Statistical Data Mining

SNACKCHAIN FINAL PROJECT

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Introduction

Our objective in the final project is to present our findings from analyzing sales and promotions data from a large retail chain. The sales data is comprised of over 500,000 transactions from 79 stores and 58 products belonging to four product categories (bagged snacks, cold cereal, frozen pizza, and oral hygiene products) over a period of 156 weeks. For this assignment, we have excluded products belonging to the oral hygiene category. In this paper we will be discussing the effects of the pricing and promotion strategies on total spending for that product, the number of households who purchased that product, the number of store visits, and the most elastic and inelastic products. At the end of the analysis, we are interested in answering the following questions:

- 1) What is the effect of promotions, displays, or being featured in the circular on product sales (spend), unit sales, and the number of household purchasers?
- 2) How do the above effects vary by product categories (cold cereals, frozen pizza, bag snacks) and store segments (mainstream, upscale, value)?
- 3) What are the five most prices elastic and five least price-elastic products? Price elasticity is the change in sales for a unit change in product price.
- 4) As the retailer, which products would you lower the price to maximize (a) product sales and (b) unit sales, and why?

Details of the data files are listed below.

File	Description	Columns
Stores	Contains	Store ID, Store Name, City, State,
	information about	Metropolitan Statistical Area, Store
	each store location	Type, Number of Parking Space,

		Square Footage, Average Weekly Baskets
Products	Contains information about each product that is sold	Universal Product Code, Description, Manufacturer, Category, Subcategory, Product Size
Transactions	Contains information about each transaction that is performed at each store	Week-End Date, Store Num, Universal Product Code, Units Sold, Number of Unique Purchases That Included The Product, Number Of Purchasing Households, Total Spend, Price, Base Price, If Product Was In In-Store Circular, If Product Was A Part Of In- Store Promotional Display, Temporary Price Reduction Only

Data Pre-Processing and Data Cleaning

We used the R Code below to clean and pre-process the data

```
rm(list=ls())
library(rio)
#Import SnackChain.Xlsx file.
stores df
               <- import("~/Downloads/SnackChain.xlsx", sheet="stores")</pre>
#79 stores
products df
                <- import("~/Downloads/SnackChain.xlsx", sheet="products")</pre>
#58 products
transactions df <- import("~/Downloads/SnackChain.xlsx",</pre>
sheet="transactions") #524950 transactions
#Joining Tables.
temp <- merge(transactions df, products df, by.x=c("UPC"), by.y=c("UPC"))</pre>
#join by UPCs between transactions and products
    <- merge(temp, stores df, by.x=c("STORE NUM"), by.y=c("STORE ID"))</pre>
#join by adding the stores.
#Removing temporary Files.
rm(transactions df)
rm(stores df)
rm(temp)
rm(products df)
#Data Preprocessing
#Remove oral hygiene products
df <- df[df$CATEGORY != "ORAL HYGIENE PRODUCTS", ] #this could be for</pre>
another project
#Check for missing values
colSums(is.na(df))
```

```
#' 282548 missing PARKING values; we will not use this data since it is
higher (store) level,
#' 10 NA values for price and 173 for BASE PRICE
df <- subset(df, select = -c(PARKING))</pre>
df <- df[complete.cases(df), ] #Removing missing values</pre>
View(df)
#Renaming columns to make them easier to understand
colnames(df)[colnames(df) == "STORE NUM"] = "store id"
colnames(df) [colnames(df) == "UPC"] = "product id"
colnames(df) [colnames(df) == "WEEK END DATE"] = "week ending date"
colnames(df)[colnames(df) == "UNITS"] = "units sold"
colnames(df) [colnames(df) == "VISITS"] = "unique purchases"
colnames(df) [colnames(df) == "HHS"] = "purchasing households"
colnames(df)[colnames(df) == "SPEND"] = "total spend"
colnames(df)[colnames(df) == "PRICE"] = "price product charged"
colnames(df)[colnames(df) == "BASE PRICE"] = "base price product"
colnames(df) [colnames(df) == "FEATURE"] = "circular"
colnames(df)[colnames(df) == "DISPLAY"] = "promotional display"
colnames(df)[colnames(df) == "TPR ONLY"] = "temp price reduction"
colnames(df)[colnames(df) == "DESCRIPTION"] = "product"
colnames(df)[colnames(df) == "MANUFACTURER"] = "manufacturer"
colnames(df) [colnames(df) == "CATEGORY"] = "category"
colnames(df) [colnames(df) == "SUB CATEGORY"] = "subcategory"
colnames(df)[colnames(df) == "PRODUCT SIZE"] = "size"
colnames(df)[colnames(df) == "STORE NAME"] = "store name"
colnames(df)[colnames(df) == "CITY"] = "city"
colnames(df) [colnames(df) == "STATE"] = "state"
colnames(df)[colnames(df) == "MSA"] = "metropilitan area"
colnames(df) [colnames(df) == "SEGMENT"] = "type_of_store"
colnames(df)[colnames(df) == "SIZE"] = "store sqft"
colnames(df) [colnames(df) == "AVG WEEKLY BASKETS"] =
"avg weekly baskets sold"
#Converting Categorical variables into factor variables.
df$store id = factor(df$store id)
df$product id = factor(df$product id)
df$category = factor(df$category)
df$subcategory = factor(df$subcategory)
df$category = relevel(df$category, "BAG SNACKS")
df$city = factor(df$city)
df$state = factor(df$state)
df$type of store = factor(df$type of store)
df$type of store = relevel(df$type of store, "VALUE")
df$product = factor(df$product)
#Extracting year, month, and week ending date from date.
df$year = format(df$week ending date, "%\overline{Y}")
df$year = factor(df$year)
df$month = format(df$week ending date, "%b")
df$month = factor(df$month)
df$month = relevel(df$month, "Jan")
```

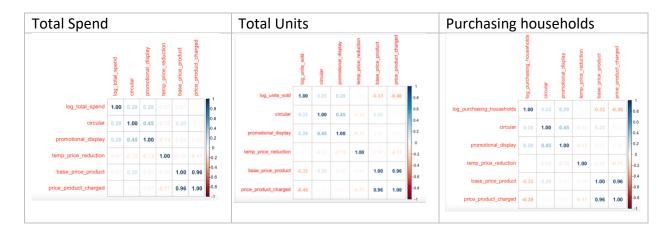
```
df$week_num = difftime(df$week_ending_date, df$week_ending_date[1],
units="weeks")
df$week_num = df$week_num + 1
attach(df)
str(df)
View(df)
```

Data after cleaning:

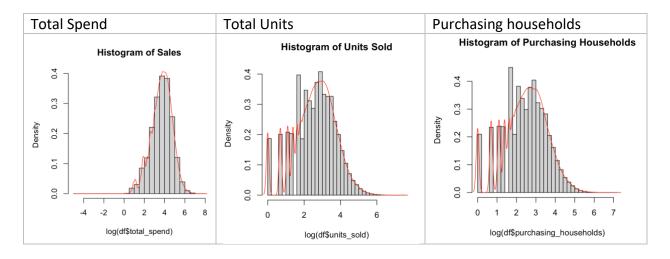
•	store_id [‡]	product	t_id 🗦	week_end	ding_date	un	its_sold 🗦	unique_p	ourchases 🚊	purchasing_hou	seholds 🗦	total_sp	end 🗦	price_product_char	ged 🏺 ba	se_price_p	oroduct 🗦	circular
1	367	111100	9477	2009-01-	-14		13		13		13		18.07		1.39		1.57	
2	367	702731	6204	2009-06-	-03		15		9		9		26.25		1.75		2.47	
4	367	111108	5319	2009-01-	-14		14		13		13		26.32		1.88		1.88	
5	367	719210	0336	2010-02-	-24		1		1		1		6.99		6.99		6.99	
6	367	111108	5350	2009-01-	-14		35		27		25		69.30		1.98		1.98	
	promotional_di:	splay	temp_	price_redu	ction ‡	product			manufacturer	category	subcatego	ory ‡	size	store_name ‡	city	state	metropili	tan_area 🌼
0		0			1	PL MINI	TWIST PRETZ	ELS	PRIVATE LABEL	BAG SNACKS	PRETZELS		15 OZ	15TH & MADISON	COVINGTO	N KY		17140
0		0			1	SHURGE	MINI PRETZE	LS	SHULTZ	BAG SNACKS	PRETZELS		16 OZ	15TH & MADISON	COVINGTO	N KY		17140
0		0			0	PL HON	EY NUT TOAS	TD OATS	PRIVATE LABEL	COLD CEREAL	. ALL FAMIL	Y CEREAL	12.25 O	Z 15TH & MADISON	COVINGTO	N KY		17140
0		0			0	DIGIORN	O THREE ME	AT	TOMBSTONE	FROZEN PIZZA	A PIZZA/PRE	MIUM	29.8 OZ	15TH & MADISON	COVINGTO	N KY		17140
0		0			0	PL BT SZ	FRSTD SHRD	WHT	PRIVATE LABEL	COLD CEREAL	ALL FAMIL	Y CEREAL	18 OZ	15TH & MADISON	COVINGTO	N KY		17140
typ	e_of_store		ore_s	qft 🗦	avg_we	eekly_	baskets_s	old [‡]	year ‡	month [‡]	week_nu	m ÷						
VA	LUE			24721			1	2706.53	2009	Jan	1 weeks							
VA	LUE			24721			1	2706.53	2009	Jun	21 weeks	5						
VA	LUE			24721			1	2706.53	2009	Jan	1 weeks							
VA	LUE			24721			1	2706.53	2010	Feb	59 weeks	5						
VA	LUE			24721			1	2706.53	2009	Jan	1 weeks							

Data Visualization

Correlation matrix



Histograms



Effect of promotional displays or being featured in the circular

PLM Models

Variable	Model	R2 Value
Total Spend	spendrandom <- plm(log(total_spend) ~ circular	0.126
	+ promotional_display	
	+ temp_price_reduction	
	+ price_product_charged	
	+ week_num	
	+ category	
	+ month	
	+ type_of_store,	
	data=df, index=c("store_id"),model= "random")	
Total Units	unitsrandom <- plm(log(units_sold) ~ circular	0.289
	+ promotional_display	
	+ temp_price_reduction	
	+ price_product_charged	
	+ week_num	
	+ category	
	+ month	
	+ type_of_store,	
	data=df, index=c("store_id"),model= "random")	
Purchasing	hhsrandom <- plm(log(purchasing_households) ~ circular	0.284
Households	+ promotional_display	
	+ temp_price_reduction	
	+ price_product_charged	
	+ week_num	
	+ category	
	+ month	
	+ type_of_store,	
	data=df, index=c("store_id"), model = "random")	

Interpretation – PLM models

Interpretation – PLM mod			
Variables	Coefficient	P-Value	Interpretation
Effect of a product being featured in the <u>circular</u> on <u>total spend</u>	0.758	(0.005)	A correlation matrix and plm model output show a strong positive correlation between a store having a promotional display for a product and the total amount spent on an order, meaning if a product is featured on the circular, the customer is more likely to spend more on their order.
Effect of a product having a promotional display on total spend	0.534	(0.005)	The correlation matrix and plm model output shows strong positive correlation between a store having a promotional display for a product and the total amount spent on an order, meaning if a promotional display is present, the customer is more likely to make a more expensive order.
Effect of a product having a temporary price reduction on total spend	-0.084	(0.004)	The correlation matrix and plm model output shows a slight negative correlation between a product having a temporary price reduction and the total amount spent on an order, meaning if a product has a temporary price reduction, the customer is likely to spend less on their order.
Effect of a product being featured in the <u>circular</u> on <u>the number of units</u> sold	0.727	(0.005)	The correlation matrix and plm model output shows strong positive correlation between a product being featured on the circular and the number of units that a customer purchases, meaning if a product is featured on the circular, the customer is more likely to purchase more units.
Effect of a product having a promotional display on the number of units sold	0.574	(0.005)	The correlation matrix and plm model output shows strong positive correlation between a store having a promotional display for a product and the number of units that a customer purchases, meaning if a promotional display is present, the customer is more likely to purchase more units.
Effect of a product having a temporary price reduction on the number of units sold	-0.039	(0.004)	The correlation matrix and plm model output shows slight negative correlation between a product having a temporary price reduction and the number of units that a customer purchases, meaning if a product has a temporary price reduction, the customer is more likely to purchase less units.
Effect of a product being featured in the <u>circular</u> on <u>the number of</u> <u>purchasing households</u>	0.679	(0.005)	The correlation matrix and plm model output shows strong positive correlation between a product being featured on the circular and the number household purchasers, meaning if a product is featured on the circular, there is likely to be more household purchasers of the product.
Effect of a product having a promotional display on the number of purchasing households	0.570	(0.005)	The correlation matrix and plm model output shows strong positive correlation between a product being featured on the circular and the number household purchasers, meaning if a promotional display is present,

			there is likely to be more household purchasers of the product.
Effect of a product having a temporary price reduction on the number of purchasing households	-0.090	(0.004)	The correlation matrix and plm model output shows very slight negative correlation between a product having a temporary price reduction and the number household purchasers, meaning if a product has a temporary price reduction, there is likely to be less household purchasers of the product.

Effects by Product Category and Store Segments

LMER Models

Variable	Model	R2 Value
Total Spend	lm19 <- lme4::lmer(log_total_spend ~ promotional_display	R2C: 0.4148
(Category)	+ circular	
	+ temp_price_reduction	
	+ price_product_charged	
	+ week_num	
	+ month	
	+ category	
	+ (1 store_id) , data=df , REML = FALSE)	
Total Spend	Im22 = Ime4::Imer(log_total_spend ~ promotional_display	R2C: 0.2223
(Store Type)	+ circular	
	+ temp_price_reduction	
	+ price_product_charged	
	+ week_num	
	+ month	
	+ type_of_store + (1 store_id), data=df, REML = FALSE)	
Units Sold	Im20 = Ime4::Imer(log_units_sold ~ promotional_display	R2C: 0.4889
(Category)	+ circular	
	+ temp_price_reduction	
	+ price_product_charged	
	+ week_num	
	+ month	
	+ category	
	+ (1 store_id) , data=df , REML = FALSE)	
Units Sold	Im23 = Ime4::Imer(log_units_sold ~ promotional_display	R2C: 0.3525
(Store Type)	+ circular	
	+ temp_price_reduction	
	+ price_product_charged	
	+ week_num	
	+ month	
	+ type_of_store	
	+ (1 store_id) , data=df , REML = FALSE)	

Purchasing Households (Category)	<pre>Im21 <- Ime4::Imer(log_purchasing_households ~ promotional_display</pre>	R2C: 0.4984
Purchasing Households (Store Type)	<pre>Im24 <- Ime4::Imer(log_purchasing_households ~ promotional_display</pre>	R2C: 0.3537

Interpretation – LMER model (Category Only)

Variables	Correlation Coefficient	P-Value	Interpretation
Effect of a product being featured in the circular on total spend (Category)	0.530	(0.005)	There is a positive correlation between log(total spend) and being featured on the circular. Compared to the PLM model, the product category of an item on display at a store has less impact on the total amount spent on an order than and item being on display in general.
Effect of a <u>product</u> <u>promotion</u> on <u>total</u> <u>spend</u> (Category)	-0.022	(0.004)	There is a slight negative correlation between log(total spend) and product promotion. Compared to the PLM model without the Category fixed effect, both models show that a price reduction has no impact (or slightly less) on the total spend of a customer order.
Effect of a product on promotional display on total spend (Category)	0.686	(0.004)	There is a positive correlation between log(Total Spend) and a product on promotional display. Compared to the PLM model without the Category fixed effect, the category of an item on display does provide a greater positive impact on the total spend of an order then grouping the items together.
Effect of a product being featured in the circular on the number of units sold (Category)	0.507	(0.005)	There is a positive correlation between log(Units Sold) and being featured on the circular. Compared to the PLM model, the category of item being featured in the circular has less of a positive effect on the number of units sold than an item in general being featured in the circular.

Effect of a product promotion on the number of units sold (Category)	0.012	(0.004)	There is a slight positive correlation between log(Units Sold) and product promotion. Compared to the PLM model, the category of an item has little impact on number units of sold for an order.
Effect of a product on promotional display on the number of units sold (Category)	0.708	(0.004)	There is a positive correlation between log(Units Sold) and a product on promotional display. Compared to the PLM Model, the category of and item on display has a greater impact in number of units sold versus grouping all items together.
Effect of a product being featured in the circular on the number of purchasing households (Category)	0.481	(0.005)	There is a positive correlation between log(Units Sold) and being featured in the circular. Compared to the PLM model, the category of an item being featured in the circular has less of an impact of number of purchasing households versus grouping all items together.
Effect of product promotion on the number of purchasing households (Category)	-0.025	(0.004)	There is a negative correlation between log(Purchasing Households) and promotions. Compared to the PLM model, the category of an item with a product promotion has little change of an impact of number of purchasing households versus grouping all items together.
Effect of a product on promotional display on the number of purchasing households (Category)	0.715	(0.004)	There is a positive correlation between log(Purchasing Households) and a product on promotional display. Compared to the PLM model, the category of an item on promotion display has a greater impact on number of purchasing households versus grouping all items together.

Interpretation – LMER model (Store Type Only)

Interpretation – LMER m			
Variables	Correlation Coefficient	P-Value	Interpretation
Effect of a product being featured in the circular on total spend (Store Type)	0.717	(0.005)	There is a positive correlation between log (total spend) and being featured on the circular. Compared to the PLM model, the type of store an item is being featured on the circular in has less impact on the total amount spent on an order than an item being on display in a store regardless of store type.
Effect of a product promotion on total spend (Store Type)	0.524	(0.005)	There is a positive correlation between log(total spend) and product promotion. Compared to the PLM model, the type of store a product promotion has greater positive impact on total spend then of then if an item were displayed in any store type.
Effect of a product on promotional display on total spend (Store Type)	-0.082	(0.004)	There is a light negative correlation between log(total spend) and a product on promotional display. Compared to the PLM model, the type of store a product is on promotional display in has a very slight negative effect on total spend compared to if an item was on promotional display in any store type.
Effect of a product being featured in the circular on the number of units sold (Store Type)	0.685	(0.005)	There is a positive correlation between log(Units Sold) and being featured on the circular. Compared to the PLM model, the type of store an item is being featured in the circular in has less of an impact on units sold then if an item was featured in the circular in any type of store.
Effect of a product promotion on the number of units sold (Store Type)	-0.037	(0.004)	There is a negative correlation between log(Units Sold) and product promotion. Compared to the PLM model, the type of store and item is on promotion in has no effect on number of units sold compared to if an item was on promotion in any store type.
Effect of a product on promotional display on the number of units sold (Store Type)	0.564	(0.005)	There is a positive correlation between log(Units Sold) and a product on promotional display. Compared to the PLM model, the type of store an item is promotional display in has nearly the same impact on units sold compared to an item being on promotional display in any store type.
Effect of a product being featured in the	0.640	(0.005)	There is a positive correlation between log(Purchasing Households) and being and promotional display. Compared to the PLM

circular on the number of purchasing households (Store Type)			model, the type of store an item is being featured in the circular in has slightly less impact on the number of purchasing households compared to an item being featured on the circular in any store type.
Effect of a product promotion on the number of purchasing households (Store Type)	-0.088	(0.004)	There is a negative correlation between log(Purchasing Households) and product promotion. Compared to the PLM model, the type of store a product an item is on promotion in has a slightly worse impact on the number of purchasing households for an item compared to the item being promotion in any story type.
Effect of a product on promotional display on the number of purchasing households (Store Type)	0.561	(0.005)	There is a positive correlation between log(Purchasing Households) and a product on promotional display. Compared to the PLM model, the type of store a product is on promotion display in has a worse impact on the number of purchasing households for an item compared to an item being on promotional display in any store type.

Price-Elasticity of Products

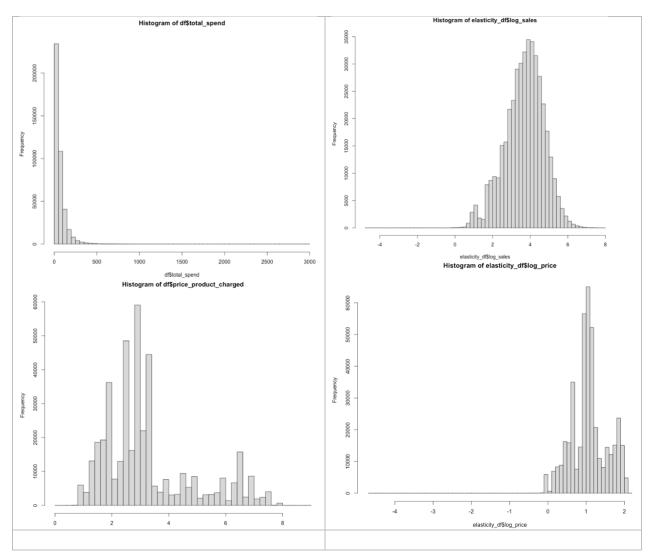
The elasticity of demand indicates how sensitive our customers are to price changes for a particular product so the product sales and units can be affected by price changes. To get coefficients for the formula for elasticity, we used a log-log linear model for each product in the dataset. To calculate the Elasticity, we use the formula:

$$PE = rac{\Delta Sales}{\Delta \, Price} * rac{Price}{Sales}$$
; having Sales as DV $PE = rac{\Delta UnitsSold}{\Delta \, Price} * rac{Price}{UnitsSold}$; having Units Sold as DV

Where (Δ Sales/ Δ Price) and Δ UnitsSold/ Δ Price) are given by the coefficient of each regression model, and Price, Sales, and Unit Sold are determined using mean (Sales), mean (Price), and mean(Units old) in R, respectively. Total spend has been renamed to Sales for a better understanding of the interpretation.

"total_spend", "units_sold", and "price_product_charged" in this dataset were transformed into logarithmic values due to their dispersion. Below is a figure showing how the dependent variables differ before and after a logarithmic transformation.

Histograms



Model

The model and elasticity can be obtained in R as follows:

```
model_for_elasticity = lm(log_sales ~ log_price,
data=only_one_product_at_a_time) #Sales as DV

PE = as.numeric(model_for_elasticity$coefficients["log_price"] *
mean(only_one_product_at_a_time$log_price)/mean(only_one_product_at_a_time
$log_sales)) #Sales as DV

model_for_elasticity = lm(log_units ~ log_price,
data=only_one_product_at_a_time)#Units as DV

PE = as.numeric(model_for_elasticity$coefficients["log_price"] *
mean(only_one_product_at_a_time$log_price)/mean(only_one_product_at_a_time
$log_units)) #Units as DV
```

A for loop has been used to create a temporal subset of data for each product in order to calculate its elasticity. The results have been introduced into a new dataset called "elasticity by product" using the rbind() function (see R code part 3 for reference).

```
list_of_products = unique(elasticity_df$product_name)
for (i in list_of_products) {
   elasticity_by_product = rbind(elasticity_by_product, calc_elasticity(i))
}
```

Due to a log transformation of price, units sold, and sales transform units on demand into the percentage change in demand resulting from a percentage change in price.

Using sales and units sold as dependent variables, the top 5 elastic and inelastic products are generated after elasticity is calculated for each product.

Top 5 Elastic and inelastic products by sales as DV

> top_five_elastic			
product_name	elasticity_num	categor	y direction
1 FRSC PEPPERONI PIZZA	1.69	FROZEN PIZZ	[-] AY
2 FRSC BRCK OVN ITL PEP PZ	1.53	FROZEN PIZZ	ZA [-]
3 DIGIORNO THREE MEAT	1.39	FROZEN PIZZ	ZA [-]
4 FRSC 4 CHEESE PIZZA	1.34	FROZEN PIZZ	ZA [-]
5 NWMN OWN SUPREME PIZZA	1.27	FROZEN PIZZ	ZA [-]
> tope_five_inelastic			
product_name e	elasticity_num	category	direction
1 SHURGD PRETZEL STICKS	0.08	BAG SNACKS	[+]
2 PL RAISIN BRAN	0.08 0	OLD CEREAL	[+]
3 SHURGD PRETZEL RODS	0.06	BAG SNACKS	[+]
4 PL BT SZ FRSTD SHRD WHT	0.03 0	OLD CEREAL	[+]
5 GM CHEERIOS	0.01 0	OLD CEREAL	[-]
•			

Top 5 Elastic and inelastic products by Units as DV

> top_five_elastic_units

product_name elasticity_num category direction FRSC PEPPERONI PIZZA 5.12 FROZEN PIZZA [-] 2 FRSC BRCK OVN ITL PEP PZ 4.53 FROZEN PIZZA [-] 3 FRSC 4 CHEESE PIZZA 4.47 FROZEN PIZZA [-] NWMN OWN SUPREME PIZZA 4.43 FROZEN PIZZA [-] 5 NWMN OWN PEPPERONI PIZZA 3.60 FROZEN PIZZA Γ-٦ > tope_five_inelastic_units product_name elasticity_num category direction SHURGD MINI PRETZELS 1 0.10 BAG SNACKS [-] 2 SHURGD PRETZEL STICKS 0.10 BAG SNACKS [-] 3 PL PRETZEL STICKS 0.08 BAG SNACKS [+] PL RAISIN BRAN 0.07 COLD CEREAL [-] 5 PL HONEY NUT TOASTD OATS 0.04 COLD CEREAL [+]

Interpretation

Considering a hypothetical product with an elasticity equal to 0 is perfectly inelastic, meaning a price increase will not affect sales; therefore, based on the results, the Manager should increase the price of the top five inelastic products to maximize product sales, since a price increase will not have a significant impact on sales. In contrast, he should also consider decreasing the price of the top five elastic products to maximize unit sales, since a ten percent price reduction will result in a 5.12% increase in unit sales, for example on FRSC PEPPERONI PIZZA.

Lessons Learned & Course Feedback

Lessons Learned

As a whole, this class has demonstrated how powerful statistics can be in predicting real-world models. As a result of out-of-class projects, the ability to analyze dependent and independent variables using the multicollinearity test has increased, as well as the proficiency in the use of tools provided to verify model assumptions, heteroskedasticity, and homoskedasticity for non-linear models.

Course Feedback

Overall, the course was challenging, the professor did a good job at the start of the course refreshing on key concepts from QMB 6304. The material was challenging (and most of it) went over

Appendix

Stargazer Output for PLM Models

	Dependent variable:			
	log(total_spend)	log(units_sold)	log(purchasing_households)	
	(1)	(2)	(3)	
circular	0.758***	0.727***	0.679***	
	(0.005)	(0.005)	(0.005)	
promotional_display	0.534***	0.574***	0.570***	
	(0.005)	(0.005)	(0.005)	
temp_price_reduction	-0.084***	-0.039***	-0.090***	
	(0.004)	(0.004)	(0.004)	
price_product_charged	-0.0002	-0.280***	-0.271***	
	(0.001)	(0.001)	(0.001)	
week_num	-0.001***	-0.001***	-0.001***	
	(0.00003)	(0.00003)	(0.00003)	
monthApr	-0.052***	-0.050***	-0.053***	
	(0.007)	(0.007)	(0.007)	
monthAug	-0.045***	-0.043***	-0.042***	
	(0.007)	(0.007)	(0.007)	
monthDec	0.033***	0.038***	0.024***	
	(0.007)	(0.007)	(0.007)	
monthFeb	0.007	0.010	0.009	
	(0.007)	(0.007)	(0.007)	
monthJul	-0.064***	-0.076***	-0.073***	
	(0.007)	(0.007)	(0.007)	
monthJun	-0.041***	-0.048***	-0.046***	
	(0.007)	(0.007)	(0.007)	
monthMar	-0.097***	-0.108***	-0.108***	
	(0.007)	(0.007)	(0.007)	
monthMay	-0.039***	-0.041***	-0.044***	
	(0.007)	(0.007)	(0.007)	
monthNov	-0.025***	-0.028***	-0.037***	
	(0.007)	(0.007)	(0.007)	
monthOct	-0.003	-0.017**	-0.021***	
	(0.007)	(0.007)	(0.007)	
monthSep	-0.030***	-0.036***	-0.034***	
	(0.007)	(0.007)	(0.007)	
Constant	3.617***	3.457***	3.300***	
	(0.023)	(0.023)	(0.023)	
Observations	418,554	418,554	418,554	
R ²	0.126	0.289	0.284	

Adjusted R ²	0.126	0.289	0.284
F Statistic	60,633.110***	170,437.300***	166,321.500***
Note:			*p**p***p<0.01

Stargazer Output For Store Type Only Model

	Dependent variable:		
	log_total_spend	log_units_sold	log_purchasing_households
	(1)	(2)	(3)
promotional_displayYes	0.524***	0.564***	0.561***
	(0.005)	(0.005)	(0.005)
circularYes	0.717***	0.685***	0.640***
	(0.005)	(0.005)	(0.005)
temp_price_reductionYes	-0.082***	-0.037***	-0.088***
	(0.004)	(0.004)	(0.004)
price_product_charged	0.002*	-0.279***	-0.270***
	(0.001)	(0.001)	(0.001)
week_num	-0.001***	-0.001***	-0.001***
	(0.00003)	(0.00003)	(0.0003)
monthApr	-0.055***	-0.053***	-0.056***
	(0.007)	(0.007)	(0.007)
monthAug	-0.053***	-0.052***	-0.050***
	(0.007)	(0.007)	(0.007)
monthDec	0.025***	0.030***	0.016**
	(0.007)	(0.007)	(0.007)
monthFeb	-0.004	-0.001	-0.001
	(0.007)	(0.007)	(0.007)
monthJul	-0.068***	-0.080***	-0.077***
	(0.007)	(0.007)	(0.007)
monthJun	-0.044***	-0.050***	-0.049***
	(0.007)	(0.007)	(0.007)
monthMar	-0.101***	-0.112***	-0.111***
	(0.007)	(0.007)	(0.007)
monthMay	-0.043***	-0.045***	-0.048***
	(0.007)	(0.007)	(0.007)
monthNov	-0.032***	-0.034***	-0.042***
	(0.007)	(0.007)	(0.007)
monthOct	-0.005	-0.019***	-0.022***
	(0.007)	(0.007)	(0.007)
monthSep	-0.033***	-0.040***	-0.037***
	(0.007)	(0.007)	(0.007)
type_of_storeMAINSTREAM	0.383***	0.385***	0.419***

	(0.083)	(0.082)	(0.082)
type_of_storeUPSCALE	0.388***	0.389***	0.423***
	(0.083)	(0.082)	(0.082)
Constant	3.326***	3.165***	2.983***
	(0.072)	(0.071)	(0.071)
Observations	417,188	417,188	417,188
Log Likelihood	-545,587.600	-540,531.400	-531,086.600
Akaike Inf. Crit.	1,091,217.000	1,081,105.000	1,062,215.000
Bayesian Inf. Crit.	1,091,447.000	1,081,335.000	1,062,445.000
Note:			*p**p***p<0.01

Stargazer Output for Category Only model

	Dependent variable:		
	log_total_spend	log_units_sold	log_purchasing_households
	(1)	(2)	(3)
promotional_displayYes	0.686***	0.708***	0.715***
	(0.004)	(0.004)	(0.004)
circularYes	0.530***	0.507***	0.481***
	(0.005)	(0.005)	(0.005)
temp_price_reductionYes	-0.022***	0.012***	-0.025***
	(0.004)	(0.004)	(0.004)
price_product_charged	-0.016***	-0.304***	-0.272***
	(0.001)	(0.001)	(0.001)
week_num	-0.001***	-0.001***	-0.001***
	(0.00003)	(0.00003)	(0.0003)
monthApr	-0.055***	-0.052***	-0.056***
	(0.006)	(0.006)	(0.006)
monthAug	-0.057***	-0.055***	-0.054***
	(0.006)	(0.006)	(0.006)
monthDec	0.024***	0.029***	0.015***
	(0.006)	(0.006)	(0.006)
monthFeb	-0.010	-0.007	-0.006
	(0.006)	(0.006)	(0.006)
monthJul	-0.078***	-0.089***	-0.086***
	(0.006)	(0.006)	(0.006)
monthJun	-0.053***	-0.058***	-0.058***
	(0.006)	(0.006)	(0.006)
monthMar	-0.104***	-0.114***	-0.113***
	(0.006)	(0.006)	(0.006)
monthMay	-0.046***	-0.047***	-0.050***
	(0.006)	(0.006)	(0.006)

monthNov	-0.026***	-0.030***	-0.037***
	(0.006)	(0.006)	(0.006)
monthOct	-0.013**	-0.027***	-0.029***
	(0.006)	(0.006)	(0.006)
monthSep	-0.048***	-0.053***	-0.051***
	(0.006)	(0.006)	(0.006)
categoryCOLD CEREAL	1.023***	0.936***	0.928***
	(0.003)	(0.003)	(0.003)
categoryFROZEN PIZZA	0.508***	0.508***	0.400***
	(0.005)	(0.005)	(0.005)
Constant	3.090***	2.996***	2.791***
	(0.045)	(0.044)	(0.045)
Observations	417,188	417,188	417,188
Log Likelihood	-492,445.000	-496,565.700	-483,755.600
Akaike Inf. Crit.	984,932.000	993,173.300	967,553.200
Bayesian Inf. Crit.	985,161.800	993,403.100	967,783.000
Note:			*p**p***p<0.01

Full R Code

```
rm(list=ls())
library(rio)
#Import SnackChain.Xlsx file.
<- import("SnackChain.xlsx", sheet="products") #58</pre>
products df
products
transactions df <- import("SnackChain.xlsx", sheet="transactions") #524950
transactions
#Joining Tables.
temp <- merge(transactions df, products df, by.x=c("UPC"), by.y=c("UPC"))</pre>
#join by UPCs between transactions and products
df <- merge(temp, stores df, by.x=c("STORE NUM"), by.y=c("STORE ID"))</pre>
#join by adding the stores.
#Removing temporary Files.
rm(transactions df)
rm(stores df)
rm(temp)
rm(products df)
                         #Data Preprocessing
#Remove oral hygiene products
df <- df[df$CATEGORY != "ORAL HYGIENE PRODUCTS", ] #this could be for</pre>
another project
#Check for missing values
```

```
colSums(is.na(df))
#' 282548 missing PARKING values; we will not use this data since it is
higher (store) level,
#' 10 NA values for price and 173 for BASE PRICE
df <- subset(df, select = -c(PARKING))</pre>
df <- df[complete.cases(df), ] #Removing missing values</pre>
#Renaming columns to make them easier to understand
colnames(df)[colnames(df) == "STORE NUM"] = "store id"
colnames(df)[colnames(df) == "UPC"] = "product id"
colnames(df) [colnames(df) == "WEEK END DATE"] = "week ending date"
colnames(df) [colnames(df) == "UNITS"] = "units sold"
colnames(df) [colnames(df) == "VISITS"] = "unique purchases"
colnames(df) [colnames(df) == "HHS"] = "purchasing households"
colnames(df)[colnames(df) == "SPEND"] = "total spend"
colnames(df)[colnames(df) == "PRICE"] = "price product charged"
colnames(df)[colnames(df) == "BASE PRICE"] = "base price product"
colnames(df) [colnames(df) == "FEATURE"] = "circular"
colnames(df)[colnames(df) == "DISPLAY"] = "promotional display"
colnames(df)[colnames(df) == "TPR ONLY"] = "temp price reduction"
colnames(df)[colnames(df) == "DESCRIPTION"] = "product"
colnames(df) [colnames(df) == "MANUFACTURER"] = "manufacturer"
colnames(df) [colnames(df) == "CATEGORY"] = "category"
colnames(df) [colnames(df) == "SUB CATEGORY"] = "subcategory"
colnames(df)[colnames(df) == "PRODUCT SIZE"] = "size"
colnames(df)[colnames(df) == "STORE NAME"] = "store name"
colnames(df)[colnames(df) == "CITY"] = "city"
colnames(df)[colnames(df) == "STATE"] = "state"
colnames(df)[colnames(df) == "MSA"] = "metropilitan area"
colnames(df) [colnames(df) == "SEGMENT"] = "type_of_store"
colnames(df)[colnames(df) == "SIZE"] = "store sqft"
colnames(df) [colnames(df) == "AVG WEEKLY BASKETS"] =
"avg weekly baskets sold"
#Converting Categorical variables into factor variables.
df$store id = factor(df$store id)
df$product id = factor(df$product id)
df$category = factor(df$category)
df$subcategory = factor(df$subcategory)
df$category = relevel(df$category, "BAG SNACKS")
df$city = factor(df$city)
df$state = factor(df$state)
df$type of store = factor(df$type of store)
df$type of store = relevel(df$type of store, "VALUE")
df$product = factor(df$product)
#Extracting year, month, and week ending date from date.
df$year = format(df$week ending date, "%\overline{Y}")
df$year = factor(df$year)
df$month = format(df$week ending date, "%b")
df$month = factor(df$month)
df$month = relevel(df$month, "Jan")
```

```
df$week num = difftime(df$week ending date, df$week ending date[1],
units="weeks")
df$week num = df$week num + 1
attach(df)
str(df)
df = df[df$price product charged != 0, ] #eliminating 0's on price product
to avoid errors when performing log()
df = df[df$total spend != 0, ] #eliminating 0's on total spend
df$log total spend <- log(df$total spend)</pre>
df$log units sold <- log(df$units sold)</pre>
df$log purchasing households <- log(df$purchasing households)</pre>
df$log price product charged <- log(df$price product charged)
df <- subset(df, df$log total spend != -Inf)</pre>
     1. Effect of promotional displays or being featured in the circular
#Data Visualization
hist(df$total spend)
hist(log(df$total spend))
hist(df$units sold)
hist(log(df$units sold))
hist(df$purchasing households)
hist(log(df$purchasing households))
#Correlations
library(corrplot)
correlation = cor(df[c("units_sold", "promotional_display",
"purchasing households", "total spend", "temp price reduction",
                       "circular", "price product charged",
"base price product", "metropilitan area",
                        "store sqft", "avg weekly baskets sold")],
use="pairwise.complete.obs")
corrplot(correlation)
#Plots
boxplot(df$total spend ~ df$promotional display)
boxplot(df$total spend ~ df$circular)
boxplot(df$total spend ~ df$city)
boxplot(df$total spend ~ df$temp price reduction)
boxplot(df$total spend ~ df$type of store)
library(car)
library(lmtest)
library(plm)
# Random Effect Model for spend
spendrandom <- plm(log(total spend) ~ circular</pre>
                   + promotional display
                   + temp price reduction
                   + price product charged
```

```
+ week num
                    + month,
                   data=df, index=c("store id"), model= "random")
# Random Effect Model for spend
unitsrandom <- plm(log(units sold) ~ circular</pre>
                   + promotional display
                   + temp price reduction
                   + price product charged
                    + week num
                    + month,
                   data=df, index=c("store id"), model= "random")
# Random Effect Model for spend
hhsrandom <- plm(log(purchasing households) ~ circular</pre>
                 + promotional display
                 + temp price reduction
                 + price product charged
                 + week num
                 + month,
                 data=df, index=c("store id"), model= "random")
library(stargazer)
stargazer(spendrandom, unitsrandom, hhsrandom, type = "html",
out="~/Downloads/SnackChain.html")
#
                2. Models w/out category and type of store
#Best models from question 1 to be used as the base for question 2
#Total Spend base model
lm10 = lm(log total spend ~ promotional display + circular +
temp price reduction + store id + week num + month , data=df)
summary(lm10 )
par(mfrow=c(2,2))
plot(lm10)
#Random Effect Week Number
lm11 = lme4::lmer(log total spend ~ promotional display + circular +
temp price reduction + week num + month + store id + (1 | week num),
data=df, REML = FALSE)
summary(lm11)
par(mfrow=c(2,2))
plot(lm11)
qqnorm(resid(lm10))
qqline(resid(lm10))
#Random Effect Week Number and Store Number
lm12 = lme4::lmer(log total spend ~ promotional display + circular +
temp price reduction + price product charged + week num + month + (1 |
store id) \overline{} data=df, REML = \overline{} FALSE)
summary(lm12)
```

```
par(mfrow=c(2,2))
plot(lm12)
ggnorm(resid(lm11))
qqline(resid(lm11))
library('MuMIn')
r.squaredGLMM(lm11)
r.squaredGLMM(lm12)
library(stargazer)
stargazer(lm10, lm11, lm12, type="html", out="totalspend.html")
AIC(lm10, lm11, lm12)
#Units Sold base model
lm13 = lm(log units sold ~ promotional display + circular +
temp price reduction + store id + week num + month + category +
type of store , data=df)
summary(lm13)
lm13$coefficients
par(mfrow=c(2,2))
plot(lm13)
#Random Effect Week Number
lm14 = lme4::lmer(log units sold ~ promotional display + circular +
temp price reduction + store id + week num + month + category +
type of store + (1 | week num), data=df, REML = FALSE)
summary(lm14)
par(mfrow=c(2,2))
plot(lm14)
gqnorm(resid(lm14))
qqline(resid(lm14))
#Random Effect Week Number and Store Number
lm15 = lme4::lmer(log units sold ~ promotional display + circular +
temp price reduction + price product charged + week num + month +
category + type of store + (1 | store id) , data=df, REML = FALSE)
summary(lm15)
par(mfrow=c(2,2))
plot(lm15)
qqnorm(resid(lm15))
qqline(resid(lm15))
library('MuMIn')
```

```
r.squaredGLMM(lm14)
r.squaredGLMM(lm15)
library(stargazer)
stargazer(lm13, lm14, lm15, type="html", out="unitssold.html")
AIC(lm13, lm14, lm15)
#Purchasing household base model
lm16 = lm(log purchasing households ~ promotional display + circular +
temp price reduction + store id + week num + month , data=df)
summary(lm16)
lm16$coefficients
par(mfrow=c(2,2))
plot(lm16)
#Random Effect Week Number
lm17 = lme4::lmer(log purchasing households ~ promotional display +
circular + temp price reduction + store id + month + (1 | week num),
data=df, REML = FALSE)
summary(lm17)
par(mfrow=c(2,2))
plot(lm17)
gqnorm(resid(lm17))
qqline(resid(lm17))
#Random Effect Week Number and Store Number
lm18 <- lme4::lmer(log purchasing households ~ promotional display +</pre>
circular + temp price reduction + price product charged + week num +
month + (1 | store_id) , data=df, REML = FALSE)
summary(lm18)
par(mfrow=c(2,2))
plot(lm18)
qqnorm(resid(lm18))
qqline(resid(lm18))
install.packages('MuMIn')
library('MuMIn')
r.squaredGLMM(lm17)
r.squaredGLMM(lm18)
library(stargazer)
stargazer(lm16, lm17, lm18, type="html", out="PurchasingHouseholds.html")
AIC(lm16, lm17, lm18)
```

```
df CC <- df[df$category == "COLD CEREAL", ]</pre>
df FP <- df[df$category == "FROZEN PIZZA", ]</pre>
df MS <- df[df$type of store == "MAINSTREAM", ]</pre>
df UP <- df[df$type of store == "UPSCALE", ]</pre>
                               2. Category Only
#Random Effect Week Number and Store Number
lm19 <- lme4::lmer(log total spend ~ promotional display</pre>
                   + circular
                    + temp price reduction
                   + price product charged
                    + week num
                   + month
                    + category
                    + (1 | store id) , data=df , REML = FALSE)
summary(lm19)
par(mfrow=c(2,2))
plot(lm19)
#Random Effect Week Number and Store Number
lm20 = lme4::lmer(log units sold ~ promotional display
                  + circular
                  + temp price reduction
                   + price product charged
                  + week num
                   + month
                   + category
                   + (1 | store id) , data=df , REML = FALSE)
summary(lm20)
par(mfrow=c(2,2))
plot(lm20)
#Random Effect Week Number and Store Number
lm21 <- lme4::lmer(log purchasing households ~ promotional display</pre>
                    + circular
                    + temp price reduction
                    + price product charged
                    + week num
                    + month
                    + category
                    + (1 | store id) , data=df , REML = FALSE)
summary(lm21)
par(mfrow=c(2,2))
plot(lm21)
library('MuMIn')
r.squaredGLMM(lm19)
r.squaredGLMM(lm20)
```

```
r.squaredGLMM(lm21)
library(stargazer)
stargazer(lm19, lm20, lm21, type="html", out="category.html")
#
                              2. Type of Store Only
#Random Effect Week Number and Store Number
lm22 = lme4::lmer(log total spend ~ promotional display
                  + circular
                  + temp price reduction
                  + price product charged
                  + week num
                  + month
                  + type of store + (1 | store id) , data=df , REML =
FALSE)
summary(lm22)
par(mfrow=c(2,2))
plot(lm22)
#Random Effect Week Number and Store Number
lm23 = lme4::lmer(log units sold ~ promotional display
                  + circular
                  + temp price reduction
                  + price product charged
                  + week num
                  + month
                  + type of store
                  + (1 | store id) , data=df , REML = FALSE)
summary(lm23)
par(mfrow=c(2,2))
plot(lm23)
#Random Effect Week Number and Store Number
lm24 <- lme4::lmer(log_purchasing_households ~ promotional_display</pre>
                   + circular
                   + temp price reduction
                   + price product charged
                   + week num
                   + month
                   + type of store
                   + (1 | store id) , data=df , REML = FALSE)
summary(lm24)
par(mfrow=c(2,2))
plot(lm24)|
  library('MuMIn')
r.squaredGLMM(lm22)
r.squaredGLMM(lm23)
r.squaredGLMM(lm24)
library(stargazer)
```

```
stargazer(lm22, lm23, lm24, type="html", out="type of store.html")
                               3. Price Elasticity
#Data exploration
table(product)
table(product id)
table(category)
summary(df)
hist(df$price product charged, breaks = 50)
hist(df$total spend, breaks = 50)
df = df[df$units sold != 1800, ]
hist(log(df\$units sold), breaks = 30)
#summary(df)
#Creating a dataframe to store log(sales), log(price), category, and
product name separately to avoid row disparity.
sales = as.vector(df[,'total_spend'])
units = as.vector(df[, 'units sold'])
price = as.vector(df[,'price product charged'])
category = as.vector(df[,'category'])
product name = as.vector(df[,'product'])
households = as.vector(df[,'purchasing households'])
elasticity df = data.frame(log(sales), log(price), log(units),
log(households), category, product name)
colnames(elasticity_df) = c("log_sales", "log_price", "log_units",
"log_purchasing_households","category", "product_name")
hist(elasticity df$log sales, breaks = 50)
hist(elasticity df$log price, breaks = 50)
hist(elasticity_df$log_units, breaks = 50)
rm(sales, units, price, category, product name)
#summary(elasticity df)
#Creating a function that calculates the elasticity given a dependent
variable and a product name (product name can be iterated from a list).
#The function returns the product name, elasticity and its category. PE =
Price Elasticity
elasticity by product = data.frame(product name=c("Perfectly Inelastic
Test product name"), elasticity num=c(0), category=c("Test name"))
calc elasticity = function(x){
  only one product at a time = subset(elasticity df, product name==x)
  model for elasticity = lm(log sales ~ log price, data =
only one product at a time)
  PE = as.numeric(model for elasticity$coefficients["log price"] *
mean(only one product at a time$log price)/mean(only one product at a time
$log sales))
  category name = (only one product at a time$category[1])
  aux vector = c(x, PE, category name)
  return(aux vector)
}
#Iterating and adding each product with its respective PE to
elasticity by product dataframe.
```

```
list of products = unique(elasticity df$product name) # Making a list of
the 41 unique products.
for (i in list of products) {
 elasticity by product = rbind(elasticity by product, calc elasticity(i))
#Data transformation on elasticity by product dataset.
elasticity by product$elasticity num =
as.numeric(elasticity_by_product$elasticity num) #Converting to Number
elasticity by product <- elasticity by product[-1,] #Deleting the test
product with elasticity = 0
library(dplyr)
elasticity by product <- elasticity by product %>%
 mutate(direction = if else(elasticity num > 0, "[+]", "[-]"))#Preserving
the symbol before to perform abs()
library(tidyverse)
elasticity by product$elasticity num =
abs(elasticity by product$elasticity num) #Making absolute values
elasticity by product$elasticity num =
round(elasticity by product$elasticity num, digits = 2)
elasticity by product = elasticity by product[order(-
elasticity by product$elasticity num),]#Sorting data frame
#Filtering the Top 5, most and least elastic products:
top five elastic = elasticity by product[1:5,]
row.names(top five elastic) <- NULL</pre>
tope five inelastic = tail(elasticity by product, n = 5)
row.names(tope five inelastic) <- NULL</pre>
top five elastic
tope five inelastic
     #Analysis of elasticity using units sold as a dependent variable.
elasticity by product units = data.frame(product name=c("Perfectly
Inelastic Test product name"), elasticity num=c(0),
category=c("Test name"))
calc elasticity units = function(x){
 only one product at a time = subset(elasticity df, product name==x)
 model for elasticity = lm(log units ~ log price, data =
only one product at a time)
 PE = as.numeric(model for elasticity$coefficients["log price"] *
mean(only one product at a time$log price)/mean(only one product at a time
$log units))
 category name = (only one product at a time$category[1])
 aux vector = c(x, PE, category name)
 return(aux vector)
for (i in list of products) {
 elasticity by product units = rbind(elasticity by product units,
calc elasticity units(i))
elasticity by product units$elasticity num =
as.numeric(elasticity by product units$elasticity num) #Converting to
Number
```

```
elasticity by product units <- elasticity by product units[-1,] #Deleting
the test product with elasticity = 0
elasticity by product units <- elasticity_by_product_units %>%
 mutate(direction = if else(elasticity num > 0, "[+]", "[-]"))#Preserving
the symbol before to perform abs()
elasticity_by_product units$elasticity num =
abs(elasticity by product units$elasticity num) #Making absolute values
elasticity by product units$elasticity num =
round(elasticity by product units$elasticity num, digits = 2)
elasticity_by_product_units = elasticity_by_product_units[order(-
elasticity by product units$elasticity num),]#Sorting data frame
#Top 5, most and least elastic products for units sold:
top five elastic units = elasticity by product units[1:5,]
row.names(top five elastic units) <- NULL</pre>
tope five inelastic units = tail(elasticity by product units, n = 5)
row.names(tope five inelastic units) <- NULL</pre>
top five elastic units
tope five inelastic units
#Determining the LINE assumptions of regression for one product.
assumptions LINE = function(product name) {
 only one product = subset(df, product==product name)
 m1 = lm(log total spend ~ log price product charged +
log purchasing households, data=only one product)
  #m1 = lm(total spend ~ price product charged + units sold +
purchasing households, data=only one product)
 par(mfrow=c(2,2))
  # Linearity
 plot(only one product$total spend,m1$fitted.values, pch=19,main="Actuals
v. Fitteds, total spend")
 abline (0, 1, col = "red", lwd = 3)
  # Normality
 qqnorm(m1$residuals,pch=19,
         main="Normality Plot, total spend")
 qqline(m1$residuals,lwd=3,col="red")
 hist(m1$residuals,col="red",
       main="Residuals, total spend",
       probability=TRUE)
  curve (dnorm(x, mean (m1$residuals),
              sd(m1$residuals)),
        from=min(m1$residuals),
        to=max(m1$residuals),
        lwd=3,col="Black",add=TRUE)
  # Equality of Variances
 plot(m1$fitted.values, rstandard(m1),
       pch=19,main="Equality of Variances, total spend")
  abline(0,0,lwd=3,col="red")
 par(mfrow=c(1,1))
 summary(m1)
#assumptions LINE("FRSC PEPPERONI PIZZA")
```