Tutorial on NLPP, Poisson and Normal Distribution

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1) Use Kuhn Tucker conditions to solve the NLPP

Maximise.
$$z = -7x_1^2 + 2x_2^2 + 12x_1x_2$$

Subject to, $5x_1 + 2x_2 \le 98$
with $x_1, x_2 \ge 0$

2) Using the method of Lagrange's multiplier, solve the following NLPP

Optimise
$$z = 5x_1^2 + 6x_2^2$$

Subject to, $5x_1 + x_2 = 7$
with $x_1, x_2 \ge 0$

- 3) An Auto hire firm has two Auto which it hires out day by day. The number of demands for an Auto on each day is distributed as Poisson variate with mean 1.5. Calculate the proportion of days on which neither Auto is used.
- 4) Find the probability that a random variable having standard normal distribution will take a value between 0.87 and 1.28.
- 5) If $X \sim N(25, 5)$ find X = c such that

(i)
$$p(X \le c) = 0.01$$
 (ii) $p(X \le c) = 0.68$ (iii) $p(c < X) = 0.23$