

MST Stereo Matching Algorithm

What we need at beginning:

Filename of left image

Filename of right image

Max disparity (disparity range)

Scale (used to enhance the final disparity image usually $\text{scale} = 256 / \text{max_disparity}$)

Input: Left & Right (RGB) image (*.ppm)

`unsigned char*** left, ***right; // Range: left[0~height-1][0~width-1][0~2]`
`left[y][x][0]`, `left[y][x][1]` and `left[y][x][2]` represent R, G, B value (0~255) of pixel in yth row xth line individually.

Function: qx_ppm.h

`unsigned char*** loadimage_ppm_u(char* filename, int &h, int&w);`

Usage

`int h, w;`
`char* filename = "left.ppm";`
`unsigned char*** left = loadimage_ppm_u(filename, h, w);`

Output: disparity (gray-scale) image (*.pgm)

`unsigned char** disparity_left; // Range: disparity_left[0~height-1][0~width-1];`
`disparity_left[y][x]` represents the disparity value of the pixel in yth row xth line. (0~255).

Function: qx_ppm.h

`void saveimage_pgm(char* filename, unsigned char** image, int h, int w, int scale);`
`// scale is used to enhance the gray-scale image, making it clear to recognize.`

Stereo Matching Algorithm

1st step: construct minimum spanning tree of left image / right image

Node: every pixel

Edge: edges that connect neighboring nodes.

Weight: for neighboring node p, q in the left image:

Left Tree:

$dR = \text{abs}(\text{left}[yp][xp][0] - \text{left}[yq][xq][0]);$

$dG = \text{abs}(\text{left}[yp][xp][1] - \text{left}[yq][xq][1]);$

$dB = \text{abs}(\text{left}[yp][xp][2] - \text{left}[yq][xq][2]);$

$W = \max(dR, dG, dB);$

Use unsigned char* **weight_left** to store W between the node and its parent.

(weight_left[node_id] = w)

Weight: for neighboring node p, q in the left image:

Right Tree:

$dR = \text{abs}(\text{right}[yp][xp][0] - \text{right}[yq][xq][0]);$

$dG = \text{abs}(\text{right}[yp][xp][1] - \text{right}[yq][xq][1]);$

$dB = \text{abs}(\text{right}[yp][xp][2] - \text{right}[yq][xq][2]);$

$W = \max(dR, dG, dB);$

Use unsigned char* **weight_right** to store W between the node and its parent.

2nd step: compute matching cost for each pixel at disparity level d.

(Do for left image and right image at the same time)

Input: unsigned char*** left, unsigned char*** right, **float** left_gradient, float** right_gradient;**

// range: left_gradient[0~height-1][0~width-1]

// As for how to compute left_gradient, right_gradient,

// please check **qx_nonlocal_cost_aggregation.h**

// void compute_gradient(float** gradient, unsigned char*** image)

// Usage: compute_gradient(left_gradient, left);

// compute_gradient(right_gradient, right);

Output: double* cost_vol_left, ***cost_vol_right;**

// range: cost_vol_left[0~height-1][0~width-1][0~max_disparity-1]

// do for cost_vol_left

for d = 0 to **max_disparity - 1**

for y = 0 to height - 1

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for x = 0 to width - 1
    for c = 0 to 2
        double cost = 0;
        cost += abs (left[y][x][c] - right[y][max(0, x-d)][c]);

    cost = min(cost_vol_left[y][x][d] / 3, max_color_difference);
    // double max_color_difference = 7.0

    double cost_gradient =
        min ((double)abs(gradient_left[y][x] - gradient_right[y][max(0,x-d)]),
            max_gradient_color_difference);
    // double max_gradient_color_difference = 2.0
    cost_vol_left[y][x][d] = weight_on_color * cost +
        (1 - weight_on_color) * cost_gradient;
    // weight_on_color = 0.11

// update cost_vol_right
for y = 0 to height - 1
    for x = 0 to width - max_disparity - 1
        for d = 0 to max_disparity_range
            cost_vol_right[y][x][d] = cost_vol_left[y][x+d][d];

    for x = width - max_disparity to width - 1
        for d = 0 to max_disprity_range
            if ( x + d < width) cost_vol_right[y][x][d] = cost_vol_left[y][x+d][d];
            else cost_vol_right[y][x][d] = cost_vol_right[y][x][d-1];

```

3rd: update aggregated matching cost

*Left image: aggregate matching cost **cost_vol_left** on the **left_tree***

Input: **cost_vol_left** (double***) // Obtained from 2nd step

Output: **cost_vol_left** (double***)

Unsigned double* cost_backup =**

memcpy(cost_backup, cost_vol_left, sizeof(double) * height * width * max_disparity);

// 1st part: from **leaf** node to the **root** node

for all node **p** in the **left_tree**

for all children node **q** of **p**

double w = e^ ((double) **-1** * weight_left[q] / (MAX_CHAR * sigma));

// MAX_CHAR = 255

// sigma = 0.1

```

// weight_left is used in the tree construction.
for d = 0 to max_disparity - 1
    double value_p = cost_backup[yp][xp][d];
    double value_q = cost_backup[yq][xq][d];
    value_p += w * value_q;
    cost_backup[yp][xp][d] = value_p;

// 2nd part: from root node to the leaf node
for all node q in the left_tree
    for the parent node p of q
        double w = e^ ((double) -1 * weight_left[q] / (MAX_CHAR * sigma));
        for d = 0 to max_disparity - 1
            double value_q_current = cost_backup[yq][xq][d];
            double value_p = cost_vol_left [yp][xp][d]; //Not cost_backup!!!

            cost_vol_left[yq][xq][d] = w * (value_p - w * value_q_current) + value_q_current;

Return cost_vol_left

```

*Left image: aggregate matching cost **cost_vol_right** on the **right_tree***

Input: cost_vol_right (double*)**

Output: cost_vol_right (double***)

// Same as aggregating matching cost on left_tree.

// Use cost_vol_right, cost_backup, weight_right

Return cost_vol_right

4th: find disparity for each pixel

unsigned char** disparity_left_tmp, unsigned char** disparity_left,

Left Image:

for y = 0 to height - 1

for x = 0 to width - 1

current_min = cost_vol_left[y][x][0];

disparity_left_tmp[y][x] = 0;

for d = 1 to max_disparity - 1

if (cost_vol_left[y][x][d] < current_min)

disparity_left_tmp[y][x] = d;

current_min = cost_vol_left[y][x][d];

ctmf(disparity_left_tmp[0], disparity_left[0], width, height, width, width, 2.0, 1, height * width);

// As for ctmf, please check ctmf.h & ctmf.cpp

unsigned char** disparity_right_tmp, unsigned char** disparity_right,

Right Image:

```
for y = 0 to height - 1
  for x = 0 to width - 1
    current_min = cost_vol_right[y][x][0];
    disparity_right_tmp[y][x] = 0;
    for d = 1 to max_disparity - 1
      if (cost_vol_left[y][x][d] < current_min)
        disparity_right_tmp[y][x] = d;
        current_min = cost_vol_right[y][x][d];
ctmf(disparity_right_tmp[0], disparity_right[0], width, height, width, width, 2.0, 1, height * width);
```