Al 2002 Artificial Intelligence

Beyond Classical Search

Beyond Classical Search

- We have addressed a single category of problems: observable, deterministic, known environments
 - where the <u>solution</u> is a sequence of actions
- The search algorithms that we have seen so far are designed to explore search spaces systematically.
 - When a goal is found, the path to that goal also constitutes a solution to the problem.

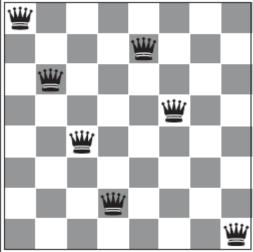
What happens when these assumptions are relaxed?

Beyond Classical Search

In many problems, however, the path to the goal is irrelevant.

For example:

- 8-queens problem
 - what matter, is the final configuration of queens, not the order.
- The factory-floor layout problem
- The vehicle routing problem



- Operate using a single current node and generally move only to neighbors of that node.
 - No concern with paths followed by the search
 - They are *NOT systematic*
- Local search algorithms have two key advantages:
 - they use very *little memory*
 - they can often find reasonable solutions in large or infinite (continuous) state spaces

 The local search algorithms are useful for solving pure optimization problems,

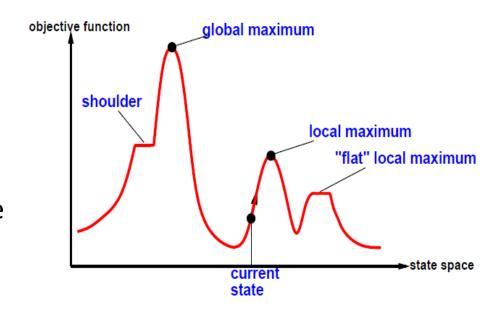
Optimization problems:

- the aim is to find the best state according to an objective function.
- ▶ The standard search methods do not fit well with optimization problems.

State-space landscape

A landscape has both

- "location"
 - defined by the state
- "elevation"
 - defined by the value of the heuristic cost function or objective function.

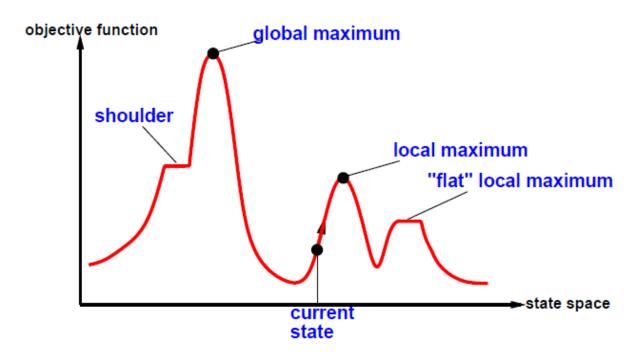


State-space landscape

Goal/Aim:

- If elevation corresponds to <u>cost</u>, then the aim is to find the lowest valley—a global minimum;
- If elevation corresponds to an objective function, then the aim is to find the highest peak—a global maximum.

State-space landscape

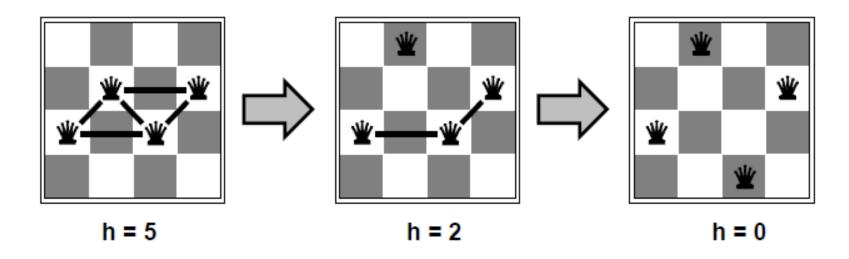


A one-dimensional state-space landscape in which *elevation* corresponds to the objective function. The aim is to find the global maximum.

- A complete local search algorithm always finds a goal if one exists;
- An optimal algorithm always finds a global minimum/maximum.
- Local search algorithms typically use a <u>complete-state</u> <u>formulation</u>,
 - In 8-queen problem, where each state has 8 queens on the board, one per column.

Example: n-queens Problems

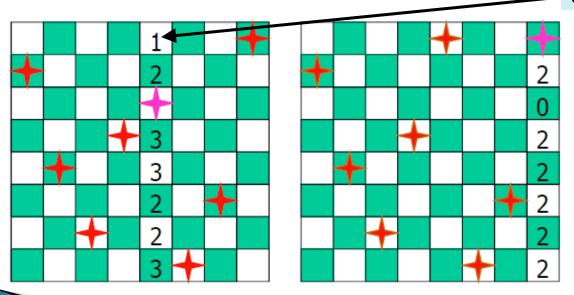
- Put n queens on an $n \times n$ board with no two queens on the same row, column, or diagonal.
- Move a queen to reduce number of conflicts
- Heuristic h: number of 'attacks'

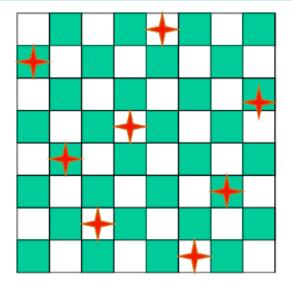


Example: n-queens Problems

- Put n queens on an $n \times n$ board with no two queens on the same row, column, or diagonal
- Move a queen to reduce number of conflicts
- ▶ Heuristic **h**: number of 'attacks'

If queen is placed here, there is only one attack then,



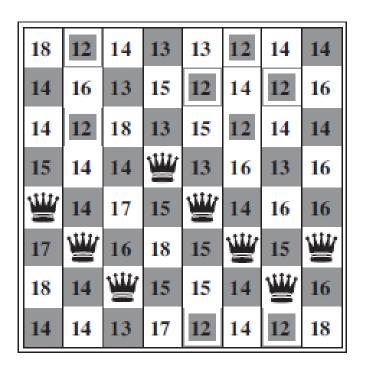


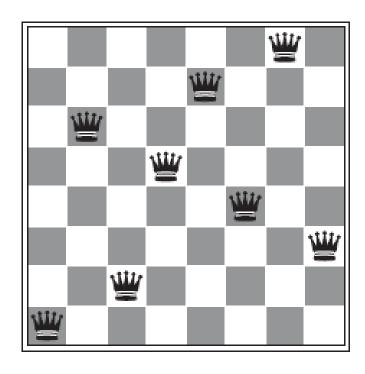
- It is simply a **loop** that continuously moves in the direction of increasing value—that is, uphill.
- It terminates when it reaches a "peak" where no neighbor has a higher value.
 - does not maintain a search tree
 - need only
 - record the state and
 - the value of the objective function.
- Hill climbing only looks towards the immediate neighbors of the current state.

function HILL-CLIMBING(problem) returns a state that is a local maximum

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\begin{array}{l} \textit{current} \leftarrow \mathsf{MAKE\text{-}NODE}(\textit{problem}.\mathsf{INITIAL\text{-}STATE}) \\ \textbf{loop do} \\ \textit{neighbor} \leftarrow \mathsf{a highest\text{-}valued successor of } \textit{current} \\ \textbf{if neighbor}.\mathsf{VALUE} \leq \mathsf{current}.\mathsf{VALUE} \textbf{ then return } \textit{current}.\mathsf{STATE} \\ \textit{current} \leftarrow \textit{neighbor} \end{array}
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- At each step the current node is replaced by the best neighbor; the neighbor with the highest VALUE,
- If a heuristic cost estimate h is used, we would find the neighbor with the lowest h.





(a) An 8-queens state with heuristic cost estimate h = 17, showing the value of h for each possible successor. (b) A local minimum: the state has h = 1 but every successor has a higher cost.

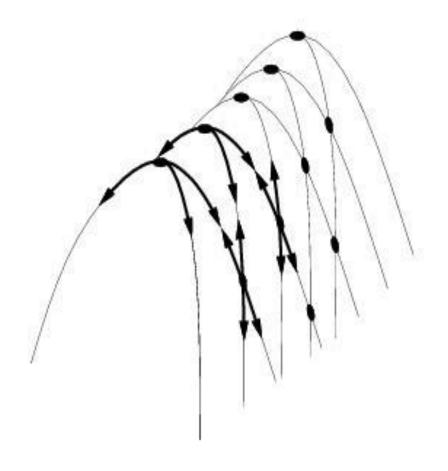
The hill climbing often gets stuck for the following reasons:

Local maxima:

A local maximum is a peak that is higher than each of its neighboring states but lower than the global maximum.

Ridges:

- A sequence of local maxima
- Its difficult for greedy algorithms to navigate



Plateaux:

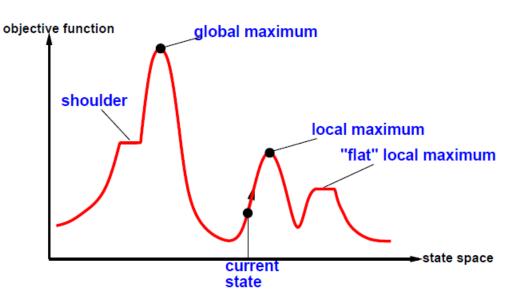
An area of the state space where the evaluation function is flat.

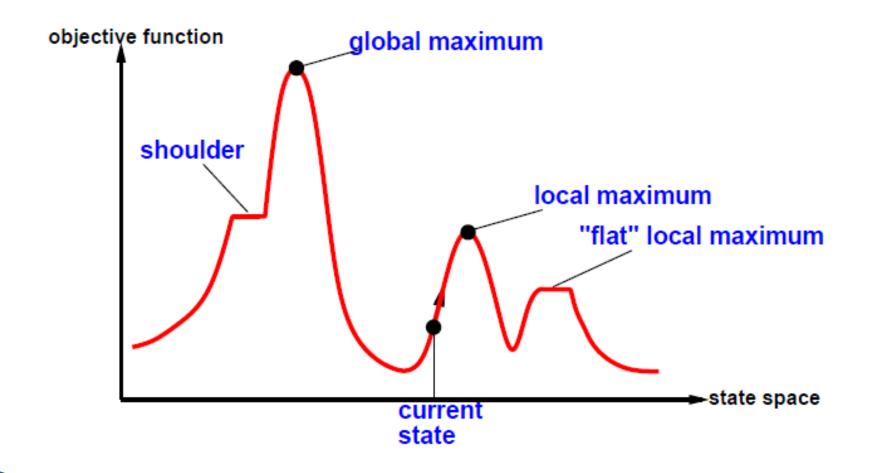
It can be a flat local maximum, from which no uphill

exit exists,

Shoulder:

from which progress is possible





Reading Material

- Artificial Intelligence, A Modern Approach Stuart J. Russell and Peter Norvig
 - Chapter 3 & 4.