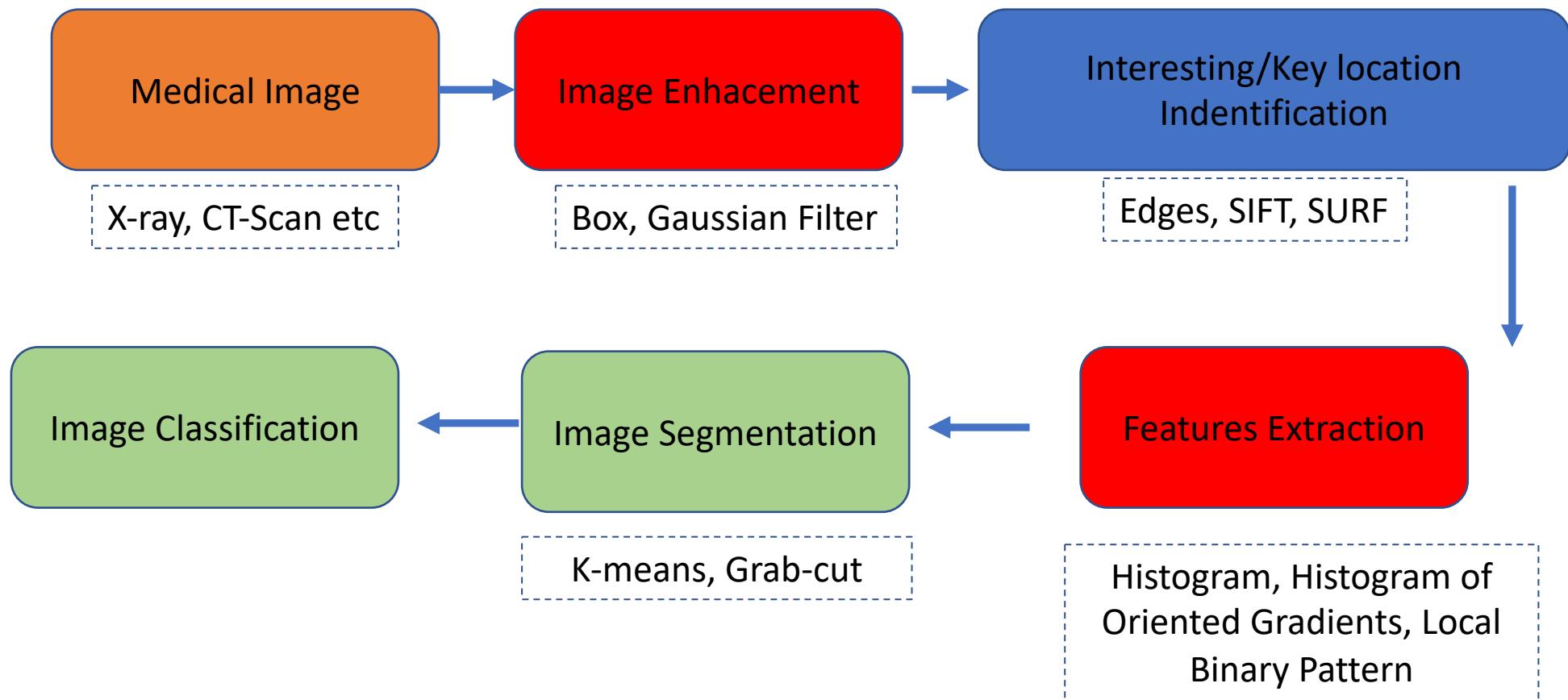




# Medical Images Computing

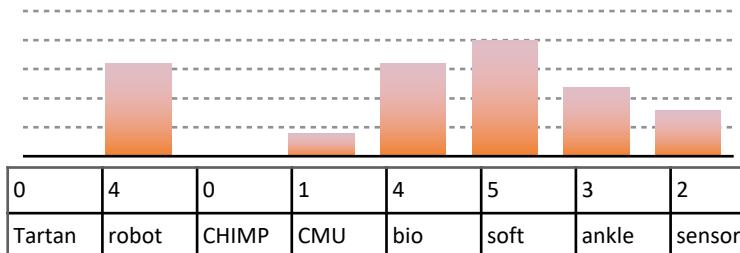
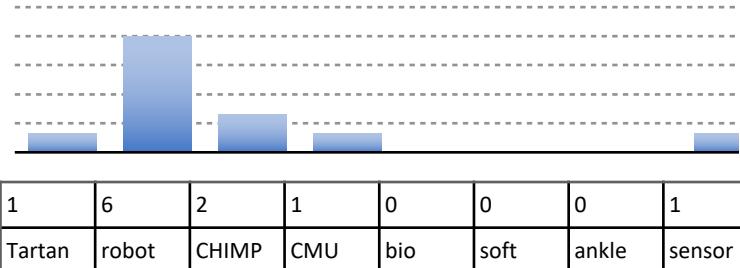
## Lecture 9 – Medical Image Classification

Waqas Sultani  
Information Technology University



# Vector Space Model

G. Salton. 'Mathematics and Information Retrieval' Journal of Documentation, 1979



A document (datapoint) is a vector of counts over each word (feature)

$$\mathbf{v}_d = [n(w_{1,d}) \ n(w_{2,d}) \ \cdots \ n(w_{T,d})]$$

$n(\cdot)$  counts the number of occurrences

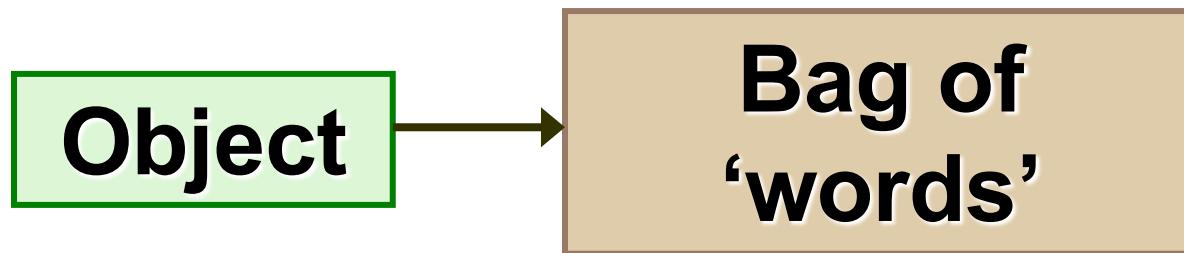


just a histogram over words

What is the similarity between two documents?



# Bag-of-features models



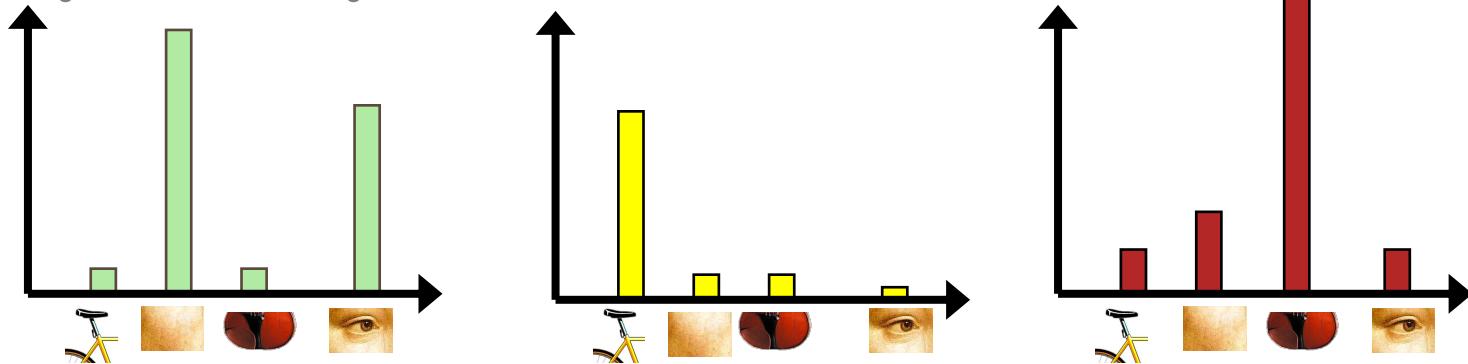
Svetlana Lazebnik



Visual words

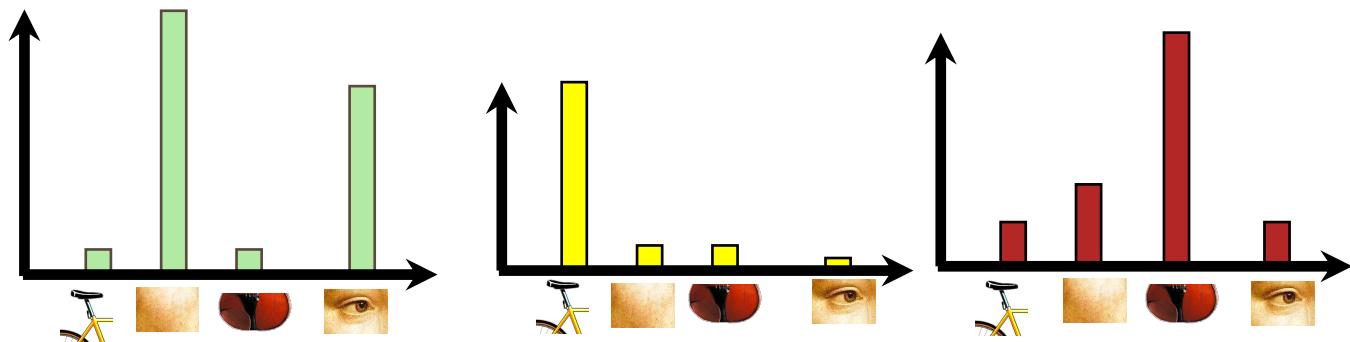


Bag of visual words histograms



**Encode:**  
build Bags-of-Words (BOW) vectors  
for each image

2. Histogram: count the  
number of visual word  
occurrences



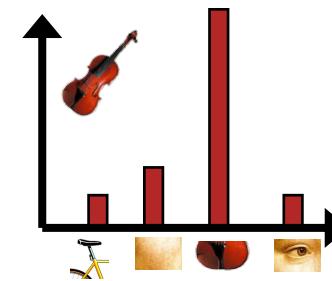
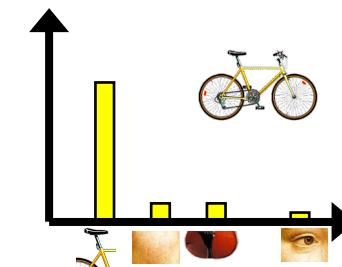
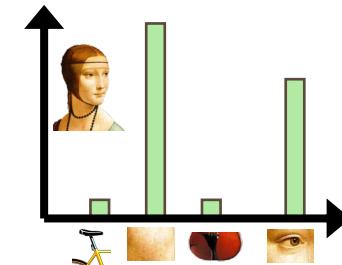
# Bags of visual words

- Summarize entire image based on its distribution (histogram) of word occurrences.
- Analogous to bag of words representation commonly used for documents.

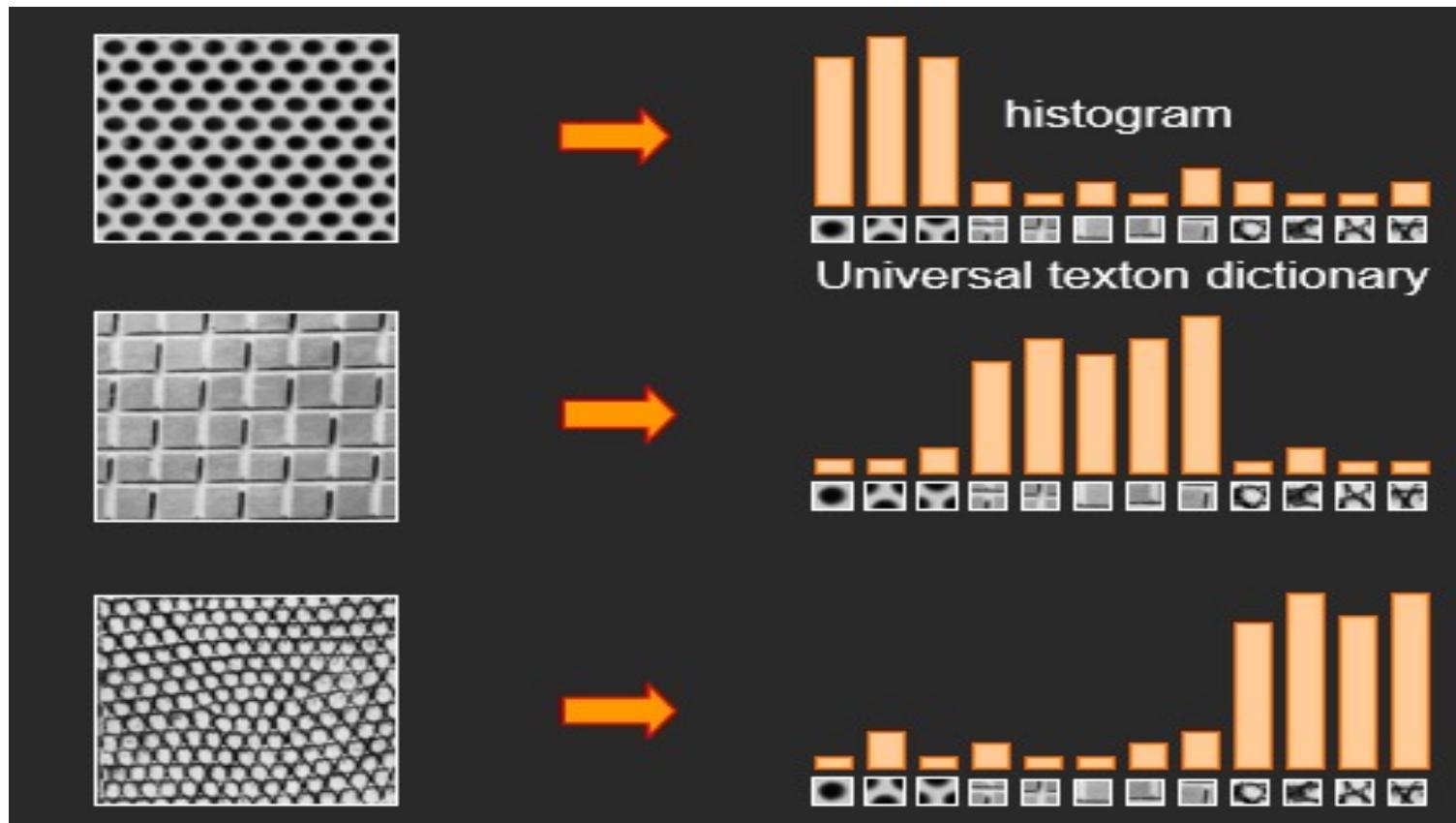
Visual words



Bag of visual words histograms

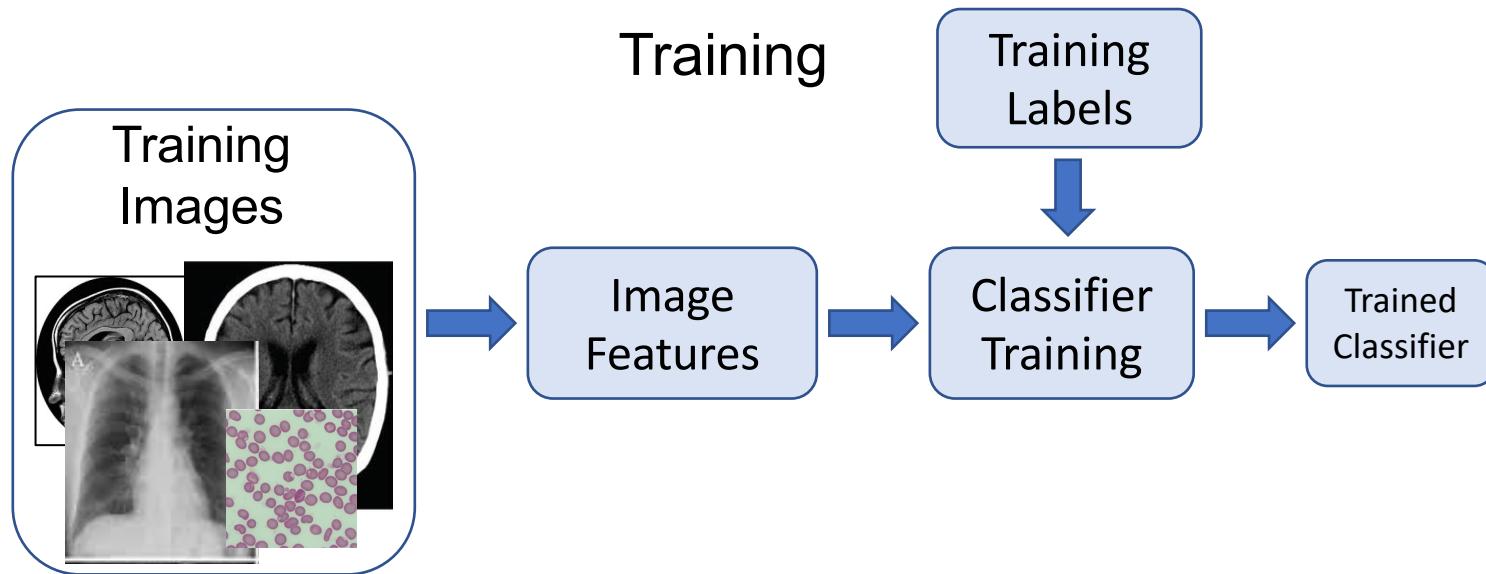


## Origin 2: Texture recognition

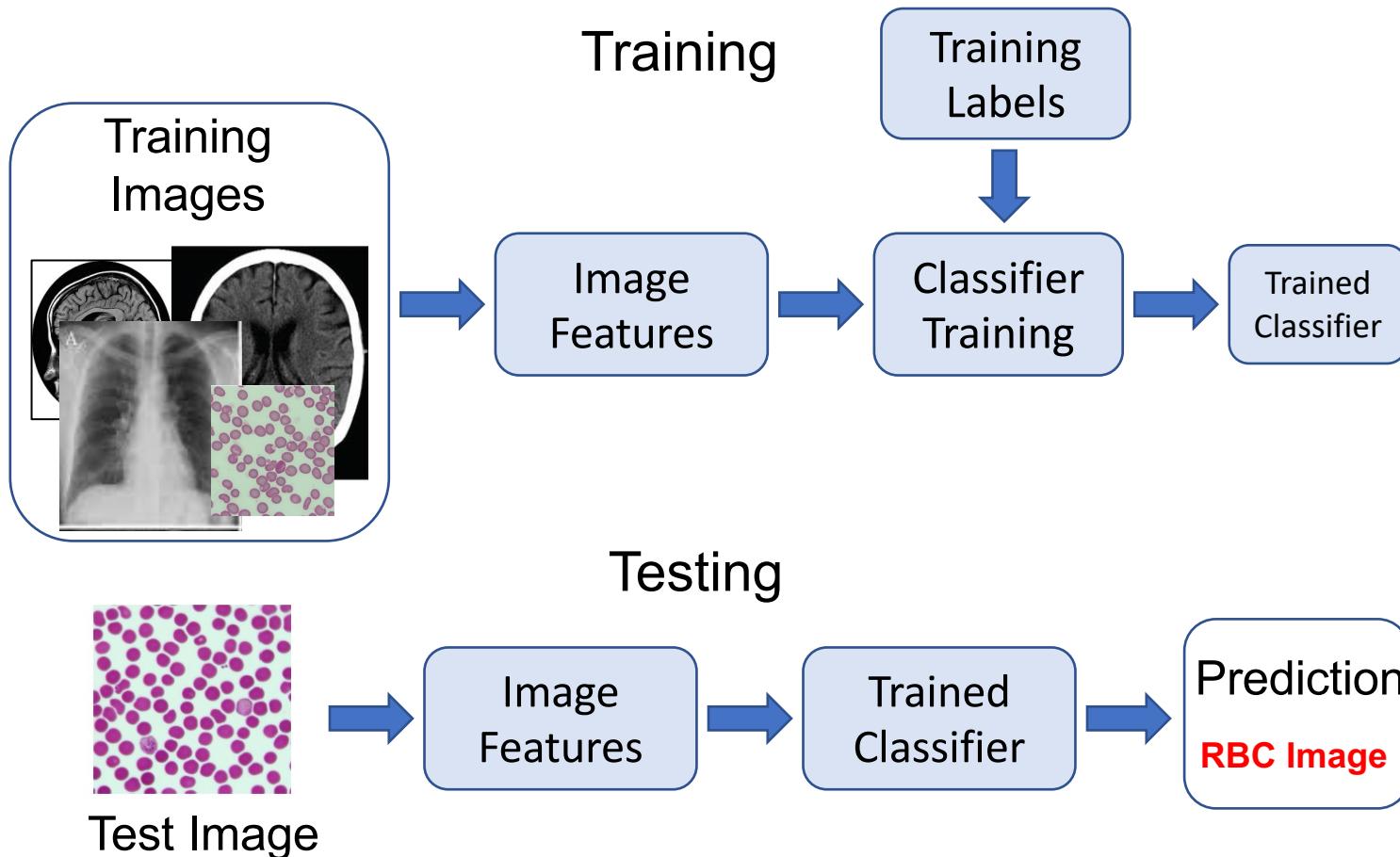


Julesz, 1981; Cula & Dana, 2001; Leung & Malik 2001; Mori, Belongie & Malik, 2001;  
Schmid 2001; Varma & Zisserman, 2002, 2003; Lazebnik, Schmid & Ponce, 2003

# Image Categorization/Classification



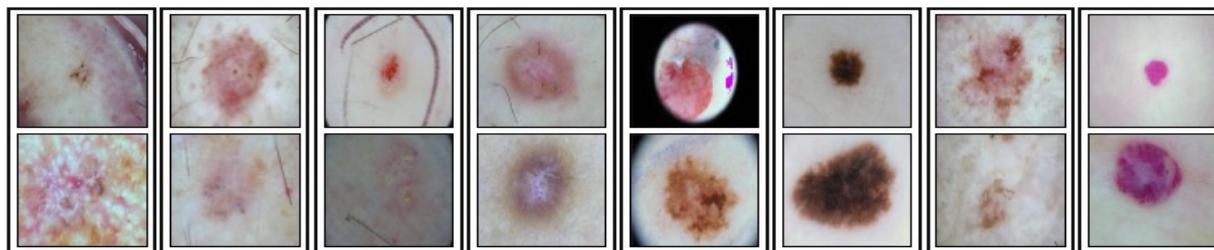
# Image Categorization/Classification



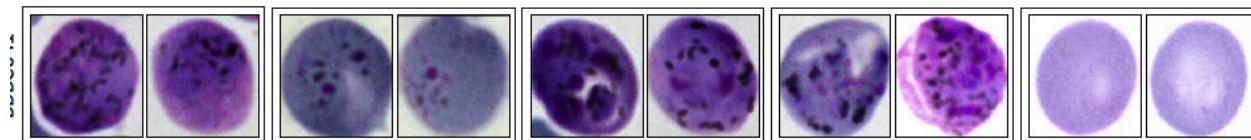
# Image classification

- Given

Positive training images containing an object class



Negative training images that don't



- Classify

A test image as to whether it contains the object class or not



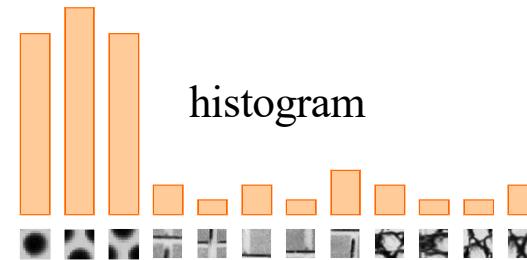
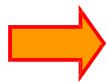
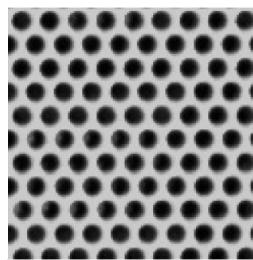
?

# Bag-of-features – Origin: texture recognition

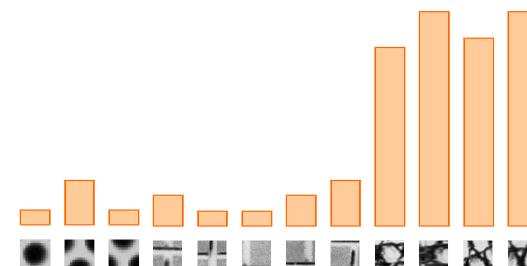
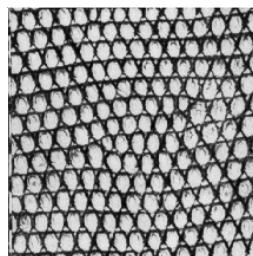
- Texture is characterized by the repetition of basic elements or *textons*

Julesz, 1981; Cula & Dana, 2001; Leung & Malik 2001; Mori, Belongie & Malik, 2001  
Schmid 2001; Varma & Zisserman, 2002, 2003; Lazebnik, Schmid & Ponce, 2003

# Bag-of-features – Origin: texture recognition



histogram



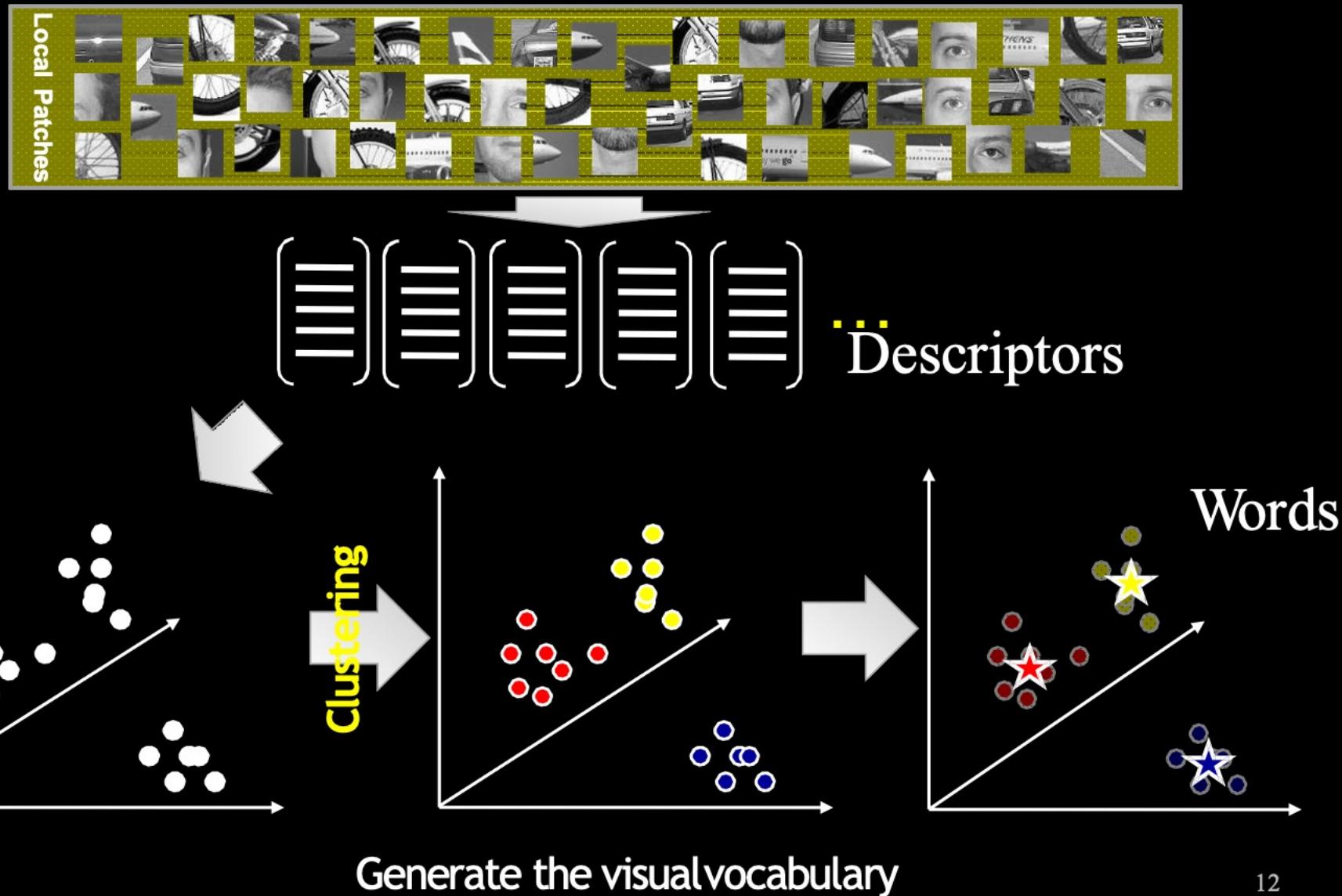
Cula & Dana,  
2001; Varma &

Malik 2001; Mori, Belongie &  
2003; Lazebnik,  
& Ponce,

# Bag of Visual Words model



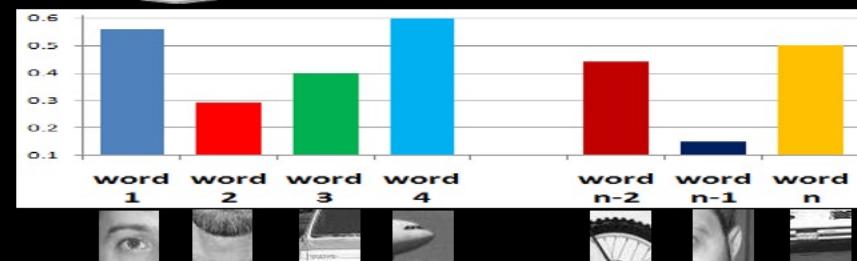
# Bag of Visual Words model

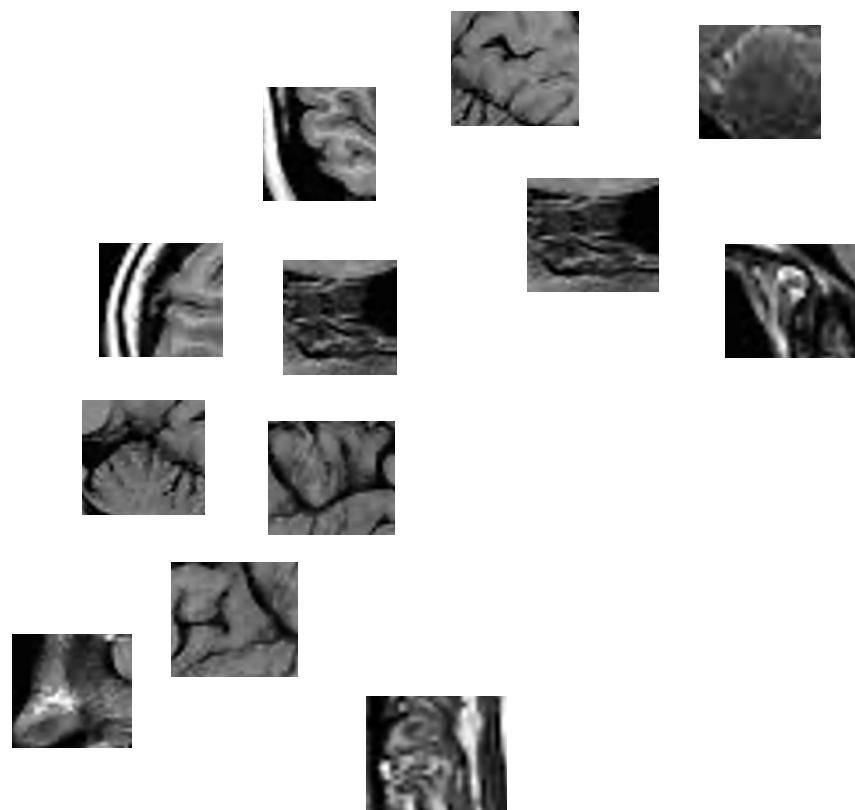


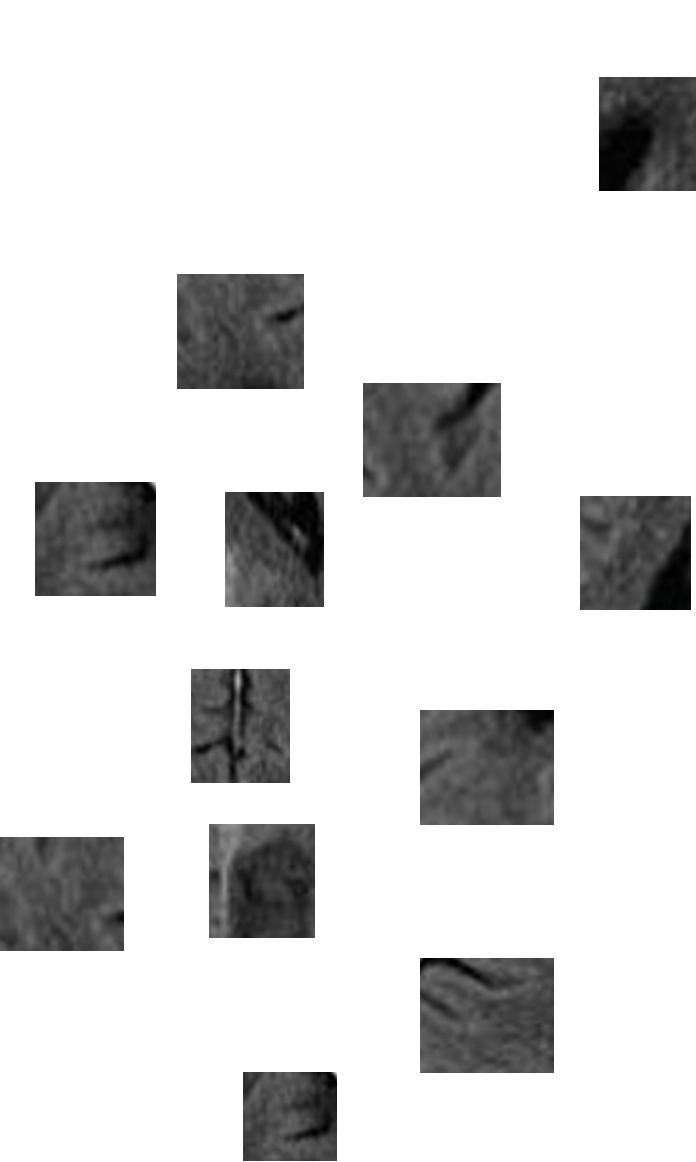
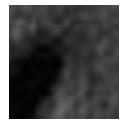
# Bag of Visual Words model

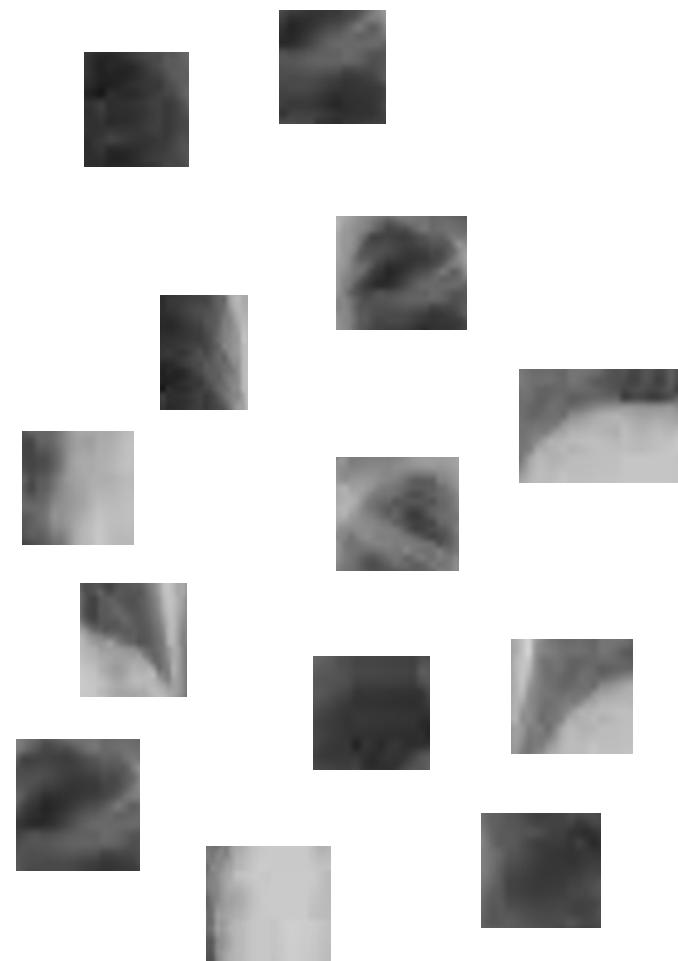


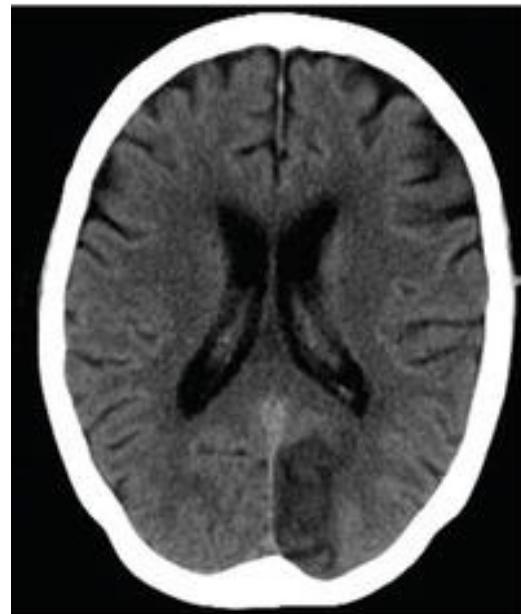
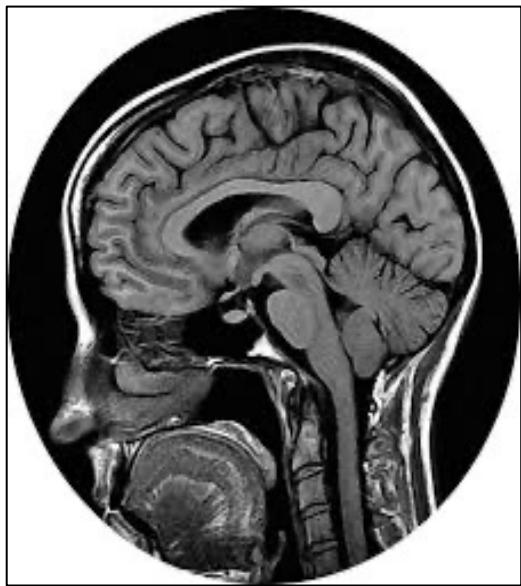
Represent an image as a histogram or bag of words

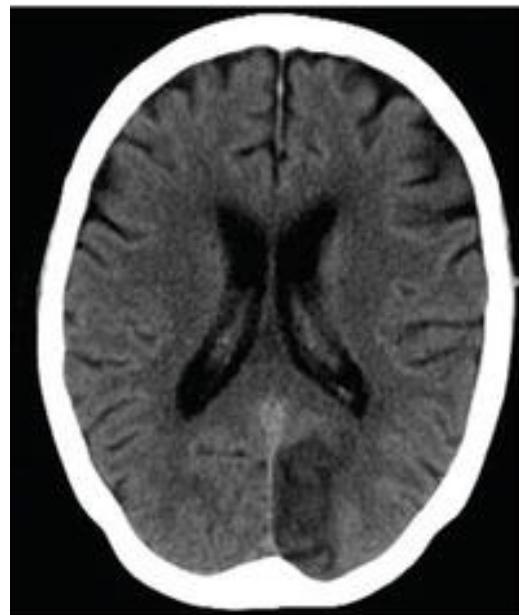
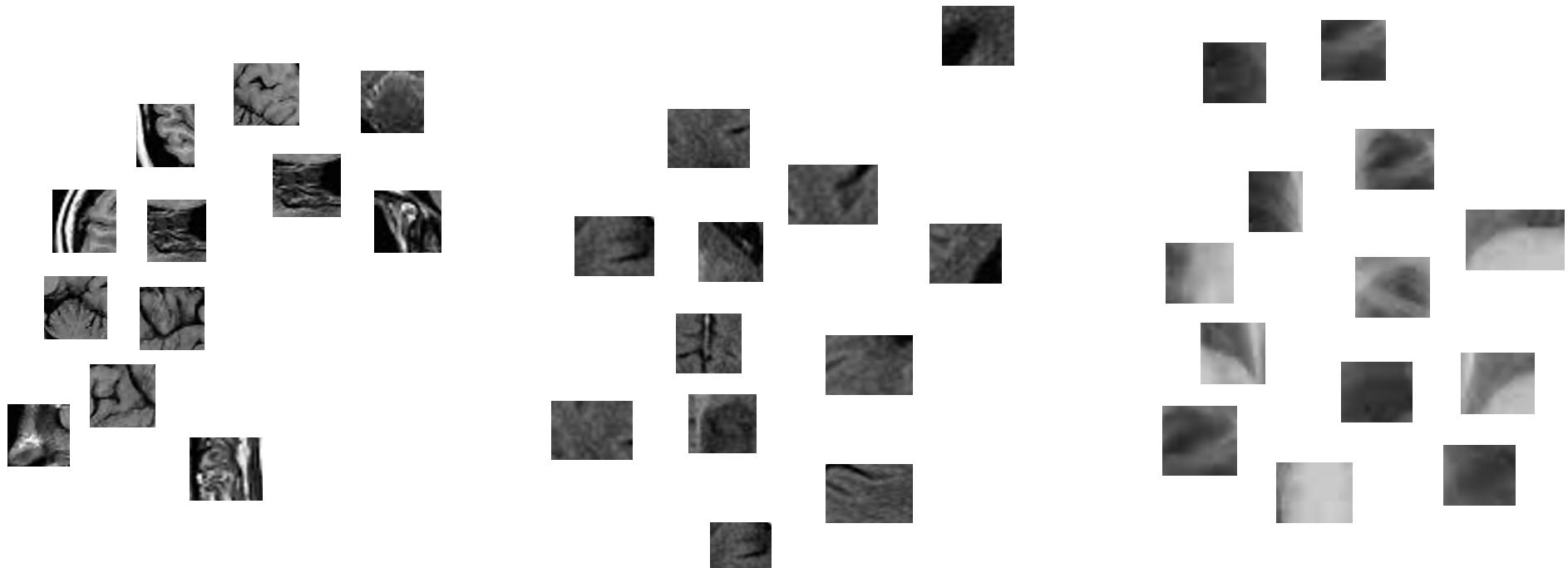




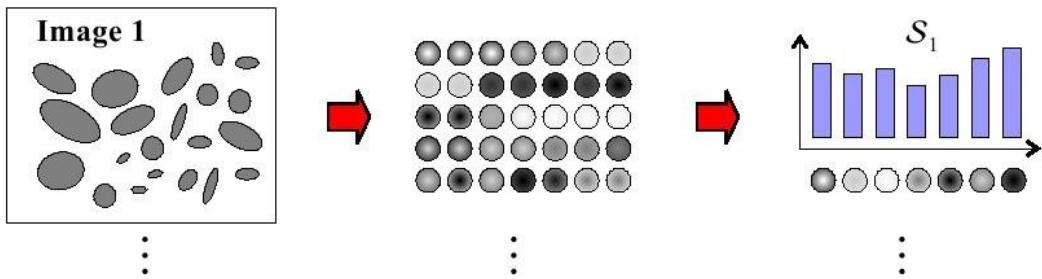








# Bag-of-features for image classification

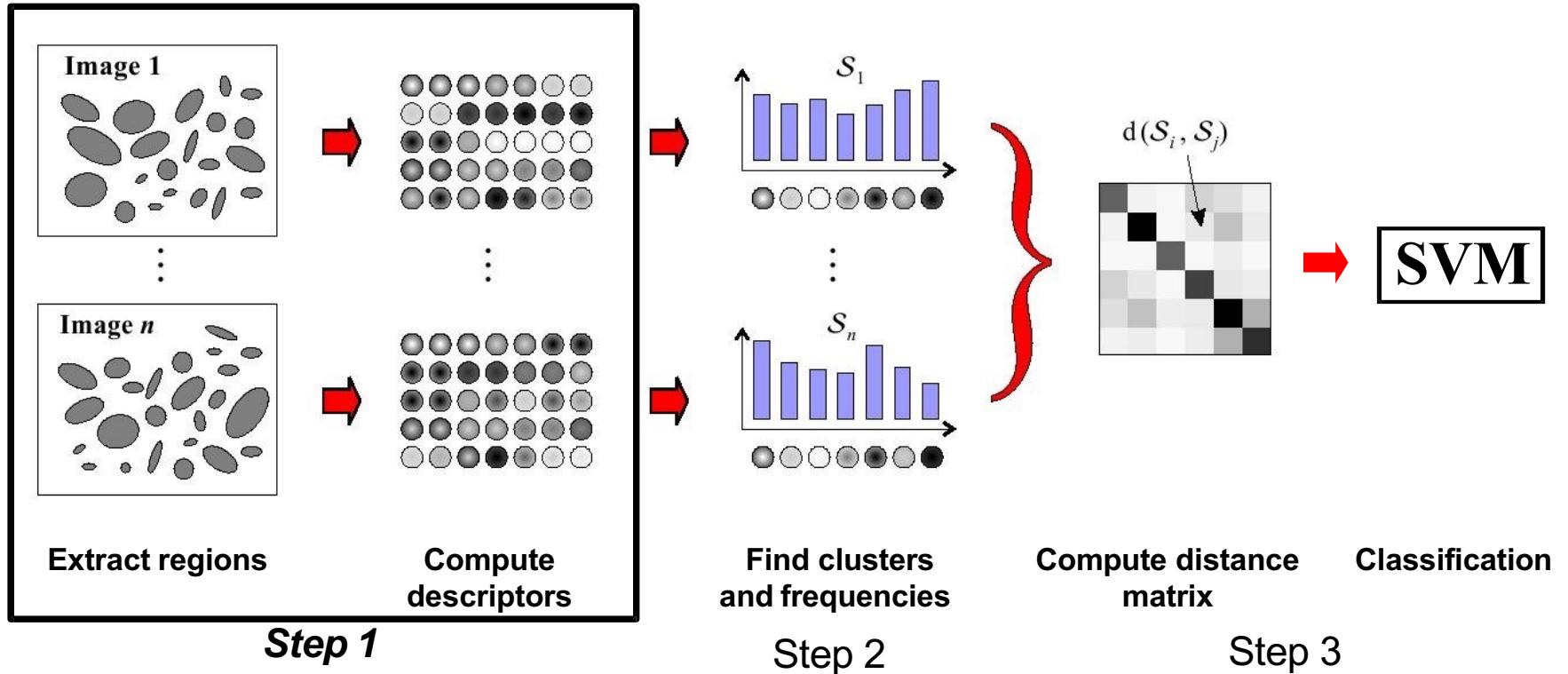


**Extract regions  
or  
Interest Points**

**Compute  
descriptors**

**Find clusters  
and frequencies**

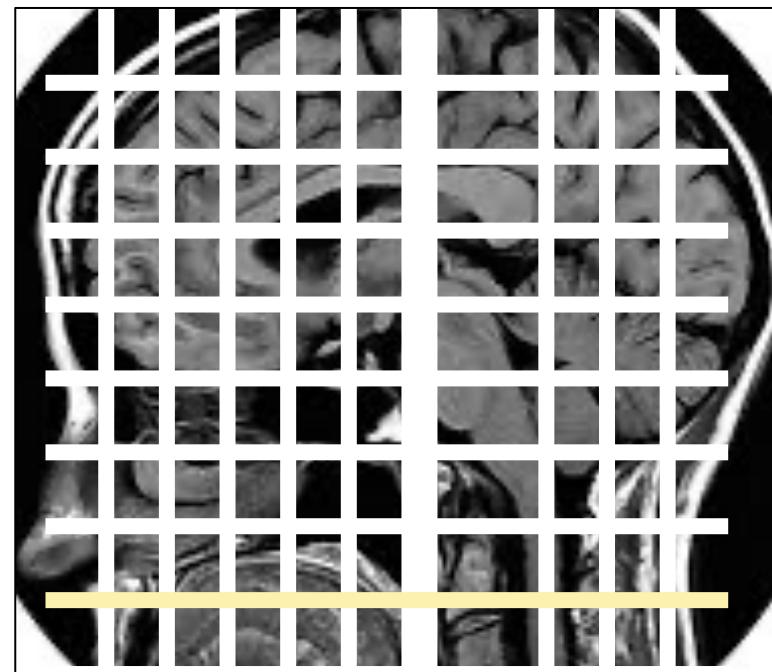
# Bag-of-features for image classification



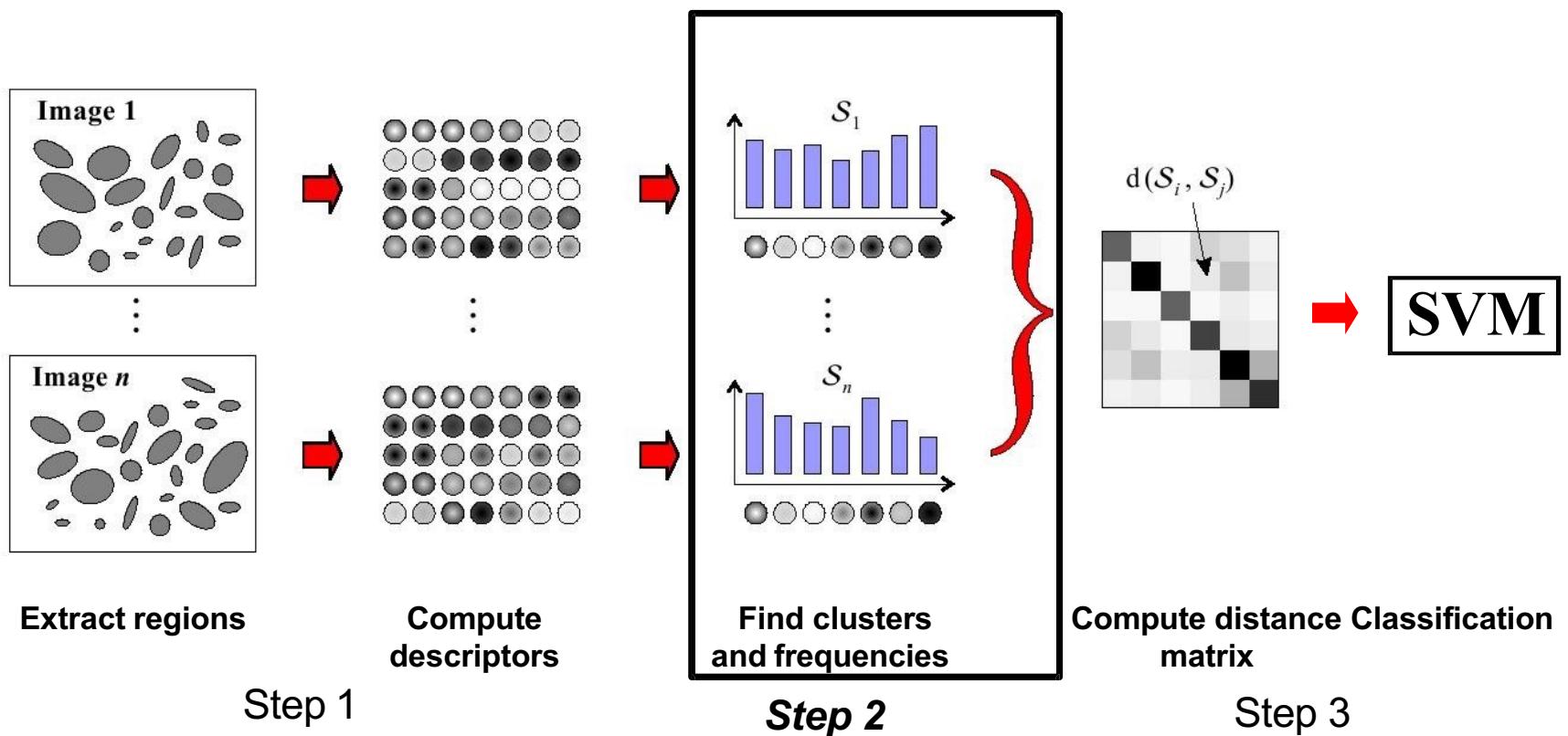
# Step 1: feature extraction

- Detect Interest Points
  - SIFT
  - Harris
  - Dense (take every nth pixel as interest point)
- Compute Descriptor around each interest point
  - SIFT
  - HOG

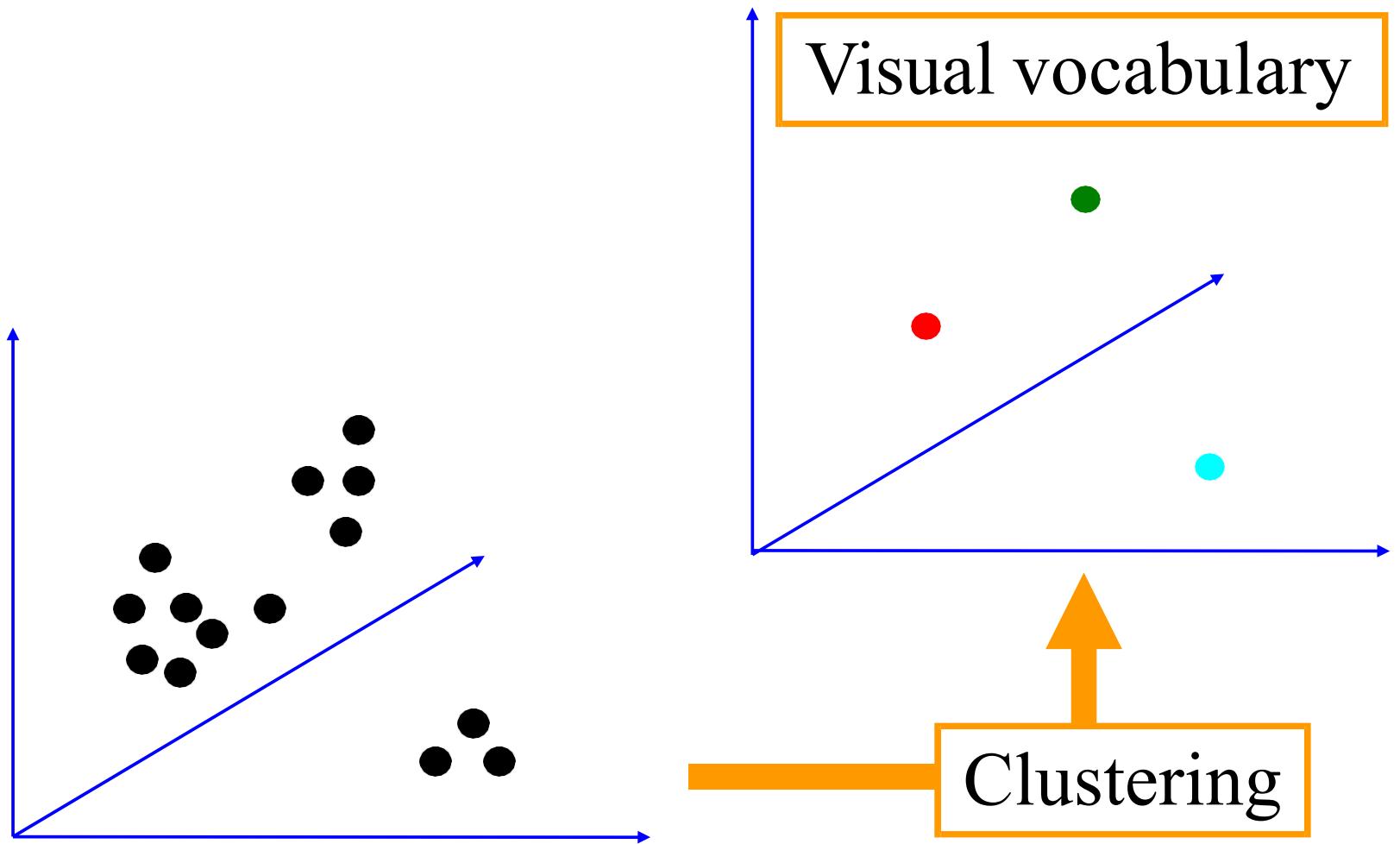
# Dense features



# Bag-of-features for image classification



## Step 2: Quantization



## Step 2: Quantization

- Cluster descriptors
  - K-means
- Assign each visual word to a cluster
- Build frequency histogram

---

# K-Means

```
Choose  $k$  data points to act as cluster centers  
Until the cluster centers are unchanged  
    Allocate each data point to cluster whose center is nearest  
    Replace the cluster centers with the mean of the elements  
    in their clusters.  
end
```

**Algorithm 16.5:** *Clustering by K-Means*

# K-means Clustering: Step 1

- Algorithm: k-means, Distance Metric: Euclidean Distance

- 5

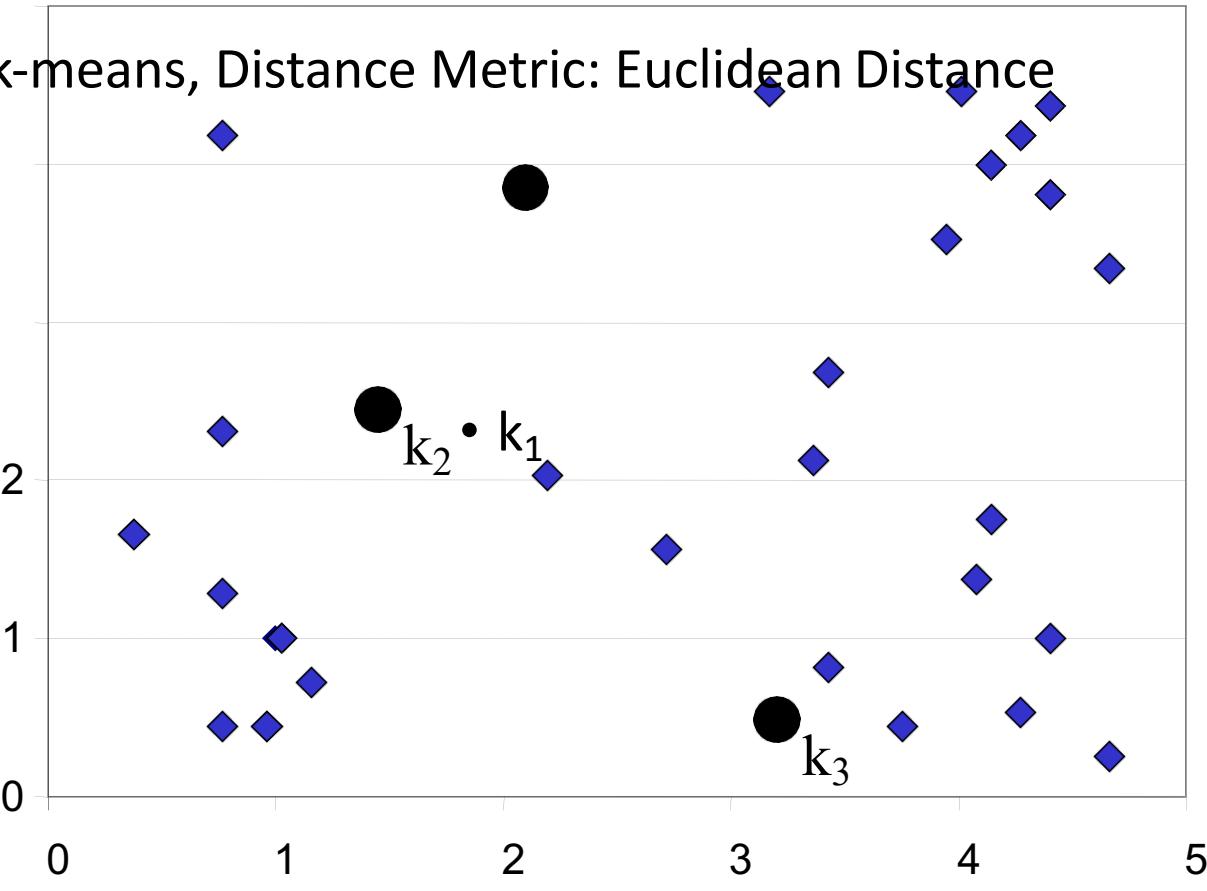
- 4

- 3

- 2

- 1

- 0



From unknown source on internet

# K-means Clustering: Step 2

- Algorithm: k-means, Distance Metric: Euclidean Distance

- 5

- 4

- 3

- 2

- 1

- 0

0

1

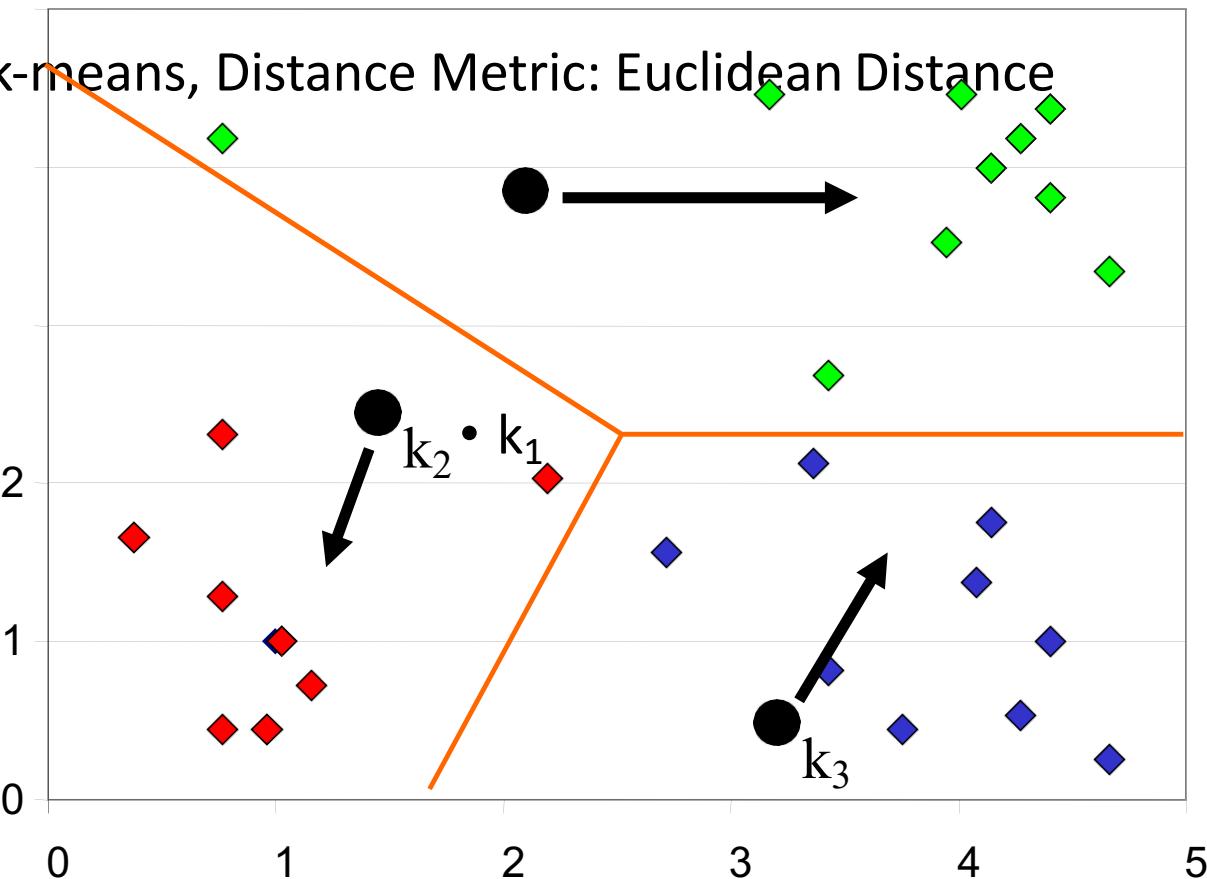
2

3

4

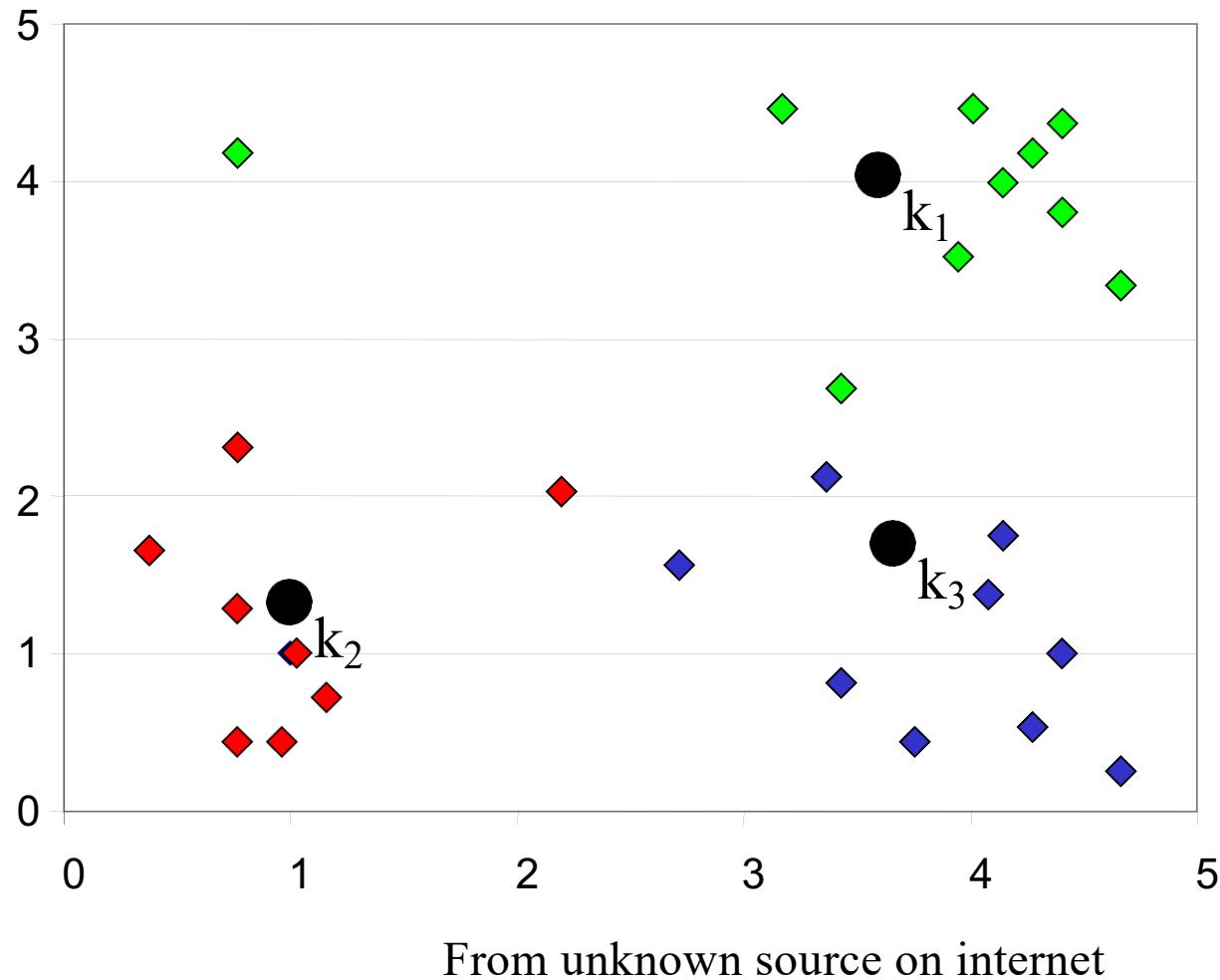
5

From unknown source on internet



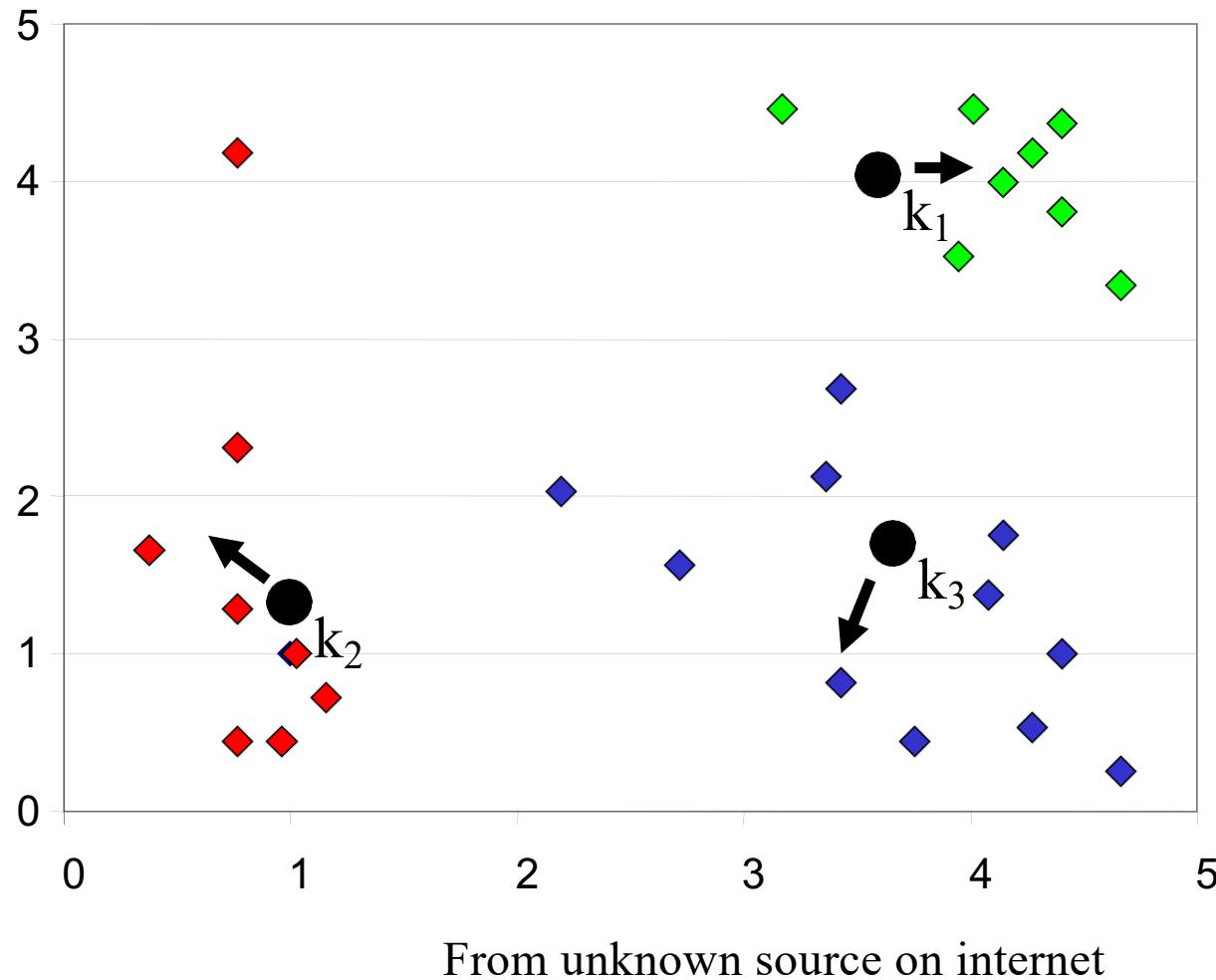
# K-means Clustering: Step 3

Algorithm: k-means, Distance Metric: Euclidean Distance



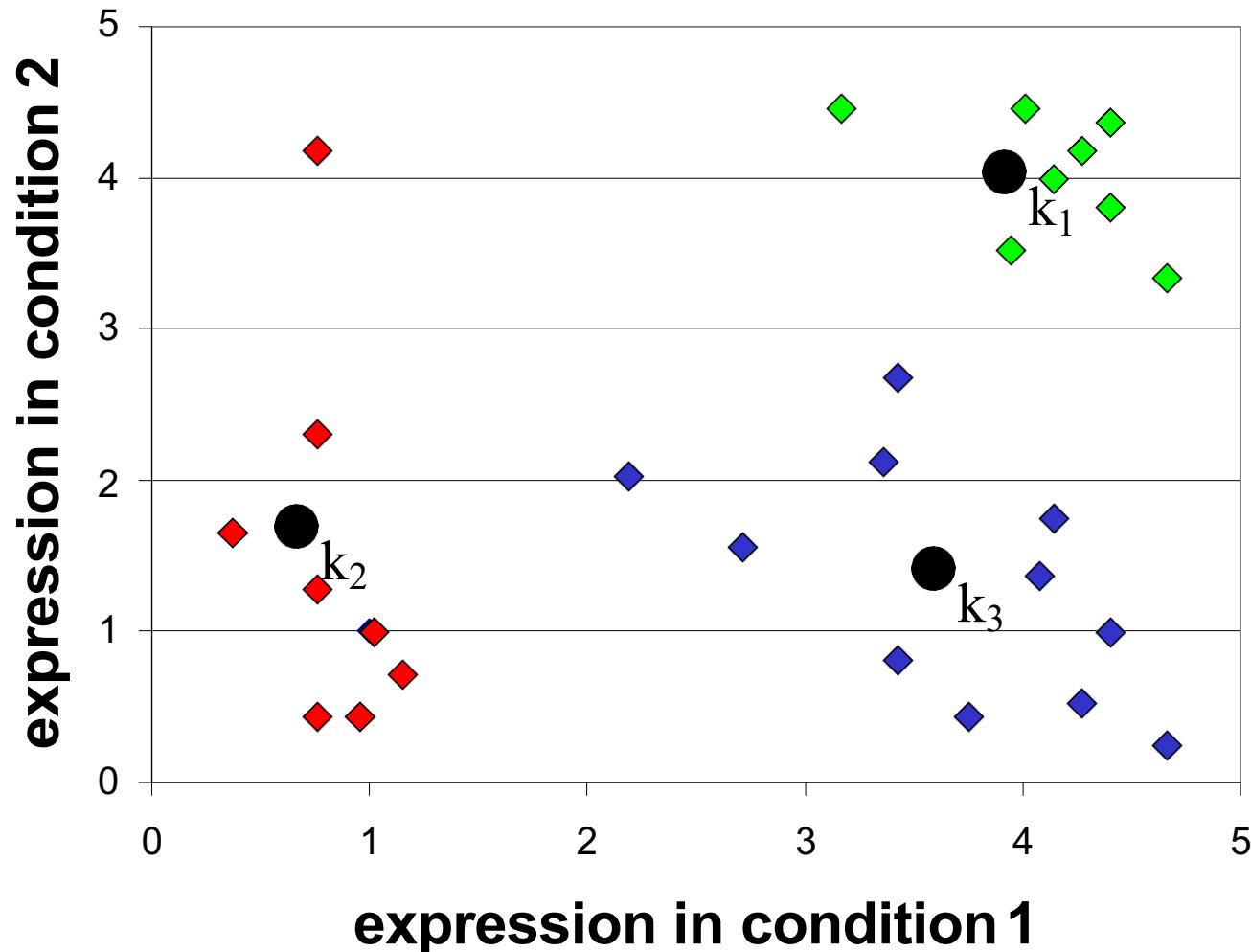
# K-means Clustering: Step 4

Algorithm: k-means, Distance Metric: Euclidean Distance



# K-means Clustering: Step 5

Algorithm: k-means, Distance Metric: Euclidean Distance



From unknown source on internet

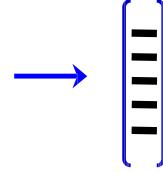
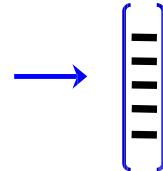
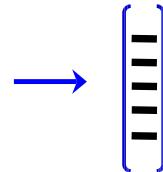
## Step 3: Classification

- Learn a decision rule (classifier) assigning bag-of-features representations of images to different classes

# Training data

Vectors are histograms, one from each training image

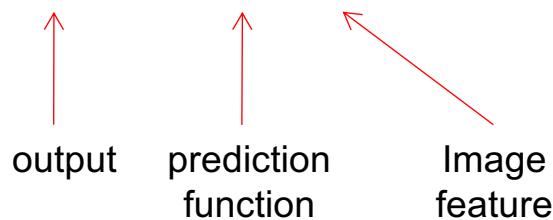
positive



Train classifier,e.g.SVM

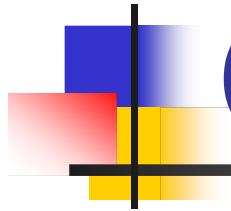
# Supervised learning

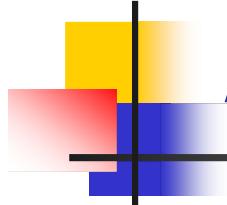
$$y = f(x)$$



- **Training:** given a *training set* of labeled examples  $\{(x_1, y_1), \dots, (x_N, y_N)\}$ , estimate the prediction function  $f$  by minimizing the prediction error on the training set
- **Testing:** apply  $f$  to a never before seen *test example*  $x$  and output the predicted value  $y = f(x)$

# Support Vector Machines (SVM)

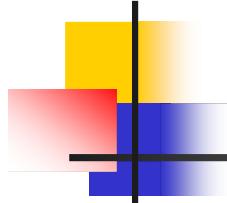




# Application

---

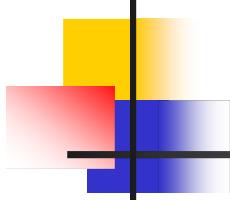
- Pattern recognition
  
- Object classification/detection



# Usage

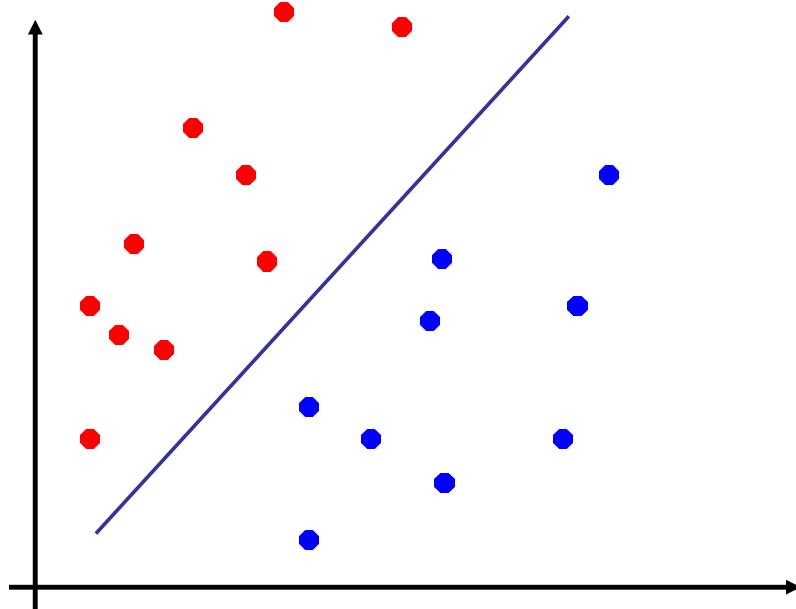
---

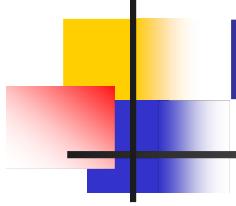
- The classifier must be trained using a set of negative and positive examples.
- The classifier “learns” the regularities in the data
- If training was successful classifier is capable of classifying an unknown example with a high degree of accuracy.



# Linear Classifier

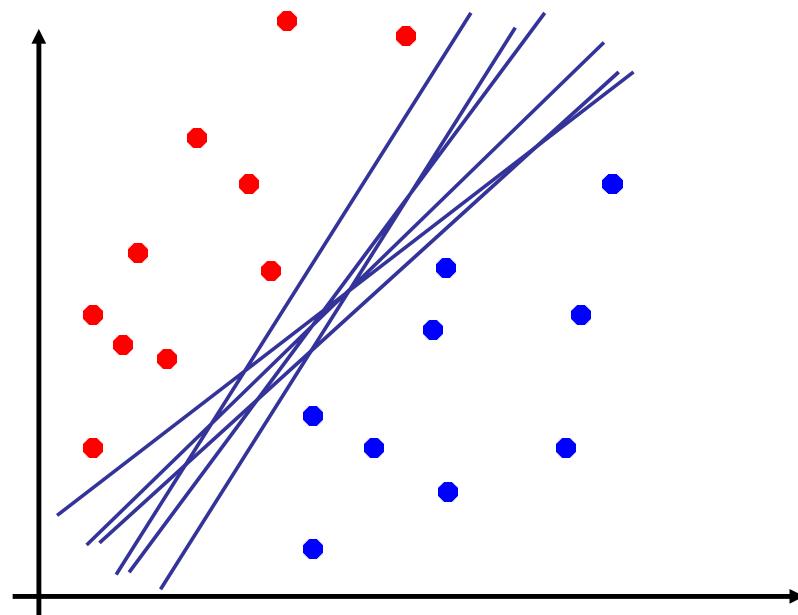
- Binary classifier → Task of separating classes in feature space

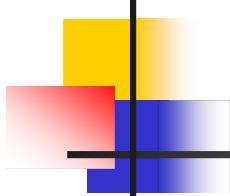




# Linear Classifier cont'd

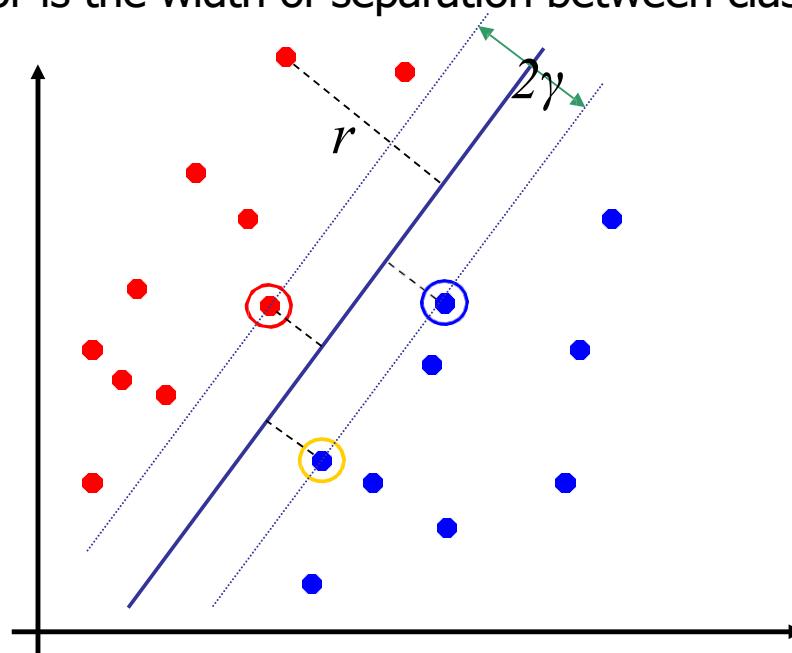
- Which of the linear separators is optimal?

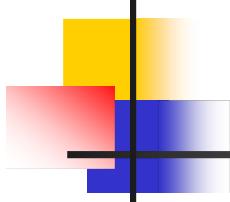




# Margin

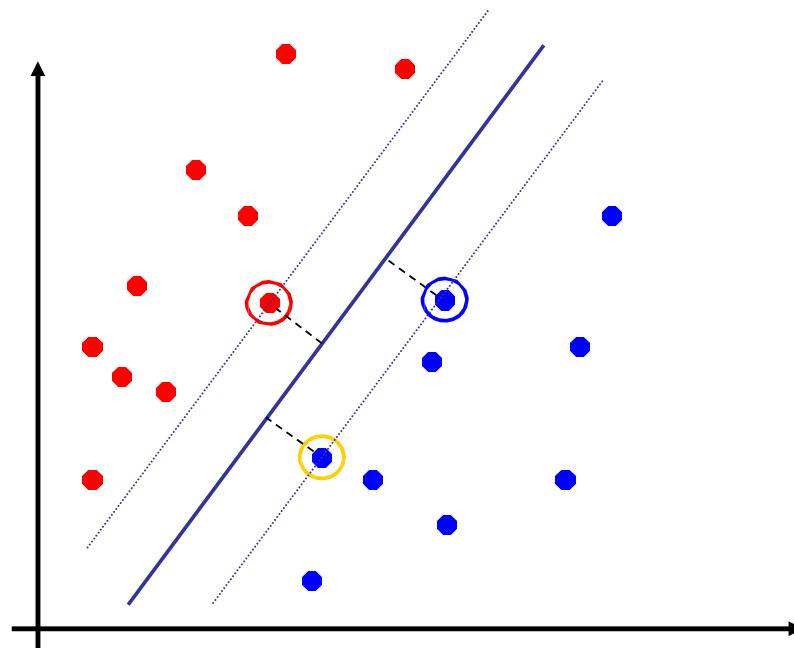
- Distance from example to the separator is (Point to Plane Distance Equation)
- Examples closest to the hyperplane are ***support vectors***.
- ***Margin***
- $2\gamma$  of the separator is the width of separation between classes.

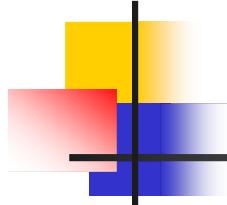




# Maximum Margin Classification

- Maximizing the margin is good according to intuition.
- Implies that only support vectors are important; other training examples are ignorable.





# LibSVM

## SVM implementation

- <http://www.csie.ntu.edu.tw/~cjlin/libsvm/>
- <http://www.cs.wisc.edu/dmi/svm/>

# Kernels for bags of features

---

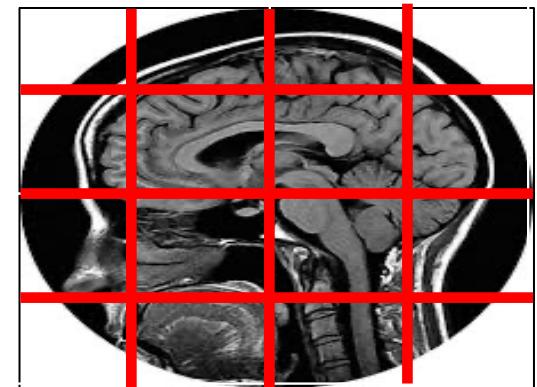
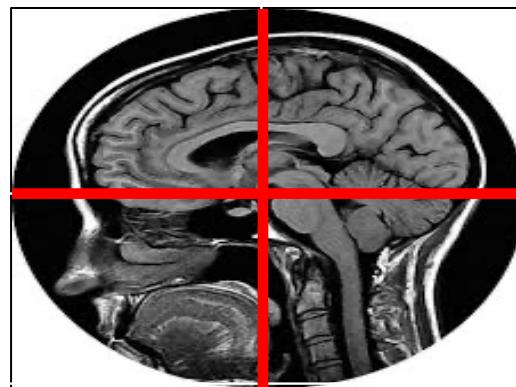
- Histogram intersection kernel:  $I(h_1, h_2) = \sum_{i=1}^N \min(h_1(i), h_2(i))$
- Generalized Gaussian kernel:

$$K(h_1, h_2) = \exp\left(-\frac{1}{A} D(h_1, h_2)^2\right)$$

- $D$  can be Euclidean distance  $\rightarrow$  RBF kernel
- $D$  can be  $\chi^2$  distance  $D(h_1, h_2) = \sum_{i=1}^N \frac{(h_1(i) - h_2(i))^2}{h_1(i) + h_2(i)}$
- Earth mover's distance

# Spatial pyramid matching

- Add spatial information to the bag-of-features
- Perform matching in 2D image space



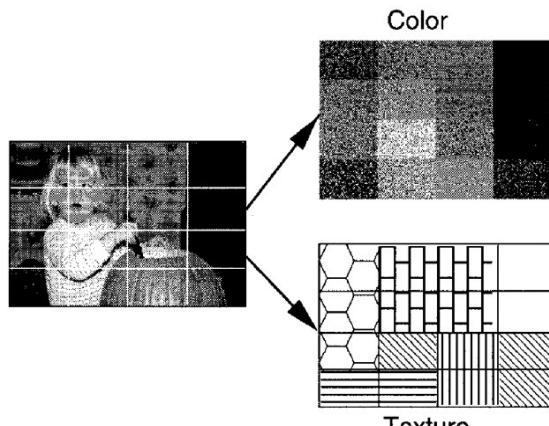
# Related work

Similar approaches:

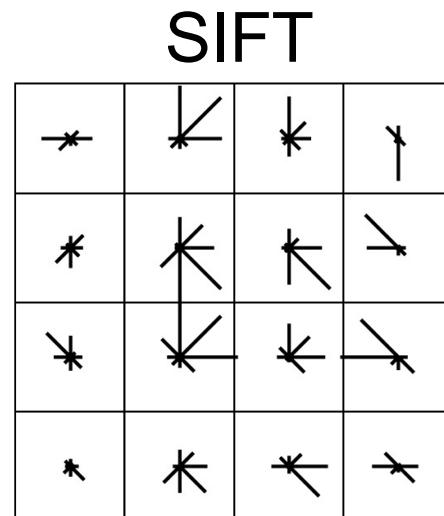
Subblock description [Szummer & Picard, 1997]

SIFT [Lowe, 1999]

GIST [Torralba et al., 2003]



Szummer & Picard (1997)

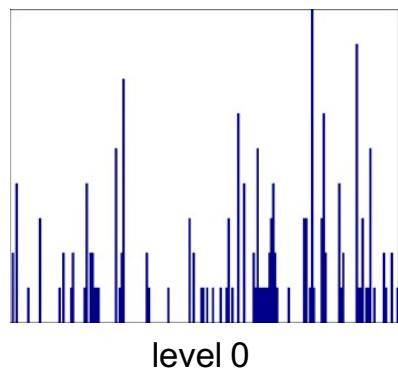


Lowe (1999, 2004)

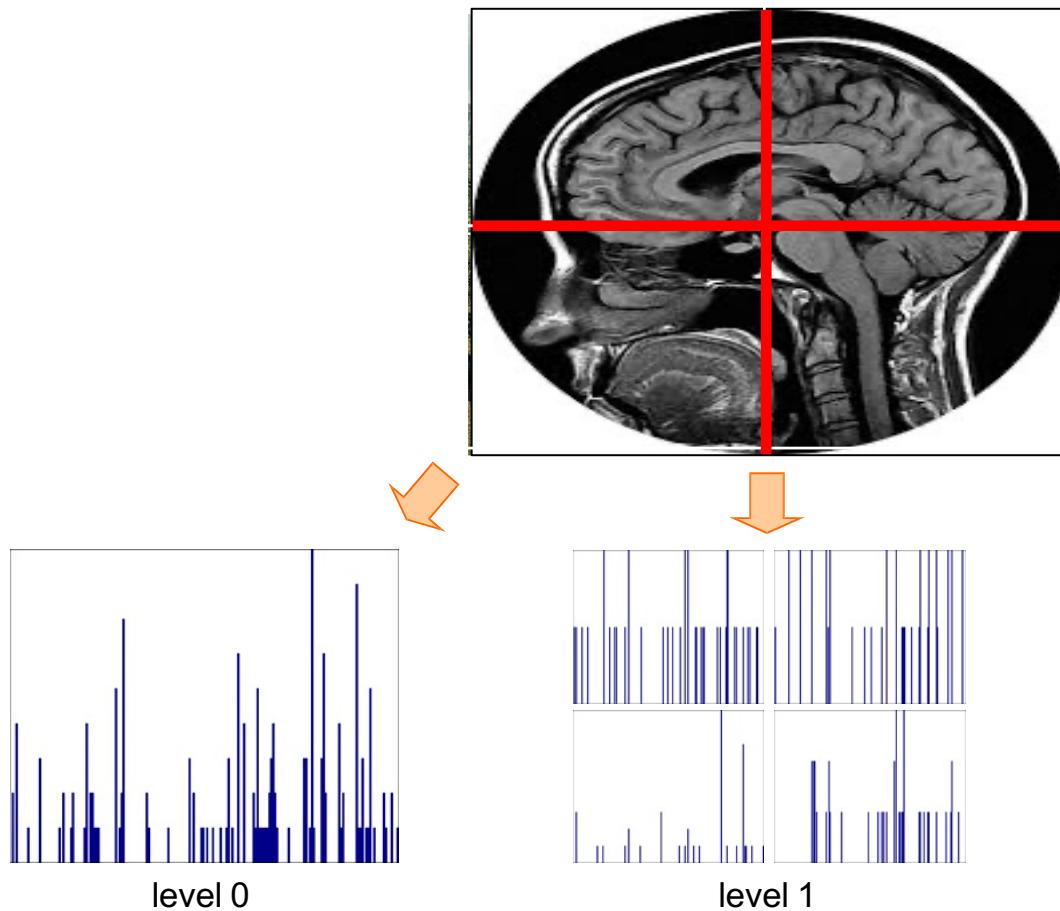
# Spatial pyramid representation



Locally orderless representation at several levels of spatial resolution

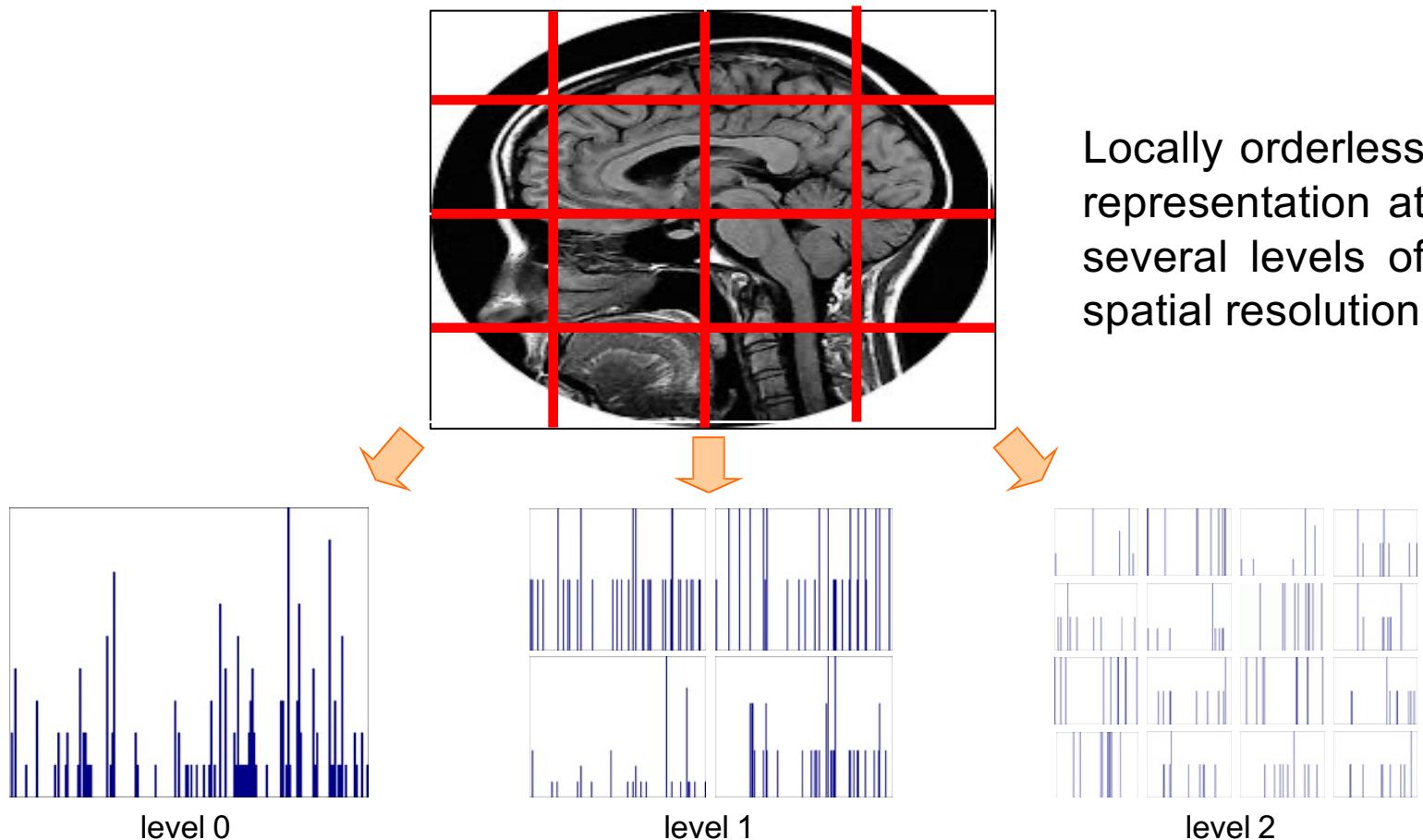


# Spatial pyramid representation



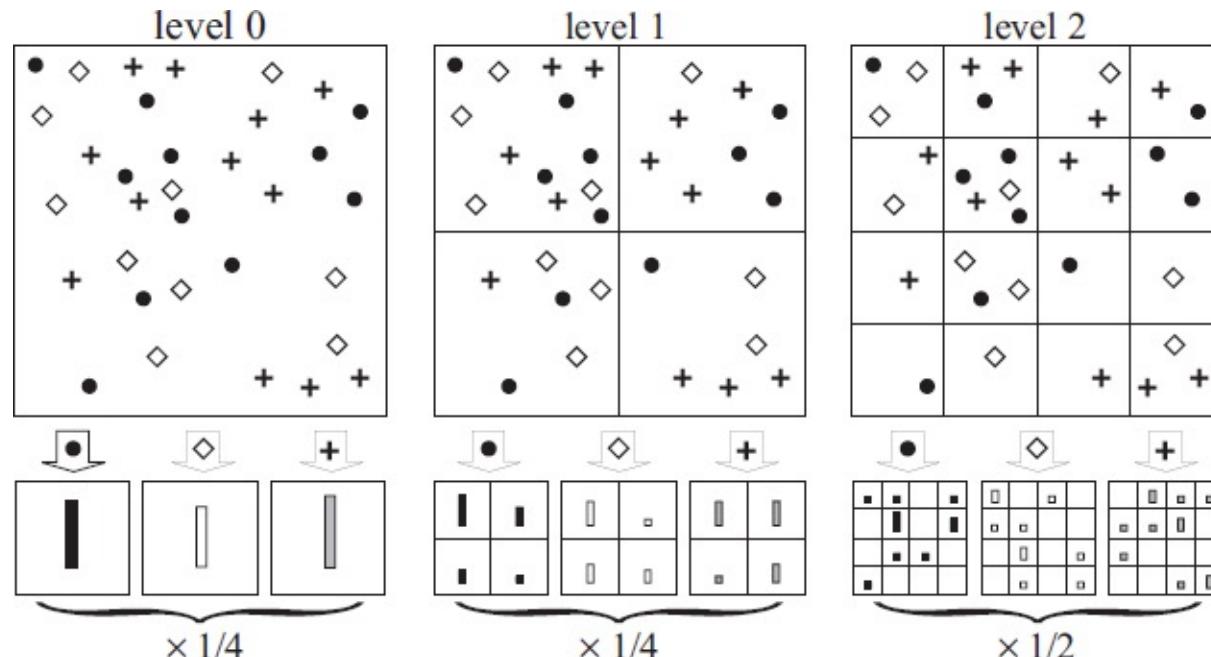
Locally orderless representation at several levels of spatial resolution

# Spatial pyramid representation



# Spatial pyramid matching

- Combination of spatial levels with pyramid match kernel [Grauman & Darrell'05]
- Intersect histograms, more weight to finer grids



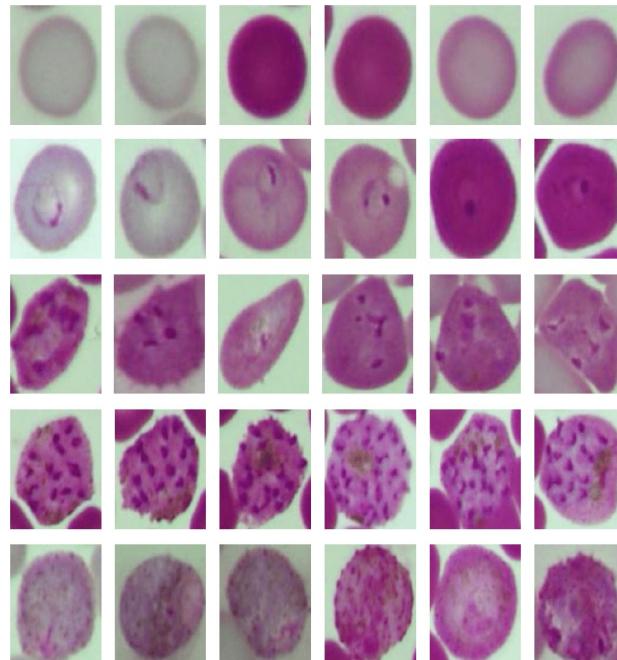
# Machine Learning Approaches

- Supervised Approaches All Labels available
- Unsupervised Approaches No Labels available
- Weakly Supervised Approaches No Complete Labels available
- Few shot approaches A few Labels available
- Single shot approaches Only One Labels available
- Semi Supervised approaches Label and Unlabeled data available

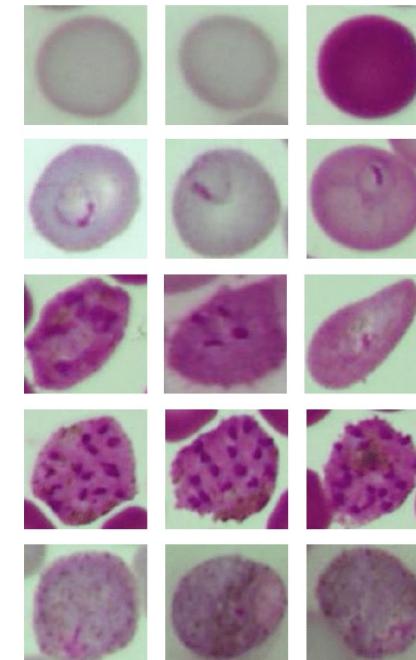
- **Self Supervised approaches**

Unsupervised learning concentrates on clustering, grouping, and dimensionality reduction, while self-supervised learning aims to draw conclusions for regression and classification tasks.

### Pretext Task



(a)



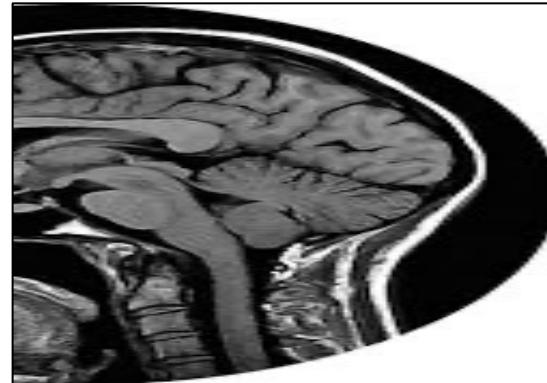
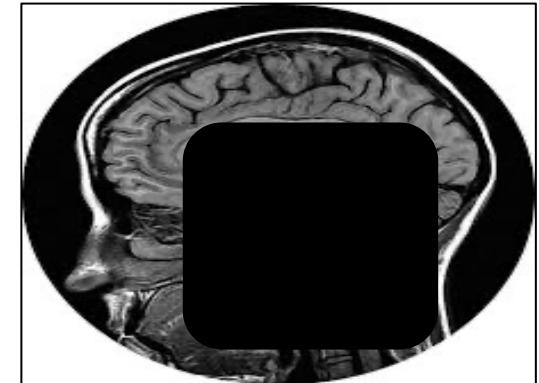
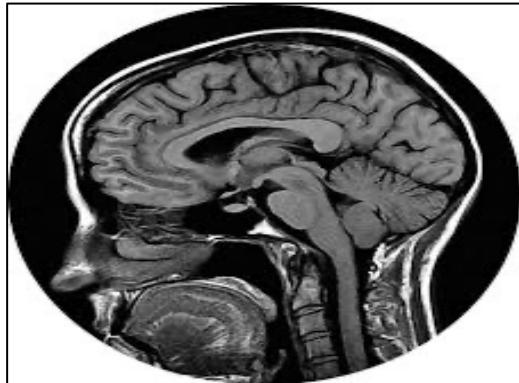
(b)

Number of cells in (a) are greater than number of cells in (b)

- **Self Supervised approaches**

Unsupervised learning concentrates on clustering, grouping, and dimensionality reduction, while self-supervised learning aims to draw conclusions for regression and classification tasks.

### Pretext Task



# References and Slide Credits

- Jayaram K. Udupa, MIPG of University of Pennsylvania, PA.
- P. Suetens, Fundamentals of Medical Imaging, Cambridge Univ. Press.
- N. Bryan, Intro. to the science of medical imaging, Cambridge Univ. Press.
- CAP 5415 Computer Vision (Fall 2016) Lecture Presentations
  - Computer Vision (Lecture Presentations) by Dr. Mohsen Ali