

# Particle physics seminar

## Three particle Bose-Einstein correlation

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# HBT

- 1956. Robert Hanbury Brown and Richard Q. Twiss: A test of a new type of stellar interferometer on Sirius
- Two photomultiplier, different distances  $\Rightarrow$  correlation in two measured intensity distributions
- Measured correlation as function of detector distance  $\rightarrow$  radius of Sirius



# HBT in particle physics

- 1959. G. Goldhaber, S. Goldhaber, W.Y. Lee and A. Pais:  
proton-antiproton collisions at 1.05 GeV/c:
  - investigating  $\rho^0 \rightarrow \pi^+ \pi^-$  decay
  - unexpected correlation between  $\pi^+$  and  $\pi^+$ ,  $\pi^-$  and  $\pi^-$
  - 1960: reason pions are bosons
- Latter was found out correlations contain info about geometry of source

# HBT in particle physics

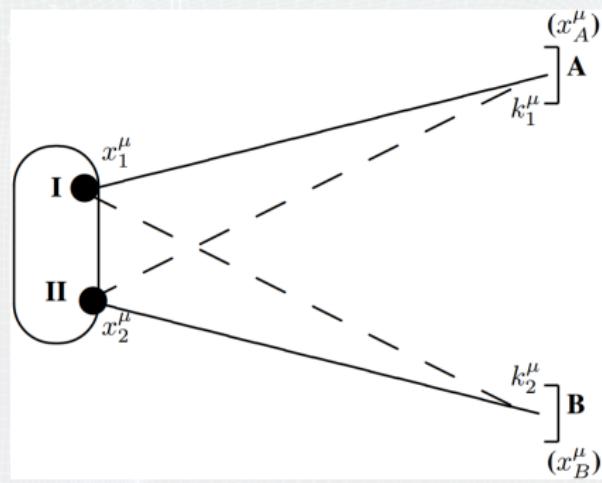
- Amplitude:

$$A(k_1, k_2) = \frac{1}{\sqrt{2}} \left( e^{-ik_1(x_A - x_1) + i\Phi_1} e^{-ik_2(x_B - x_2) + i\Phi_2} \right. \\ \left. \pm e^{-ik_1(x_A - x_2) + i\phi'_2} e^{-ik_2(x_B - x_1) + i\Phi'_1} \right)$$

- Probability of joint observation of the two particle with  $k_1, k_2$  momentum:

$$P_2(k_1, k_2) = \langle |A(k_1, k_2)|^2 \rangle \\ = 1 \pm \cos(k_1 - k_2)(x_1 - x_2)$$

- Chaotic emission: average over random phases  $\rightarrow \Phi_i$  not present



# HBT in particle physics

- Single particle amplitude:

$$A(k_i) = \frac{1}{\sqrt{2}} \left( e^{-ik_i(x_A - x_1) + i\Phi_1} \pm e^{-ik_i(x_A - x_2) + i\Phi_2} \right)$$

- One particle probability distribution:

$$P_1(k_i) = \langle |A(k_i)|^2 \rangle = 1$$

- Two particle correlation:

$$C_2(k_1, k_2) = \frac{P_2(k_1, k_2)}{P_1(k_1)P_1(k_2)} = 1 \pm \cos(k_1 - k_2)(x_1 - x_2)$$

# HBT in particle physics

- More generally, for extended sources ( $\rho(x)$  normalized space-time distribution):

$$P_2(k_1, k_2) = P_1(k_1)P_1(k_2) \int d^4x_1 d^4x_2 |A(k_1, k_2)|^2 \rho(x_1)\rho(x_2)$$
$$= P_1(k_1)P_1(k_2) [1 \pm |\tilde{\rho}(q)|^2]$$

- $q^\mu = k_1^\mu - k_2^\mu$  and

$$\tilde{\rho}(q) = \int d^4x e^{iq^\mu x_\mu} \rho(x)$$

- Correlation function:

$$C_2(k_1, k_2) = \frac{P_2(k_1, k_2)}{P_1(k_1)P_1(k_2)} = 1 \pm |\tilde{\rho}(q)|^2$$

- Correlation function  $\rightarrow$  Fourier transform  $\rightarrow$  Source function

# Three particle HBT

- Invariant momentum distributions:  $N_1(p_i)$ ,  $N_2(p_1, p_2)$ ,  $N_3(p_1, p_2, p_3)$
- The definition of the correlation function:

$$C_n(p_1, \dots, p_n) = \frac{N_n(p_1, \dots, p_n)}{N_1(p_1) \cdots N_1(p_n)}$$

for chaotic emission:

$$N_n(p_1, \dots, p_n) = \int \prod_{i=1}^n \mathcal{S}(x_i, p_i) |\Psi_n(\{x_i\})|^2 d^4x_1 \dots d^4x_n$$

- $\mathcal{S}(x, p)$  source function (usually assumed to be Gaussian - Levy is more general)

# Core-Halo

- Not all particles comes from QGP freeze out
- they also can come from decays
- Both part contribute to source function:

$$\mathcal{S} = \mathcal{S}_{\text{core}} + \mathcal{S}_{\text{halo}}$$

- Particle distribution:

$$N_n(p_1, \dots, p_n) = N_n^c(p_1, \dots, p_n) + N_n^h(p_1, \dots, p_n)$$

- Two particle correlation:

$$C_2(k_1, k_2) = 1 + \lambda_2 |\mathcal{S}(q)|^2$$

where

$$\sqrt{\lambda_2} = f_C \equiv \frac{N^c}{N^c + N^h}$$

# Coherence

- If the core partially emits particles in coherent manner:

$$\mathcal{S}_{\text{core}} = \mathcal{S}_{\text{core}}^{\text{pc}} + \mathcal{S}_{\text{core}}^i$$

where pc refers to partially coherent, i to incoherent

- Particle distribution:

$$N_n^c(p_1, \dots, p_n) = N_n^{c,\text{pc}}(p_1, \dots, p_n) + N_n^{c,i}(p_1, \dots, p_n)$$

- Two particle correlation:  $C_2(k_1, k_2) = 1 + \lambda_2 |\mathcal{S}(q)|^2$ , but  $\lambda_2 \neq f_C^2$
- Fraction of coherently produced pions:

$$p_C \equiv \frac{N_{\text{coherent}}}{N_{\text{coherent}} + N_{\text{incoherent}}} \rightarrow \lambda_2(f_C, p_C)$$

- Can this happen? Yes, e.g. due to formation of pion laser or Bose-Einstein condensate of pions

# Motivation behind three particle HBT analysis

- Reminder:  $C_2(k) = 1 + \lambda_2 |\mathcal{S}(q)|^2$
- Two particle correlation strength:  $\lambda_2 \equiv C_2(q=0) - 1$
- Similar definition of three particle correlation strength:  
 $\lambda_3 \equiv C_3(0) - 1$
- Core-Halo:  
$$\lambda_2 = f_C^2, \quad \lambda_3 = 2f_C^3 + 3f_C^2$$
$$\kappa_3 = (\lambda_3 - 3\lambda_2) / (2\sqrt{\lambda_2^3}) = 1$$
- Partial coherence ( $p_C$  fraction of coherently produced  $\pi$ ):  
$$\lambda_2 = f_C^2 [(1 - p_C)^2 + 2p_C(1 - p_C)]$$
$$\lambda_3 = 2f_C^3 [(1 - p_C)^3 + 3p_C(1 - p_C)^2] + 3f_C^2 [(1 - p_C)^2 + 2p_C(1 - p_C)]$$
$$\kappa_3 = \kappa_3(p_C)$$
- From  $\lambda_2, \lambda_3$  we can investigate the deviation from simple Core-Halo

# Dimension

- Definition of correlation function:

$$C_3(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) = \frac{N_3(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3)}{N_1(\mathbf{k}_1)N_1(\mathbf{k}_2)N_1(\mathbf{k}_3)} \quad (9D) \quad (1)$$

- Transverse momentum:

$$p_T = |\mathbf{p}_{T1} + \mathbf{p}_{T2} + \mathbf{p}_{T3}|/3 \quad (2)$$

- Momentum differences:  $\mathbf{k}_{ij} = \mathbf{k}_i - \mathbf{k}_j$
- So we want to measure  $C_3(\mathbf{k}_{12}, \mathbf{k}_{13}, \mathbf{k}_{23})$  for different  $p_T$  bins (6D)

# Correlation function

- We use side-out-longitudinal decomposition:
  - long direction: beam direction
  - out direction: direction of average transverse momentum
  - side: orthogonal to long and out
- Coordinate system: LCMS (longitudinal co-moving system) of the triplet: Lorentz boost in long direction
- Instead of  $\mathbf{k}_{ij}^{\text{LCMS}}$  we measure correlation as function of

$$k_{ij} = |\mathbf{k}_{ij}^{\text{LCMS3}}| \quad (3D)$$

- Reason: not enough statistics

## Details of measurement

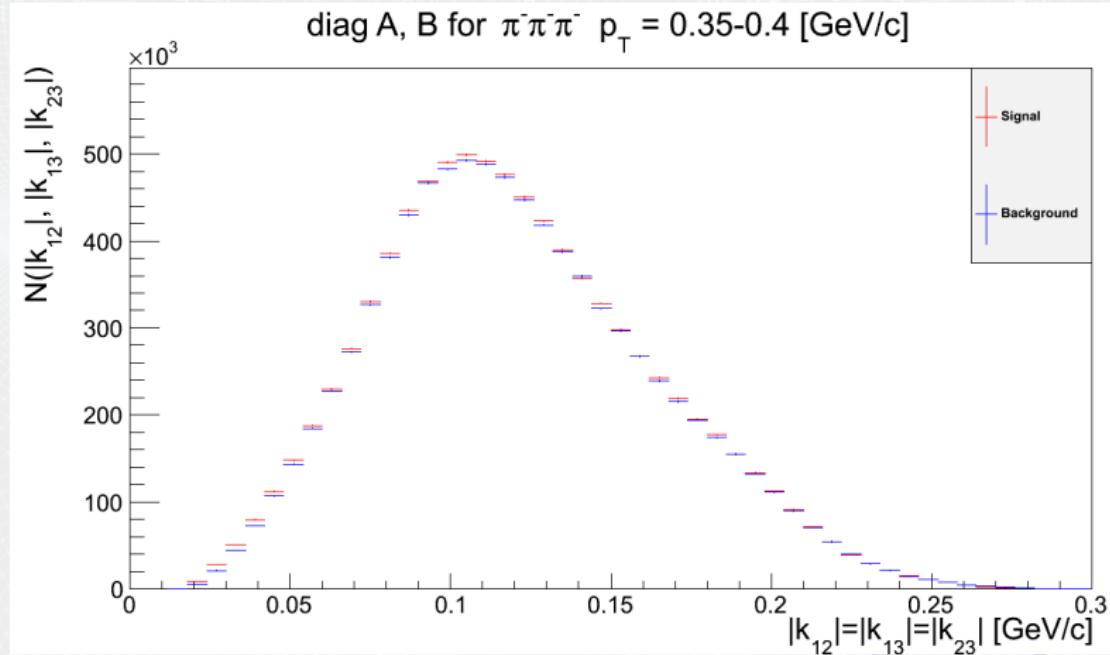
- BNL RHIC, PHENIX experiment, 200GeV Au+Au collision
- Event-mixing method to measure correlation
- Momentum difference distributions of pion pairs within the triplet from same event:  $A(k_{12}, k_{13}, k_{23})$
- Background distribution (triplets from different events):  
 $B(k_{12}, k_{13}, k_{23})$
- MinBias: no centrality filtering
- Lot of cuts (single track, matching cuts, pair cuts)

# Details of measurement

- Low bin behavior:

$$k_{ij} \rightarrow 0 \xrightarrow{?} A, B \rightarrow 0$$

(3)

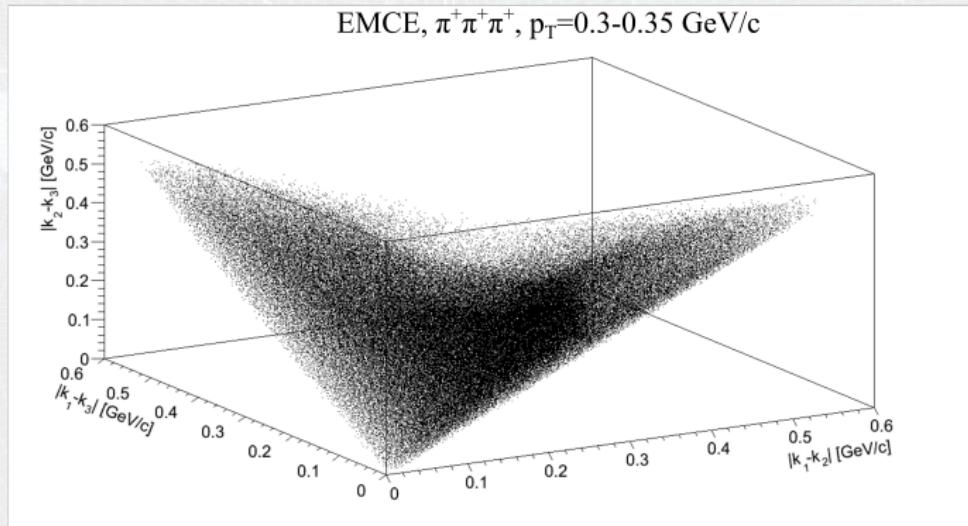


# Details of measurement

- The correlation:

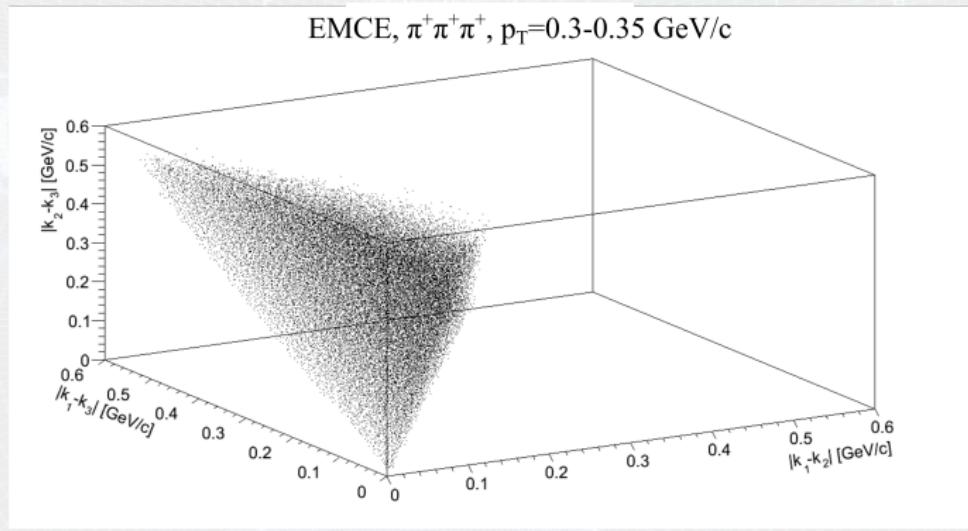
$$C_3(k_{12}, k_{13}, k_{23}) = \frac{A(k_{12}, k_{13}, k_{23})}{B(k_{12}, k_{13}, k_{23})} \frac{\int B}{\int A} \quad (4)$$

- Triangle inequality for  $\vec{k}_{12}$ ,  $\vec{k}_{13}$ ,  $\vec{k}_{23}$



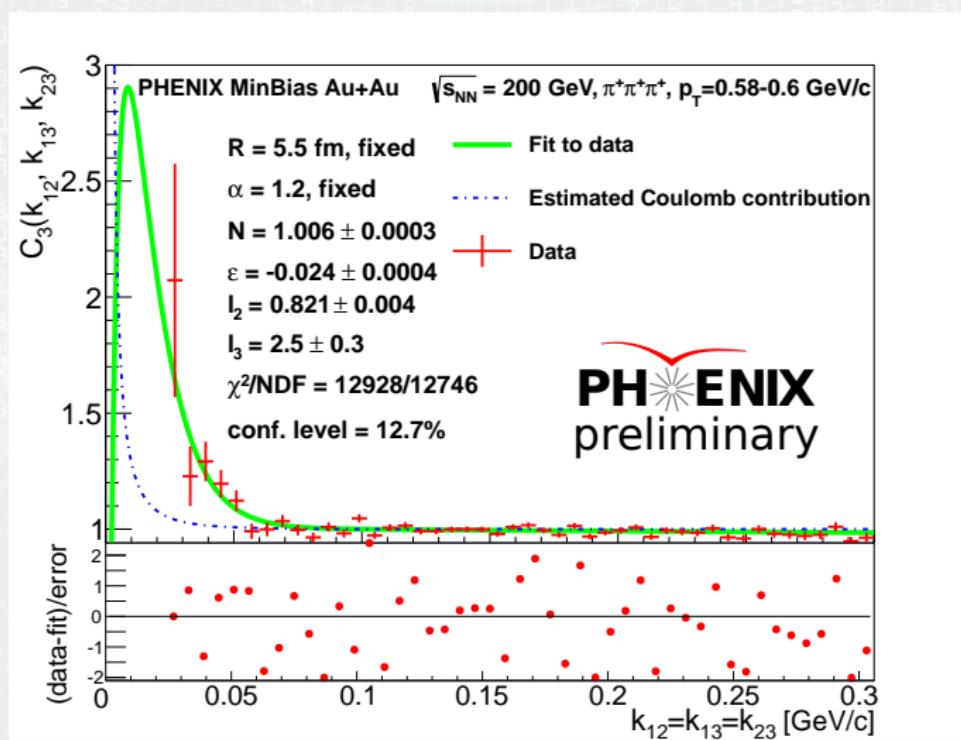
# Details of measurement

- Order within triplet doesn't matter
- But when we measure do matter  $\Rightarrow$  we have to fold the histogram  
$$A(5, 6, 7) + = A(6, 7, 5) + A(7, 5, 6) + A(5, 7, 6)$$
$$+ A(7, 6, 5) + A(6, 5, 7)$$



# Details of measurement

## ■ Diagonal correlation function



# Model without Coulomb correction

- Assumption for source: Levy-distribution

$$\mathcal{L}(\alpha, R, r) = (2\pi)^{-3} \int d^3 q e^{iqr} e^{-\frac{1}{2}|qR|^\alpha}$$

- Approximation for  $C_3$  can be derived ( $\mathcal{L}_3 = 2f_C^3$ ):

$$C_3^{(0)}(k_{12}, k_{13}, k_{23}) = 1 + \ell_3 e^{-0.5(|2k_{12}R_C|^\alpha + |2k_{13}R_C|^\alpha + |2k_{23}R_C|^\alpha)} \\ + \ell_2 \left( e^{|2k_{12}R_C|^\alpha} + e^{|2k_{13}R_C|^\alpha} + e^{|2k_{23}R_C|^\alpha} \right)$$

- Background:  $N(1 + \epsilon k_{12})(1 + \epsilon k_{13})(1 + \epsilon k_{23})$
- Fit parameters:  $\ell_3, \ell_2, R_C, \alpha, N, \epsilon$
- We are looking for:  $\lambda_3 \equiv C_3(k_{12} = k_{13} = k_{23} = 0) - 1 = \ell_3 + 3\ell_2$
- In an other analysis  $\lambda_2$  was measured

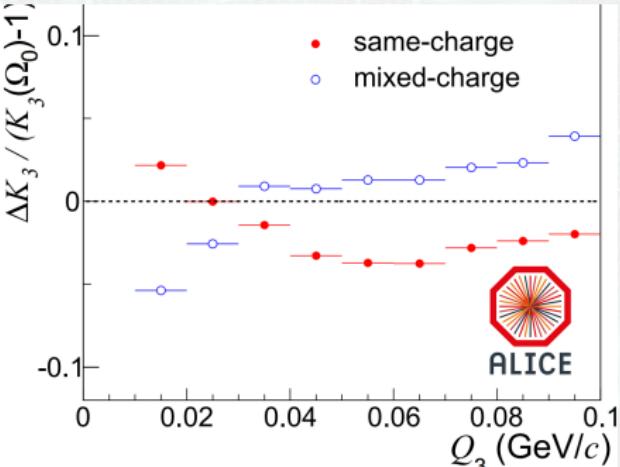
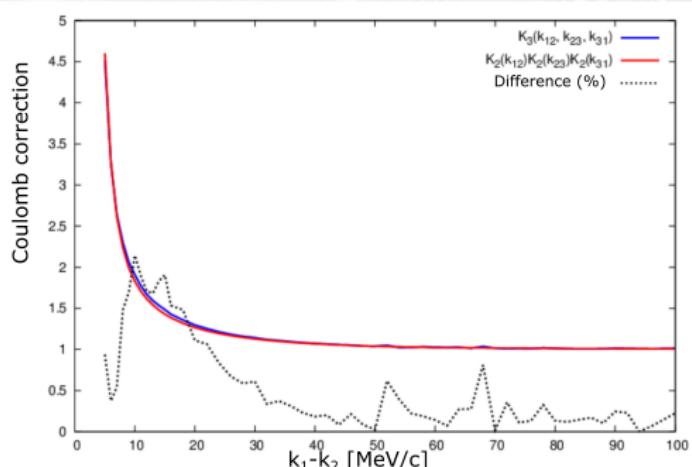
# Coulomb correction

- Corrected model:

$$C_3(k_{12}, k_{13}, k_{23}) = C_3^{(0)}(k_{12}, k_{13}, k_{23}) \cdot K_3(k_{12}, k_{13}, k_{23})$$

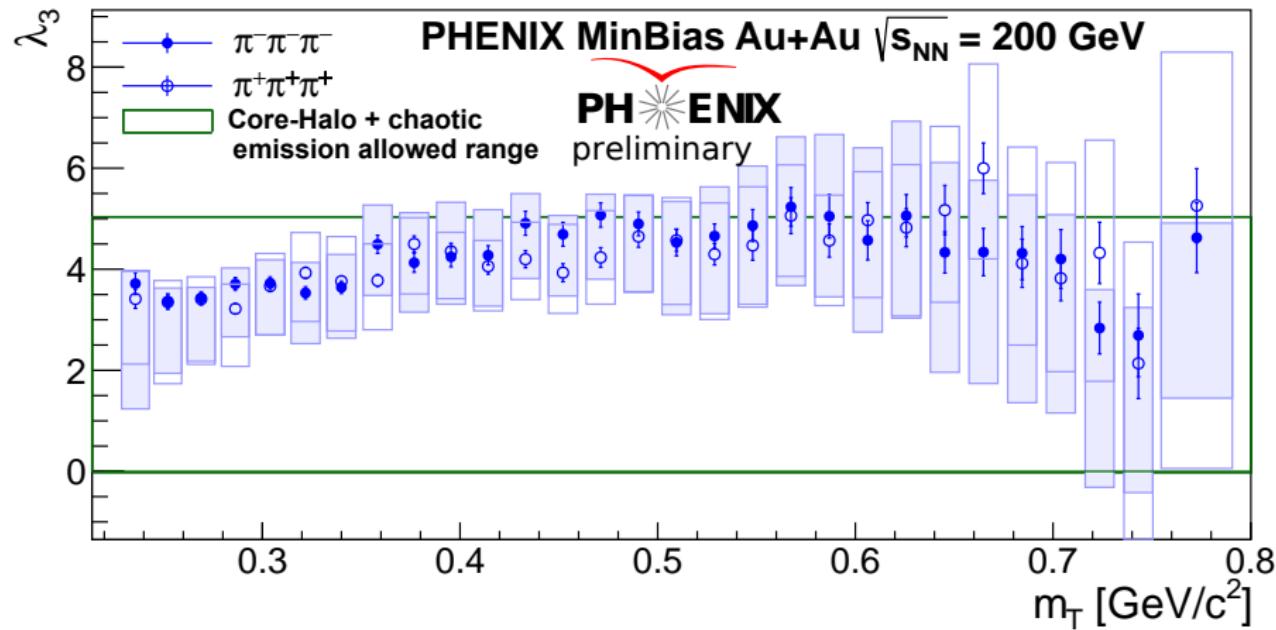
- "Generalized Riverside" method for 3 particle Coulomb problem

$$K_3(k_{12}, k_{13}, k_{23}) \approx K_1(k_{12})K_1(k_{13})K_1(k_{23})$$



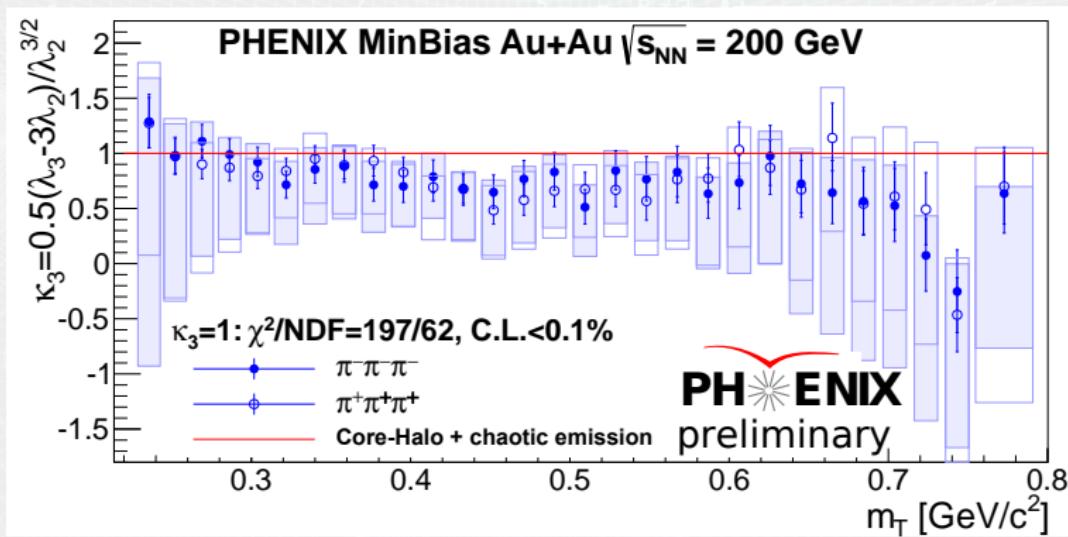
# Three particle correlation strength: $\lambda_3$

- $\lambda_3$  within Core-Halo + chaotic emission range for all  $m_T$



# Core-Halo independent parameter

- $\kappa_3 \equiv \frac{\lambda_3 - 3\lambda_2}{2\sqrt{\lambda_2^3}}$  not depend on  $f_C$  ( $f_C = \text{core}/(\text{core} + \text{halo})$ )
- Core-Halo + chaotic emission:  $\kappa_3 = 1$
- additional effect (eg. not fully thermal):  $\kappa_3 \neq 1$
- Statistically significant deviation from  $\kappa_3 = 1$



# Partial coherence ( $p_c$ ) vs fractional core

- Simple theoretical model:  $\lambda_2(f_c, p_c), \lambda_3(f_c, p_c)$
- Measured  $\lambda_2^{\text{meas.}} \rightarrow \lambda_2^{\text{meas.}} = \lambda_2(f_c, p_c) \Rightarrow f_c(p_c)$  (green lines)
- Measured  $\lambda_3^{\text{meas.}} \rightarrow \lambda_3^{\text{meas.}} = \lambda_3(f_c, p_c) \Rightarrow f_c(p_c)$  (blue lines)
- $f_c < 0.82$  and  $p_c > 0.5$  can be excluded,  $p_c < 0.5$  can't be excluded

