

$$Z \sim N\left(x+y, \sqrt{\sigma_x^2 + \sigma_y^2 + 2\rho\sigma_x\sigma_y}\right)$$

