

[PRACTICE]

BASIC SOLUTIONS [TYPE I]

① $Z = x_1 - 2x_2 + 4x_3$
 SUB, $x_1 + 2x_2 + 3x_3 = 7$
 $3x_1 + 4x_2 + 6x_3 = 15$
 WH, $x_1, x_2, x_3 \geq 0$

BASIC VAR	NON VAR	EQUATION	FEASIBLE	DEGENERATE	VALUE	OPTIMAL
x_1, x_2	$x_3 = 0$	$x_1 + 2x_2 = 7$ $3x_1 + 4x_2 = 15$ $x_1 = 1, x_2 = 3$	Y	N	-5	N
x_1, x_3	$x_2 = 0$	$x_1 + 3x_3 = 7$ $3x_1 + 6x_3 = 15$ $x_1 = 1, x_3 = 2$	Y	N	9	Y
x_2, x_3	$x_1 = 0$	$2x_2 + 3x_3 = 7$ $4x_2 + 6x_3 = 15$ UNBOUNDED SOLUTION	-	-	-	-

③ $Z = 2x_1 - 2x_2 + 4x_3 - 5x_4$

SUB, $x_1 + 4x_2 - 2x_3 + 8x_4 \leq 2$

$-x_1 + 2x_2 + 3x_3 + 4x_4 \leq 1$

WHERE, $x_1, x_2, x_3, x_4 \geq 0$

BASIC VAR.	NON BASIC VAR.	EQUATION	FEASIBLE	DEGENERATE	Z VALUE	OPTIMAL
x_1 x_2	$x_3 = 0$ $x_4 = 0$	$x_1 + 4x_2 = 2$ $-x_1 + 2x_2 = 1$ $x_1 = 0, x_2 = 1/2$	Y	Y	-1	N
x_1 x_3	$x_2 = 0$ $x_4 = 0$	$x_1 - 2x_3 = 2$ $-x_1 + 3x_3 = 1$ $x_1 = 8, x_3 = 3$	Y	N	28	Y
x_1 x_4	$x_2 = 0$ $x_3 = 0$	$x_1 + 8x_4 = 2$ $-x_1 + 4x_4 = 1$ $x_1 = 0, x_4 = 1/4$	Y	Y	$-\frac{5}{4}$	N
x_2 x_3	$x_1 = 0$ $x_4 = 0$	$4x_2 - 2x_3 = 2$ $2x_2 + 3x_3 = 1$ $x_2 = 1/2, x_3 = 0$	Y	Y	-1	N
x_2 x_4	$x_1 = 0$ $x_3 = 0$	$4x_2 + 8x_4 = 2$ $2x_2 + 4x_4 = 1$ $x_2 = ?, x_4 = ?$	—	—	—	—
x_3 x_4	$x_1 = 0$ $x_2 = 0$	$-2x_3 + 8x_4 = 2$ $3x_3 + 4x_4 = 1$ $x_3 = 0, x_4 = 1/4$	Y	Y	$-\frac{5}{4}$	N