

## Homework 3

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Due April 2

1. If  $S$  is a set of  $n$  element, the power set of  $S$  is the set of all possible subsets of  $S$ . For example, if  $S = \{a, b, c\}$ , then  $\text{powerset}(S) = \{\{\}, \{a\}, \{b\}, \{c\}, \{a,b\}, \{a,c\}, \{b,c\}, \{a,b,c\}\}$ . Write in pseudocode a recursive function to compute  $\text{powerset}(S)$ .
2. Why is the order of an algorithm generally more important than the speed of the processor?
3. Convert each time formula to the best possible big-O notation. Do not include any spurious constants in your big-O answer.

Time Formula	Big-O
$10n$	.
$2n^2$	.
3 times log (base 2) of $n$	.
$2n^2 + 10n$	.

5. What will be the big-O expression for  $1+2+3+\dots+n$ ?
6. What formula in big-O notation will represent the expression  $n^2+35n+6$ ?
7. Here is some code for an *integer* variable  $n$ :

```
while (n > 0)
{
    n = n/10; // Use integer division
}
```

What is the worst-case time analysis for the above loop?

8. Express the formula  $(n - 2) * (n - 4)$  using the big-O notation.
9. Write a program containing a recursive function that prints out the sequence of moves needed to accomplish the task of the Towers of Hanoi problem discussed in class.