Cluster Analysis of Customers with R

QA

Problem Definition

- 1. Research Question Perform cluster analysis to identify customer groups on a Russian brand, Kira Plastinina to help the sales team understand the customer characteristics.
- 2. Metrics of success Identification of customer groups characteristics.
- **3.** Understanding the context Kira Plastinina is a Russian brand that is sold through a defunct chain of retail stores in Russia, Ukraine, Kazakhstan, Belarus, China, Philippines, and Armenia. The brand's Sales and Marketing team would like to understand their customer's behavior from data that they have collected over the past year. More specifically, they would like to learn the characteristics of customer groups.
- 4. Recording the experimental design
 - 1. Data Sourcing
 - 2. Check the Data
 - 3. Perform Data Cleaning
 - 4. Perform Exploratory Data Analysis
 - 5. Implement the Solution
 - 6. Challenge the Solution
 - 7. Follow up Questions

1. Data Sourcing

[http://bit.ly/EcommerceCustomersDataset]

Data Loading and Inspection

```
# Load libraries
library(readr)

## Warning: package 'readr' was built under R version 4.0.4

library(tidyverse)

## Warning: package 'tidyverse' was built under R version 4.0.4

## -- Attaching packages ------ tidyverse 1.3.0 --
```

```
## v ggplot2 3.3.3 v dplyr 1.0.5
## v tibble 3.1.0 v stringr 1.4.0
## v tidyr
           1.1.3 v forcats 0.5.1
## v purrr 0.3.4
## Warning: package 'ggplot2' was built under R version 4.0.4
## Warning: package 'tibble' was built under R version 4.0.4
## Warning: package 'tidyr' was built under R version 4.0.4
## Warning: package 'purrr' was built under R version 4.0.4
## Warning: package 'dplyr' was built under R version 4.0.4
## Warning: package 'stringr' was built under R version 4.0.4
## Warning: package 'forcats' was built under R version 4.0.4
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
library(psych)
## Warning: package 'psych' was built under R version 4.0.4
##
## Attaching package: 'psych'
## The following objects are masked from 'package:ggplot2':
##
      %+%, alpha
library(corrplot)
## Warning: package 'corrplot' was built under R version 4.0.4
## corrplot 0.84 loaded
library(BBmisc)
## Warning: package 'BBmisc' was built under R version 4.0.4
## Attaching package: 'BBmisc'
```

```
## The following objects are masked from 'package:dplyr':
##
##
       coalesce, collapse
## The following object is masked from 'package:base':
##
##
       isFALSE
library(caret)
## Warning: package 'caret' was built under R version 4.0.4
## Loading required package: lattice
##
## Attaching package: 'caret'
## The following object is masked from 'package:purrr':
##
##
      lift
library(cluster)
library(factoextra)
## Warning: package 'factoextra' was built under R version 4.0.4
## Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa
library(NbClust)
df <- read_csv("C:\\Users\\Lenovo\\Downloads\\online_shoppers_intention.csv")</pre>
##
## -- Column specification -------
## cols(
##
    Administrative = col_double(),
##
    Administrative_Duration = col_double(),
##
     Informational = col_double(),
     Informational_Duration = col_double(),
##
##
    ProductRelated = col_double(),
    ProductRelated_Duration = col_double(),
##
##
    BounceRates = col_double(),
##
    ExitRates = col_double(),
    PageValues = col_double(),
##
##
     SpecialDay = col_double(),
    Month = col_character(),
##
##
    OperatingSystems = col_double(),
##
    Browser = col_double(),
##
    Region = col_double(),
    TrafficType = col_double(),
##
```

```
##
     VisitorType = col_character(),
##
     Weekend = col_logical(),
     Revenue = col_logical()
##
## )
# Preview data
head(df)
## # A tibble: 6 x 18
     Administrative Administrative_D~ Informational Informational_D~ ProductRelated
                                                                 <dbl>
##
              <dbl>
                                 <dbl>
                                               <dbl>
## 1
                  0
                                                                                     1
                  0
                                     0
                                                                                     2
## 2
                                                   0
                                                                     0
## 3
                  0
                                    -1
                                                   0
                                                                    -1
                                                                                     1
## 4
                  0
                                     0
                                                   Ω
                                                                     0
                                                                                     2
                                     0
                  0
                                                                                    10
## 6
                  0
                                     0
                                                   0
                                                                     0
                                                                                    19
## # ... with 13 more variables: ProductRelated_Duration <dbl>, BounceRates <dbl>,
      ExitRates <dbl>, PageValues <dbl>, SpecialDay <dbl>, Month <chr>,
       OperatingSystems <dbl>, Browser <dbl>, Region <dbl>, TrafficType <dbl>,
       VisitorType <chr>, Weekend <lgl>, Revenue <lgl>
## #
```

2. Check the Data

```
# Shape of data
dim(df);
## [1] 12330
               18
# Column datatypes
str(df);
## spec tbl df [12,330 x 18] (S3: spec tbl df/tbl df/tbl/data.frame)
## $ Administrative
                            : num [1:12330] 0 0 0 0 0 0 0 1 0 0 ...
## $ Administrative_Duration: num [1:12330] 0 0 -1 0 0 0 -1 -1 0 0 ...
                           : num [1:12330] 0 0 0 0 0 0 0 0 0 0 ...
## $ Informational
## $ Informational Duration : num [1:12330] 0 0 -1 0 0 0 -1 -1 0 0 ...
## $ ProductRelated
                           : num [1:12330] 1 2 1 2 10 19 1 1 2 3 ...
## $ ProductRelated Duration: num [1:12330] 0 64 -1 2.67 627.5 ...
## $ BounceRates
                      : num [1:12330] 0.2 0 0.2 0.05 0.02 ...
## $ ExitRates
                           : num [1:12330] 0.2 0.1 0.2 0.14 0.05 ...
                           : num [1:12330] 0 0 0 0 0 0 0 0 0 0 ...
## $ PageValues
                           : num [1:12330] 0 0 0 0 0 0 0 0.4 0 0.8 0.4 ...
## $ SpecialDay
                           : chr [1:12330] "Feb" "Feb" "Feb" "Feb" ...
## $ Month
                           : num [1:12330] 1 2 4 3 3 2 2 1 2 2 ...
## $ OperatingSystems
## $ Browser
                            : num [1:12330] 1 2 1 2 3 2 4 2 2 4 ...
## $ Region
                           : num [1:12330] 1 1 9 2 1 1 3 1 2 1 ...
## $ TrafficType
                           : num [1:12330] 1 2 3 4 4 3 3 5 3 2 ...
                          : chr [1:12330] "Returning_Visitor" "Returning_Visitor" "Returning_Visitor
## $ VisitorType
## $ Weekend
                            : logi [1:12330] FALSE FALSE FALSE FALSE TRUE FALSE ...
```

```
$ Revenue
                              : logi [1:12330] FALSE FALSE FALSE FALSE FALSE ...
##
    - attr(*, "spec")=
##
     .. cols(
##
          Administrative = col_double(),
##
          Administrative_Duration = col_double(),
          Informational = col double(),
##
          Informational Duration = col double(),
##
     . .
          ProductRelated = col_double(),
##
     . .
##
          ProductRelated_Duration = col_double(),
     . .
##
          BounceRates = col_double(),
##
          ExitRates = col_double(),
     . .
##
          PageValues = col_double(),
##
          SpecialDay = col_double(),
     . .
          Month = col_character(),
##
     . .
##
          OperatingSystems = col_double(),
##
          Browser = col_double(),
     . .
##
          Region = col_double(),
##
          TrafficType = col_double(),
     . .
##
          VisitorType = col_character(),
##
     . .
          Weekend = col_logical(),
##
          Revenue = col_logical()
##
     ..)
```

Data Summary summary(df)

```
Administrative
                     Administrative_Duration Informational
##
   Min.
          : 0.000
                     Min.
                           : -1.00
                                              Min.
                                                    : 0.000
##
   1st Qu.: 0.000
                     1st Qu.:
                                0.00
                                              1st Qu.: 0.000
  Median : 1.000
                     Median:
                                8.00
                                              Median : 0.000
##
  Mean
          : 2.318
                               80.91
                                             Mean
                                                   : 0.504
                     Mean
   3rd Qu.: 4.000
                     3rd Qu.:
                               93.50
                                             3rd Qu.: 0.000
##
## Max.
           :27.000
                     Max.
                            :3398.75
                                             Max.
                                                    :24.000
  NA's
           :14
                     NA's
                                             NA's
                                                     :14
                            :14
   Informational_Duration ProductRelated
##
                                            ProductRelated_Duration
##
   \mathtt{Min}.
          : -1.00
                           Min.
                                  : 0.00
                                            Min.
                                                        -1.0
               0.00
##
   1st Qu.:
                           1st Qu.: 7.00
                                            1st Qu.: 185.0
  Median :
               0.00
                           Median : 18.00
                                            Median: 599.8
          : 34.51
                                  : 31.76
                                                    : 1196.0
##
  Mean
                           Mean
                                            Mean
##
   3rd Qu.:
               0.00
                           3rd Qu.: 38.00
                                            3rd Qu.: 1466.5
##
  {\tt Max.}
           :2549.38
                           Max.
                                  :705.00
                                            Max.
                                                    :63973.5
##
  NA's
           :14
                           NA's
                                  :14
                                            NA's
                                                    :14
##
    BounceRates
                         ExitRates
                                           PageValues
                                                              SpecialDay
##
   Min.
           :0.000000
                       Min.
                              :0.00000
                                                : 0.000
                                                            Min.
                                                                   :0.00000
                                         Min.
##
   1st Qu.:0.000000
                       1st Qu.:0.01429
                                         1st Qu.: 0.000
                                                            1st Qu.:0.00000
  Median :0.003119
                       Median :0.02512
                                         Median : 0.000
                                                            Median :0.00000
##
   Mean
           :0.022152
                       Mean
                              :0.04300
                                         Mean
                                                : 5.889
                                                            Mean
                                                                   :0.06143
                       3rd Qu.:0.05000
##
   3rd Qu.:0.016684
                                         3rd Qu.: 0.000
                                                            3rd Qu.:0.00000
##
   Max.
           :0.200000
                       Max.
                              :0.20000
                                         Max.
                                                 :361.764
                                                            Max.
                                                                   :1.00000
  NA's
                       NA's
                              :14
##
           :14
##
                       OperatingSystems
                                                              Region
       Month
                                           Browser
##
  Length: 12330
                       Min.
                              :1.000
                                        Min. : 1.000
                                                          Min.
                                                                 :1.000
                       1st Qu.:2.000
                                         1st Qu.: 2.000
  Class : character
                                                          1st Qu.:1.000
## Mode :character
                       Median :2.000
                                        Median : 2.000
                                                          Median :3.000
```

```
##
                        Mean
                               :2.124
                                                 : 2.357
                                                                   :3.147
                                          Mean
                                                           Mean
##
                        3rd Qu.:3.000
                                          3rd Qu.: 2.000
                                                           3rd Qu.:4.000
                                                                   :9.000
##
                        Max.
                               :8.000
                                         Max.
                                                 :13.000
                                                           Max.
##
     TrafficType
##
                     VisitorType
                                         Weekend
                                                           Revenue
##
   Min.
           : 1.00
                    Length: 12330
                                         Mode :logical
                                                          Mode :logical
    1st Qu.: 2.00
                     Class : character
                                         FALSE: 9462
                                                          FALSE: 10422
##
   Median: 2.00
                                         TRUE :2868
                                                          TRUE :1908
##
                    Mode :character
##
    Mean
           : 4.07
##
    3rd Qu.: 4.00
##
   Max.
           :20.00
##
```

 $\label{lem:contain_some_NA's: -Administrative - Administrative - Duration - Informational - Informational - Duration - ProductRelated - ProductRelated - Duration - BounceRates - ExitRates - PageValues$

Worth noting: There are durations that have -1 as values that may need to be dropped.

3. Data Cleaning

```
# Checking for duplicated data
anyDuplicated(df)
```

[1] 159

There are 159 duplicated rows

```
# Dropping the Duplicated rows
df <- df[!duplicated(df),]
anyDuplicated((df))</pre>
```

[1] 0

BOOM! Duplicates gone

```
# Get number of rows with null values
df[!complete.cases(df),]
```

```
## # A tibble: 12 x 18
##
      Administrative Administrative_~ Informational Informational_D~ ProductRelated
##
                <dbl>
                                   <dbl>
                                                   <dbl>
                                                                     <dbl>
                                                                                      <dbl>
##
    1
                   NA
                                      NA
                                                      NA
                                                                         NA
                                                                                         NA
                                                                         NA
##
    2
                   NA
                                      NA
                                                      NA
                                                                                         NA
##
   3
                   NA
                                      NA
                                                                         NA
                                                                                         NA
                                                      NA
   4
##
                   NA
                                      NA
                                                      NA
                                                                         NA
                                                                                         NA
##
    5
                   NA
                                      NA
                                                      NA
                                                                         NA
                                                                                         NA
   6
##
                   NA
                                      NA
                                                      NA
                                                                         NA
                                                                                         NA
##
   7
                   NA
                                      NA
                                                      NA
                                                                         NA
                                                                                         NA
                                                      NA
                                                                                         NA
##
    8
                   NA
                                      NA
                                                                         NA
```

```
NA
                                                                                   NA
                  NA
                                                  NA
## 10
                                                                    NΑ
                  NΑ
                                    NΑ
                                                  NΑ
                                                                                   NΑ
## 11
                  NA
                                    NA
                                                  NA
                                                                    NA
                                                                                   NA
## 12
                  NΑ
                                    NΑ
                                                  NΑ
                                                                    NΑ
                                                                                   NΑ
## # ... with 13 more variables: ProductRelated_Duration <dbl>, BounceRates <dbl>,
       ExitRates <dbl>, PageValues <dbl>, SpecialDay <dbl>, Month <chr>,
       OperatingSystems <dbl>, Browser <dbl>, Region <dbl>, TrafficType <dbl>,
## #
       VisitorType <chr>, Weekend <lgl>, Revenue <lgl>
```

It is the same rows with missing values!!! Drop them!!!

```
# Drop the NA rows
df <- df[complete.cases(df),]</pre>
```

Investigating the -1 values in the duration columns
anomalies <- df %>% select(c(Administrative_Duration, Administrative, Informational_Duration, Informati
anomalies

```
## # A tibble: 33 x 6
      Administrative_Duration Administrative Informational_Duration Informational
##
##
                          <dbl>
                                          <dbl>
                                                                    <dbl>
## 1
                             -1
                                               0
                                                                                       0
## 2
                             -1
                                               0
                                                                                       0
                                                                       -1
## 3
                             -1
                                               1
                                                                       -1
##
                             -1
                                               0
                                                                       -1
                                                                                       0
   5
                                                                       -1
                                                                                       0
##
                             -1
                                               0
##
   6
                                               0
                                                                                       0
                             -1
                                                                       -1
##
   7
                             -1
                                               0
                                                                       -1
                                                                                       0
##
  8
                             -1
                                               0
                                                                       -1
                                                                                       0
##
                             -1
                                               0
                                                                       -1
                                               0
## 10
                             -1
                                                                       -1
```

... with 23 more rows, and 2 more variables: ProductRelated_Duration <dbl>,

ProductRelated <dbl>

A total of 33 rows have the anomalies.

```
# Dropping the anomalies anomalous data

df <- df %>% filter(Administrative_Duration != -1, Informational_Duration != -1, ProductRelated_Duration
```

```
# describe each column
describe(df[, c(1:9)])
```

```
##
                                        mean
                                                  sd median trimmed
                                                                       mad min
                          vars
                                                       1.00
## Administrative
                             1 12164
                                        2.35
                                                3.33
                                                               1.66
                                                                      1.48
## Administrative_Duration
                             2 12164
                                       81.92 177.73
                                                      10.00
                                                              43.06
                                                                    14.83
## Informational
                             3 12164
                                                       0.00
                                                               0.18
                                                                      0.00
                                        0.51
                                                1.28
## Informational_Duration
                             4 12164
                                       34.94 141.65
                                                       0.00
                                                               3.76
                                                                      0.00
                             5 12164
## ProductRelated
                                       32.15
                                               44.63 18.00
                                                              23.14 19.27
## ProductRelated_Duration
                             6 12164 1210.99 1921.59 613.24 835.59 747.59
## BounceRates
                             7 12164
                                        0.02
                                                0.04
                                                       0.00
                                                               0.01
                                                                      0.00
## ExitRates
                             8 12164
                                        0.04
                                                0.05
                                                       0.03
                                                               0.03
                                                                      0.02
## PageValues
                             9 12164
                                        5.97
                                                               1.34
                                               18.68 0.00
                                                                      0.00
```

```
##
                                      range skew kurtosis
                               max
## Administrative
                             27.00
                                      27.00 1.94
                                                    4.62 0.03
## Administrative Duration 3398.75 3398.75 5.58
                                                   49.97 1.61
## Informational
                             24.00
                                      24.00 4.01
                                                   26.56 0.01
                         2549.38 2549.38 7.53
## Informational_Duration
                                                   75.23 1.28
## ProductRelated
                           705.00
                                                   31.01 0.40
                                    705.00 4.33
## ProductRelated_Duration 63973.52 63973.52 7.25
                                                  136.43 17.42
## BounceRates
                                                    9.71 0.00
                              0.20
                                      0.20 3.21
## ExitRates
                              0.20
                                      0.20 2.26
                                                    4.79 0.00
## PageValues
                            361.76
                                     361.76 6.34
                                                   64.75 0.17
```

Observations - All the numerical columns data values are positively skewed - All the numerical columns data are leptokurtic

```
# Outlier function
outlier_detector <- function(x){
  out <- boxplot.stats(x)$out
  return((length(out)/ length(x)*100))
}</pre>
```

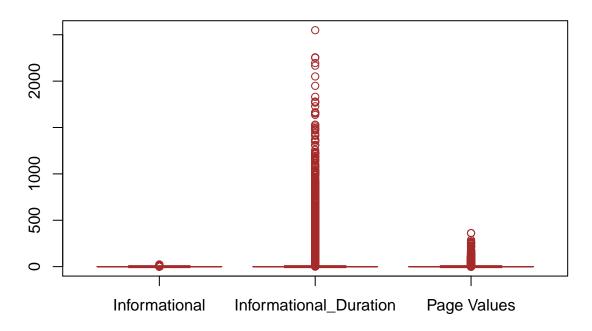
```
# Get outlier count per column
sapply(df[,c(1:9)], outlier_detector)
```

```
Administrative Administrative_Duration
                                                               Informational
##
##
                  3.321276
                                           9.363696
                                                                   21.621177
##
   Informational_Duration
                                     ProductRelated ProductRelated_Duration
##
                 19.763236
                                           8.278527
                                                                    7.809931
##
               BounceRates
                                          ExitRates
                                                                  PageValues
##
                 11.649129
                                          10.637948
                                                                   22.443275
```

Observations - PageValues column has the most outliers at 22.14%

```
# Plot boxplots of columns with high % of outliers
boxplot(df$Informational, df$Informational_Duration, df$PageValues,
main = "Columns with high values of outliers",
names = c("Informational", "Informational_Duration", "Page Values"),
col = c("orange", "red"),
border = "brown",
notch = TRUE)
```

Columns with high values of outliers



Observations - All outliers are contained above the third quantile. - The outliers may be true values as sometimes durations spent on a page may be long

4. Exploratory Data Analysis

```
# Frequency distribution of categorical columns
sapply(df[, c(10:18)], table)
## $SpecialDay
##
##
       0
                              0.8
           0.2
                 0.4
                       0.6
                                      1
## 10918
           178
                 242
                       348
                              324
                                    154
##
## $Month
##
                   Jul June
                             Mar May Nov
##
    Aug Dec Feb
##
    433 1706
             169
                   431
                       285 1842 3321 2980
                                                  448
## $OperatingSystems
##
##
                                     7
                                          8
           2
                3
                          5
                                6
## 2539 6519 2523
                   476
                               19
                                         75
##
## $Browser
##
```

```
3
                        4
                             5
                                   6
                                         7
                                                         10
                                                               11
                                                                     12
                                                                          13
                                               8
                                174
## 2418 7859
               104
                     727
                           464
                                        49
                                            134
                                                        162
                                                                6
                                                                     10
                                                                          56
                                                    1
##
## $Region
##
            2
                                         7
                                               8
                                                    9
##
                  3
                        4
                             5
                                   6
      1
   4701 1122 2374 1164
                           315
                                 800
                                      755
                                            431
##
## $TrafficType
##
##
                  3
                        4
                             5
                                   6
                                         7
                                               8
                                                    9
                                                         10
                                                               11
                                                                     12
                                                                          13
                                                                                14
                                                                                      15
                                                                                           16
                                                                         727
##
   2373 3905
              2002 1064
                           259
                                 440
                                        40
                                            343
                                                        450
                                                             247
                                                                                      36
                                                                                            3
                                                   41
                                                                      1
                                                                                13
##
     17
           18
                 19
                      20
##
      1
           10
                 17
                     192
##
##
   $VisitorType
##
##
          New_Visitor
                                     Other Returning_Visitor
##
                  1693
                                                          10390
                                         81
##
##
   $Weekend
##
## FALSE
           TRUE
    9311 2853
##
##
##
   $Revenue
##
## FALSE
           TRUE
## 10256
           1908
```

Summary of frequency table - SpecialDay 0 has the highest count - May and November receives the highest traffic - Operating system 2 is the most used to visit the site - Browser 2 is most used by visitors - Most visitors to the site are from Region 1 - Most of the traffic to the website is of type 2 and 1 - Most of the visitors to the site are mostly returning visitors - Most visitors visit the site during the weekday - Most visits to the site do not earn revenue

```
# Number of visits to product related pages per month
product_stats <- df %>% select(ProductRelated, ProductRelated_Duration, Month)%>%group_by(Month)%>% sum
product_stats[order(product_stats$ProductRelated, decreasing = TRUE),]
```

```
## # A tibble: 10 x 3
##
      Month ProductRelated ProductRelated_Duration
##
                       <dbl>
                                                  <dbl>
      <chr>
##
    1 Nov
                        46.3
                                                  1769.
##
    2 Aug
                        38.3
                                                  1273.
##
    3 Jul
                        36.5
                                                  1220.
##
    4 June
                        36.4
                                                  1226.
##
    5 Oct
                        33.6
                                                  1117.
##
    6 Sep
                        33.1
                                                  1253.
                        28.3
                                                  1125.
##
    7 Dec
    8 May
                        26.8
                                                   995.
    9 Mar
                        20.5
                                                   841.
##
## 10 Feb
                        12.1
                                                   513.
```

November had the highest number of visits to product related pages with the highest duration

```
# Distribution of revenue generating visits among visitors
df %>% select(VisitorType, Revenue)%>% group_by(VisitorType, Revenue)%>% summarise(visits = n())%>% fil
## 'summarise()' has grouped output by 'VisitorType'. You can override using the '.groups' argument.
## # A tibble: 3 x 3
## # Groups: VisitorType [3]
    VisitorType
                      Revenue visits
##
     <chr>
                       <lgl>
                                <int>
## 1 New Visitor
                       TRUE
                                  422
## 2 Other
                       TRUE
                                   16
## 3 Returning_Visitor TRUE
                                 1470
```

Returning visitors have the generate the most revenue.

```
# Distribution of revenue generating visits among regions
df %>% select(Region, Revenue)%>% group_by(Region, Revenue)%>% summarise(visits = n())%>% filter(Revenu
## 'summarise()' has grouped output by 'Region'. You can override using the '.groups' argument.
## # A tibble: 9 x 3
## # Groups: Region [9]
    Region Revenue visits
##
##
      <dbl> <lgl>
                     <int>
## 1
          1 TRUE
                       771
## 2
          2 TRUE
                       188
## 3
          3 TRUE
                       349
## 4
         4 TRUE
                       175
         5 TRUE
## 5
                        52
         6 TRUE
                       112
## 6
```

Visitors from Region 1 make most revenue generating visits

119

56

86

7

8

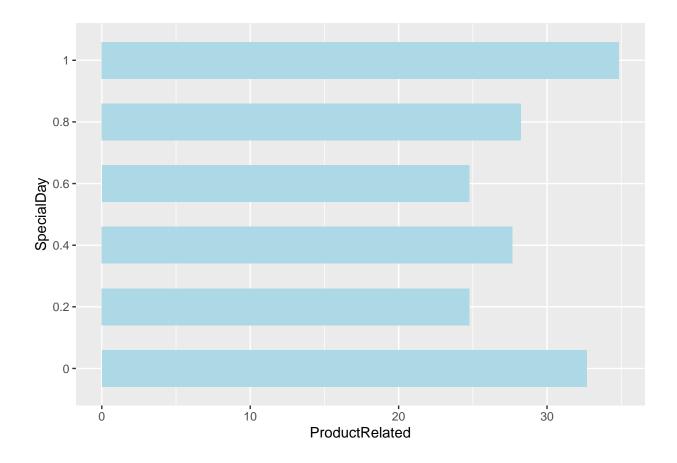
9

7 TRUE

8 TRUE

9 TRUE

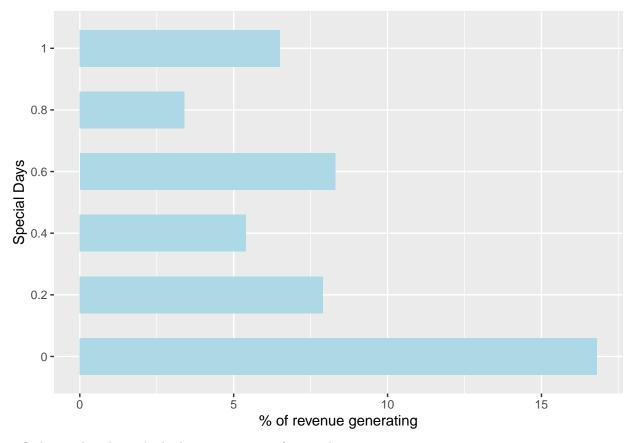
```
# Get page values and visits to product pages based on proximity to a special day
special_product <- df %>% select(SpecialDay, PageValues, ProductRelated, ProductRelated_Duration)%>% gr
ggplot(special_product, aes(x = factor(SpecialDay), y=ProductRelated))+
  geom_bar(fill = 'lightblue', stat = "identity", width = 0.6) +
 labs(x = 'SpecialDay')+
  coord_flip()
```



On special days customers visit the highest number of product related pages, with the highest mean number of pages visited.

```
# Distribution of revenue generating visits based on proximity to special days
revenue_special <- df %>% select(SpecialDay, Revenue)%>% group_by(SpecialDay, Revenue)%>% summarise(courselection)
## 'summarise()' has grouped output by 'SpecialDay'. You can override using the '.groups' argument.

revenue_special <- revenue_special[order(revenue_special$freq, decreasing = TRUE),]
ggplot(revenue_special, aes(x = factor(SpecialDay), y=freq))+
    geom_bar(fill = 'lightblue', stat = "identity", width = 0.6) +
    labs(y = '% of revenue generating', x = 'Special Days')+
    coord_flip()</pre>
```



> Ordinary days have the highest percentage of visits that are income generating

```
# Get bounce rates and exit rates among visitor groups
visitor_stats <- df %>% select(VisitorType, ExitRates, BounceRates)%>% group_by(VisitorType)%>%summaris
visitor_stats
```

```
## # A tibble: 3 x 3
##
     VisitorType
                        ExitRates BounceRates
     <chr>
##
                            <dbl>
                                        <dbl>
## 1 New_Visitor
                           0.0206
                                       0.00515
                           0.0566
                                       0.0306
## 2 Other
## 3 Returning_Visitor
                           0.0443
                                       0.0223
```

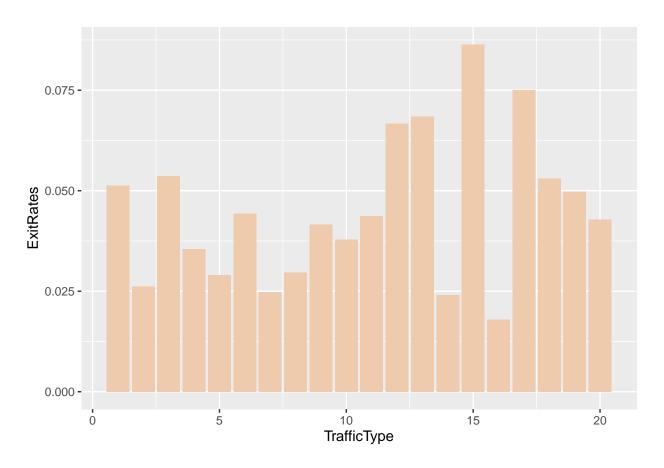
Observations - Other visitors have the highest exit rates and bounce rates - New_Visitor have the lowest exit and bounce rates

```
# Page views and durations based on visitor type
df %>% select(VisitorType, Administrative:ProductRelated_Duration)%>% group_by(VisitorType)%>%summarise
```

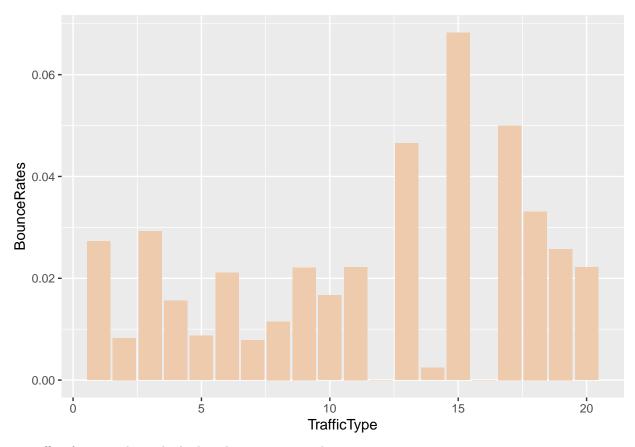
```
## # A tibble: 3 x 7
                   Administrative Administrative_D~ Informational Informational_Du~
##
     VisitorType
     <chr>>
                             <dbl>
                                               <dbl>
                                                              <dbl>
                                                                                 <dbl>
## 1 New_Visitor
                             2.55
                                                              0.334
                                                                                 19.2
                                                92.0
## 2 Other
                             1.54
                                                65.8
                                                              0.185
                                                                                 12.3
                             2.32
                                                80.4
                                                              0.542
## 3 Returning_Vi~
                                                                                 37.7
## # ... with 2 more variables: ProductRelated <dbl>,
     ProductRelated_Duration <dbl>
```

Observations - On average that New_Vistor have the longest Administrative_Duration followed by Returning_Visitor and lastly Other - Returning_Visitor have on average the longest Informational_Duration and ProductRelated_Duration

```
traffic_stats <- df %>% select(TrafficType, ExitRates, BounceRates)%>% group_by(TrafficType)%>% summari
par(mfrow = c(1,2))
ggplot(traffic_stats, aes(x=TrafficType, y = ExitRates))+
   geom_bar(stat = "identity", fill="peachpuff2")
```

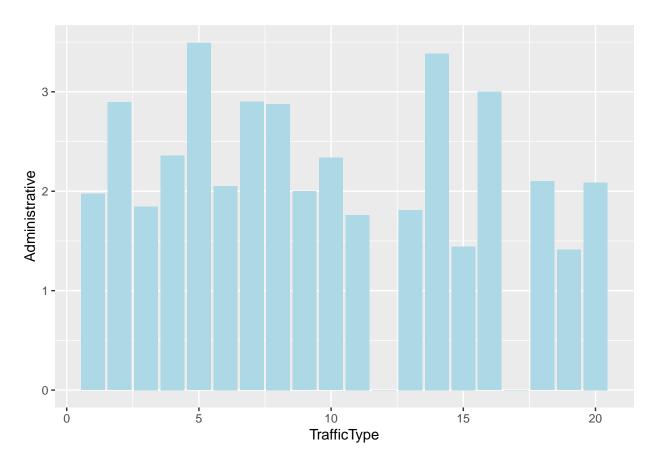


```
ggplot(traffic_stats, aes(x=TrafficType, y = BounceRates))+
geom_bar(stat = "identity", fill="peachpuff2")
```

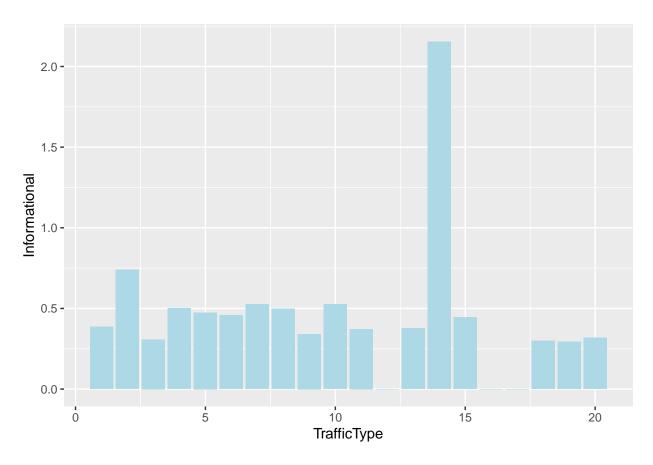


> Traffic of type 15 have the highest bounce rates and average rates on average

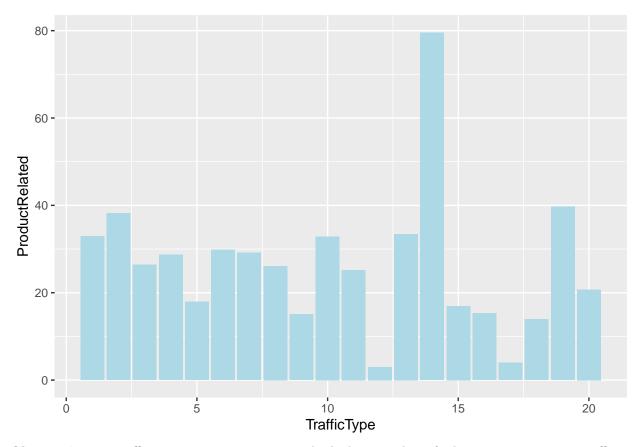
```
traffic_page_stats <- df %>% select(TrafficType, Administrative:ProductRelated_Duration)%>% group_by(Tr
par(mfrow = c(1,3))
ggplot(traffic_page_stats, aes(x=TrafficType, y = Administrative))+
    geom_bar(stat = "identity", fill="lightblue")
```



```
ggplot(traffic_page_stats, aes(x=TrafficType, y = Informational))+
geom_bar(stat = "identity", fill="lightblue")
```

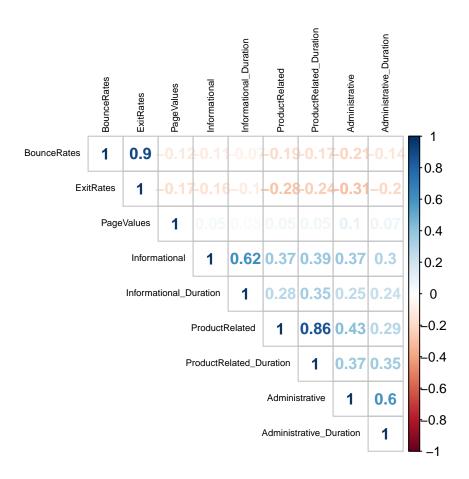


```
ggplot(traffic_page_stats, aes(x=TrafficType, y = ProductRelated))+
geom_bar(stat = "identity", fill="lightblue")
```



Observations - Traffic 5 on average experiences the highest number of administrative visits - Traffic 14 on average experiences the highest number of informational visits - Traffic 14 on average experiences the highest number of ProductRelated visits

```
# Correlational plot
corrplot(corr = cor(df[, c(1:9)]), method = "number", type = "upper", order = "hclust", tl.col = "black")
```



5. Solution Implementation

K-Means Clustering

```
# One hot encode categorical features
new_shoppers <- df[, 1:17]</pre>
# new_shoppers[, 10:16] <- as.character(new_shoppers[, 10:16])</pre>
dmy <- dummyVars("~ SpecialDay + Month + OperatingSystems + Browser + Region + TrafficType + VisitorTyp
ohe <- data.frame(predict(dmy, newdata = new_shoppers))</pre>
model_data <- cbind(new_shoppers[ , 1:9], ohe)</pre>
model_data$Weekend <- as.numeric(df$Weekend)</pre>
head(model_data)
##
     Administrative Administrative_Duration Informational Informational_Duration
## 1
                   0
                                                                                     0
## 2
                   0
                                             0
                                                            0
                                                                                     0
                                                                                     0
## 3
                   0
                                             0
                                                            0
## 4
                   0
                                             0
                                                            0
                                                                                     0
## 5
                   0
                                             0
                                                                                     0
## 6
                   0
                                             0
                                                                                     0
##
     ProductRelated ProductRelated_Duration BounceRates ExitRates PageValues
## 1
                                     0.000000 0.20000000 0.2000000
                   1
## 2
                   2
                                    64.000000 0.00000000 0.1000000
```

```
## 5
                  19
                                   154.216667 0.01578947 0.0245614
                                                                               0
## 6
                  2
                                    37.000000 0.00000000 0.1000000
                                                                               Λ
##
     SpecialDay MonthAug MonthDec MonthFeb MonthJul MonthJune MonthMar MonthMay
## 1
            0.0
                        0
                                                     0
                                                               0
                                 0
                                           1
            0.0
                                 0
                                                     0
                                                               0
                                                                         0
                                                                                   0
                                           1
            0.0
                                                                                   0
## 3
                        0
                                 0
                                           1
                                                     0
                                                               0
                                                                         0
## 4
            0.0
                        0
                                 0
                                           1
                                                     0
                                                               0
                                                                                   0
                        0
                                 0
                                                     0
                                                               0
                                                                                   0
## 5
            0.0
                                           1
## 6
            0.8
                        0
                                  0
                                           1
                                                     0
                                                                0
                                                                                   0
     MonthNov MonthOct MonthSep OperatingSystems Browser Region TrafficType
##
## 1
            0
                      0
                               0
                                                                  1
                                                 1
                                                          1
## 2
            0
                      0
                               0
                                                  2
                                                          2
                                                                              2
                                                                  1
## 3
            0
                      0
                               0
                                                  3
                                                          2
                                                                  2
                                                                              4
## 4
            0
                      0
                               0
                                                  3
                                                          3
                                                                              4
## 5
            0
                      0
                               0
                                                  2
                                                          2
                                                                              3
                                                                  1
                                                  2
## 6
            0
                      0
                                                          2
                                                                  2
     {\tt VisitorTypeNew\_Visitor~VisitorTypeOther~VisitorTypeReturning\_Visitor~Weekend}
##
## 1
## 2
                           0
                                             0
                                                                            1
                                                                                     0
## 3
                           0
                                             0
                                                                            1
                                                                                     0
## 4
                           0
                                             0
                                                                            1
                                                                                     1
## 5
                           0
                                             0
                                                                                     0
## 6
                                             0
                                                                                     0
                                                                            1
colnames(df)
##
    [1] "Administrative"
                                    "Administrative_Duration"
    [3] "Informational"
##
                                    "Informational_Duration"
                                    "ProductRelated_Duration"
   [5] "ProductRelated"
##
##
    [7] "BounceRates"
                                    "ExitRates"
   [9] "PageValues"
                                    "SpecialDay"
##
## [11] "Month"
                                    "OperatingSystems"
## [13] "Browser"
                                    "Region"
## [15] "TrafficType"
                                    "VisitorType"
## [17] "Weekend"
                                    "Revenue"
# Normalizing the continuous features
model_data[, 1:9] <- normalize(model_data[, 1:9], method = "range")</pre>
# Performing k-mean clustering with 5 clusters
customer_groups <- kmeans(model_data, centers = 5, nstart = 25)</pre>
str(customer_groups)
## List of 9
                  : Named int [1:12164] 4 4 4 4 4 4 2 4 4 4 ...
     ..- attr(*, "names")= chr [1:12164] "1" "2" "3" "4" ...
##
                  : num [1:5, 1:28] 0.0871 0.0781 0.0793 0.0911 0.0747 ...
##
  $ centers
     ..- attr(*, "dimnames")=List of 2
     .. ..$ : chr [1:5] "1" "2" "3" "4" ...
##
     ....$: chr [1:28] "Administrative" "Administrative_Duration" "Informational" "Informational_Dura
```

2.666667 0.05000000 0.1400000

0

627.500000 0.02000000 0.0500000

3

4

2

10

```
## $ totss : num 329285

## $ withinss : num [1:5] 15834 13026 23894 34071 9369

## $ tot.withinss: num 96194

## $ betweenss : num 233091

## $ size : int [1:5] 2253 1250 1855 6584 222

## $ iter : int 4

## $ ifault : int 0

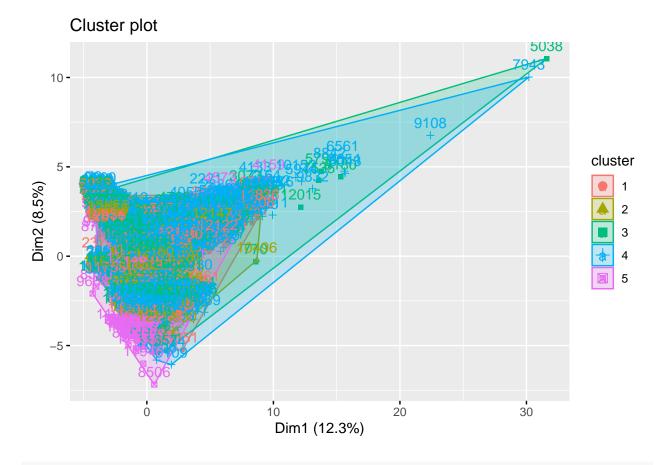
## - attr(*, "class") = chr "kmeans"
```

Cluster sizes customer_groups\$size

[1] 2253 1250 1855 6584 222

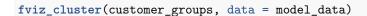
The first cluster has the most components

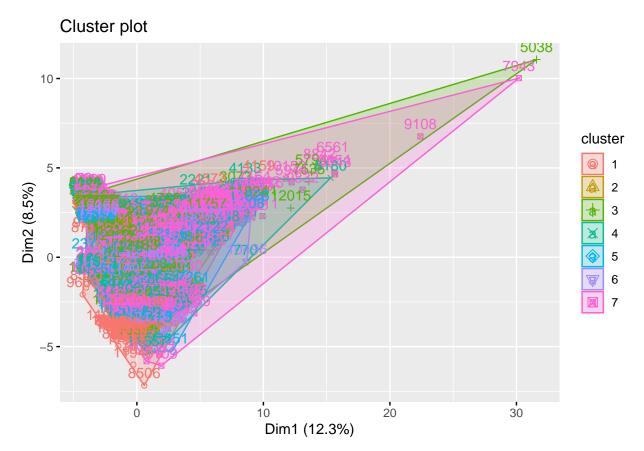
```
# Visualizing the clusters
fviz_cluster(customer_groups, data = model_data)
```



```
# 7 clusters
customer_groups <- kmeans(model_data, centers = 7, nstart = 25)
customer_groups$size</pre>
```

[1] 221 410 1185 1569 2183 727 5869

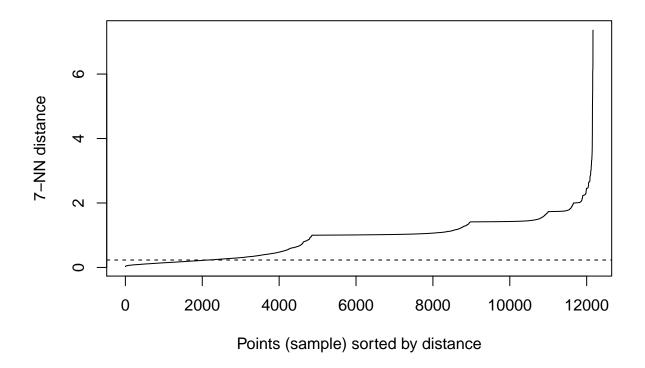




After dimension reduction using PCA, the data has been separated into 7 distinct clusters.

Hierachical Clustering

```
# Determining the optimal value for epislon
dbscan::kNNdistplot(model_data, k = 7)
abline(h = 0.23, lty = 2)
```



```
db_groups <- dbscan::dbscan(model_data, eps = 0.23, minPts = 7)
db_groups</pre>
```

```
## DBSCAN clustering for 12164 objects.
   Parameters: eps = 0.23, minPts = 7
   The clustering contains 206 cluster(s) and 8886 noise points.
##
##
##
             1
                   2
                         3
                               4
                                     5
                                           6
                                                  7
                                                       8
                                                                   10
                                                                         11
                                                                               12
                                                                                     13
                                                                                           14
                                                                                                 15
##
   8886
             9
                  29
                        83
                              15
                                    43
                                          19
                                                57
                                                       9
                                                              9
                                                                   24
                                                                         25
                                                                                7
                                                                                      8
                                                                                            7
                                                                                                  7
                                                                         27
                                                                                     29
##
      16
            17
                  18
                        19
                              20
                                    21
                                          22
                                                23
                                                      24
                                                             25
                                                                   26
                                                                               28
                                                                                           30
                                                                                                 31
##
      17
                               9
                                    16
                                          14
                                                25
                                                      26
                                                             16
                                                                          9
                                                                                8
                                                                                      7
            14
                   8
                        14
                                                                   11
                                                                                           11
                                                                                                 11
##
      32
            33
                  34
                        35
                              36
                                    37
                                          38
                                                39
                                                      40
                                                             41
                                                                   42
                                                                         43
                                                                               44
                                                                                                 47
                                                                                     45
                                                                                           46
##
      8
             8
                  11
                         7
                              12
                                    21
                                           7
                                                       8
                                                             7
                                                                    7
                                                                         15
                                                                               10
                                                                                     19
                                                                                           16
                                                                                                 29
      48
            49
                  50
                              52
                                    53
                                                55
                                                            57
                                                                  58
##
                        51
                                          54
                                                      56
                                                                         59
                                                                               60
                                                                                     61
                                                                                           62
                                                                                                 63
      20
            73
                                                32
                                                                   12
##
                  13
                         9
                               7
                                     7
                                           7
                                                      27
                                                             15
                                                                          9
                                                                               73
                                                                                     21
                                                                                            8
                                                                                                 11
##
                        67
                              68
                                    69
                                          70
                                                71
                                                      72
                                                             73
                                                                   74
                                                                         75
                                                                                     77
                                                                                           78
      64
            65
                  66
                                                                               76
                                                                                                 79
                  33
                                                                   13
                                                                         17
##
       9
            14
                        13
                               9
                                    13
                                           8
                                                11
                                                      10
                                                             9
                                                                               10
                                                                                     10
                                                                                            8
                                                                                                  8
                  82
                                    85
                                                      88
                                                                   90
                                                                         91
                                                                               92
                                                                                     93
                                                                                           94
##
      80
            81
                        83
                              84
                                          86
                                                87
                                                            89
                                                                                                 95
            10
                               8
                                                              7
                                                                    7
                                                                                            9
##
       8
                   7
                        12
                                    11
                                          11
                                                11
                                                       8
                                                                          7
                                                                                7
                                                                                      7
                                                                                                  7
##
      96
            97
                  98
                        99
                             100
                                   101
                                         102
                                               103
                                                     104
                                                           105
                                                                 106
                                                                       107
                                                                              108
                                                                                    109
                                                                                          110
                                                                                                111
                   7
                         7
##
       7
             7
                               7
                                     7
                                           7
                                                20
                                                       8
                                                             13
                                                                   23
                                                                         13
                                                                               16
                                                                                      7
                                                                                           11
                                                                                                 28
    112
           113
                 114
                       115
                             116
                                   117
                                         118
                                               119
                                                     120
                                                           121
                                                                 122
                                                                        123
                                                                              124
                                                                                    125
                                                                                          126
                                                                                                127
##
##
       8
            19
                   8
                        10
                              12
                                   168
                                           8
                                                51
                                                       9
                                                             15
                                                                   42
                                                                         69
                                                                                9
                                                                                      7
                                                                                           20
                                                                                                 55
##
     128
           129
                 130
                       131
                             132
                                   133
                                         134
                                               135
                                                     136
                                                           137
                                                                 138
                                                                        139
                                                                              140
                                                                                    141
                                                                                          142
                                                                                                143
                                                  7
                                                        7
##
      13
            10
                  41
                        16
                              20
                                    27
                                          33
                                                             18
                                                                    8
                                                                          7
                                                                                     38
                                                                                                 20
```

```
##
   144 145 146 147 148 149 150
                                       151 152 153 154 155
                                                                 156
                                                                      157 158
                                                                                159
##
    36
         30
               20
                         13
                              37
                                   26
                                                   11
                                                        23
                                                             14
                                                                  30
                                                                       10
                                                                            21
                                                                                 11
                   12
                                         7
                                             11
##
   160
        161
              162
                   163
                        164
                             165
                                  166
                                       167
                                             168
                                                  169
                                                       170
                                                            171
                                                                 172
                                                                      173
                                                                           174
                                                                                175
##
    11
           8
                         23
                              16
                                   18
                                        26
                                               8
                                                    7
                                                        13
                                                              7
                                                                             8
                                                                                  20
               11
                    10
                                                                   9
                                                                       17
##
   176
        177
              178
                   179
                        180
                             181
                                  182
                                       183
                                             184
                                                  185
                                                       186
                                                            187
                                                                 188
                                                                      189
                                                                           190
                                                                                191
                                    9
                                                    7
                                                             10
                                                                            14
##
    12
           8
               12
                     8
                          7
                              13
                                         12
                                              10
                                                        11
                                                                   7
                                                                        7
       193
                   195
                        196
                             197
                                  198
                                       199
                                                  201
                                                       202
                                                            203
                                                                           206
##
   192
              194
                                            200
                                                                 204
                                                                      205
                                         7
                                               7
                                                    7
                                                                   7
                                                                        7
                                                                             7
##
          10
                7
                     7
                          8
                               7
                                    8
                                                         9
                                                             11
##
## Available fields: cluster, eps, minPts
fviz_cluster(db_groups, model_data, geom="point")
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '26'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '27'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '29'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '30'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '30'
## Warning in grid.Call.graphics(C points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '31'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '31'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '27'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '27'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '30'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '31'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '31'
```

```
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '29'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '26'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '26'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '31'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '31'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '30'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '29'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '26'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '30'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '29'
## Warning in grid.Call.graphics(C points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '26'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '29'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '27'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '27'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '29'
```

```
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '26'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '27'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '31'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '30'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '31'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '26'
## Warning in grid.Call.graphics(C points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '26'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '30'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '30'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '31'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '31'
## Warning in grid.Call.graphics(C points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '27'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '26'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '26'
```

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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '27'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '27'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '30'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '31'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '29'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '30'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '26'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '30'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
## unknown for character 0x7f
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font metrics
## unknown for character 0x7f
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
## unknown for character 0x81
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
## unknown for character 0x4
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font metrics
## unknown for character 0x81
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
## unknown for character 0x7f
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font metrics
## unknown for character 0x7f
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
## unknown for character 0x8f
```

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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
## unknown for character 0x4
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font metrics
## unknown for character 0x8f
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
## unknown for character 0x7f
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font metrics
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
## unknown for character 0x8d
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font metrics
## unknown for character 0x8d
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## unknown for character 0x8f
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font metrics
## unknown for character 0x8f
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
## unknown for character 0x4
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font metrics
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## unknown for character 0x7f
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font metrics
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font metrics
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font metrics
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font metrics
## unknown for character 0x90
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font metrics
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
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## unknown for character 0x81
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
## unknown for character 0x4
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font metrics
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## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): font width
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## pch value '27'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
## pch value '29'
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## pch value '30'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplemented
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       cluster
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  200
1 (12
            8
                    27
                             46
                                      65
                                              84
                                                       103
                                                                 122
                                                                           141
                                                                                     160
                                                                                               179
                                                                                                        19
```

The clusters in our data are spherical

Cluster Analysis

```
df <- df %>% mutate(group = customer_groups$cluster)
head(df)
## # A tibble: 6 x 19
##
     Administrative Administrative_D~ Informational Informational_D~ ProductRelated
##
               <dbl>
                                  <dbl>
                                                 <dbl>
                                                                    <dbl>
                                                                                    <dbl>
## 1
                   0
                                                      0
                                       0
                                                                        0
                                                                                        1
## 2
                   0
                                       0
                                                      0
                                                                        0
                                                                                        2
## 3
                   0
                                       0
                                                      0
                                                                        0
                                                                                        2
## 4
                   0
                                       0
                                                      0
                                                                        0
                                                                                       10
## 5
                   0
                                       0
                                                      0
                                                                                       19
## 6
                   0
                                       0
                                                      0
                                                                                        2
## # ... with 14 more variables: ProductRelated_Duration <dbl>, BounceRates <dbl>,
```

```
## # ExitRates <dbl>, PageValues <dbl>, SpecialDay <dbl>, Month <chr>,
```

VisitorType <chr>, Weekend <lgl>, Revenue <lgl>, group <int>

Summary Statistics

summary_stats <- df %>% group_by(group)%>% select(Administrative:PageValues, group)%>% summarise_all(me summary_stats

A tibble: 7 x 10

##		group	${\tt Administrative}$	Administrative_Durati~	${\tt Informational}$	<pre>Informational_Durat~</pre>
##		<int></int>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>
##	1	1	2.02	78.3	0.312	30.8
##	2	2	1.99	75.0	0.405	19.7
##	3	3	2.00	73.0	0.449	28.5
##	4	4	2.56	85.0	0.516	32.7
##	5	5	2.33	78.7	0.469	30.2
##	6	6	2.18	74.3	0.398	31.3
##	7	7	2.42	85.7	0.565	40.3

^{## # ...} with 5 more variables: ProductRelated <dbl>,

^{## #} OperatingSystems <dbl>, Browser <dbl>, Region <dbl>, TrafficType <dbl>,

^{## #} ProductRelated_Duration <dbl>, BounceRates <dbl>, ExitRates <dbl>,

^{## #} PageValues <dbl>