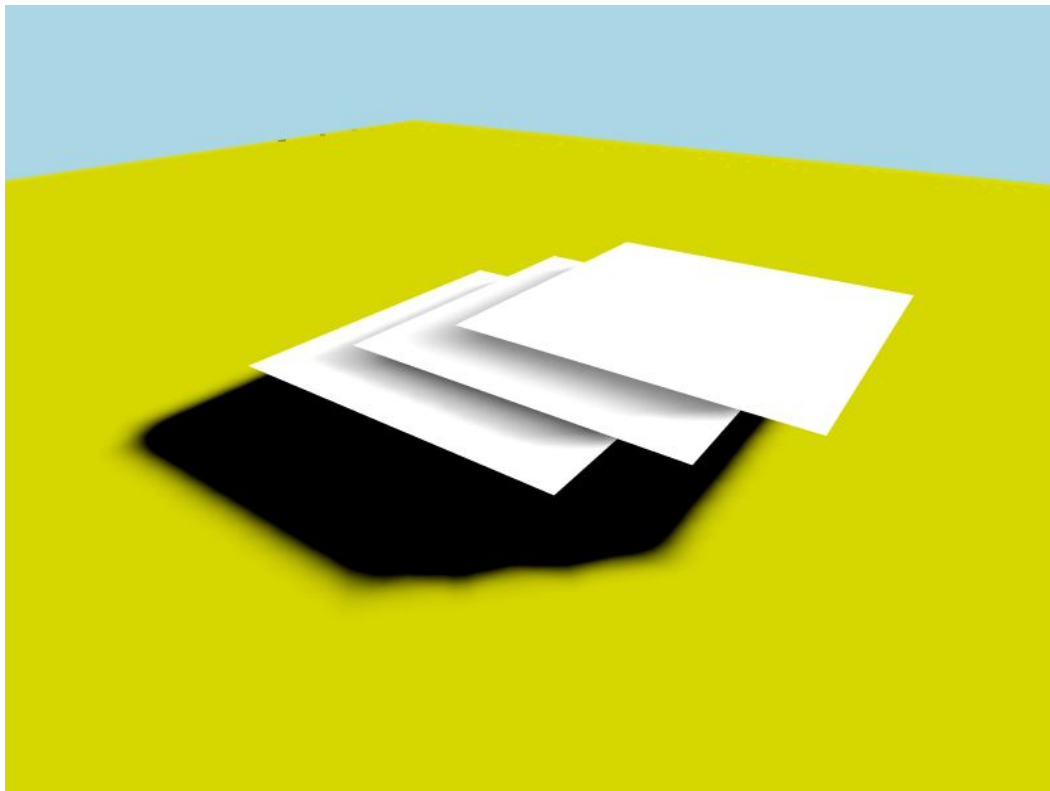
Shadow Maps + PCF



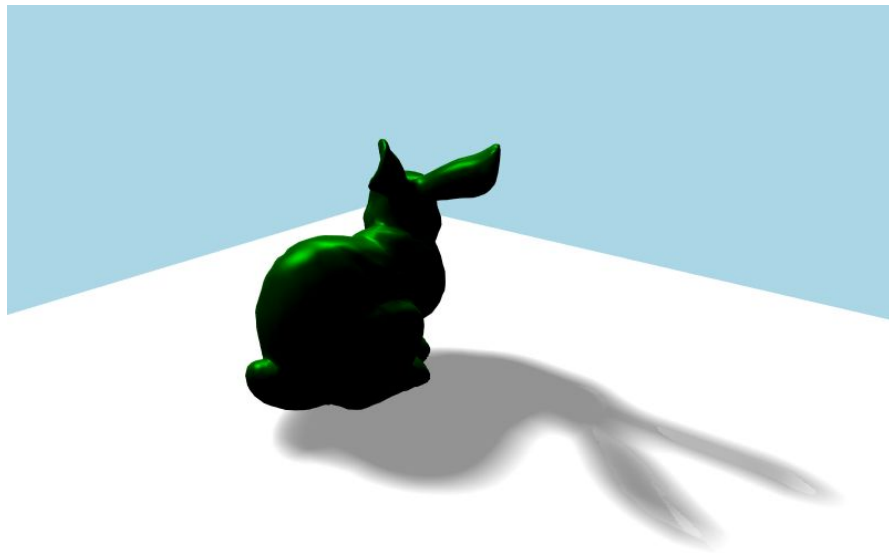
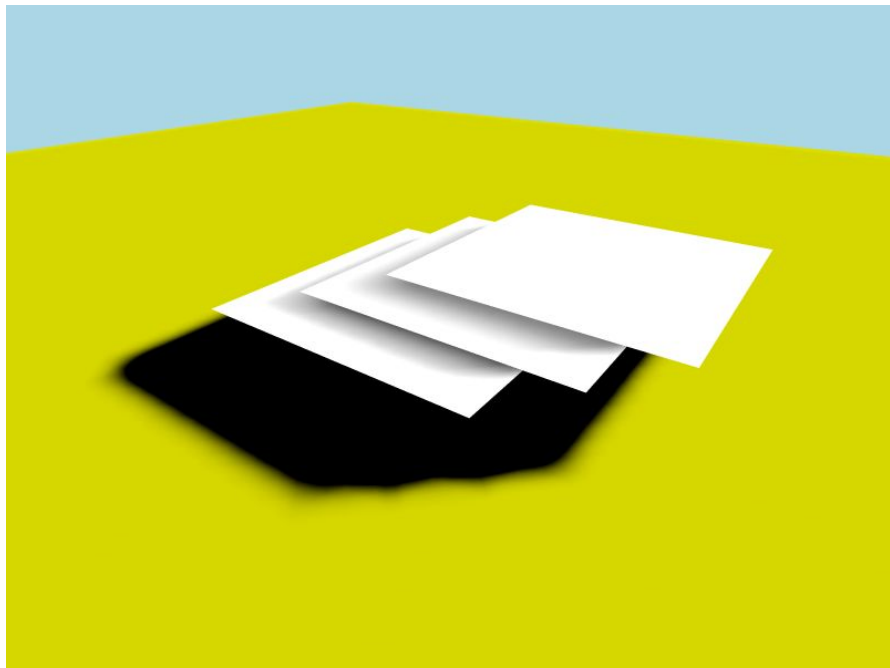
Shadow Maps + PCSS



VSM



VSM+PCSS



VSSM

**Thank you**