G is an undirected simple graph. G has n nodes and m edges, and G is connected. Each edge in G has an integral weight  $\omega(e) \geq 1$ . We define the **minimum product spanning tree** of G to be a spanning tree T so that T has the minimum **product** 

$$\rho(T) \equiv \prod_{e \in T} \omega(e)$$

among all spanning trees of G. Write a program to output the minimum product spanning tree of the input graph G.

#### Hint

- 1.  $\log ab = \log a + \log b$  for a, b > 0.
- 2. Using floating-point numbers in a program is like opening a Pandora's box.

### **Input**

The first line contains n and m, where n is an integer in  $[2,10^3]$  and m is an integer in  $\left[n-1,\binom{n}{2}\right]$ . Each of subsequent m lines contains three integers  $u,v,\omega(u,v)$ , where u< v, indicating that G has an undirected edge (u,v) with weight  $\omega(u,v)$ . Note that we label each node in G with a unique number in  $\{1,2,\ldots,n\}$ , and thus u and v are integers in [1,n]. Each edge weight  $\omega(u,v)$  is an integer in  $[1,2^{61}]$ .

### Output

The edges in the minimum product spanning tree T of the input graph G. You need to output the edges in the lexicographic order, one edge per line; i.e.  $(u_i, v_i)$  needs to be outputted before  $(u_i, v_i)$  iff any of the following conditions holds:

- (a)  $u_i < u_i$
- (b)  $u_i = u_j$  and  $v_i < v_j$ .

If there are multiple minimum product spanning trees, it suffices to output the edges of any of them.

# **Sample Input**

- 4 6
- 1 2 6
- 1 3 3
- 1 4 5
- 2 3 2
- 2 4 4
- 3 4 1

# **Sample Output**

- 1 3
- 2 3
- 3 4