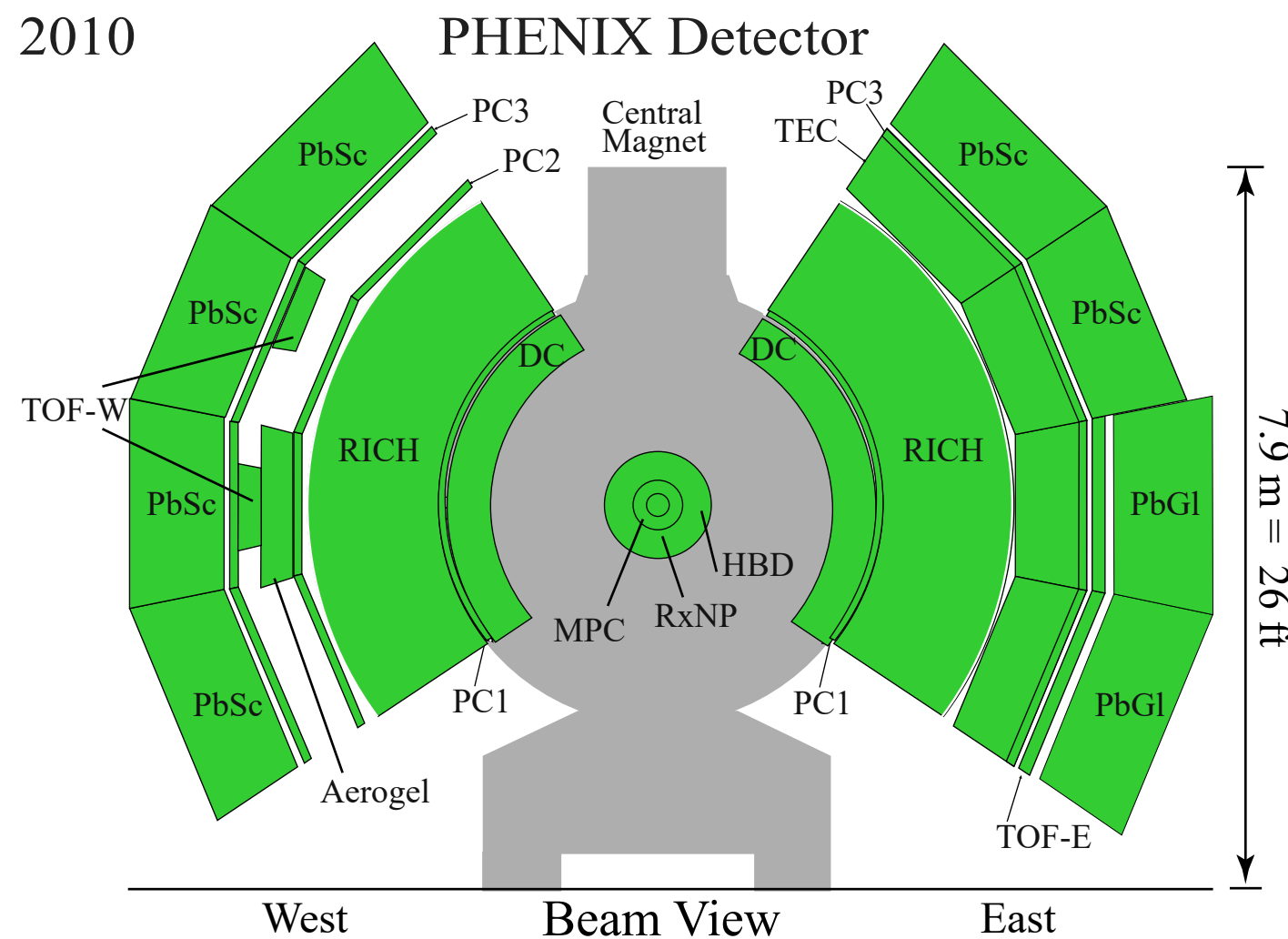
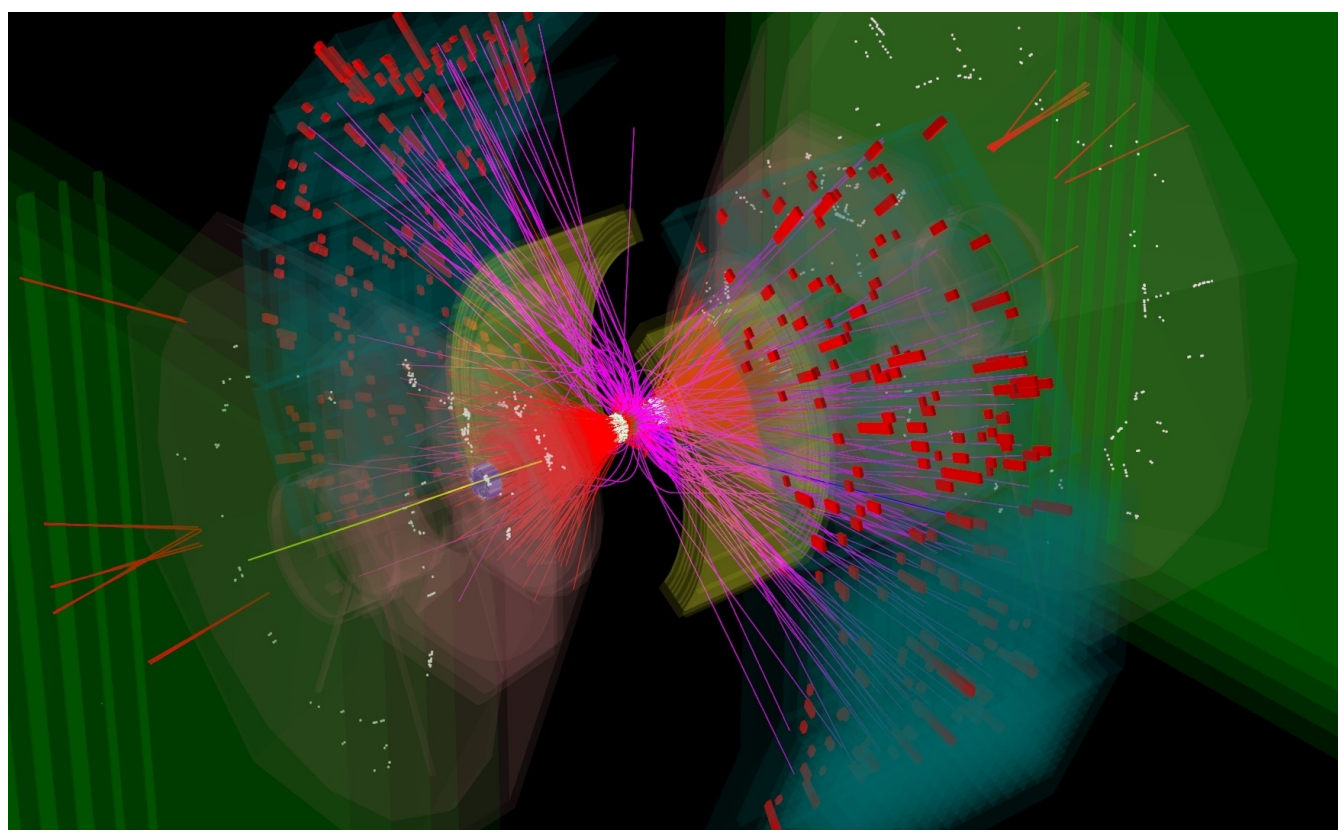


## The PHENIX experiment at RHIC



- Charged pion ID from  $\sim 0.2$  to  $2 \text{ GeV}/c$

## Introduction to three particle Bose-Einstein correlations

- Invariant momentum distributions:  $N_1(p_i), N_2(p_1, p_2), N_3(p_1, p_2, p_3)$
- The definition of the correlation function:

$$C_n(p_1, \dots, p_n) = \frac{N_n(p_1, \dots, p_n)}{N_1(p_1) \dots N_1(p_n)}, \text{ for chaotic emission: } N_n(x_1, \dots, x_n) = \int \prod_{i=1}^n S(x_i, p_i) |\Psi_n(\{x_i\})|^2 d^4x_1 \dots d^4x_n$$

- $S(x, p)$  source function (usually assumed to be Gaussian - Levy is more general)
- $\Psi_n$   $n$ -particle wave function - interaction free case: symmetrized combination of plane waves  $\rightarrow C_n^{(0)}$
- Coordinate transformation:  $q_{ij} = p_i - p_j \Rightarrow C_3(q_{12}, q_{13}, q_{23})$  for various  $p_T = |p_{T1} + p_{T2} + p_{T3}|/3$
- Longitudinal co-moving system of triplet:  $k_{ij} = |q_{ij}^{\text{LCMS}}|$
- Three dimensional correlation function:  $C_3(k_{12}, k_{13}, k_{23})$

## Final state interactions, pion production mechanisms

- Identical charged pions - Coulomb interaction distort the simple picture
- Coulomb-corrected correlation:  $C_3(k_{12}, k_{13}, k_{23}) = K_3(k_{12}, k_{13}, k_{23}) \cdot C_3^{(0)}(k_{12}, k_{13}, k_{23})$
- Coulomb-correction from Generalized Riverside [1, 2]:  $K_3(k_{12}, k_{13}, k_{23}) \approx K_1(k_{12})K_1(k_{13})K_1(k_{23})$
- Resonance pions contribute to the full source:  $S = S_{\text{core}} + S_{\text{halo}}$
- Reduce the measurable correlation function to  $C_2(0) = 1 + \lambda_2$  with  $\lambda_2 = f_c^2 = \left(\frac{\text{core}}{\text{core} + \text{halo}}\right)^2$  [3, 4]
- Non-chaotic emission also possible; coherent fraction:  $p_c = \frac{\text{coherent}}{\text{coherent} + \text{incoherent}}$

## The Levy-distribution and the three particle correlation strength

- Generalized Gaussian from anomalous diffusion: Levy-distribution,  $\alpha = 2$ : Gauss,  $\alpha = 1$ : Cauchy

$$\mathcal{L}(\alpha, R, r) = (2\pi)^{-3} \int d^3q e^{iqr} e^{-\frac{1}{2}|qR|^\alpha}$$

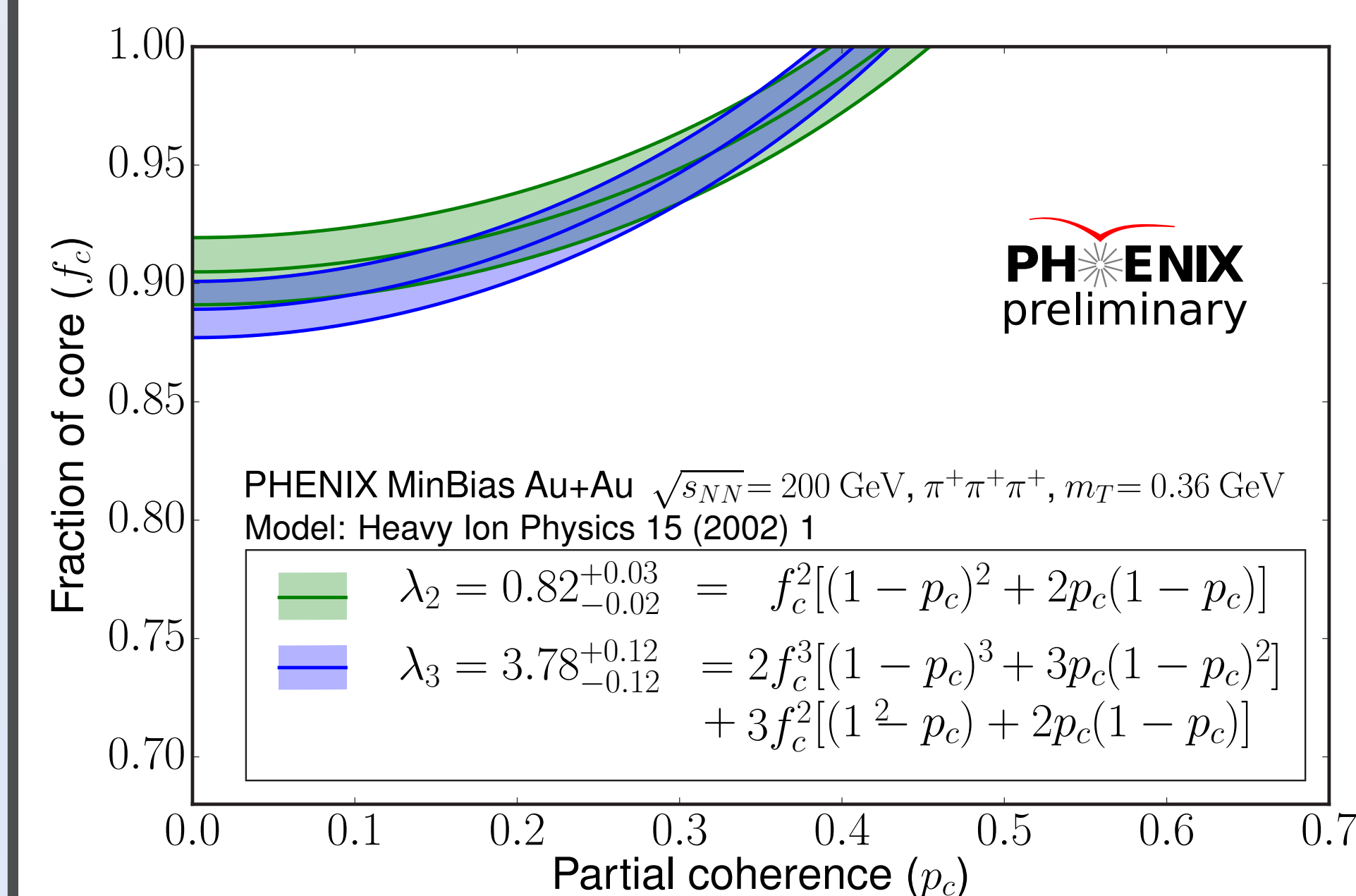
- Interaction free correlation function with Levy source:

$$C_3^{(0)}(k_{12}, k_{13}, k_{23}) = 1 + \ell_3 e^{-0.5(|2k_{12}R|^\alpha + |2k_{13}R|^\alpha + |2k_{23}R|^\alpha)} + \ell_2 (e^{|2k_{12}R|^\alpha} + e^{|2k_{13}R|^\alpha} + e^{|2k_{23}R|^\alpha})$$

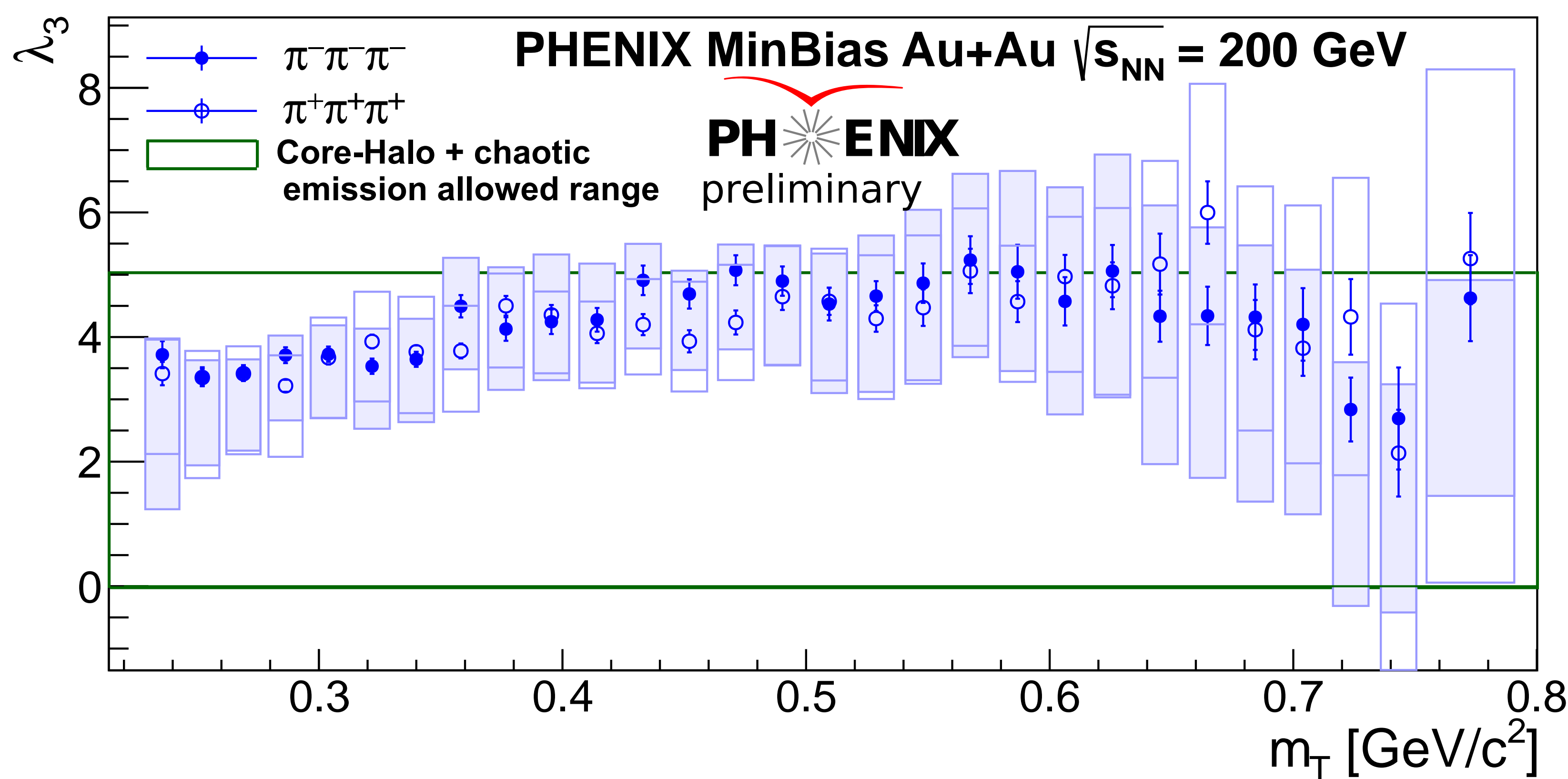
- Three particle correlation strength:  $\lambda_3 \equiv C_3(k_{12} = k_{13} = k_{23} = 0) - 1 = \ell_3 + 3\ell_2$
- Core-Halo independent parameter:  $\kappa_3 = (\lambda_3 - 3\lambda_2)/(2\lambda_2^{3/2})$ , where  $\lambda_2 \equiv C_2(k = 0) - 1$  (two particle corr. strength)

## Partial coherence ( $p_c$ ) vs fractional core ( $f_c$ )

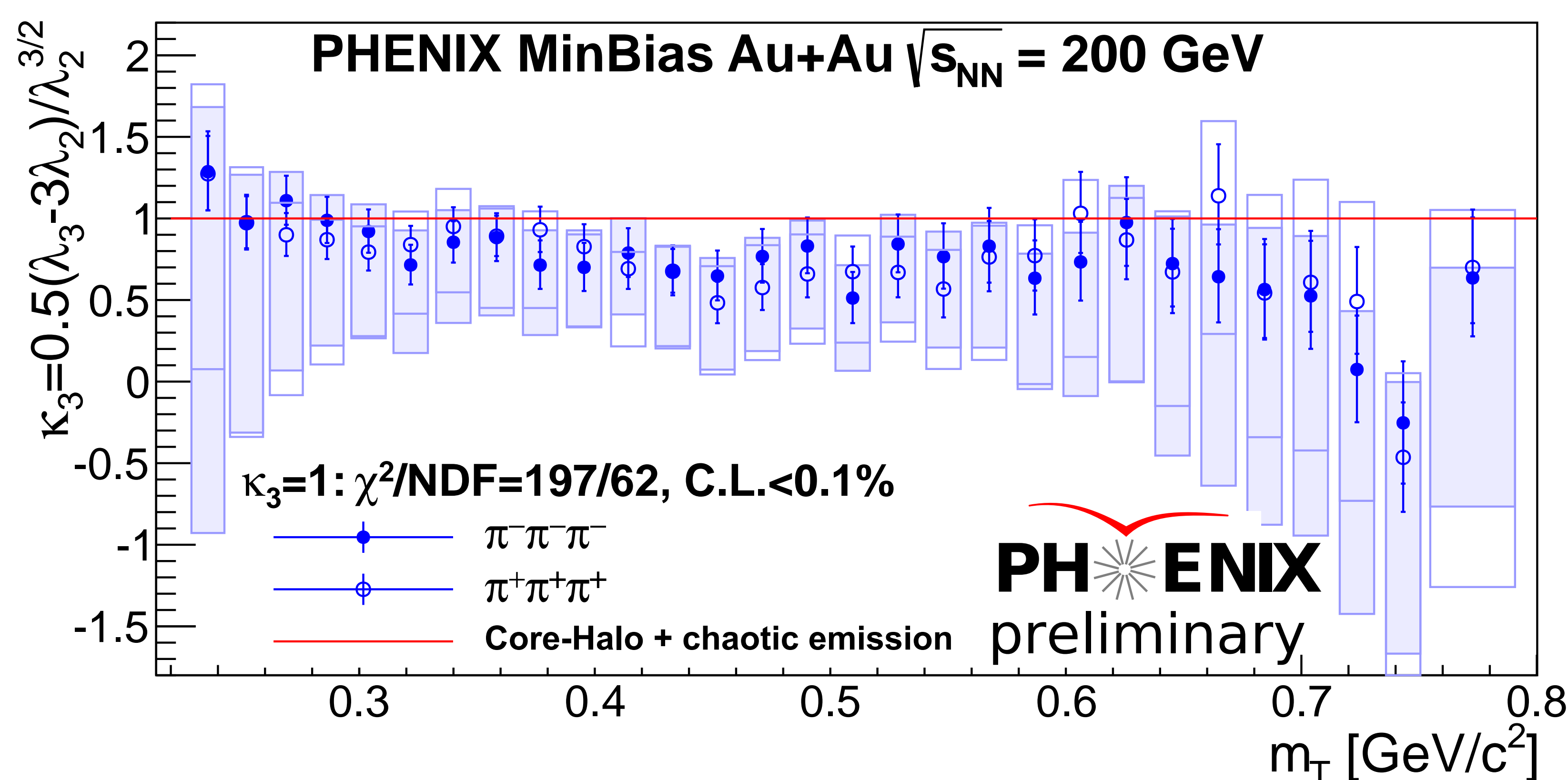
- Simple theoretical model [5]:  $\lambda_2(f_c, p_c), \lambda_3(f_c, p_c)$
- Measured  $\lambda_2^{\text{meas.}} \rightarrow \lambda_2^{\text{meas.}} = \lambda_2(f_c, p_c) \Rightarrow f_c(p_c)$  (green lines)
- Measured  $\lambda_3^{\text{meas.}} \rightarrow \lambda_3^{\text{meas.}} = \lambda_3(f_c, p_c) \Rightarrow f_c(p_c)$  (blue lines)
- Example 2D plot at  $m_T = 0.36 \text{ GeV}/c^2$ :



## Correlation strength $\lambda_3$ is within core-halo + chaotic emission range of $[0, 5]$ for all $m_T$



## Core-halo independent parameter $\kappa_3$ vs $m_T$ : $\kappa_3 \neq 1$ is statistically significant



## Summary

- 3 pion B-E correlations with Levy-source are shown
- Good agreement with data
- $\lambda_3$  within Core-Halo + chaotic emission limits (0-5)
- $\lambda_2, \lambda_3$  are consistent within  $1\sigma$  region on  $(f_c, p_c)$  plots
- Core-Halo + chaotic emission  $\kappa_3 = 1$
- Statistically significant deviation from  $\kappa_3 = 1$
- Statistically significant exclusion region: analyzed at  $m_T = 0.36 \text{ GeV}/c^2$ 
  - $f_c < 0.82$  can be excluded
  - $p_c > 0.5$  can be excluded
  - Small ( $p_c < 0.5$ ) partial coherence cannot be excluded
- Further  $m_T$  regions will be investigated
- $m_T$  dependent exclusion limits on  $f_c, p_c$  to be analyzed

## References

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- [2] J. Adams et al. (STAR Collaboration) Phys. Rev. Lett. 91 262301 (2003)
- [3] J. Bolz et al., Phys. Rev. D 47 (1993) 3860
- [4] T. Csörgő et al., Z. Phys. C 71 (1996) 491
- [5] T. Csörgő, Heavy Ion Physics 15 (2002) 1

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