

Probability & Statistics Formulas



Mean.	variance	and	standard	deviation
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	Population	Sample
# of subjects	N	n
Mean	$\mu = \frac{\sum_{i=1}^{N} x_i}{N}$	$\bar{x} = \frac{\sum_{i=1}^{n} x_i}{n}$
Variance	$\sigma^2 = \frac{\sum_{i=1}^{N} (x_i - \mu)^2}{N}$	$S^{2} = \frac{\sum_{i=1}^{n} (x_{i} - \bar{x})^{2}}{n-1}$

Note: S^2 is the formula for unbiased sample variance, since we're dividing by n-1.

Standard deviation
$$\sigma = \sqrt{\frac{\sum_{i=1}^{N} (x_i - \mu)^2}{N}} \qquad S = \sqrt{\frac{\sum_{i=1}^{n} (x_i - \bar{x})^2}{n-1}}$$

Note: Finding S by taking $\sqrt{S^2}$ reintroduces bias.

Five-number summary

Min	Q1	Median	Q3	Max

Outliers

Low outliers: anything less than $Q_1 - 1.5(IQR)$

High outliers: anything greater than $Q_3 + 1.5(IQR)$

Empirical rule

For normal distributions, there's a

- ullet 68% chance a data point falls within 1 standard deviation of the mean
- ullet 95% chance a data point falls within 2 standard deviations of the mean
- \bullet $99.7\,\%$ chance a data point falls within 3 standard deviations of the mean

Z-score

$$z = \frac{x - \mu}{\sigma}$$



z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
-3.4	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0002
-3.3	.0005	.0005	.0005	.0004	.0004	.0004	.0004	.0004	.0004	.0003
-3.2	.0007	.0007	.0006	.0006	.0006	.0006	.0006	.0005	.0005	.0005
-3.1	.0010	.0009	.0009	.0009	.0008	.0008	.0008	.0008	.0007	.0007
-3.0	.0013	.0013	.0013	.0012	.0012	.0011	.0011	.0011	.0010	.0010
-2.9	.0019	.0018	.0018	.0017	.0016	.0016	.0015	.0015	.0014	.0014
-2.8	.0026	.0025	.0024	.0023	.0023	.0022	.0021	.0021	.0020	.0019
-2.7	.0035	.0034	.0033	.0032	.0031	.0030	.0029	.0028	.0027	.0026
-2.6	.0047	.0045	.0044	.0043	.0041	.0040	.0039	.0038	.0037	.0036
-2.5	.0062	.0060	.0059	.0057	.0055	.0054	.0052	.0051	.0049	.0048
-2.4	.0082	.0080	.0078	.0075	.0073	.0071	.0069	.0068	.0066	.0064
-2.3	.0107	.0104	.0102	.0099	.0096	.0094	.0091	.0089	.0087	.0084
-2.2	.0139	.0136	.0132	.0129	.0125	.0122	.0119	.0116	.0113	.0110
-2.1	.0179	.0174	.0170	.0166	.0162	.0158	.0154	.0150	.0146	.0143
-2.0	.0228	.0222	.0217	.0212	.0207	.0202	.0197	.0192	.0188	.0183
-1.9	.0287	.0281	.0274	.0268	.0262	.0256	.0250	.0244	.0239	.0233
-1.8	.0359	.0351	.0344	.0336	.0329	.0322	.0314	.0307	.0301	.0294
-1.7	.0446	.0436	.0427	.0418	.0409	.0401	.0392	.0384	.0375	.0367
-1.6	.0548	.0537	.0526	.0516	.0505	.0495	.0485	.0475	.0465	.0455
-1.5	.0668	.0655	.0643	.0630	.0618	.0606	.0594	.0582	.0571	.0559
-1.4	.0808	.0793	.0778	.0764	.0749	.0735	.0721	.0708	.0694	.0681
-1.3	.0968	.0951	.0934	.0918	.0901	.0885	.0869	.0853	.0838	.0823
-1.2	.1151	.1131	.1112	.1093	.1075	.1056	.1038	.1020	.1003	.0985
-1.1	.1357	.1335	.1314	.1292	.1271	.1251	.1230	.1210	.1190	.1170
-1.0	.1587	.1562	.1539	.1515	.1492	.1469	.1446	.1423	.1401	.1379
-0.9	.1841	.1814	.1788	.1762	.1736	.1711	.1685	.1660	.1635	.1611
-0.8	.2119	.2090	.2061	.2033	.2005	.1977	.1949	.1922	.1894	.1867
-0.7	.2420	.2389	.2358	.2327	.2296	.2266	.2236	.2206	.2177	.2148
-0.6	.2743	.2709	.2676	.2643	.2611	.2578	.2546	.2514	.2483	.2451
-0.5	.3085	.3050	.3015	.2981	.2946	.2912	.2877	.2843	.2810	.2776
-0.4	.3446	.3409	.3372	.3336	.3300	.3264	.3228	.3192	.3156	.3121
-0.3	.3821	.3783	.3745	.3707	.3669	.3632	.3594	.3557	.3520	.3483
-0.2	.4207	.4168	.4129	.4090	.4052	.4013	.3974	.3936	.3897	.3859
-0.1	.4602	.4562	.4522	.4483	.4443	.4404	.4364	.4325	.4286	.4247
0.0	.5000	.4960	.4920	.4880	.4840	.4801	.4761	.4721	.4681	.4641



z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359
0.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753
0.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141
0.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517
0.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879
0.5	.6915	.6950	.6985	.7019	.7054	.7088	.7123	.7157	.7190	.7224
0.6	.7257	.7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549
0.7	.7580	.7611	.7642	.7673	.7704	.7734	.7764	.7794	.7823	.7852
0.8	.7881	.7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133
0.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.8790	.8810	.8830
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9279	.9292	.9306	.9319
1.5	.9332	.9345	.9357	.9370	.9382	.9394	.9406	.9418	.9429	.9441
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9686	.9693	.9699	.9706
1.9	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	.9761	.9767
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9916
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936
2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	.9951	.9952
2.6	.9953	.9955	.9956	.9957	.9959	.9960	.9961	.9962	.9963	.9964
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	.9973	.9974
2.8	.9974	.9975	.9976	.9977	.9977	.9978	.9979	.9979	.9980	.9981
2.9	.9981	.9982	.9982	.9983	.9984	.9984	.9985	.9985	.9986	.9986
3.0	.9987	.9987	.9987	.9988	.9988	.9989	.9989	.9989	.9990	.9990
3.1	.9990	.9991	.9991	.9991	.9992	.9992	.9992	.9992	.9993	.9993
3.2	.9993	.9993	.9994	.9994	.9994	.9994	.9994	.9995	.9995	.9995
3.3	.9995	.9995	.9995	.9996	.9996	.9996	.9996	.9996	.9996	.9997
3.4	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9998



Regression line

$$m = \frac{n(\sum xy) - (\sum x)(\sum y)}{n(\sum x^2) - (\sum x)^2}$$

$$b = \frac{(\sum y) - m(\sum x)}{n}$$

Correlation coefficient

$$r = \frac{1}{n-1} \sum \left(\frac{x_i - \bar{x}}{s_x} \right) \left(\frac{y_i - \bar{y}}{s_y} \right)$$

$$r = \frac{1}{n-1} \sum_{i} \left(z_{x_i} \right) \left(z_{y_i} \right)$$

Residual

residual = actual - predicted

Probability of an event

 $P(\text{event}) = \frac{\text{outcomes that meet our criteria}}{\text{all possible outcomes}}$



Addition rule

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

Multiplication rule

For independent events: $P(A \text{ and } B) = P(A) \cdot P(B)$

For dependent events: $P(A \text{ and } B) = P(A) \cdot P(B|A)$

Bayes' theorem

$$P(A \mid B) = \frac{P(B \mid A) \cdot P(A)}{P(B)}$$

Combination of two random variables

Sum: S = A + B

Difference: D = A - B

Mean of the sum: $\mu_S = \mu_A + \mu_B$

Mean of the difference: $\mu_D = \mu_A - \mu_B$

Variance of the sum or difference: $\sigma^2 = \sigma_A^2 + \sigma_B^2$

Standard deviation of the sum or difference: $\sigma = \sqrt{\sigma_A^2 + \sigma_B^2}$

Permutations

$$_{n}P_{k} = \frac{n!}{(n-k)!}$$

Combinations

$$_{n}C_{k} = \binom{n}{k} = \frac{n!}{k!(n-k)!}$$

Binomial probability

$$P(k \text{ successes in } n \text{ attempts}) = \binom{n}{k} p^k (1-p)^{n-k}$$

At least one success or failure

P(at least 1 success) = 1 - P(all failures)

P(at least 1 failure) = 1 - P(all successes)

Binomial mean, variance and standard deviation

Mean: $\mu_X = E(X) = np$

Variance: $\sigma_X^2 = np(1-p)$

Standard deviation: $\sigma_X = \sqrt{np(1-p)}$

Bernoulli random variables

Mean: $\mu = (percentage of failures)(0) + (percentage of successes)(1)$

Variance: $\sigma^2 = p(1-p)$

Standard deviation: $\sigma = \sqrt{p(1-p)}$

Geometric random variables

Success on the *n*th attempt: $P(S = n) = p(1 - p)^{n-1}$

Mean: $\mu_X = E(X) = \frac{1}{p}$

Normal condition for samples

$$np \ge 10$$

$$n(1-p) \geq 10$$

Sample distributions

Mean: $\mu_{\hat{p}} = p$

Standard deviation: $\sigma_{\hat{p}} = \sqrt{\frac{p(1-p)}{n}}$

Sampling distribution of the sample mean

Mean: $\mu_{\bar{x}} = \mu$

Variance: $\sigma_{\bar{x}}^2 = \frac{\sigma^2}{n}$

Standard deviation: $\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$

Sample mean

$$\mu_{\hat{p}} = n\hat{p}$$

Standard error

$$SE_{\hat{p}} = \sigma_{\hat{p}} = \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

Confidence interval

$$\hat{p} \pm z * SE_{\hat{p}}$$



$$\hat{p} \pm z^* \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

Margin of error

$$z^*\sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$



t-table

1 1.000 1.376 1.963 3.078 6.314 12.71 31.82 63.66 318.31 636.6 2 0.816 1.061 1.386 1.886 2.920 4.303 6.965 9.925 22.327 31.59 3 0.765 0.987 1.250 1.638 2.353 3.182 4.541 5.841 10.215 12.92 4 0.741 0.941 1.190 1.533 2.132 2.776 3.747 4.604 7.173 8.616 5 0.727 0.920 1.156 1.476 2.015 2.571 3.365 4.032 5.893 6.866 6 0.718 0.906 1.134 1.440 1.943 2.447 3.143 3.707 5.208 5.956 7 0.711 0.896 1.119 1.415 1.895 2.365 2.998 3.499 4.785 5.406 8 0.706 0.883 1.100 1.383 1.260 2.365		Upper-tail probability p										
2 0.816 1.061 1.386 1.886 2.920 4.303 6.965 9.925 22.327 31.59 3 0.765 0.987 1.250 1.638 2.353 3.182 4.541 5.841 10.215 12.92 4 0.741 0.941 1.190 1.533 2.132 2.776 3.747 4.604 7.173 8.610 5 0.727 0.920 1.156 1.476 2.015 2.571 3.365 4.032 5.893 6.866 6 0.718 0.906 1.134 1.440 1.943 2.447 3.143 3.707 5.208 5.956 7 0.711 0.896 1.119 1.415 1.895 2.365 2.998 3.499 4.785 5.401 8 0.706 0.889 1.108 1.397 1.860 2.306 2.896 3.355 4.501 5.04 9 0.703 0.863 1.093 1.372 1.812 2.228	df	0.25	0.20	0.15	0.10	0.05	0.025	0.01	0.005	0.001	0.0005	
3 0.765 0.987 1.250 1.638 2.353 3.182 4.541 5.841 10.215 12.92 4 0.741 0.941 1.190 1.533 2.132 2.776 3.747 4.604 7.173 8.610 5 0.727 0.920 1.156 1.476 2.015 2.571 3.365 4.032 5.893 6.866 6 0.718 0.906 1.134 1.440 1.943 2.447 3.143 3.707 5.208 5.956 7 0.711 0.896 1.119 1.415 1.895 2.365 2.998 3.499 4.785 5.401 8 0.706 0.889 1.108 1.397 1.860 2.306 2.896 3.355 4.501 5.04 9 0.703 0.883 1.100 1.383 1.833 2.262 2.821 3.250 4.297 4.78* 10 0.700 0.879 1.093 1.372 1.812 2.228	1	1.000	1.376	1.963	3.078	6.314	12.71	31.82	63.66	318.31	636.62	
4 0.741 0.941 1.190 1.533 2.132 2.776 3.747 4.604 7.173 8.616 5 0.727 0.920 1.156 1.476 2.015 2.571 3.365 4.032 5.893 6.866 6 0.718 0.906 1.134 1.440 1.943 2.447 3.143 3.707 5.208 5.956 7 0.711 0.986 1.119 1.415 1.895 2.365 2.998 3.499 4.785 5.406 8 0.706 0.889 1.108 1.397 1.860 2.306 2.896 3.355 4.501 5.04 9 0.703 0.883 1.100 1.383 1.833 2.262 2.821 3.250 4.297 4.78 10 0.700 0.879 1.093 1.372 1.812 2.228 2.764 3.169 4.144 4.581 11 0.697 0.876 1.088 1.363 1.796 2.201	2	0.816	1.061	1.386	1.886	2.920	4.303	6.965	9.925	22.327	31.599	
5 0.727 0.920 1.156 1.476 2.015 2.571 3.365 4.032 5.893 6.868 6 0.718 0.906 1.134 1.440 1.943 2.447 3.143 3.707 5.208 5.956 7 0.711 0.896 1.119 1.415 1.895 2.365 2.998 3.499 4.785 5.406 8 0.706 0.889 1.108 1.397 1.860 2.306 2.896 3.355 4.501 5.04* 9 0.703 0.883 1.100 1.383 1.833 2.262 2.821 3.250 4.297 4.78* 10 0.700 0.879 1.093 1.372 1.812 2.228 2.764 3.169 4.144 4.58* 11 0.697 0.876 1.088 1.363 1.796 2.201 2.718 3.106 4.025 4.43* 12 0.695 0.873 1.083 1.356 1.771 2.160	3	0.765	0.987	1.250	1.638	2.353	3.182	4.541	5.841	10.215	12.924	
6 0.718 0.906 1.134 1.440 1.943 2.447 3.143 3.707 5.208 5.956 7 0.711 0.896 1.119 1.415 1.895 2.365 2.998 3.499 4.785 5.408 8 0.706 0.889 1.108 1.397 1.860 2.306 2.896 3.355 4.501 5.04* 9 0.703 0.883 1.100 1.383 1.833 2.262 2.821 3.250 4.297 4.78* 10 0.700 0.879 1.093 1.372 1.812 2.228 2.764 3.169 4.144 4.580 11 0.697 0.876 1.088 1.363 1.796 2.201 2.718 3.106 4.025 4.433 12 0.695 0.873 1.083 1.350 1.771 2.160 2.650 3.012 3.852 4.22* 14 0.692 0.868 1.076 1.345 1.761 2.145 <th>4</th> <th>0.741</th> <th>0.941</th> <th>1.190</th> <th>1.533</th> <th>2.132</th> <th>2.776</th> <th>3.747</th> <th>4.604</th> <th>7.173</th> <th>8.610</th>	4	0.741	0.941	1.190	1.533	2.132	2.776	3.747	4.604	7.173	8.610	
7 0.711 0.896 1.119 1.415 1.895 2.365 2.998 3.499 4.785 5.406 8 0.706 0.889 1.108 1.397 1.860 2.306 2.896 3.355 4.501 5.04 9 0.703 0.883 1.100 1.383 1.833 2.262 2.821 3.250 4.297 4.78 10 0.700 0.879 1.093 1.372 1.812 2.228 2.764 3.169 4.144 4.587 11 0.697 0.876 1.088 1.363 1.796 2.201 2.718 3.106 4.025 4.433 12 0.695 0.873 1.083 1.356 1.782 2.179 2.681 3.055 3.930 4.318 13 0.694 0.870 1.079 1.350 1.771 2.160 2.650 3.012 3.852 4.22 14 0.692 0.868 1.074 1.341 1.753 2.131	5	0.727	0.920	1.156	1.476	2.015	2.571	3.365	4.032	5.893	6.869	
8 0.706 0.889 1.108 1.397 1.860 2.306 2.896 3.355 4.501 5.04 9 0.703 0.883 1.100 1.383 1.833 2.262 2.821 3.250 4.297 4.78 10 0.700 0.879 1.093 1.372 1.812 2.228 2.764 3.169 4.144 4.587 11 0.697 0.876 1.088 1.363 1.796 2.201 2.718 3.106 4.025 4.437 12 0.695 0.873 1.083 1.356 1.782 2.179 2.681 3.055 3.930 4.318 13 0.694 0.870 1.079 1.350 1.771 2.160 2.650 3.012 3.852 4.22* 14 0.692 0.868 1.076 1.345 1.761 2.145 2.624 2.977 3.787 4.140 15 0.691 0.866 1.074 1.341 1.753 2.131 <th>6</th> <th>0.718</th> <th>0.906</th> <th>1.134</th> <th>1.440</th> <th>1.943</th> <th>2.447</th> <th>3.143</th> <th>3.707</th> <th>5.208</th> <th>5.959</th>	6	0.718	0.906	1.134	1.440	1.943	2.447	3.143	3.707	5.208	5.959	
9 0.703 0.883 1.100 1.383 1.833 2.262 2.821 3.250 4.297 4.783 10 0.700 0.879 1.093 1.372 1.812 2.228 2.764 3.169 4.144 4.583 11 0.697 0.876 1.088 1.363 1.796 2.201 2.718 3.106 4.025 4.431 12 0.695 0.873 1.083 1.356 1.782 2.179 2.681 3.055 3.930 4.318 13 0.694 0.870 1.079 1.350 1.771 2.160 2.650 3.012 3.852 4.227 14 0.692 0.868 1.076 1.345 1.761 2.145 2.624 2.977 3.787 4.144 15 0.691 0.866 1.074 1.341 1.753 2.131 2.602 2.947 3.733 4.073 16 0.690 0.865 1.071 1.337 1.746 2.120<	7	0.711	0.896	1.119	1.415	1.895	2.365	2.998	3.499	4.785	5.408	
10 0.700 0.879 1.093 1.372 1.812 2.228 2.764 3.169 4.144 4.587 11 0.697 0.876 1.088 1.363 1.796 2.201 2.718 3.106 4.025 4.431 12 0.695 0.873 1.083 1.356 1.782 2.179 2.681 3.055 3.930 4.318 13 0.694 0.870 1.079 1.350 1.771 2.160 2.650 3.012 3.852 4.22* 14 0.692 0.868 1.076 1.345 1.761 2.145 2.624 2.977 3.787 4.140 15 0.691 0.866 1.074 1.341 1.753 2.131 2.602 2.947 3.733 4.073 16 0.690 0.865 1.071 1.337 1.746 2.120 2.583 2.921 3.686 4.015 17 0.688 0.862 1.067 1.330 1.734 2.101	8	0.706	0.889	1.108	1.397	1.860	2.306	2.896	3.355	4.501	5.041	
11 0.697 0.876 1.088 1.363 1.796 2.201 2.718 3.106 4.025 4.437 12 0.695 0.873 1.083 1.356 1.782 2.179 2.681 3.055 3.930 4.318 13 0.694 0.870 1.079 1.350 1.771 2.160 2.650 3.012 3.852 4.22 14 0.692 0.868 1.076 1.345 1.761 2.145 2.624 2.977 3.787 4.140 15 0.691 0.866 1.074 1.341 1.753 2.131 2.602 2.947 3.733 4.073 16 0.690 0.865 1.071 1.337 1.746 2.120 2.583 2.921 3.686 4.015 17 0.689 0.863 1.069 1.333 1.740 2.110 2.567 2.898 3.646 3.968 18 0.688 0.861 1.066 1.328 1.729 2.093<	9	0.703	0.883	1.100	1.383	1.833	2.262	2.821	3.250	4.297	4.781	
12 0.695 0.873 1.083 1.356 1.782 2.179 2.681 3.055 3.930 4.318 13 0.694 0.870 1.079 1.350 1.771 2.160 2.650 3.012 3.852 4.22 14 0.692 0.868 1.076 1.345 1.761 2.145 2.624 2.977 3.787 4.144 15 0.691 0.866 1.074 1.341 1.753 2.131 2.602 2.947 3.733 4.073 16 0.690 0.865 1.071 1.337 1.746 2.120 2.583 2.921 3.686 4.015 17 0.689 0.863 1.069 1.333 1.740 2.110 2.567 2.898 3.646 3.961 18 0.688 0.862 1.067 1.330 1.734 2.101 2.552 2.878 3.610 3.922 19 0.688 0.861 1.066 1.328 1.729 2.093<	10	0.700	0.879	1.093	1.372	1.812	2.228	2.764	3.169	4.144	4.587	
13 0.694 0.870 1.079 1.350 1.771 2.160 2.650 3.012 3.852 4.22 14 0.692 0.868 1.076 1.345 1.761 2.145 2.624 2.977 3.787 4.140 15 0.691 0.866 1.074 1.341 1.753 2.131 2.602 2.947 3.733 4.073 16 0.690 0.865 1.071 1.337 1.746 2.120 2.583 2.921 3.686 4.015 17 0.689 0.863 1.069 1.333 1.740 2.110 2.567 2.898 3.646 3.968 18 0.688 0.862 1.067 1.330 1.734 2.101 2.552 2.878 3.610 3.922 19 0.688 0.861 1.066 1.328 1.729 2.093 2.539 2.861 3.579 3.863 20 0.687 0.860 1.064 1.323 1.725 2.086<	11	0.697	0.876	1.088	1.363	1.796	2.201	2.718	3.106	4.025	4.437	
14 0.692 0.868 1.076 1.345 1.761 2.145 2.624 2.977 3.787 4.144 15 0.691 0.866 1.074 1.341 1.753 2.131 2.602 2.947 3.733 4.073 16 0.690 0.865 1.071 1.337 1.746 2.120 2.583 2.921 3.686 4.018 17 0.689 0.863 1.069 1.333 1.740 2.110 2.567 2.898 3.646 3.968 18 0.688 0.862 1.067 1.330 1.734 2.101 2.552 2.878 3.610 3.922 19 0.688 0.861 1.066 1.328 1.729 2.093 2.539 2.861 3.579 3.883 20 0.687 0.860 1.064 1.325 1.725 2.086 2.528 2.845 3.527 3.816 21 0.686 0.859 1.063 1.323 1.721 2.080	12	0.695	0.873	1.083	1.356	1.782	2.179	2.681	3.055	3.930	4.318	
15 0.691 0.866 1.074 1.341 1.753 2.131 2.602 2.947 3.733 4.073 16 0.690 0.865 1.071 1.337 1.746 2.120 2.583 2.921 3.686 4.015 17 0.689 0.863 1.069 1.333 1.740 2.110 2.567 2.898 3.646 3.965 18 0.688 0.862 1.067 1.330 1.734 2.101 2.552 2.878 3.610 3.922 19 0.688 0.861 1.066 1.328 1.729 2.093 2.539 2.861 3.579 3.883 20 0.687 0.860 1.064 1.325 1.725 2.086 2.528 2.845 3.552 3.850 21 0.686 0.859 1.063 1.323 1.721 2.080 2.518 2.831 3.527 3.816 22 0.686 0.858 1.061 1.321 1.717 2.074	13	0.694	0.870	1.079	1.350	1.771	2.160	2.650	3.012	3.852	4.221	
16 0.690 0.865 1.071 1.337 1.746 2.120 2.583 2.921 3.686 4.018 17 0.689 0.863 1.069 1.333 1.740 2.110 2.567 2.898 3.646 3.968 18 0.688 0.862 1.067 1.330 1.734 2.101 2.552 2.878 3.610 3.922 19 0.688 0.861 1.066 1.328 1.729 2.093 2.539 2.861 3.579 3.883 20 0.687 0.860 1.064 1.325 1.725 2.086 2.528 2.845 3.552 3.860 21 0.686 0.859 1.063 1.323 1.721 2.080 2.518 2.831 3.527 3.818 22 0.686 0.858 1.061 1.321 1.717 2.074 2.508 2.819 3.505 3.792 23 0.685 0.857 1.059 1.318 1.711 2.06	14	0.692	0.868	1.076	1.345	1.761	2.145	2.624	2.977	3.787	4.140	
17 0.689 0.863 1.069 1.333 1.740 2.110 2.567 2.898 3.646 3.968 18 0.688 0.862 1.067 1.330 1.734 2.101 2.552 2.878 3.610 3.922 19 0.688 0.861 1.066 1.328 1.729 2.093 2.539 2.861 3.579 3.883 20 0.687 0.860 1.064 1.325 1.725 2.086 2.528 2.845 3.552 3.850 21 0.686 0.859 1.063 1.323 1.721 2.080 2.518 2.831 3.527 3.819 22 0.686 0.858 1.061 1.321 1.717 2.074 2.508 2.819 3.505 3.792 23 0.685 0.858 1.060 1.319 1.714 2.069 2.500 2.807 3.485 3.768 24 0.685 0.856 1.058 1.316 1.708 2.06	15	0.691	0.866	1.074	1.341	1.753	2.131	2.602	2.947	3.733	4.073	
18 0.688 0.862 1.067 1.330 1.734 2.101 2.552 2.878 3.610 3.922 19 0.688 0.861 1.066 1.328 1.729 2.093 2.539 2.861 3.579 3.883 20 0.687 0.860 1.064 1.325 1.725 2.086 2.528 2.845 3.552 3.850 21 0.686 0.859 1.063 1.323 1.721 2.080 2.518 2.831 3.527 3.819 22 0.686 0.858 1.061 1.321 1.717 2.074 2.508 2.819 3.505 3.792 23 0.685 0.858 1.060 1.319 1.714 2.069 2.500 2.807 3.485 3.768 24 0.685 0.857 1.059 1.318 1.711 2.064 2.492 2.797 3.467 3.745 25 0.684 0.856 1.058 1.315 1.706 2.056	16	0.690	0.865	1.071	1.337	1.746	2.120	2.583	2.921	3.686	4.015	
19 0.688 0.861 1.066 1.328 1.729 2.093 2.539 2.861 3.579 3.883 20 0.687 0.860 1.064 1.325 1.725 2.086 2.528 2.845 3.552 3.850 21 0.686 0.859 1.063 1.323 1.721 2.080 2.518 2.831 3.527 3.819 22 0.686 0.858 1.061 1.321 1.717 2.074 2.508 2.819 3.505 3.792 23 0.685 0.858 1.060 1.319 1.714 2.069 2.500 2.807 3.485 3.768 24 0.685 0.857 1.059 1.318 1.711 2.064 2.492 2.797 3.467 3.745 25 0.684 0.856 1.058 1.316 1.708 2.060 2.485 2.787 3.435 3.707 26 0.684 0.856 1.058 1.315 1.706 2.05	17	0.689	0.863	1.069	1.333	1.740	2.110	2.567	2.898	3.646	3.965	
20 0.687 0.860 1.064 1.325 1.725 2.086 2.528 2.845 3.552 3.850 21 0.686 0.859 1.063 1.323 1.721 2.080 2.518 2.831 3.527 3.818 22 0.686 0.858 1.061 1.321 1.717 2.074 2.508 2.819 3.505 3.792 23 0.685 0.858 1.060 1.319 1.714 2.069 2.500 2.807 3.485 3.768 24 0.685 0.857 1.059 1.318 1.711 2.064 2.492 2.797 3.467 3.748 25 0.684 0.856 1.058 1.316 1.708 2.060 2.485 2.787 3.450 3.705 26 0.684 0.856 1.058 1.315 1.706 2.056 2.479 2.779 3.435 3.705 27 0.684 0.855 1.057 1.314 1.703 2.05	18	0.688	0.862	1.067	1.330	1.734	2.101	2.552	2.878	3.610	3.922	
21 0.686 0.859 1.063 1.323 1.721 2.080 2.518 2.831 3.527 3.819 22 0.686 0.858 1.061 1.321 1.717 2.074 2.508 2.819 3.505 3.792 23 0.685 0.858 1.060 1.319 1.714 2.069 2.500 2.807 3.485 3.768 24 0.685 0.857 1.059 1.318 1.711 2.064 2.492 2.797 3.467 3.745 25 0.684 0.856 1.058 1.316 1.708 2.060 2.485 2.787 3.450 3.725 26 0.684 0.856 1.058 1.315 1.706 2.056 2.479 2.779 3.435 3.707 27 0.684 0.855 1.057 1.314 1.703 2.052 2.473 2.771 3.421 3.690	19	0.688	0,.861	1.066	1.328	1.729	2.093	2,539	2.861	3.579	3.883	
22 0.686 0.858 1.061 1.321 1.717 2.074 2.508 2.819 3.505 3.792 23 0.685 0.858 1.060 1.319 1.714 2.069 2.500 2.807 3.485 3.768 24 0.685 0.857 1.059 1.318 1.711 2.064 2.492 2.797 3.467 3.748 25 0.684 0.856 1.058 1.316 1.708 2.060 2.485 2.787 3.450 3.728 26 0.684 0.856 1.058 1.315 1.706 2.056 2.479 2.779 3.435 3.707 27 0.684 0.855 1.057 1.314 1.703 2.052 2.473 2.771 3.421 3.690	20	0.687	0.860	1.064	1.325	1.725	2.086	2.528	2.845	3.552	3.850	
23 0.685 0.858 1.060 1.319 1.714 2.069 2.500 2.807 3.485 3.768 24 0.685 0.857 1.059 1.318 1.711 2.064 2.492 2.797 3.467 3.745 25 0.684 0.856 1.058 1.316 1.708 2.060 2.485 2.787 3.450 3.725 26 0.684 0.856 1.058 1.315 1.706 2.056 2.479 2.779 3.435 3.707 27 0.684 0.855 1.057 1.314 1.703 2.052 2.473 2.771 3.421 3.690	21	0.686	0.859	1.063	1.323	1.721	2.080	2.518	2.831	3.527	3.819	
24 0.685 0.857 1.059 1.318 1.711 2.064 2.492 2.797 3.467 3.745 25 0.684 0.856 1.058 1.316 1.708 2.060 2.485 2.787 3.450 3.725 26 0.684 0.856 1.058 1.315 1.706 2.056 2.479 2.779 3.435 3.707 27 0.684 0.855 1.057 1.314 1.703 2.052 2.473 2.771 3.421 3.690	22	0.686	0.858	1.061	1.321	1.717	2.074	2.508	2.819	3.505	3.792	
25 0.684 0.856 1.058 1.316 1.708 2.060 2.485 2.787 3.450 3.725 26 0.684 0.856 1.058 1.315 1.706 2.056 2.479 2.779 3.435 3.707 27 0.684 0.855 1.057 1.314 1.703 2.052 2.473 2.771 3.421 3.690	23	0.685	0.858	1.060	1.319	1.714	2.069	2.500	2.807	3.485	3.768	
26 0.684 0.856 1.058 1.315 1.706 2.056 2.479 2.779 3.435 3.707 27 0.684 0.855 1.057 1.314 1.703 2.052 2.473 2.771 3.421 3.690	24	0.685	0.857	1.059	1.318	1.711	2.064	2.492	2.797	3.467	3.745	
27 0.684 0.855 1.057 1.314 1.703 2.052 2.473 2.771 3.421 3.690	25	0.684	0.856	1.058	1.316	1.708	2.060	2.485	2.787	3.450	3.725	
	26	0.684	0.856	1.058	1.315	1.706	2.056	2.479	2.779	3.435	3.707	
28 0.683 0.855 1.056 1.313 1.701 2.048 2.467 2.763 3.408 3.674	27	0.684	0.855	1.057	1.314	1.703	2.052	2.473	2.771	3.421	3.690	
	28	0.683	0.855	1.056	1.313	1.701	2.048	2.467	2.763	3.408	3.674	
29 0.683 0.854 1.055 1.311 1.699 2.045 2.462 2.756 3.396 3.659	29	0.683	0.854	1.055	1.311	1.699	2.045	2.462	2.756	3.396	3.659	
30 0.683 0.854 1.055 1.310 1.697 2.042 2.457 2.750 3.385 3.646	30	0.683	0.854	1.055	1.310	1.697	2.042	2.457	2.750	3.385	3.646	
50% 60% 70% 80% 90% 95% 98% 99% 99.8% 99.9%		50%	60%	70%	80%	90%	95%	98%	99%	99.8%	99.9%	
Confidence level C						Confiden	ce level C					



