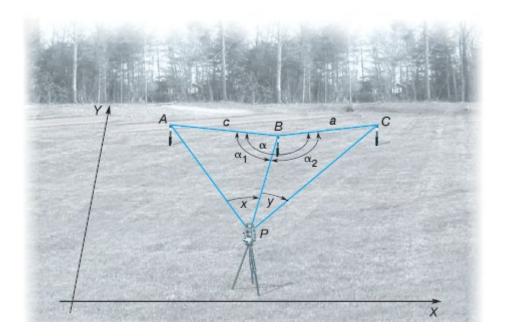
Three-point resection

This procedure locates a point of unknown position by observing horizontal angles from that point to three visible stations whose positions are known. Referring to the figure below, a total station instrument occupies station P, and angles x and y are observed. A summary of the method used to compute the coordinates of station P follows:



- 1. From the known coordinates of A, B, and C calculate lengths a and c, and angle α at station B.
- 2. Subtract the sum of angles x, y, and α in figure ABCP from 360° to obtain the sum of angles A + C

$$A + C = 360^{\circ} - (\alpha + x + y)$$

3. Calculate angles A and C using the following:

$$A = \tan^{-1} \left(\frac{a \sin x \sin (A + C)}{c \sin y + a \sin x \cos (A + C)} \right)$$
$$C = \tan^{-1} \left(\frac{c \sin y \sin (A + C)}{a \sin x + c \sin y \cos (A + C)} \right)$$

- 4. From angle A and azimuth AB, calculate azimuth AP in triangle ABP. Then solve for length AP using the law of sines, where α_1 = 180° A x. Calculate the Δ E and Δ N of AP followed by the coordinates of P.
- 5. In the manner outlined in step 4, use triangle *BCP* to calculate the coordinates of P to obtain a check.

Reference:

Elementary Surveying - An Introduction to Geomatics 13th ed - E. Ghilani, P. Wolf (Pearson, 2012)