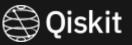
# 2023 부산시 양자컴퓨팅 개발자 교육 프로그램

#### **Lecture 1**

Inho Choi

Qiskit Advocate



#### 2023 부산시 양자컴퓨팅 개발자 교육 프로그램

#### Qiskit Advocate 멘토물을 소개합니다!







RESE Quant Advocate



**WORK QUANT Advances** 



GER, Onka Advocate



MARI CHERADOC

#### 함께 양자컴퓨팅 개발자가 되어 봅시다!

#### 어떤 걸 공부하게 되나요?

여러분들은 스터디 과장을 통해

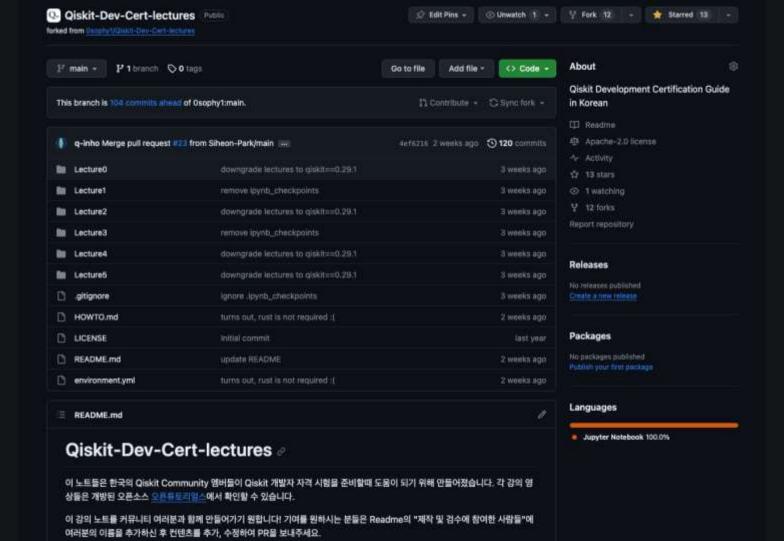
1) 파이번을 사용하여

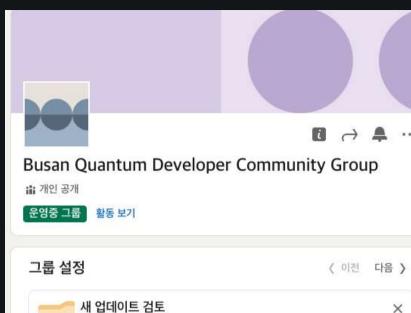
- 변수를 정의하고, 조건문을 산언하며
- 함수를 선언하고, 파일의 자료를 읽고 쓰며
- Numpy Array를 다위됩니다.

2) Qiskit을 사용하여

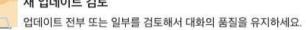
- \* 양자 회로를 작성하고 시뮬레이터를 포함한 백엔드에서 삼쌀하고
- 양자 회로와 그 실행 결과를 시각화 하며
- 망자 회로를 실행하는 대 필요한 부가 기능을 학습할 수 있습니다.

추가적으로, IBM Quantum의 learning platform에서 짜공하는 학습 자료를 사용하여 망자정보이론의 기초를 학습하게 됩니다.











그룹에 업데이트 올리기









### Syllabus



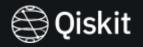
- Lecture 1: 게이트와 양자 회로 기본 작성법
  - Single qubit gate
  - Multiple qubit gate
  - Barriers and Properties of Quantum Circuit
- Lecture 2: 양자 회로의 측정과 OpenQasm
- Lecture 3: 양자 백엔드에 양자회로 실행하기
- Lecture 4: 양자 회로 및 회로의 실행 결과 시각화 및 해석
- Lecture 5: 유용한 기능들

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### Syllabus



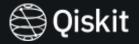
- 게이트와 양자 회로 기본 작성법
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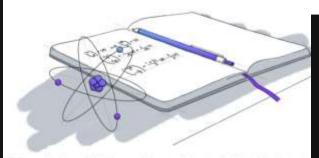
· Lecture 3

Lecture 4

Lecture 5

#### Single systems





This lesson introduces the basic framework of guantum information, including the description of a states as vectors with complex number entries, measurements that allow classical information to from quantum states, and operations on quantum states that are described by unitary matrices. Vi our attention in this lesson to the comparatively simple setting in which a single system is considiliculation. In the next lesson, we will expand our view to multiple systems, which can interact with and be correlated, for instance.

There are, in fact, two common mamematical descriptions of quantum information. The one introlesson is the simpler of the two. This description is sufficient for understanding many (or perhaps quantum signrithms, and is a natural place to start from a pedagogical viewpoint.

#### Qiskit Textbook: Single systems

#### Lecture 1 - 게이트와 양자 회로

#### 1-0 단일 큐비트 게이트

#### 1. 파울리 게이트 (Pauli Gates)

#### 파울리-X 게이트

파울리-X 게이트는 고전 회로에서 NOT gate와 유사한 특성을 나타내고 있으며 bit-flip 게이트라고도 알려져있습니다. 파울리-X 게이트는  $|0\rangle$  상태인 큐비트를  $|1\rangle$ 로 만들며 반대로  $|1\rangle$ 인 상태인 큐비트를  $|0\rangle$ 로 만듭니다. 파울리-X 게이트의 수학적 표현은 아래와 같습니다.

$$X = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} = |0\rangle\langle 1| + |1\rangle\langle 0|$$

#### 코드 구현

 $|0\rangle$ 의 상태인 큐비트를  $|1\rangle$ 로 만들기

시작하기에 앞서 코드에 관한 내용은 추후 장에서 자세히 설명합니다. 이번 장에서는 게이트의 사용과 양자 회로의 output으로부터 개념을 이해해봅시다.

게이트와 양자회로를 그리기 위해 Python 라이브러리인 Qiskit을 불러오겠습니다

```
from qiskit import * #qiskit 전체 라이브러리 불러오기
from qiskit.providers.aer import StatevectorSimulator #StatevectorSimulator를 사용하여 양자회로의 최종 양자 statevector
from math import pi, sqrt #math 라이브러리에서 pi와 sqrt 불러오기
from qiskit.visualization import * #양자상태를 시각화 하기 위해 qiskit.visualization 불러오기
from qiskit.quantum_info import Statevector
```

### Single Qubit Gate



- 1. Classical Information
- 2. Quantum Information
- 3. Single Qubit Gate with Qiskit

### Classical States and Probability Vectors



X: Physical system with information

 $\Sigma$ : Classical state set

- If X is a **bit**, then classical state set is  $\Sigma = \{0,1\}$
- If X is six-sided **die**, then classical state is  $\Sigma = \{1, 2, 3, 4, 5, 6\}$

uncertainty

probability

### Classical States and Probability Vectors



#### **Example:**

X is bit

Classical state 0 with probability 1/5

Classical state 1 with probability 4/5

Probability state of X

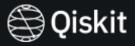
$$Pr(X = 0) = 1/5 \text{ and } Pr(X = 1) = 4/5$$

#### Column Vector

$$\begin{pmatrix} \frac{1}{5} \\ \frac{4}{5} \end{pmatrix}$$
 Classical state 0 Classical state 1

**Probability Vector** 

### Measuring Probabilities States



#### Column Vector -> **Dirac Notation**

If X is **bit**,  $\sum = \{0,1\}$ 

- 1 in corresponding entry
- 0 for all other entries

$$|0\rangle = {1 \choose 0}$$
 and  $|1\rangle = {0 \choose 1}$ 

Standard basis vector

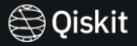
Row Vector -> Dirac Notation

$$\langle 0| = (1 \quad 0) \text{ and } \langle 1| = (0 \quad 1)$$

**Conjugate Transpose** 

$$\langle \psi | = | \psi \rangle^{\dagger}$$

### Measuring Probabilities States



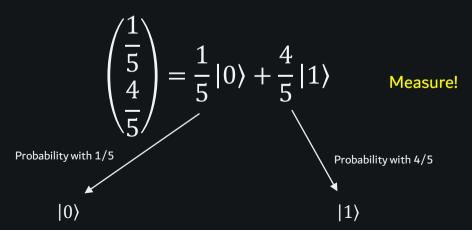
#### Column Vector -> **Dirac Notation**

- 1 in corresponding entry
- 0 for all other entries

If X is **bit**,  $\Sigma = \{0, 1\}$ 

$$|0\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$
 and  $|1\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$ 

Standard basis vector



### Single Qubit Gate



- 1. Classical Information
- 2. Quantum Information
- 3. Single Qubit Gate with Qiskit

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#### Quantum State Vector



Quantum State of a system is denoted by a <u>column vector</u>

**Entries: Complex numbers** 

Euclidean norm for vectors must equal 1



$$v = \begin{pmatrix} \alpha_1 \\ \vdots \\ \alpha_n \end{pmatrix} \qquad ||v|| = \sqrt{\sum_{k=1}^n |\alpha_k|^2}$$

#### Quantum State Vector



Quantum State of a system is denoted by a <u>column vector</u>

**Entries: Complex numbers** 

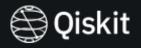
Euclidean norm for vectors must equal 1

- Example of qubit states
  - Standard basis states:  $|0\rangle$  and  $|1\rangle$
- Plus and minus state:  $|+\rangle$  and  $|-\rangle$

$$|+\rangle = \frac{1}{\sqrt{2}}|0\rangle + \frac{1}{\sqrt{2}}|1\rangle$$

$$|-\rangle = \frac{1}{\sqrt{2}}|0\rangle - \frac{1}{\sqrt{2}}|1\rangle$$

#### Quantum State Vector



Quantum State of a system is denoted by a <u>column vector</u>

**Entries: Complex numbers** 

Euclidean norm for vectors must equal 1

- Example of qubit states
  - Standard basis states:  $|0\rangle$  and  $|1\rangle$
  - Plus and minus state:  $|+\rangle$  and  $|-\rangle$
  - No special name:

$$\frac{1+2i}{3}|0\rangle - \frac{2}{3}|1\rangle = \begin{pmatrix} \frac{1+2i}{3} \\ -\frac{2}{3} \end{pmatrix} \xrightarrow{\text{norm}} \mathbf{1}$$

### Measuring Quantum States



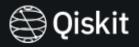
- Outcomes: Classical states
- Probability for each classical states: Absolute value squared of entry

$$\frac{1+2i}{3}|0\rangle - \frac{2}{3}|1\rangle$$

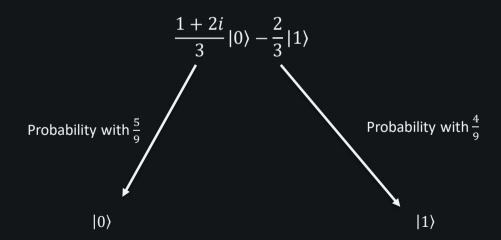
$$Pr(outcome \ is \ 0) = \left| \frac{1+2i}{3} \right|^2 = \frac{5}{9}$$

$$Pr(outcome \ is \ 1) = \left| -\frac{2}{3} \right|^2 = \frac{4}{9}$$

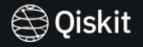
### Measuring Quantum States



- Outcomes: Classical states
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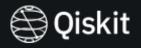
#### Unitary operations



Operations on quantum state vectors -> Unitary Matrices

$$U^{\dagger}U = UU^{\dagger} = \mathbb{I}$$
 Identiy matrix  $U^{-1}U = UU^{-1} = \mathbb{I}$ 

#### Unitary operations



Operations on quantum state vectors -> Unitary Matrices

$$U^{\dagger}U = UU^{\dagger} = \mathbb{I}$$
 Identiy matrix  $||Uv|| = ||v||$ 

### Single Qubit Gate



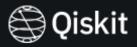
- 1. Classical Information
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#### **Pauli operations**

$$\mathbb{I} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, \qquad \sigma_x = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, \qquad \sigma_y = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}, \qquad \sigma_z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix},$$
 
$$\mathsf{X}\text{-gate} \qquad \mathsf{Y}\text{-gate} \qquad \mathsf{Z}\text{-gate}$$



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#### **Hadamard** operation

$$H = \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix} \qquad H|0\rangle = |+\rangle$$

$$H|1\rangle = |-\rangle$$

H-gate

$$\begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix}^{\dagger} \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix} = \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix} \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix} = \begin{pmatrix} \frac{1}{2} + \frac{1}{2} & \frac{1}{2} - \frac{1}{2} \\ \frac{1}{2} - \frac{1}{2} & \frac{1}{2} + \frac{1}{2} \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

Unitary!!



#### **Phase operation**

$$P_{ heta} = \begin{pmatrix} 1 & 0 \\ 0 & e^{i heta} \end{pmatrix}$$
P-gate

$$S = P_{\pi/2} = \begin{pmatrix} 1 & 0 \\ 0 & i \end{pmatrix}$$

$$\mathsf{T} = P_{\pi/4} = \begin{pmatrix} 1 & 0 \\ 0 & \frac{1+i}{\sqrt{2}} \end{pmatrix}$$

T-gate



Other operation

- 1. Rotational (X, Y, Z) Gate
- 2. U gate

### Take-away message



- What single quantum gate does exist
- How do they change quantum state?
- How do they use in Qiskit

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## QnA



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