ФЕДЕРАЛЬНОЕ ГОСУДАРСТВЕННОЕ АВТОНОМНОЕ ОБРАЗОВАТЕЛЬНОЕ УЧРЕЖДЕНИЕ ВЫСШЕГО ОБРАЗОВАНИЯ

САНКТ-ПЕТЕРБУРГСКИЙ ПОЛИТЕХНИЧЕСКИЙ УНИВЕРСИТЕТ ПЕТРА ВЕЛИКОГО

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ЛАБОРАТОРНАЯ РАБОТА №2

по дисциплине: «Вычислительная матиматика» Вариант №27

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Задание

Написать процедуру формирования матрицы A по заданному вектору B

$$pA = \begin{pmatrix} 1 & a_1 & a_1 & \dots & a_1 \\ 1 & 1 & a_2 & \dots & a_2 \\ \dots & \dots & \dots & \dots \\ 1 & 1 & 1 & \dots & a_{n-1} \\ 1 & 1 & 1 & \dots & 1 \end{pmatrix}, B = \begin{pmatrix} a_1 & a_2 & \dots & a_{n-1} \end{pmatrix}^T$$

Задавая $n=5, a_1=4, a_2=3, a_3=2, a_4=var=1.5; 1.01; 1.001; 1.0001$ и вычисляя A^{-1} с помощью DECOMP и SOLVE, найти нормы матриц $R=AA^{-1}-E$ для всех вариантов a_4 .

Код программы

```
чргоgram FormAndInvert
2
       implicit none
       integer, parameter :: N = 5
3
       integer :: i, j, k, variant
4
       real :: A(N,N), A_{copy}(N,N), AINV(N,N), R(N,N)
       real :: B(N-1), bvec(N)
6
       real :: cond, work(N)
       integer :: ipvt(N)
       real :: normR, rowSum
       real :: a1, a2, a3, a4
10
       real, dimension(4) :: a4_values
11
12
       data a4_values / 1.5, 1.01, 1.001, 1.0001 /
13
       a1 = 4.0
14
       a2 = 3.0
15
       a3 = 2.0
16
17
       do variant = 1, 4
18
19
           a4 = a4_values(variant)
20
          B(1) = a1
21
          B(2) = a2
22
          B(3) = a3
23
          B(4) = a4
25
          A(1,1) = 1.0
26
           do j = 2, N
27
              A(1,j) = a1
           end do
29
30
          A(2,1) = 1.0
31
           A(2,2) = 1.0
32
           do j = 3, N
33
              A(2,j) = a2
34
           end do
35
36
           A(3,1) = 1.0
37
           A(3,2) = 1.0
38
           A(3,3) = 1.0
           do j = 4, N
40
              A(3,j) = a3
41
           end do
42
          A(4,1) = 1.0
```

```
A(4,2) = 1.0
45
           A(4,3) = 1.0
46
           A(4,4) = 1.0
47
           A(4,5) = a4
49
           do j = 1, N
50
               A(5,j) = 1.0
51
           end do
52
53
           do i = 1, N
54
               do j = 1, N
55
                  A_{copy}(i,j) = A(i,j)
56
               end do
57
           end do
58
59
           ! Печать матрицы А
           write(*, '(A, F10.6)') 'For var = ', a4
61
           write(*,'(A)') 'Matrix A:'
62
           do i = 1, N
63
               write (*, '(5F12.4)') (A(i,j), j=1,N)
           end do
65
66
           call DECOMP(N, N, A_copy, cond, ipvt, work)
67
68
           ! Вычисляем обратную матрицу AINV
69
           do k = 1, N
70
               do i = 1, N
                  if (i == k) then
72
                      bvec(i) = 1.0
73
                  else
74
                      bvec(i) = 0.0
                  end if
76
               end do
77
               call SOLVE(N, N, A_copy, bvec, ipvt)
78
               do i = 1, N
79
                  AINV(i,k) = bvec(i)
80
               end do
81
           end do
82
           ! Печать обратной матрицы AINV
84
           write(*,'(A)') 'Inverse Matrix A_inv:'
85
           do i = 1, N
86
               write(*,'(5F12.4)') (AINV(i,j), j=1,N)
           end do
88
89
           ! Вычисляем R = A*A_inv - I
90
           do i = 1, N
91
               do j = 1, N
92
                  R(i,j) = 0.0
93
                  do k = 1, N
                     R(i,j) = R(i,j) + A(i,k) * AINV(k,j)
95
                  end do
96
                  if (i == j) then
97
                     R(i,j) = R(i,j) - 1.0
98
                  end if
99
               end do
100
           end do
101
           ! Печать матрицы R
103
           write(*,'(A)') 'Matrix R = A*A_inv - I:'
104
           do i = 1, N
105
```

```
write (*, '(5F12.4)') (R(i,j), j=1,N)
           end do
107
108
           ! Норма матрицы R
           normR = 0.0
110
           do i = 1, N
111
               rowSum = 0.0
112
               do j = 1, N
113
                  rowSum = rowSum + abs(R(i,j))
114
               end do
115
               if (rowSum > normR) then
116
                  normR = rowSum
117
               end if
118
           end do
119
120
           write(*,'(A, F12.6)') 'Norm of R: ', normR
           write(*,'(A)') '-----
122
123
        end do
124
      end program FormAndInvert
126
127
      subroutine DECOMP(NDIM, N, A, COND, IPVT, WORK)
128
        implicit none
        integer, intent(in) :: NDIM, N
130
        real, intent(inout) :: A(NDIM, N)
131
        real, intent(out) :: COND
        integer, intent(out) :: IPVT(N)
133
        real, intent(inout) :: WORK(N)
134
        real :: EK, T, ANORM, YNORM, ZNORM
135
        integer :: NM1, I, J, K, KP1, KB, M
137
        IPVT(N) = 1
138
        if (N == 1) then
139
           COND = 1.0
140
           if (A(1,1) /= 0.0) return
141
           COND = 1.0e + 32
142
           return
143
        end if
145
        NM1 = N - 1
146
        ANORM = 0.0
147
        do J = 1, N
           T = 0.0
149
           do I = 1, N
150
               T = T + abs(A(I,J))
151
           end do
152
           if (T > ANORM) then
153
               ANORM = T
154
           end if
        end do
156
157
        do K = 1, NM1
158
           KP1 = K + 1
159
           M = K
160
           do I = KP1, N
161
               if (abs(A(I,K)) > abs(A(M,K))) then
162
                  M = I
               end if
164
           end do
165
           IPVT(K) = M
```

```
if (M /= K) then
167
               IPVT(N) = -IPVT(N)
168
            end if
169
            T = A(M,K)
            A(M,K) = A(K,K)
171
            A(K,K) = T
172
            if (T == 0.0) cycle
173
            do I = KP1, N
174
               A(I,K) = -A(I,K) / T
175
            end do
176
            do J = KP1, N
177
               T = A(M,J)
178
               A(M,J) = A(K,J)
179
               A(K,J) = T
180
               if (T == 0.0) cycle
181
               do I = KP1, N
                  A(I,J) = A(I,J) + A(I,K) * T
183
               end do
184
            end do
185
        end do
186
187
        do K = 1, N
188
            T = 0.0
189
            if (K /= 1) then
190
               do I = 1, K-1
191
                   T = T + A(I,K) * WORK(I)
192
               end do
            end if
194
            EK = 1.0
195
            if (T < 0.0) EK = -1.0
196
            if (A(K,K) == 0.0) then
197
               COND = 1.0e + 32
198
               return
199
            end if
200
            WORK(K) = -(EK + T) / A(K,K)
201
        end do
202
203
        do KB = 1, NM1
204
            K = N - KB
            T = WORK(K)
206
            do I = K+1, N
207
               T = T + A(I,K) * WORK(I)
208
            end do
            WORK(K) = T
210
            if (IPVT(K) /= K) then
211
               T = WORK(IPVT(K))
212
               WORK(IPVT(K)) = WORK(K)
213
               WORK(K) = T
214
            end if
215
        end do
216
217
        YNORM = 0.0
218
        do I = 1, N
219
            YNORM = YNORM + abs(WORK(I))
220
        end do
221
        call SOLVE(NDIM, N, A, WORK, IPVT)
222
        ZNORM = 0.0
223
        do I = 1, N
            ZNORM = ZNORM + abs(WORK(I))
225
        end do
226
        COND = ANORM * ZNORM / YNORM
```

```
if (COND < 1.0) then
           COND = 1.0
229
        end if
230
231
        return
      end subroutine DECOMP
232
233
      subroutine SOLVE(NDIM, N, A, B, IPVT)
234
        implicit none
235
        integer, intent(in) :: NDIM, N
236
        integer, intent(in) :: IPVT(N)
237
        real, intent(inout) :: A(NDIM, N)
238
        real, intent(inout) :: B(N)
        integer :: KB, NM1, KP1, I, K, M
240
        real :: T
241
242
        if (N == 1) then
243
           B(1) = B(1) / A(1,1)
244
           return
245
        end if
246
        NM1 = N - 1
248
        do K = 1, NM1
249
           KP1 = K + 1
250
           M = IPVT(K)
251
           T = B(M)
252
           B(M) = B(K)
253
           B(K) = T
254
           do I = KP1, N
255
               B(I) = B(I) + A(I,K) * T
256
           end do
257
        end do
259
        do KB = 1, NM1
260
           K = N - KB + 1
261
           B(K) = B(K) / A(K,K)
262
           T = -B(K)
263
           do I = 1, K-1
264
              B(I) = B(I) + A(I,K) * T
265
           end do
        end do
267
        B(1) = B(1) / A(1,1)
268
        return
269
      end subroutine SOLVE
```

Выполнение программы

Matrix A:				
1.0000	4.0000	4.0000	4.0000	4.0000
1.0000	1.0000	3.0000	3.0000	3.0000
1.0000	1.0000	1.0000	2.0000	2.0000
1.0000	1.0000	1.0000	1.0000	1.5000
1.0000	1.0000	1.0000	1.0000	1.0000
Inverse Matrix	A_inv:			
-0.3333	0.0000	0.0000	0.0000	1.3333
0.3333	-0.5000	-0.0000	-0.0000	0.1667
-0.0000	0.5000	-1.0000	-0.0000	0.5000
-0.0000	-0.0000	1.0000	-2.0000	1.0000
-0.0000	-0.0000	-0.0000	2.0000	-2.0000
Matrix R = A*A	inv - I:			
0.0000	0.0000	0.0000	0.0000	0.0000
-0.0000	0.0000	0.0000	0.0000	0.0000
-0.0000	0.0000	0.0000	0.0000	0.0000
-0.0000	0.0000	0.0000	0.0000	0.0000
-0.0000	0.0000	0.0000	0.0000	0.0000
Norm of R:	0.000000			

For v	$y_{ar} = 1.010$	0000			
Matr					
	1.0000	4.0000	4.0000	4.0000	4.0000
	1.0000	1.0000	3.0000	3.0000	3.0000
	1.0000	1.0000	1.0000	2.0000	2.0000
	1.0000	1.0000	1.0000	1.0000	1.0100
	1.0000	1.0000	1.0000	1.0000	1.0000
Inve	rse Matrix A_	inv:			
	-0.3333	0.0000	0.0000	0.0000	1.3333
	0.3333	-0.5000	-0.0000	-0.0000	0.1667
	-0.0000	0.5000	-1.0000	-0.0000	0.5000
	-0.0000	-0.0000	1.0000	-100.0001	99.0001
	-0.0000	-0.0000	-0.0000	100.0001	-100.0001
Matr	ix	nv - I:			
	0.0000	0.0000	0.0000	0.0000	0.0000
	-0.0000	0.0000	0.0000	0.0000	0.0000
	-0.0000	0.0000	0.0000	0.0000	0.0000
	-0.0000	0.0000	0.0000	0.0000	0.0000
	-0.0000	0.0000	0.0000	0.0000	0.0000
Norm	of R:	0.000000			

I OI Vai	1.001000			
Matrix A:				
1.0000	4.0000	4.0000	4.0000	4.0000
1.0000	1.0000	3.0000	3.0000	3.0000
1.0000	1.0000	1.0000	2.0000	2.0000
1.0000	1.0000	1.0000	1.0000	1.0010
1.0000	1.0000	1.0000	1.0000	1.0000
Inverse Matr	rix A_inv:			
-0.3333	0.0000	0.0000	0.0000	1.3333
0.3333	-0.5000	-0.0000	-0.0000	0.1667
-0.0000	0.5000	-1.0000	-0.0000	0.5000
-0.0000		1.0000	-1000.0725	999.0725
-0.0000	-0.0000	-0.0000	1000.0725	-1000.0725
Matrix R = R	_			
0.0000		0.0000	0.0000	0.0000
-0.0000		0.0000	0.0000	0.0000
-0.0000		0.0000	0.0000	0.0000
-0.0000		0.0000	0.0001	-0.0001
-0.0000		0.0000	0.0000	0.0000
Norm of R:	0.000244			
For var =	1.000100			
Matrix A:				
Matrix A: 1.0000	4.0000	4.0000	4.0000	4.0000
		4.0000	4.0000	4.0000 3.0000
1.0000	1.0000			
1.0000 1.0000 1.0000 1.0000	1.0000 1.0000 1.0000	3.0000 1.0000 1.0000	3.0000 2.0000 1.0000	3.0000 2.0000 1.0001
1.0000 1.0000 1.0000 1.0000	1.0000 1.0000 1.0000 1.0000	3.0000 1.0000	3.0000 2.0000	3.0000 2.0000
1.0000 1.0000 1.0000 1.0000 1.0000 Inverse Matr	1.0000 1.0000 1.0000 1.0000 ix A_inv:	3.0000 1.0000 1.0000 1.0000	3.0000 2.0000 1.0000 1.0000	3.0000 2.0000 1.0001 1.0000
1.0000 1.0000 1.0000 1.0000	1.0000 1.0000 1.0000 1.0000 ix A_inv:	3.0000 1.0000 1.0000	3.0000 2.0000 1.0000	3.0000 2.0000 1.0001
1.0000 1.0000 1.0000 1.0000 1.0000 Inverse Matr -0.3333 0.3333	1.0000 1.0000 1.0000 1.0000 ix A_inv: 0.0000 -0.5000	3.0000 1.0000 1.0000 1.0000 -0.0000	3.0000 2.0000 1.0000 0.0000 -0.0000	3.0000 2.0000 1.0001 1.0000 1.3333 0.1667
1.0000 1.0000 1.0000 1.0000 1.0000 Inverse Matr -0.3333 0.3333	1.0000 1.0000 1.0000 1.0000 ix A_inv: 0.0000 -0.5000	3.0000 1.0000 1.0000 1.0000 -0.0000 -1.0000	3.0000 2.0000 1.0000 1.0000 -0.0000 -0.0000	3.0000 2.0000 1.0001 1.0000 1.3333 0.1667 0.5000
1.0000 1.0000 1.0000 1.0000 1.0000 Inverse Matr -0.3333 0.3333 -0.0000	1.0000 1.0000 1.0000 1.0000 ix A_inv: 0.0000 -0.5000 0.5000 -0.0000	3.0000 1.0000 1.0000 1.0000 0.0000 -0.0000 -1.0000	3.0000 2.0000 1.0000 0.0000 -0.0000 -0.0000 -9986.4385	3.0000 2.0000 1.0001 1.0000 1.3333 0.1667 0.5000 9985.4385
1.0000 1.0000 1.0000 1.0000 1.0000 Inverse Matr -0.3333 0.3333 -0.0000 -0.0000	1.0000 1.0000 1.0000 1.0000 ix A_inv: 0.0000 -0.5000 0.5000 -0.0000 -0.0000	3.0000 1.0000 1.0000 1.0000 -0.0000 -1.0000	3.0000 2.0000 1.0000 1.0000 -0.0000 -0.0000	3.0000 2.0000 1.0001 1.0000 1.3333 0.1667 0.5000
1.0000 1.0000 1.0000 1.0000 1.0000 Inverse Matr -0.3333 0.3333 -0.0000 -0.0000 -0.0000 Matrix R = A	1.0000 1.0000 1.0000 1.0000 ix A_inv: 0.0000 -0.5000 0.5000 -0.0000 -0.0000 *A_inv - I:	3.0000 1.0000 1.0000 0.0000 -0.0000 -1.0000 -0.0000	3.0000 2.0000 1.0000 0.0000 -0.0000 -0.0000 -9986.4385 9986.4385	3.0000 2.0000 1.0001 1.0000 1.3333 0.1667 0.5000 9985.4385 -9986.4385
1.0000 1.0000 1.0000 1.0000 1.0000 Inverse Matr -0.3333 -0.3333 -0.0000 -0.0000 Matrix R = A	1.0000 1.0000 1.0000 1.0000 ix A_inv: 0.0000 -0.5000 -0.5000 -0.0000 -0.0000 *A_inv - I: 0.0000	3.0000 1.0000 1.0000 0.0000 -0.0000 -1.0000 -0.0000	3.0000 2.0000 1.0000 0.0000 -0.0000 -0.0000 -9986.4385 9986.4385	3.0000 2.0000 1.0001 1.0000 1.3333 0.1667 0.5000 9985.4385 -9986.4385
1.0000 1.0000 1.0000 1.0000 1.0000 Inverse Matr -0.3333 0.3333 -0.0000 -0.0000 -0.0000 Matrix R = A 0.0000 -0.0000	1.0000 1.0000 1.0000 1.0000 ix A_inv: 0.0000 -0.5000 -0.5000 -0.0000 -0.0000 *A_inv - I: 0.0000 0.0000	3.0000 1.0000 1.0000 0.0000 -0.0000 -1.0000 -0.0000 -0.0000	3.0000 2.0000 1.0000 0.0000 -0.0000 -0.0000 -9986.4385 9986.4385	3.0000 2.0000 1.0001 1.0000 1.3333 0.1667 0.5000 9985.4385 -9986.4385
1.0000 1.0000 1.0000 1.0000 1.0000 Inverse Matr -0.3333 0.3333 -0.0000 -0.0000 -0.0000 Matrix R = A 0.0000 -0.0000 -0.0000	1.0000 1.0000 1.0000 1.0000 ix A_inv: 0.0000 -0.5000 -0.5000 -0.0000 -0.0000 *A_inv - I: 0.0000 0.0000 0.0000	3.0000 1.0000 1.0000 0.0000 -0.0000 -1.0000 -0.0000 -0.0000 0.0000	3.0000 2.0000 1.0000 1.0000 0.0000 -0.0000 -0.0000 -9986.4385 9986.4385	3.0000 2.0000 1.0001 1.0000 1.3333 0.1667 0.5000 9985.4385 -9986.4385 0.0000 0.0000
1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 -0.3333 -0.0000 -0.0000 -0.0000 -0.0000 -0.0000 -0.0000 -0.0000	1.0000 1.0000 1.0000 1.0000 ix A_inv: 0.0000 -0.5000 -0.5000 -0.0000 -0.0000 0.0000 0.0000 0.0000	3.0000 1.0000 1.0000 0.0000 -0.0000 -1.0000 -1.0000 -0.0000 0.0000 0.0000	3.0000 2.0000 1.0000 1.0000 0.0000 -0.0000 -0.0000 -9986.4385 9986.4385 0.0000 0.0000 0.0000 -0.0010	3.0000 2.0000 1.0001 1.0000 1.3333 0.1667 0.5000 9985.4385 -9986.4385 0.0000 0.0000 0.0000 0.0000
1.0000 1.0000 1.0000 1.0000 1.0000 Inverse Matr -0.3333 0.3333 -0.0000 -0.0000 -0.0000 Matrix R = A 0.0000 -0.0000 -0.0000	1.0000 1.0000 1.0000 1.0000 ix A_inv: 0.0000 -0.5000 -0.5000 -0.0000 -0.0000 0.0000 0.0000 0.0000	3.0000 1.0000 1.0000 1.0000 0.0000 -0.0000 -1.0000 -0.0000 0.0000 0.0000 0.0000	3.0000 2.0000 1.0000 1.0000 0.0000 -0.0000 -0.0000 -9986.4385 9986.4385	3.0000 2.0000 1.0001 1.0000 1.3333 0.1667 0.5000 9985.4385 -9986.4385 0.0000 0.0000