# Programming Assignment III

CS5691: PATTERN RECOGNITION AND MACHINE LEARNING

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# I Pattern classification on linearly separable data

### I.1 Python Code

```
#1A part I perceptron
2
   import pandas as pd
   import numpy as np
   from matplotlib import pyplot as plt
   import matplotlib.cm as cm
   import matplotlib.colors as colors
   from tqdm import tqdm
   class perceptron():
10
       def __init__(self,data1,data2):
11
           self.data1 = data1
12
           self.data2 = data2
13
           self.data = np.concatenate((data1,data2),axis=0)
14
           self.labels = [data1[0,-1],data2[0,-1]]
15
           self.weights = None
16
           self.error epoch = None
17
       def train(self,eta,epochs):
18
           y1 = np.ones((len(self.data1),1))
19
           y2 = -1*np.ones((len(self.data2),1))
20
           data = self.data
21
           N, dim = data[:,:-1].shape
22
           X = np.concatenate((np.ones((N,1)),data[:,:-1]),axis=1)
23
           y = np.concatenate((y1,y2),axis=0)
24
           Xy = np.concatenate((X,np.reshape(y,(len(y),1))),axis=1)
           w = np.random.rand(1,1+dim)
           e = 1
27
           error epoch = []
           pbar = tqdm(total=epochs,position=0,leave=True)
           while e<=epochs:</pre>
               e += 1
               pbar.update(1)
               np.random.shuffle(Xy)
               for i in range(N):
35
                    w = w + ((eta/2)*(Xy[i,-1]-np.sign(Xy[i,:-1]@w.T))*Xy[i,:-1])
               error = 0
               for i in range(N):
                    error += (1/2)*abs((Xy[i,-1]-np.sign(Xy[i,:-1]@w.T)))*
39
                    (Xy[i,:-1]@w.T)*Xy[i,-1]
               error_epoch.append(-error)
41
           pbar.close()
42
           self.weights = w
43
           self.error_epoch = np.array(error_epoch)
44
           return None
45
       def classify(self,data):
46
```

```
w = self.weights
47
           labels = self.labels
48
           l = [0] + labels
49
           return np.array([l[int(i)] for i in np.sign(np.concatenate((np.ones(
50
            (len(data),1)),data),axis=1)@w.T)])
51
       def plot error(self):
52
           plt.plot(self.error epoch)
53
           return None
54
55
   f = pd.read csv('17/train.csv', header = None)
56
   data tr0 = (f[f[2]==0]).to numpy()
57
   data tr1 = (f[f[2]==1]).to numpy()
58
   data_tr2 = (f[f[2]==2]).to_numpy()
59
   data tr3 = (f[f[2]==3]).to numpy()
   f = pd.read_csv('17/dev.csv',header = None)
61
   data_te0 = (f[f[2]==0]).to_numpy()
62
   data te1 = (f[f[2]==1]).to numpy()
   data te2 = (f[f[2]==2]).to numpy()
   data_te3 = (f[f[2]==3]).to_numpy()
   eta = 0.1
   epochs = 10
   #01
   p01 = perceptron(data tr0,data tr1)
   p01.train(eta,epochs)
   data_tr01 = np.concatenate((data_tr0,data_tr1),axis=0)
   train acc 01 = 100*((data tr01[:,-1]==p01.classify(data tr01[:,:-1]))
73
                        .mean())
74
   print('train_acc_01 = %f'%(train_acc_01))
   data te01 = np.concatenate((data te0,data te1),axis=0)
76
   test_acc_01 = 100*((data_te01[:,-1]==p01.classify(data_te01[:,:-1]))
                      .mean())
   print('test_acc_01 = %f'%(test_acc_01))
79
80
   #02
81
   p02 = perceptron(data_tr0,data_tr2)
82
   p02.train(eta,epochs)
83
   data_tr02 = np.concatenate((data_tr0,data_tr2),axis=0)
84
   train acc 02 = 100*((data tr02[:,-1]==p02.classify(data tr02[:,:-1]))
85
                        .mean())
   print('train_acc_02 = %f'%(train acc 02))
87
   data_te02 = np.concatenate((data_te0,data te2),axis=0)
88
   test acc 02 = 100*((data te02[:,-1]==p02.classify(data te02[:,:-1]))
89
                    .mean())
90
   print('test_acc_02 = %f'%(test_acc_02))
91
92
   #03
   p03 = perceptron(data tr0,data tr3)
94
   p03.train(eta,epochs)
   data tr03 = np.concatenate((data tr0,data tr3),axis=0)
```

```
train acc 03 = 100*((data tr03[:,-1]==p03.classify(data tr03[:,:-1]))
97
                       .mean())
98
   print('train acc 03 = %f'%(train acc 03))
99
   data_te03 = np.concatenate((data_te0,data te3),axis=0)
100
   test acc 03 = 100*((data te03[:,-1]==p03.classify(data te03[:,:-1]))
101
102
   print('test acc 03 = %f'%(test acc 03))
103
104
   p12 = perceptron(data tr1,data tr2)
105
   p12.train(eta,epochs)
106
   data tr12 = np.concatenate((data tr1,data tr2),axis=0)
107
   train acc 12 = 100*((data tr12[:,-1]==p12.classify(data tr12[:,:-1]))
108
                        .mean())
109
   print('train_acc_12 = %f'%(train acc 12))
110
   data te12 = np.concatenate((data te1,data te2),axis=0)
111
   test_acc_12 = 100*((data_te12[:,-1]==p12.classify(data_te12[:,:-1]))
112
                      .mean())
   print('test_acc_12 = %f'%(test_acc_12))
114
   p13 = perceptron(data_tr1,data_tr3)
   p13.train(eta,epochs)
   data tr13 = np.concatenate((data tr1,data tr3),axis=0)
   train_acc_13 = 100*((data_tr13[:,-1]==p13.classify(data_tr13[:,:-1]))
                       .mean())
120
   print('train acc 13 = %f'%(train acc 13))
121
   data_te13 = np.concatenate((data_te1,data_te3),axis=0)
   test acc 13 = 100*((data te13[:,-1]==p13.classify(data te13[:,:-1]))
123
                       .mean())
124
   print('test_acc_13 = %f'%(test_acc 13))
125
126
   p23 = perceptron(data_tr2,data_tr3)
127
   p23.train(eta,epochs)
128
   data_tr23 = np.concatenate((data_tr2,data_tr3),axis=0)
129
   train_acc_23 = 100*((data_tr23[:,-1]==p23.classify(data_tr23[:,:-1]))
130
                       .mean())
131
   print('train_acc_23 = %f'%(train_acc_23))
132
   data te23 = np.concatenate((data te2,data te3),axis=0)
133
   test acc 23 = 100*((data te23[:,-1]==p23.classify(data te23[:,:-1]))
134
                      .mean())
135
   print('test acc 23 = %f'%(test acc 23))
136
137
   #plots
138
   X train = data tr01
139
   X \text{ test} = \text{data te01}
140
   141
   # define bounds of the domain
142
   min1, max1 = X train[:, 0].min()-1, X train[:, 0].max()+1
   min2, max2 = X train[:, 1].min()-1, X train[:, 1].max()+1
144
145
   # define the x and y scale
```

```
x1 \text{ grid} = np.arange(min1, max1, 0.1)
147
   x2 grid = np.arange(min2, max2, 0.1)
148
149
   x1 grid, x2 grid = np.meshgrid(x1 grid, x2 grid)
150
151
   c1, c2 = x1 grid.flatten(), x1 grid.flatten()
152
   c1, c2 = x1 grid.reshape((len(c1), 1)), x2 grid.reshape((len(c2), 1))
153
154
   x = np.hstack((c1,c2))
155
156
   y_pred = p01.classify(x)
157
158
   x3_grid = y_pred.reshape(x1_grid.shape)
159
160
161
162
   fig = plt.figure(1,figsize=(7.5,4))
163
   ax = fig.add subplot(111)
164
   cmap =plt.get cmap('Paired',2)
   cs = ax.contourf(x1 grid, x2 grid, x3 grid, cmap=cmap)
   ax.scatter(X train[:,0],X train[:,1],marker='x',
            color = 'blue',label='train data')
168
   ax.scatter(X test[:,0],X test[:,1],marker='x',
169
            color='black',label='test data')
170
   ax.legend()
171
   ax.set_xlabel('x1',fontsize=10)
172
   ax.set ylabel('x2',fontsize=10)
173
   ax.set_title('Perceptron : Labels (0,1)', fontsize=10)
174
   cbar = plt.colorbar(cm.ScalarMappable(cmap=cmap),
175
                         ticks = [0.25, 0.75])
176
   cbar.ax.invert yaxis()
177
   cbar.set ticklabels(['0','1'])
178
179
   X_train = data_tr02
180
   X \text{ test} = \text{data te02}
181
   182
   # define bounds of the domain
183
   min1, max1 = X_train[:, 0].min()-1, X_train[:, 0].max()+1
184
   \min 2, \max 2 = X \text{ train}[:, 1].\min()-1, X \text{ train}[:, 1].\max()+1
185
186
   # define the x and y scale
187
   x1 grid = np.arange(min1, max1, 0.1)
188
   x2 grid = np.arange(min2, max2, 0.1)
189
190
   x1_grid, x2_grid = np.meshgrid(x1_grid, x2_grid)
191
192
   c1, c2 = x1 grid.flatten(), x1 grid.flatten()
193
   c1, c2 = x1 grid.reshape((len(c1), 1)),
194
            x2_grid.reshape((len(c2), 1))
195
```

```
x = np.hstack((c1,c2))
197
198
   y pred = p02.classify(x)
199
200
   x3_grid = y_pred.reshape(x1_grid.shape)
201
202
203
204
   fig = plt.figure(2,figsize=(7.5,4))
205
   ax = fig.add subplot(111)
206
   cmap =plt.get cmap('Paired',2)
207
   cs = ax.contourf(x1 grid, x2 grid, x3 grid, cmap=cmap)
208
   ax.scatter(X_train[:,0],X_train[:,1],marker='x',
209
               color = 'blue',label='train data')
210
   ax.scatter(X test[:,0],X test[:,1],marker='x',
211
                  color='black',label='test data')
212
   ax.legend()
   ax.set_xlabel('x1',fontsize=10)
214
   ax.set ylabel('x2',fontsize=10)
   ax.set title('Perceptron : Labels (0,2)', fontsize=10)
   cbar = plt.colorbar(cm.ScalarMappable(cmap=cmap), ticks = [0.25, 0.75])
   cbar.ax.invert yaxis()
   cbar.set_ticklabels(['0','2'])
219
220
   X \text{ train} = \text{data tr03}
221
   X \text{ test} = \text{data te03}
222
   223
   # define bounds of the domain
224
   min1, max1 = X_train[:, 0].min()-1, X_train[:, 0].max()+1
   \min 2, \max 2 = X \text{ train}[:, 1].\min()-1, X \text{train}[:, 1].\max()+1
226
227
   # define the x and y scale
228
   x1 \text{ grid} = np.arange(min1, max1, 0.1)
229
   x2_grid = np.arange(min2, max2, 0.1)
230
231
   x1_grid, x2_grid = np.meshgrid(x1_grid, x2 grid)
232
233
   c1, c2 = x1_grid.flatten(), x1_grid.flatten()
234
   c1, c2 = x1 grid.reshape((len(c1), 1)),
235
                x2 grid.reshape((len(c2), 1))
236
237
   x = np.hstack((c1,c2))
238
239
   y_pred = p03.classify(x)
240
241
   x3 grid = y pred.reshape(x1 grid.shape)
242
243
244
245
   fig = plt.figure(3,figsize=(7.5,4))
```

```
ax = fig.add_subplot(111)
247
   cmap =plt.get cmap('Paired',2)
248
   cs = ax.contourf(x1 grid, x2 grid, x3 grid, cmap=cmap)
249
   ax.scatter(X train[:,0],X train[:,1],marker='x',
250
                color = 'blue',label='train data')
251
   ax.scatter(X test[:,0],X test[:,1],marker='x',
252
               color='black',label='test data')
253
   ax.legend()
254
   ax.set_xlabel('x1',fontsize=10)
255
   ax.set ylabel('x2',fontsize=10)
256
   ax.set title('Perceptron : Labels (0,3)', fontsize=10)
257
   cbar = plt.colorbar(cm.ScalarMappable(cmap=cmap),
258
            ticks = [0.25, 0.75])
259
   cbar.ax.invert yaxis()
   cbar.set_ticklabels(['0','3'])
261
262
   X train = data tr12
   X \text{ test} = \text{data te} 12
   # define bounds of the domain
   min1, max1 = X train[:, 0].min()-1, X train[:, 0].max()+1
   min2, max2 = X train[:, 1].min()-1, X train[:, 1].max()+1
   # define the x and y scale
270
   x1 grid = np.arange(min1, max1, 0.1)
   x2_grid = np.arange(min2, max2, 0.1)
273
   x1 grid, x2 grid = np.meshgrid(x1 grid, x2 grid)
274
275
   c1, c2 = x1_grid.flatten(), x1_grid.flatten()
276
   c1, c2 = x1_grid.reshape((len(c1), 1)),
277
               x2 grid.reshape((len(c2), 1))
278
279
   x = np.hstack((c1,c2))
280
281
   y pred = p12.classify(x)
282
283
   x3_grid = y_pred.reshape(x1_grid.shape)
284
285
286
287
   fig = plt.figure(4,figsize=(7.5,4))
288
   ax = fig.add subplot(111)
289
   cmap =plt.get cmap('Paired',2)
290
   cs = ax.contourf(x1 grid, x2 grid, x3 grid, cmap=cmap)
291
   ax.scatter(X train[:,0],X train[:,1],marker='x',
292
               color = 'blue',label='train data')
293
   ax.scatter(X test[:,0],X test[:,1],marker='x',
294
                color='black',label='test data')
295
   ax.legend()
```

```
ax.set_xlabel('x1',fontsize=10)
297
   ax.set ylabel('x2',fontsize=10)
298
   ax.set_title('Perceptron : Labels (1,2)', fontsize=10)
299
   cbar = plt.colorbar(cm.ScalarMappable(cmap=cmap),
300
                        ticks = [0.25, 0.75])
301
   cbar.ax.invert yaxis()
302
   cbar.set ticklabels(['1','2'])
303
304
   X train = data tr13
305
   X test = data te13
306
   307
   # define bounds of the domain
308
   min1, max1 = X_train[:, 0].min()-1, X_train[:, 0].max()+1
309
   min2, max2 = X train[:, 1].min()-1, X train[:, 1].max()+1
311
   # define the x and y scale
312
   x1 grid = np.arange(min1, max1, 0.1)
   x2_grid = np.arange(min2, max2, 0.1)
314
   x1 grid, x2 grid = np.meshgrid(x1 grid, x2 grid)
   c1, c2 = x1 grid.flatten(), x1 grid.flatten()
   c1, c2 = x1_grid.reshape((len(c1), 1)),
                        x2 grid.reshape((len(c2), 1))
320
321
   x = np.hstack((c1,c2))
322
323
   y pred = p13.classify(x)
324
325
   x3_grid = y_pred.reshape(x1_grid.shape)
326
327
328
329
   fig = plt.figure(5,figsize=(7.5,4))
330
   ax = fig.add subplot(111)
331
   cmap =plt.get cmap('Paired',2)
332
   cs = ax.contourf(x1 grid, x2 grid, x3 grid, cmap=cmap)
333
   ax.scatter(X_train[:,0],X_train[:,1],marker='x',
334
                color = 'blue',label='train data')
335
   ax.scatter(X_test[:,0],X_test[:,1],marker='x',
336
                 color='black',label='test data')
337
   ax.legend()
338
   ax.set xlabel('x1',fontsize=10)
339
   ax.set ylabel('x2',fontsize=10)
340
   ax.set title('Perceptron : Labels (1,3)', fontsize=10)
341
   cbar = plt.colorbar(cm.ScalarMappable(cmap=cmap),
342
              ticks = [0.25, 0.75])
343
   cbar.ax.invert yaxis()
344
   cbar.set_ticklabels(['1','3'])
345
```

```
X_train = data_tr23
347
   X \text{ test} = \text{data te23}
348
   349
   # define bounds of the domain
350
   min1, max1 = X train[:, 0].min()-1, X train[:, 0].max()+1
351
   \min 2, \max 2 = X \text{ train}[:, 1].\min()-1, X \text{ train}[:, 1].\max()+1
352
353
   # define the x and y scale
354
   x1 grid = np.arange(min1, max1, 0.1)
355
   x2 grid = np.arange(min2, max2, 0.1)
356
357
   x1 grid, x2 grid = np.meshgrid(x1 grid, x2 grid)
358
359
   c1, c2 = x1 grid.flatten(), x1 grid.flatten()
360
   c1, c2 = x1 grid.reshape((len(c1), 1)),
361
              x2_grid.reshape((len(c2), 1))
362
   x = np.hstack((c1,c2))
364
   y_pred = p23.classify(x)
   x3 grid = y pred.reshape(x1 grid.shape)
369
370
371
   fig = plt.figure(6,figsize=(7.5,4))
372
   ax = fig.add_subplot(111)
373
   cmap =plt.get cmap('Paired',2)
374
   cs = ax.contourf(x1_grid, x2_grid, x3_grid, cmap=cmap)
   ax.scatter(X train[:,0],X train[:,1],marker='x',
376
                   color = 'blue',label='train data')
377
   ax.scatter(X_test[:,0],X_test[:,1],marker='x',
378
                color='black',label='test data')
379
   ax.legend()
380
   ax.set xlabel('x1',fontsize=10)
381
   ax.set_ylabel('x2',fontsize=10)
382
   ax.set title('Perceptron : Labels (2,3)', fontsize=10)
383
   cbar = plt.colorbar(cm.ScalarMappable(cmap=cmap),
384
                    ticks = [0.25, 0.75])
385
   cbar.ax.invert yaxis()
386
   cbar.set ticklabels(['2','3'])
387
388
   #1A part II MLFNN
389
390
   from sklearn import preprocessing
391
   import pandas as pd
392
   import numpy as np
393
   import torch as tc
394
   from matplotlib import pyplot as plt
   import matplotlib.cm as cm
```

```
import matplotlib.colors as colors
397
   from tqdm import tqdm
398
399
   f = pd.read csv('17/train.csv',header = None)
400
   data tr = f.to numpy()
401
   f = pd.read csv('17/dev.csv',header = None)
402
   data te = f.to numpy()
403
   #1 to K categorial 1 hot vector transformation
404
   labelenc = preprocessing.LabelBinarizer()
405
   Xtr = (tc.from numpy(data tr[:,:-1])).float()
406
   ytr = (tc.from_numpy(labelenc.fit_transform(data_tr[:,-1])))
407
                         .float()
408
   Xte = (tc.from_numpy(data_te[:,:-1])).float()
409
   yte = (tc.from numpy(labelenc.fit transform(data te[:,-1])))
410
                        .float()
411
412
   epochs = 10000
413
414
   inp 1 = 2
415
   hid l = 4
   out 1 = 4
   #activation fxns : Sigmoid, Tanh, SOftmax, ReLU, ELU, SELU, CELU,
   mlfnn = tc.nn.Sequential(tc.nn.Linear(inp_1,hid_1),
                             tc.nn.ELU(),tc.nn.Linear(hid 1,out 1))
420
   MSE = tc.nn.MSELoss()
421
   optimizer = tc.optim.SGD(mlfnn.parameters(), lr=0.001)
   from tqdm import tqdm
423
   epochs = 10000
424
   pbar = tqdm(total=epochs,position=0,leave=True)
425
   for i in range(epochs):
426
427
        optimizer.zero grad()
428
       ytrp = mlfnn(Xtr)
429
       loss = MSE(ytrp,ytr)
430
       loss.backward()
431
        optimizer.step()
432
       pbar.update(1)
433
   pbar.close()
434
   tr acc = 100*((data tr[:,-1] == labelenc.
435
                        inverse transform(mlfnn(Xtr))).mean())
436
   te_acc = 100*((data_te[:,-1] == labelenc.
437
                         inverse transform(mlfnn(Xte))).mean())
438
   print('train acc = %f'%(tr acc))
439
   print('test acc = %f'%(te acc))
440
441
   #plotting
442
   X train = data tr[:,:-1]
443
   X \text{ test} = \text{data te}[:,:-1]
444
   # define bounds of the domain
```

```
min1, max1 = X_train[:, 0].min()-1, X_train[:, 0].max()+1
447
   min2, max2 = X_train[:, 1].min()-1, X_train[:, 1].max()+1
448
449
   # define the x and y scale
450
   x1 grid = np.arange(min1, max1, 0.1)
451
   x2 grid = np.arange(min2, max2, 0.1)
452
453
   x1_grid, x2_grid = np.meshgrid(x1_grid, x2_grid)
454
455
   c1, c2 = x1 grid.flatten(), x1 grid.flatten()
456
   c1, c2 = x1 grid.reshape((len(c1), 1)), x2 grid.
457
                                 reshape((len(c2), 1))
458
459
   x = np.hstack((c1,c2))
460
461
   y_pred = labelenc.inverse_transform(mlfnn(tc.from_numpy(x)
462
                                           .float()))
463
464
   x3 grid = y pred.reshape(x1 grid.shape)
465
   fig = plt.figure(1,figsize=(7.5,4))
468
   ax = fig.add_subplot(111)
469
   cmap =plt.get cmap('Paired',4)
470
   cs = ax.contourf(x1 grid, x2 grid, x3 grid, cmap=cmap)
   ax.scatter(X_train[:,0],X_train[:,1],marker='x',
472
                     color = 'blue',label='train data')
473
   ax.scatter(X_test[:,0],X_test[:,1],marker='x',
474
                       color='black',label='test data')
475
   ax.legend()
476
   ax.set_xlabel('x1',fontsize=10)
477
   ax.set_ylabel('x2',fontsize=10)
478
   ax.set_title('MLFNN : All Four Labels', fontsize=10)
479
   cbar = plt.colorbar(cm.ScalarMappable(cmap=cmap),
480
                       ticks=np.linspace(0.125, 1-0.125, 4)
481
   cbar.ax.invert yaxis()
482
   cbar.set ticklabels(['0','1','2','3'])
483
484
   #1A part III linear sum
485
   import numpy as np
486
   import pandas as pd
487
   from sklearn.svm import SVC
488
   from matplotlib import pyplot as plt
489
   import matplotlib.cm as cm
490
   import matplotlib.colors as colors
491
   from tqdm import tqdm
492
493
   f = pd.read csv('17/train.csv',header = None)
494
   data_tr0 = (f[f[2]==0]).to_numpy()
   data_tr1 = (f[f[2]==1]).to_numpy()
```

```
data tr2 = (f[f[2]==2]).to numpy()
497
   data tr3 = (f[f[2]==3]).to numpy()
498
   f = pd.read_csv('17/dev.csv',header = None)
499
   data te0 = (f[f[2]==0]).to numpy()
500
   data te1 = (f[f[2]==1]).to numpy()
501
   data_te2 = (f[f[2]==2]).to numpy()
502
   data te3 = (f[f[2]==3]).to numpy()
503
504
   #01
505
   data tr01 = np.concatenate((data tr0,data tr1),axis=0)
506
   data te01 = np.concatenate((data te0,data te1),axis=0)
507
   svc01 = SVC(kernel='linear')
508
   svc01.fit(data_tr01[:,:-1],data_tr01[:,-1])
509
   train acc 01 = 100*((data tr01[:,-1]==svc01.
510
                         predict(data tr01[:,:-1])).mean())
511
   print('train_acc_01 = %f'%(train_acc_01))
512
   test acc 01 = 100*((data te01[:,-1]==svc01.
                         predict(data te01[:,:-1])).mean())
514
   print('test acc 01 = %f'%(test acc 01))
   #02
   data_tr02 = np.concatenate((data_tr0,data tr2),axis=0)
   data_te02 = np.concatenate((data_te0,data_te2),axis=0)
   svc02 = SVC(kernel='linear')
520
   svc02.fit(data tr02[:,:-1],data tr02[:,-1])
   train_acc_02 = 100*((data_tr02[:,-1]==svc02.
522
                         predict(data_tr02[:,:-1])).mean())
523
   print('train_acc_02 = %f'%(train_acc_02))
524
   test acc 02 = 100*((data te02[:,-1]==svc02.
525
                         predict(data te02[:,:-1])).mean())
526
   print('test_acc_02 = %f'%(test_acc 02))
527
528
   #03
529
   data tr03 = np.concatenate((data tr0,data tr3),axis=0)
530
   data te03 = np.concatenate((data te0,data te3),axis=0)
531
   svc03 = SVC(kernel='linear')
532
   svc03.fit(data tr03[:,:-1],data tr03[:,-1])
533
   train_acc_03 = 100*((data_tr03[:,-1]==svc03.
534
                         predict(data tr03[:,:-1])).mean())
535
   print('train acc 03 = %f'%(train acc 03))
536
   test acc 03 = 100*((data te03[:,-1]==svc03.
537
                          predict(data te03[:,:-1])).mean())
538
   print('test acc 03 = %f'%(test acc 03))
539
540
   #12
541
   data tr12 = np.concatenate((data tr1,data tr2),axis=0)
542
   data te12 = np.concatenate((data te1,data te2),axis=0)
543
   svc12 = SVC(kernel='linear')
544
   svc12.fit(data_tr12[:,:-1],data_tr12[:,-1])
   train acc 12 = 100*((data tr12[:,-1]==svc12.
```

```
predict(data_tr12[:,:-1])).mean())
547
   print('train_acc_12 = %f'%(train acc 12))
548
   test_acc_12 = 100*((data_te12[:,-1]==svc12.
549
                           predict(data te12[:,:-1])).mean())
550
   print('test_acc_12 = %f'%(test_acc_12))
551
552
   #13
553
   data_tr13 = np.concatenate((data_tr1,data_tr3),axis=0)
554
   data te13 = np.concatenate((data te1,data te3),axis=0)
555
   svc13 = SVC(kernel='linear')
556
   svc13.fit(data tr13[:,:-1],data tr13[:,-1])
557
   train acc 13 = 100*((data tr13[:,-1]==svc13.
558
                           predict(data_tr13[:,:-1])).mean())
559
   print('train_acc_13 = %f'%(train acc 13))
560
   test_acc_13 = 100*((data_te13[:,-1]==svc13.
561
                           predict(data_te13[:,:-1])).mean())
562
   print('test_acc_13 = %f'%(test_acc_13))
563
564
   #23
   data tr23 = np.concatenate((data tr2,data tr3),axis=0)
   data te23 = np.concatenate((data te2,data te3),axis=0)
   svc23 = SVC(kernel='linear')
   svc23.fit(data_tr23[:,:-1],data_tr23[:,-1])
   train acc 23 = 100*((data tr23[:,-1]==svc23.
570
                          predict(data tr23[:,:-1])).mean())
   print('train_acc_23 = %f'%(train_acc_23))
   test_acc_23 = 100*((data_te23[:,-1]==svc23.
573
                          predict(data te23[:,:-1])).mean())
574
   print('test_acc_23 = %f'%(test_acc_23))
576
   #plots
577
   X train = data tr01
578
   X_test = data_te01
579
   580
   # define bounds of the domain
581
   min1, max1 = X train[:, 0].min()-1, X train[:, 0].max()+1
582
   min2, max2 = X train[:, 1].min()-1, X train[:, 1].max()+1
583
584
   # define the x and y scale
585
   x1 \text{ grid} = np.arange(min1, max1, 0.1)
586
   x2 grid = np.arange(min2, max2, 0.1)
587
588
   x1_grid, x2_grid = np.meshgrid(x1_grid, x2_grid)
589
590
   c1, c2 = x1 grid.flatten(), x1 grid.flatten()
591
   c1, c2 = x1 grid.reshape((len(c1), 1)), x2 grid.
592
                             reshape((len(c2), 1))
593
594
   x = np.hstack((c1,c2))
595
596
```

```
y pred = svc01.predict(x)
597
598
   x3 grid = y pred.reshape(x1 grid.shape)
599
600
   suppvec = svc01.support vectors
601
602
   fig = plt.figure(1, figsize=(7.5, 4))
603
   ax = fig.add subplot(111)
604
   cmap =plt.get cmap('Paired',2)
605
   cs = ax.contourf(x1 grid, x2 grid, x3 grid, cmap=cmap)
606
   ax.scatter(X train[:,0],X train[:,1],marker='x',
607
                          color = 'blue',label='train data')
608
   ax.scatter(suppvec[:,0],suppvec[:,1],marker='x',
609
                      color='yellow',label='support vector')
610
   ax.scatter(X test[:,0],X test[:,1],marker='x',
611
                              color='black',label='test data')
612
   ax.legend()
   ax.set_xlabel('x1',fontsize=10)
614
   ax.set ylabel('x2',fontsize=10)
   ax.set title('SVM : Labels (0,1)', fontsize=10)
   cbar = plt.colorbar(cm.ScalarMappable(cmap=cmap),
                                  ticks = [0.25, 0.75])
618
   cbar.ax.invert yaxis()
619
   cbar.set ticklabels(['0','1'])
620
621
622
623
   X_train = data_tr02
624
   X \text{ test} = \text{data te02}
625
   626
   # define bounds of the domain
627
   min1, max1 = X train[:, 0].min()-1, X train[:, 0].max()+1
628
   min2, max2 = X_train[:, 1].min()-1, X_train[:, 1].max()+1
629
630
   # define the x and y scale
631
   x1 \text{ grid} = np.arange(min1, max1, 0.1)
632
   x2 grid = np.arange(min2, max2, 0.1)
633
634
   x1 grid, x2 grid = np.meshgrid(x1 grid, x2 grid)
635
636
   c1, c2 = x1_grid.flatten(), x1_grid.flatten()
637
   c1, c2 = x1 grid.reshape((len(c1), 1)),
638
                 x2 grid.reshape((len(c2), 1))
639
640
   x = np.hstack((c1,c2))
641
642
   y pred = svc02.predict(x)
643
644
   x3_grid = y_pred.reshape(x1_grid.shape)
645
```

```
suppvec = svc02.support_vectors_
647
648
   fig = plt.figure(2,figsize=(7.5,4))
649
   ax = fig.add subplot(111)
650
   cmap =plt.get cmap('Paired',2)
651
   cs = ax.contourf(x1 grid, x2 grid, x3 grid, cmap=cmap)
652
   ax.scatter(X train[:,0],X train[:,1],marker='x',
653
                 color = 'blue',label='train data')
654
   ax.scatter(suppvec[:,0],suppvec[:,1],marker='x',
655
                color='yellow',label='support vector')
656
   ax.scatter(X test[:,0],X test[:,1],marker='x',
657
                      color='black',label='test data')
658
   ax.legend()
659
   ax.set xlabel('x1',fontsize=10)
660
   ax.set ylabel('x2',fontsize=10)
661
   ax.set_title('SVM : Labels (0,2)', fontsize=10)
662
   cbar = plt.colorbar(cm.ScalarMappable(cmap=cmap),
                                 ticks = [0.25, 0.75])
664
   cbar.ax.invert yaxis()
665
   cbar.set ticklabels(['0','2'])
   X \text{ train} = \text{data tr03}
   X \text{ test} = \text{data te03}
   670
   # define bounds of the domain
671
   min1, max1 = X_train[:, 0].min()-1, X_train[:, 0].max()+1
   min2, max2 = X train[:, 1].min()-1, X train[:, 1].max()+1
673
674
   # define the x and y scale
   x1 grid = np.arange(min1, max1, 0.1)
676
   x2_grid = np.arange(min2, max2, 0.1)
677
678
   x1_grid, x2_grid = np.meshgrid(x1_grid, x2_grid)
679
680
   c1, c2 = x1 grid.flatten(), x1 grid.flatten()
681
   c1, c2 = x1 grid.reshape((len(c1), 1)), x2 grid.
682
                                 reshape((len(c2), 1))
683
684
   x = np.hstack((c1,c2))
685
686
   y_pred = svc03.predict(x)
687
688
   x3 grid = y pred.reshape(x1 grid.shape)
689
690
   suppvec = svc03.support vectors
691
692
   fig = plt.figure(3,figsize=(7.5,4))
693
   ax = fig.add subplot(111)
694
   cmap =plt.get_cmap('Paired',2)
695
   cs = ax.contourf(x1 grid, x2 grid, x3 grid, cmap=cmap)
```

```
ax.scatter(X_train[:,0],X_train[:,1],marker='x',
697
                    color = 'blue',label='train data')
698
   ax.scatter(suppvec[:,0],suppvec[:,1],marker='x',
699
                color='yellow',label='support vector')
700
   ax.scatter(X_test[:,0],X_test[:,1],marker='x',
701
                      color='black',label='test data')
702
   ax.legend()
703
   ax.set xlabel('x1',fontsize=10)
704
   ax.set_ylabel('x2',fontsize=10)
705
   ax.set title('SVM : Labels (0,3)', fontsize=10)
706
   cbar = plt.colorbar(cm.ScalarMappable(cmap=cmap),
707
                                 ticks = [0.25, 0.75])
708
   cbar.ax.invert yaxis()
709
   cbar.set ticklabels(['0','3'])
   X_train = data_tr12
712
   X \text{ test} = \text{data te} 12
   # define bounds of the domain
   min1, max1 = X train[:, 0].min()-1, X train[:, 0].max()+1
   min2, max2 = X train[:, 1].min()-1, X train[:, 1].max()+1
   # define the x and y scale
719
   x1 grid = np.arange(min1, max1, 0.1)
720
   x2 grid = np.arange(min2, max2, 0.1)
722
   x1 grid, x2 grid = np.meshgrid(x1 grid, x2 grid)
723
724
   c1, c2 = x1_grid.flatten(), x1_grid.flatten()
   c1, c2 = x1 grid.reshape((len(c1), 1)), x2 grid.
726
                               reshape((len(c2), 1))
727
728
   x = np.hstack((c1,c2))
729
730
   y pred = svc12.predict(x)
731
732
   x3 grid = y pred.reshape(x1 grid.shape)
733
734
   suppvec = svc12.support vectors
735
736
   fig = plt.figure(4, figsize=(7.5, 4))
737
   ax = fig.add subplot(111)
738
   cmap =plt.get cmap('Paired',2)
739
   cs = ax.contourf(x1_grid, x2_grid, x3_grid, cmap=cmap)
740
   ax.scatter(X train[:,0],X train[:,1],marker='x',
741
                   color = 'blue',label='train data')
742
   ax.scatter(suppvec[:,0],suppvec[:,1],marker='x',
743
                 color='yellow',label='support vector')
744
   ax.scatter(X_test[:,0],X_test[:,1],marker='x',
745
                      color='black',label='test data')
```

```
ax.legend()
747
   ax.set xlabel('x1',fontsize=10)
748
   ax.set_ylabel('x2',fontsize=10)
749
   ax.set_title('SVM : Labels (1,2)', fontsize=10)
750
   cbar = plt.colorbar(cm.ScalarMappable(cmap=cmap),
751
                                 ticks = [0.25, 0.75])
752
   cbar.ax.invert yaxis()
753
   cbar.set ticklabels(['1','2'])
754
755
   X train = data tr13
756
   X \text{ test} = \text{data te13}
757
   758
   # define bounds of the domain
   min1, max1 = X train[:, 0].min()-1, X train[:, 0].max()+1
   min2, max2 = X train[:, 1].min()-1, X train[:, 1].max()+1
761
762
   # define the x and y scale
   x1 grid = np.arange(min1, max1, 0.1)
764
   x2 grid = np.arange(min2, max2, 0.1)
   x1 grid, x2 grid = np.meshgrid(x1 grid, x2 grid)
767
   c1, c2 = x1_grid.flatten(), x1_grid.flatten()
769
   c1, c2 = x1_grid.reshape((len(c1), 1)), x2_grid.
770
                               reshape((len(c2), 1))
   x = np.hstack((c1,c2))
773
774
   y_pred = svc13.predict(x)
776
   x3_grid = y_pred.reshape(x1_grid.shape)
777
778
   suppvec = svc13.support_vectors_
779
780
   fig = plt.figure(5, figsize=(7.5, 4))
781
   ax = fig.add subplot(111)
782
   cmap =plt.get cmap('Paired',2)
783
   cs = ax.contourf(x1_grid, x2_grid, x3_grid, cmap=cmap)
784
   ax.scatter(X train[:,0],X train[:,1],marker='x',
785
                           color = 'blue',label='train data')
786
   ax.scatter(suppvec[:,0],suppvec[:,1],marker='x',
787
                       color='yellow',label='support vector')
788
   ax.scatter(X test[:,0],X test[:,1],marker='x',
789
                            color='black',label='test data')
790
   ax.legend()
791
   ax.set_xlabel('x1',fontsize=10)
792
   ax.set ylabel('x2',fontsize=10)
793
   ax.set title('SVM : Labels (1,3)', fontsize=10)
794
   cbar = plt.colorbar(cm.ScalarMappable(cmap=cmap), ticks =[0.25,0.75])
   cbar.ax.invert yaxis()
```

```
cbar.set ticklabels(['1','3'])
797
798
   X train = data tr23
799
   X \text{ test} = \text{data te23}
800
   801
   # define bounds of the domain
802
   min1, max1 = X train[:, 0].min()-1, X train[:, 0].max()+1
803
   min2, max2 = X train[:, 1].min()-1, X train[:, 1].max()+1
804
805
   # define the x and y scale
806
   x1 grid = np.arange(min1, max1, 0.1)
807
   x2 grid = np.arange(min2, max2, 0.1)
808
809
   x1 grid, x2 grid = np.meshgrid(x1 grid, x2 grid)
811
   c1, c2 = x1_grid.flatten(), x1_grid.flatten()
812
   c1, c2 = x1 grid.reshape((len(c1), 1)), x2 grid.
                               reshape((len(c2), 1))
814
   x = np.hstack((c1,c2))
   y pred = svc23.predict(x)
   x3_grid = y_pred.reshape(x1 grid.shape)
820
   suppvec = svc23.support vectors
822
823
   fig = plt.figure(6,figsize=(7.5,4))
824
   ax = fig.add subplot(111)
   cmap =plt.get cmap('Paired',2)
826
   cs = ax.contourf(x1_grid, x2_grid, x3_grid, cmap=cmap)
827
   ax.scatter(X train[:,0],X train[:,1],marker='x',
828
                    color = 'blue',label='train data')
829
   ax.scatter(suppvec[:,0],suppvec[:,1],marker='x',
830
                color='yellow',label='support vector')
831
   ax.scatter(X test[:,0],X test[:,1],marker='x',
832
                      color='black',label='test data')
833
   ax.legend()
834
   ax.set xlabel('x1',fontsize=10)
835
   ax.set_ylabel('x2',fontsize=10)
836
   ax.set title('SVM : Labels (2,3)', fontsize=10)
837
   cbar = plt.colorbar(cm.ScalarMappable(cmap=cmap),
838
                                 ticks = [0.25, 0.75])
839
   cbar.ax.invert yaxis()
840
   cbar.set ticklabels(['2','3'])
841
```

# II Pattern classification on non-linearly separable data

II.1 K nearest Neighbours Method and Bayes classifier with KNN for density estimation

#### II.1.1 Python Code

```
# In[1]:
  # Import Relevant Libraries
  import numpy as np
  import pandas as pd
  import matplotlib.pyplot as plt
  from sklearn.metrics import confusion_matrix
  from mlxtend.plotting import plot confusion matrix
  from sklearn.metrics import accuracy score
  import torch
  from tqdm import tqdm
11
12
  import torch.nn as nn
  import torch.nn.functional as F
  import torch.optim as optim
  from functools import partial
  # In[2]:
20
  # Read Data
21
  # train data
  train data = pd.read csv("datasets/Dataset 1b/train.csv", header=None)
23
24
  # shuffle dataset
25
  train data = train data.sample(frac=1)
26
27
  # get train data
28
  train_data = np.array(train_data)
29
30
  # test data
31
  test data = pd.read csv("datasets/Dataset 1b/dev.csv", header=None)
32
33
  # shuffle dataset
34
  test_data = test_data.sample(frac=1)
35
36
  # get test data
37
  test data = np.array(test data)
38
39
  40
  # In[3]:
42
  # Split training data
  # length of data for fit
```

```
train len = int(np.shape(train data)[0])
45
   val len = int(np.shape(test data)[0]*0.5)
46
   test len = int(np.shape(test data)[0]*0.5)
47
  X train = train data[:,0:2]
49
  X val = test data[0:val len,0:2]
50
   X test = test data[val len:val len+test len,0:2]
51
52
  y_train = train_data[:,2]
53
   y val = test data[0:val len,2]
54
   y test = test data[val len:val len+test len,2]
55
56
   57
   # In[4]:
59
60
   # Build MLFFNN with 2 hidden layers using pytorch
61
   class Net(nn.Module):
       def __init__(self):
           super(Net, self).__init__()
           # in_features = input dimension out_features -> to be tuned
           self.fc1 = nn.Linear(in features=2, out features=4)
68
           # out_features -> to be tuned
           self.fc2 = nn.Linear(in_features=4, out_features=4)
72
           # out_features = number of classes to be predicted
           self.fc3 = nn.Linear(in features=4, out features=3)
74
75
       def forward(self, x):
76
           x = F.relu(self.fc1(x))
77
           out1 = x
78
           x = F.relu(self.fc2(x))
79
           out2 = x
80
           x = self.fc3(x)
81
           return x,out1,out2
82
83
   # In[5]:
84
85
   # Initialize neural network class
86
   net = Net()
87
88
   # # transfer the model to GPU if available
89
   # if torch.cuda.is available():
90
         print("using GPU")
        net = net.cuda()
92
  # In[6]:
```

```
95
   96
   # Define a Loss function and optimizer
97
98
   # Both variables are to be tuned
99
   num epochs = 500
                            # desired number of training epochs.
100
   learning rate = 0.001
101
102
   # loss function and optimizers can be changed
103
   criterion = nn.CrossEntropyLoss()
104
   optimizer = optim.Adam(net.parameters(), lr=learning_rate,weight_decay=5e-4)
105
106
   num_params = np.sum([p.nelement() for p in net.parameters()])
107
   print(num params, ' parameters')
108
109
   # In[7]:
110
   # create dataloader for loading data
   class myDataset(torch.utils.data.Dataset):
     #'Characterizes a dataset for PyTorch'
     def init (self, X, y, total samples):
116
           #'Initialization'
           self.X = X
118
           self.y = y
           self.total_samples = total_samples
120
121
     def __len__(self):
122
           #'Denotes the total number of samples'
123
           return self.total samples
124
125
     def __getitem__(self, index):
126
            #'Generates one sample of data'
127
            # Select sample
128
            # Load data and get label
129
130
           x data = self.X[index,:]
131
           y_data = self.y[index]
132
133
           return x data, y data
134
135
   # batch size can be changed to make epochs faster
136
   params = {'batch size': 16,
137
              'shuffle': False,
138
              'num workers': 0}
139
140
   # training dataset
141
   training set = myDataset(X train,y train,train len)
142
143
   training generator = torch.utils.data.DataLoader(training set, **params)
```

```
145
    # validation dataset
146
   validation_set = myDataset(X_val,y_val,val_len)
147
   validation generator = torch.utils.data.DataLoader(validation set, **params)
148
149
    # test dataset
150
   test set = myDataset(X test,y test,test len)
151
152
   test_generator = torch.utils.data.DataLoader(test_set, **params)
153
154
    # In[8]:
155
156
   def validation(model, loader):
157
        total loss = 0
158
        accuracy = []
159
        tq = partial(tqdm, position=0, leave=True)
160
161
        model.eval()
162
        with torch.no_grad():
             for X, y in tq(loader):
164
               X = X.float()
165
               y = y.long()
166
               # if torch.cuda.is_available():
168
                  X = X.cuda()
                   y = y.cuda()
170
171
               prediction,_,_ = model(X)
172
173
               loss = criterion(prediction, y)
174
175
               prediction = F.softmax(prediction)
176
177
               acc = np.mean(np.array((torch.argmax(prediction,1) == y)))*100
178
179
180
               total loss += loss.item()
181
               accuracy.append(acc)
182
183
        # print('Validation Accuracy: ', np.mean(np.array(accuracy)))
184
        return total_loss/len(loader),np.mean(np.array(accuracy))
185
186
187
    # In[9]:
188
189
   def test(model, loader):
190
        y pred = []
191
        accuracy = []
192
        tq = partial(tqdm, position=0, leave=True)
193
194
```

```
model.eval()
195
        with torch.no_grad():
196
            for X, y in tq(loader):
197
              X = X.float()
198
              y = y.long()
199
200
              # if torch.cuda.is available():
201
                   X = X.cuda()
202
                   y = y.cuda()
203
204
              prediction,_,_ = model(X)
205
206
              prediction = F.softmax(prediction)
207
208
              acc = np.mean(np.array((torch.argmax(prediction,1) == y)))*100
209
210
              accuracy.append(acc)
212
              prediction = torch.argmax(prediction,1)
              y_pred = y_pred + list(np.array(prediction))
        print('Test Accuracy: ', np.mean(np.array(accuracy)))
        return y_pred,np.mean(np.array(accuracy))
218
   # Tn \Gamma7:
220
   def surface_plot(x1_grid,x2_grid,out1,out2,out3):
221
222
        for i in range (0,4):
            x3_grid = out1[:,i].detach().numpy()
224
            x3_grid = x3_grid.reshape(np.shape(x1_grid))
225
226
            fig = plt.figure(figsize=(16,12))
227
            ax = fig.add_subplot(111,projection='3d')
228
            ax.plot surface(x1 grid,x2 grid,x3 grid,cmap='rainbow')
229
            ax.set_xlabel('X-axis(x1)',fontsize = 15)
230
            ax.set ylabel('Y-axis(x2)',fontsize = 15)
231
            ax.set_zlabel('Z-axis(Node Output)',fontsize = 15)
232
            ax.set title('Hidden Layer 1: Node' + str(i+1), fontsize=20)
233
234
            x3 grid = out2[:,i].detach().numpy()
235
            x3_grid = x3_grid.reshape(np.shape(x1_grid))
236
237
            fig = plt.figure(figsize=(16,12))
238
            ax = fig.add subplot(111,projection='3d')
239
            ax.plot surface(x1 grid,x2 grid,x3 grid,cmap='rainbow')
240
            ax.set xlabel('X-axis(x1)',fontsize = 15)
241
            ax.set ylabel('Y-axis(x2)',fontsize = 15)
242
            ax.set_zlabel('Z-axis(Node Output)',fontsize = 15)
243
            ax.set_title('Hidden Layer 2: Node' + str(i+1), fontsize=20)
```

```
245
        for i in range (0,3):
246
             x3 grid = out3[:,i].detach().numpy()
247
             x3_grid = x3_grid.reshape(np.shape(x1_grid))
248
249
             fig = plt.figure(figsize=(16,12))
250
             ax = fig.add subplot(111,projection='3d')
251
             ax.plot_surface(x1_grid,x2_grid,x3_grid,cmap='rainbow')
252
             ax.set_xlabel('X-axis(x1)',fontsize = 15)
253
             ax.set ylabel('Y-axis(x2)',fontsize = 15)
254
             ax.set_zlabel('Z-axis(Node Output)',fontsize = 15)
255
             ax.set title('Output Layer: Node' + str(i+1), fontsize=20)
256
257
258
259
260
    # In[10]:
262
    tq = partial(tqdm, position=0, leave=True)
    print('Start Training')
    train loss list = []
    train_accuracy_list = []
268
    validation loss list = []
269
    validation_accuracy_list = []
270
271
    for epoch in range(0,num_epochs):
272
      print('epoch ', epoch + 1)
      loss = 0
274
      train_accuracy = []
275
276
      for X,y in tq(training_generator):
277
278
        X = X.float()
279
        y = y.long()
280
        # y = torch.squeeze(y,1)
281
282
        # if torch.cuda.is available():
283
               X = X.cuda()
284
               y = y.cuda()
285
286
287
        optimizer.zero_grad()
288
289
        output,out1,out2 = net(X)
290
        loss = criterion(output,y)
291
292
        loss.backward()
293
        optimizer.step()
```

```
295
        loss += loss.item()
296
297
        prediction = F.softmax(output)
298
299
        accuracy = np.mean(np.array((torch.argmax(prediction,1) == y)))*100
300
        train accuracy.append(accuracy)
301
302
303
304
      train_loss_list.append([loss/len(training_generator)])
305
      # print(loss/len(training_generator))
306
307
      train accuracy list.append(np.mean(np.array(train accuracy)))
308
309
      val_loss,val_accuracy = validation(net, validation_generator)
310
      validation_loss_list.append(val_loss)
      validation accuracy list.append(val accuracy)
      if epoch == 0 or epoch == 4 or epoch == 19 or epoch == 99
      or epoch == num epochs-1:
          torch.save(net.state_dict(), 'models/model-'+str(epoch)+'.pth')
318
   print(train_accuracy_list[-1])
320
   print(validation_accuracy_list[-1])
321
322
    # In [7]:
323
   net = Net()
324
325
    # Import saved Model
326
   net.load_state_dict(torch.load('models/model-499.pth'))
327
   net.eval()
328
329
    # In[11]:
330
331
    # plt.plot(train_loss_list,label='Training Loss')
332
   plt.plot(validation_loss_list,label='Validation Loss')
333
   plt.xlabel('Number of Epochs')
334
   plt.ylabel('Loss')
335
   plt.title('Loss curve')
336
   plt.legend()
337
   plt.plot()
338
339
    # In[12]:
340
   plt.plot(train accuracy list,label='Training Accuracy')
342
   plt.plot(validation_accuracy_list,label='Validation Accuracy')
   plt.xlabel('Number of Epochs')
```

```
plt.ylabel('Accuracy')
   plt.title('Accuracy curve')
346
   plt.legend()
347
   plt.show()
348
349
   # In[13]:
350
351
   y_pred, test_accuracy = test(net,test_generator)
352
   print(test accuracy)
353
   c matrix = confusion matrix(y test, y pred)
354
355
   afig, ax = plot confusion matrix(conf mat=c matrix,figsize=(7,7),cmap=plt.cm.RdBu)
356
   ax.set(title = "Confusion Matrix for test data")
357
358
359
   y_pred, train_accuracy = test(net,training_generator)
360
   c_matrix = confusion_matrix(y_train, y_pred)
   afig, ax = plot confusion matrix(conf mat=c matrix,figsize=(7,7),cmap=plt.cm.RdBu)
   ax.set(title = "Confusion Matrix for train data")
   # In[14]:
367
368
   369
   # define bounds of the domain
   min1, max1 = X_train[:, 0].min()-1, X_train[:, 0].max()+1
371
   min2, max2 = X_train[:, 1].min()-1, X_train[:, 1].max()+1
372
   # define the x and y scale
374
   x1_grid = np.arange(min1, max1, 0.1)
375
   x2 grid = np.arange(min2, max2, 0.1)
376
377
   x1_grid, x2_grid = np.meshgrid(x1_grid, x2_grid)
378
379
   c1, c2 = x1_grid.flatten(), x1_grid.flatten()
380
   c1, c2 = x1 grid.reshape((len(c1), 1)), x2 grid.reshape((len(c2), 1))
381
382
   x = np.hstack((c1,c2))
383
384
   tq = partial(tqdm, position=0, leave=True)
385
386
   net.eval()
387
   y pred = []
388
389
   with torch.no grad():
390
       x = torch.from numpy(x)
391
       x = x.float()
392
393
       # if torch.cuda.is available():
```

```
x = x.cuda()
395
396
       output,out1,out2 = net(x)
397
       prediction = F.softmax(output)
398
       prediction = torch.argmax(prediction,1)
399
       y_pred = y_pred + list(np.array(prediction.cpu()))
400
       surface_plot(x1_grid,x2_grid,out1, out2, output)
401
402
   y_pred = np.array(y pred)
403
404
   x3_grid = y_pred.reshape(x1_grid.shape)
405
406
   # In[]:
407
   fig = plt.figure(figsize=(11,11))
408
   ax = fig.add subplot(111)
409
   ax.contourf(x1_grid, x2_grid, x3_grid, cmap='Pastel1')
410
   ax.scatter(X train[:,0],X train[:,1],marker='x')
   # ax.scatter(X test[:,0], X test[:,1], marker='x')
   ax.set xlabel('x1',fontsize=20)
   ax.set ylabel('x2',fontsize=20)
   ax.set_title('MLFFNN', fontsize=20)
   # In[15]:
418
419
   # Non-linear SVM
420
   from sklearn.svm import SVC
421
   from sklearn.multiclass import OneVsRestClassifier
422
423
   # In [16]:
424
425
   # Gaussian Kernel
426
   clf = OneVsRestClassifier(SVC(C=4,kernel='rbf')).fit(X train, y train)
427
428
429
   y_pred = clf.predict(X_train)
430
   train_accuracy = accuracy_score(y_train,y_pred)*100
431
   print("train accuracy: " , train_accuracy)
432
433
   c matrix = confusion matrix(y train, y pred)
434
435
   afig, ax = plot confusion matrix(conf mat=c matrix,figsize=(7,7),cmap=plt.cm.RdBu)
436
   ax.set(title = "Confusion Matrix for train data")
437
438
   y pred = clf.predict(X val)
439
   val_accuracy = accuracy_score(y_val,y_pred)*100
440
   print("validation accuracy: " , val accuracy)
441
   y_pred = clf.predict(X_test)
443
   test accuracy = accuracy score(y test,y pred)*100
```

```
print("test accuracy: " , test_accuracy)
445
446
   c matrix = confusion matrix(y test, y pred)
447
448
   afig, ax = plot confusion matrix(conf mat=c matrix,figsize=(7,7),cmap=plt.cm.RdBu)
449
   ax.set(title = "Confusion Matrix for test data")
450
451
   # In[17]:
452
453
   # Poly Kernel
454
   clf = OneVsRestClassifier(SVC(kernel='poly',degree=11)).fit(X_train, y train)
455
456
   y_pred = clf.predict(X_train)
457
   train accuracy = accuracy score(y train,y pred)*100
458
   print("train accuracy: " , train accuracy)
459
460
   c matrix = confusion matrix(y train, y pred)
   afig, ax = plot confusion matrix(conf mat=c matrix,figsize=(7,7),cmap=plt.cm.RdBu)
   ax.set(title = "Confusion Matrix for train data")
   y_pred = clf.predict(X_val)
   val_accuracy = accuracy_score(y_val,y_pred)*100
   print("validation accuracy: " , val accuracy)
468
469
   y_pred = clf.predict(X_test)
470
   test_accuracy = accuracy_score(y_test,y_pred)*100
471
   print("test accuracy: " , test_accuracy)
472
   c_matrix = confusion_matrix(y_test, y_pred)
474
475
   afig, ax = plot confusion matrix(conf mat=c matrix,figsize=(7,7),cmap=plt.cm.RdBu)
476
   ax.set(title = "Confusion Matrix for test data")
477
478
479
   # In[18]:
480
481
482
   483
   # define bounds of the domain
484
   min1, max1 = X_train[:, 0].min()-1, X_train[:, 0].max()+1
485
   min2, max2 = X train[:, 1].min()-1, X train[:, 1].max()+1
486
487
   # define the x and y scale
488
   x1 grid = np.arange(min1, max1, 0.1)
489
   x2 grid = np.arange(min2, max2, 0.1)
490
   x1 grid, x2 grid = np.meshgrid(x1 grid, x2 grid)
492
493
   c1, c2 = x1 grid.flatten(), x1_grid.flatten()
```

```
c1, c2 = x1_grid.reshape((len(c1), 1)), x2_grid.reshape((len(c2), 1))
495
496
   x = np.hstack((c1,c2))
497
498
   y_pred = clf.predict(x)
499
500
   x3 grid = y pred.reshape(x1 grid.shape)
501
502
503
   fig = plt.figure(figsize=(11,11))
504
   ax = fig.add subplot(111)
505
   ax.contourf(x1 grid, x2 grid, x3 grid, cmap='Pastel1')
506
   ax.scatter(X_train[:,0],X_train[:,1],marker='x',label='Training Points')
507
   for i in range (0,3):
508
        support vectors = clf.estimators [i].support vectors
509
        ax.scatter(support_vectors[:,0],support_vectors[:,1],marker='x',
510
                    label='Support Vectors '+str(i))
512
   ax.set_xlabel('x1',fontsize=20)
   ax.set_ylabel('x2',fontsize=20)
   ax.set_title('Support Vector Classifier', fontsize=20)
   ax.legend()
```

## III Static Pattern Classification on Real World Dataset 2A

#### III.1 Python Code

```
# In[1]:
  # Import Relevant Libraries
  import numpy as np
  import pandas as pd
  import matplotlib.pyplot as plt
  from sklearn.metrics import confusion_matrix
  from mlxtend.plotting import plot confusion matrix
  from sklearn.metrics import accuracy score
  import torch
10
  from tqdm import tqdm
11
12
  import torch.nn as nn
13
   import torch.nn.functional as F
14
   import torch.optim as optim
15
   from functools import partial
16
17
   18
19
   # In[2]:
20
   21
   # train data
22
   coast train data = np.array(pd.read csv('datasets/Dataset 2a/coast
23
                                        /train.csv'))[:,1:]
24
  forest train data = np.array(pd.read csv('datasets/Dataset 2a/forest
                                         /train.csv'))[:,1:]
26
  mountain_train_data =np.array(pd.read_csv('datasets/Dataset_2a/mountain
27
                                          /train.csv'))[:,1:]
   country train data = np.array(pd.read csv('datasets/Dataset 2a/opencountry
                                          /train.csv'))[:,1:]
  street_train_data = np.array(pd.read_csv('datasets/Dataset_2a/street
                                          /train.csv'))[:,1:]
   # populate class vector
  target 0 = np.zeros((coast train data.shape[0],1))
  target 1 = np.ones((forest train data.shape[0],1))
36
  target 2 = np.ones((mountain train data.shape[0],1))*2
  target_3 = np.ones((country_train_data.shape[0],1))*3
  target 4 = np.ones((street train data.shape[0],1))*4
39
40
  X train = np.array(np.concatenate((coast train data, forest train data,
41
               mountain_train_data,country_train_data,street_train_data),
42
               axis=0),dtype=float)
43
  y train = np.array(np.concatenate((target 0, target 1, target 2,
44
                        target 3,target 4),axis=0),dtype=float)
45
  y train = np.reshape(y train,(np.size(y train,)))
```

```
47
   # test & val data
48
   coast_test_data = np.array(pd.read csv('datasets/Dataset 2a/coast
49
                                        /dev.csv'))[:,1:]
50
  forest test data = np.array(pd.read csv('datasets/Dataset 2a/forest
51
                                        /dev.csv'))[:,1:]
52
  mountain test data = np.array(pd.read csv('datasets/Dataset 2a/mountain
53
                                         /dev.csv'))[:,1:]
54
   country test data = np.array(pd.read csv('datasets/Dataset 2a/opencountry
55
                                         /dev.csv'))[:,1:]
56
   street_test_data = np.array(pd.read csv('datasets/Dataset 2a/street
57
                                          /dev.csv'))[:,1:]
58
59
   # populate class vector
60
  target 0 = np.zeros((coast test data.shape[0],1))
61
  target 1 = np.ones((forest test data.shape[0],1))
62
  target 2 = np.ones((mountain test data.shape[0],1))*2
  target 3 = np.ones((country test data.shape[0],1))*3
  target 4 = np.ones((street test data.shape[0],1))*4
  X dev = np.array(np.concatenate((coast test data, forest test data,
                   mountain test data, country test data,
                   street test data),axis=0),dtype=float)
  y dev = np.array(np.concatenate((target 0, target 1,
70
                   target 2,target 3,target 4),axis=0),dtype=float)
  y dev = np.reshape(y dev,(np.size(y dev,)))
   73
74
   # In [3]:
75
   # Split training data
76
   # length of data for fit
77
  train len = int(np.shape(X train)[0])
78
79
  index1 = np.random.choice([True,False],size=np.shape(X dev)[0])
80
  index2 = ~index1
81
82
  X_val = X_dev[index1,:]
83
  X test = X dev[index2,:]
84
85
  y val = y dev[index1]
86
  y_test = y_dev[index2]
87
88
  val len = int(np.shape(X val)[0])
89
   test len = int(np.shape(X test)[0])
90
91
92
   93
94
   # In[4]:
95
```

```
# Build MLFFNN with 2 hidden layers using pytorch
97
98
   class Net(nn.Module):
99
       def init (self):
100
           super(Net, self). init ()
101
102
           # in_features = input dimension out_features -> to be tuned
103
           self.fc1 = nn.Linear(in_features=24, out_features=500)
104
105
           # out features -> to be tuned
106
           self.fc2 = nn.Linear(in features=500, out features=250)
107
108
           # out_features = number of classes to be predicted
109
           self.fc3 = nn.Linear(in features=250, out features=5)
111
       def forward(self, x):
112
           x = F.relu(self.fc1(x))
           out1 = x
           x = F.relu(self.fc2(x))
           out2 = x
           x = self.fc3(x)
           return x,out1,out2
118
   # In[5]:
120
121
   # Initialize neural network class
122
   net = Net()
123
124
   # # transfer the model to GPU if available
125
   # if torch.cuda.is_available():
126
         print("using GPU")
127
         net = net.cuda()
128
129
   # In[6]:
130
131
   132
   # Define a Loss function and optimizer
133
134
   # Both variables are to be tuned
135
   num epochs = 500
                            # desired number of training epochs.
136
   learning rate = 0.001
137
138
   # loss function and optimizers can be changed
139
   criterion = nn.CrossEntropyLoss()
140
   optimizer = optim.Adam(net.parameters(), lr=learning_rate,
141
                            weight decay=5e-4)
142
143
   num params = np.sum([p.nelement() for p in net.parameters()])
144
   print(num_params, ' parameters')
145
```

```
# In[7]:
147
    # create dataloader for loading data
148
149
   class myDataset(torch.utils.data.Dataset):
150
151
      #'Characterizes a dataset for PyTorch'
152
      def __init__(self,X,y,total_samples):
153
            #'Initialization'
154
            self.X = X
155
            self.y = y
156
            self.total_samples = total_samples
157
158
      def __len__(self):
159
            #'Denotes the total number of samples'
160
            return self.total samples
161
162
      def getitem (self, index):
163
            #'Generates one sample of data'
164
            # Select sample
            # Load data and get label
            x data = self.X[index,:]
            y_data = self.y[index]
169
170
            return x_data,y_data
171
172
    # batch size can be changed to make epochs faster
173
   params = {'batch_size': 32,
174
               'shuffle': False,
175
               'num workers': 0}
176
177
    # training dataset
178
   training_set = myDataset(X_train,y_train,train_len)
179
180
   training generator = torch.utils.data.DataLoader(training set,
181
                                                           **params)
182
183
    # validation dataset
184
   validation set = myDataset(X val,y val,val len)
185
   validation_generator = torch.utils.data.DataLoader(validation_set,
186
                                                             **params)
187
188
    # test dataset
189
   test_set = myDataset(X_test,y_test,test_len)
190
191
    test_generator = torch.utils.data.DataLoader(test_set,
192
                                                      **params)
193
194
    # In[8]:
195
```

```
def validation(model, loader):
197
        total loss = 0
198
        accuracy = []
199
        tq = partial(tqdm, position=0, leave=True)
200
201
        model.eval()
202
        with torch.no_grad():
203
             for X, y in tq(loader):
204
               X = X.float()
205
               y = y.long()
206
207
               # if torch.cuda.is_available():
208
                  X = X.cuda()
209
               y = y.cuda()
210
211
               prediction,_,_ = model(X)
212
               loss = criterion(prediction, y)
214
               prediction = F.softmax(prediction)
               acc = np.mean(np.array((torch.argmax(prediction,1) == y)))*100
218
219
220
               total loss += loss.item()
               accuracy.append(acc)
222
223
        # print('Validation Accuracy: ', np.mean(np.array(accuracy)))
224
        return total_loss/len(loader),np.mean(np.array(accuracy))
225
226
227
    # In [9]:
228
229
    def test(model, loader):
230
        y pred = []
231
        accuracy = []
232
        tq = partial(tqdm, position=0, leave=True)
233
234
        model.eval()
235
        with torch.no_grad():
236
             for X, y in tq(loader):
237
               X = X.float()
238
               y = y.long()
239
240
               # if torch.cuda.is_available():
241
                  X = X.cuda()
242
               y = y.cuda()
243
244
               prediction,_,_ = model(X)
245
```

```
prediction = F.softmax(prediction)
247
248
               acc = np.mean(np.array((torch.argmax(prediction,1) == y)))*100
249
250
               accuracy.append(acc)
251
252
               prediction = torch.argmax(prediction,1)
253
               y_pred = y_pred + list(np.array(prediction))
254
255
        print('Test Accuracy: ', np.mean(np.array(accuracy)))
256
        return y_pred,np.mean(np.array(accuracy))
257
258
259
    # In[10]:
260
261
    tq = partial(tqdm, position=0, leave=True)
262
    print('Start Training')
    train loss list = []
    train_accuracy_list = []
    validation loss list = []
    validation_accuracy_list = []
269
270
    for epoch in range(0,num epochs):
      print('epoch ', epoch + 1)
      loss = 0
273
      train_accuracy = []
274
      for X,y in tq(training_generator):
276
277
        X = X.float()
278
        y = y.long()
279
        # y = torch.squeeze(y,1)
280
281
        # if torch.cuda.is available():
282
               X = X.cuda()
283
               y = y.cuda()
284
285
        optimizer.zero grad()
286
287
        output,out1,out2 = net(X)
288
        loss = criterion(output,y)
289
290
        loss.backward()
291
        optimizer.step()
292
293
        loss += loss.item()
294
295
        prediction = F.softmax(output)
```

```
297
        accuracy = np.mean(np.array((torch.argmax(prediction,1) == y)))*100
298
        train accuracy.append(accuracy)
299
300
301
302
      train loss list.append([loss/len(training generator)])
303
      # print(loss/len(training generator))
304
305
     train accuracy list.append(np.mean(np.array(train accuracy)))
306
307
     val loss,val accuracy = validation(net, validation generator)
308
309
     validation loss list.append(val loss)
310
     validation accuracy list.append(val accuracy)
311
312
      # if epoch == 0 or epoch == 4 or epoch == 19 or epoch == 99 or epoch == num_epoch
            torch.save(net.state dict(), 'models/model-'+str(epoch)+'.pth')
   print(train accuracy list[-1])
   print(validation accuracy list[-1])
   # In[]:
320
   net = Net()
321
322
   # Import saved Model
323
   net.load state dict(torch.load('models/model-499.pth'))
324
   net.eval()
325
326
   # plt.plot(train_loss_list,label='Training Loss')
327
   plt.plot(validation loss list,label='Validation Loss')
328
   plt.xlabel('Number of Epochs')
329
   plt.ylabel('Loss')
330
   plt.title('Loss curve')
331
   plt.legend()
332
   plt.plot()
333
334
   # In[12]:
335
336
   plt.plot(train_accuracy_list,label='Training Accuracy')
337
   plt.plot(validation_accuracy_list,label='Validation Accuracy')
338
   plt.xlabel('Number of Epochs')
339
   plt.ylabel('Accuracy')
340
   plt.title('Accuracy curve')
   plt.legend()
342
   plt.show()
343
   # In[13]:
345
```

```
y_pred, test_accuracy = test(net,test_generator)
347
   c matrix = confusion matrix(y test, y pred)
348
349
   afig, ax = plot confusion matrix(conf mat=c matrix,figsize=(7,7)
350
                                        ,cmap=plt.cm.RdBu)
351
   ax.set(title = "Confusion Matrix for test data")
352
353
   y pred, train accuracy = test(net,training generator)
354
355
   c matrix = confusion matrix(y train, y pred)
356
357
   afig, ax = plot confusion matrix(conf mat=c matrix,figsize=(7,7)
358
                                             ,cmap=plt.cm.RdBu)
359
   ax.set(title = "Confusion Matrix for train data")
361
   362
   # In [15]:
   # Non-linear SVM
   from sklearn.svm import SVC
   from sklearn.multiclass import OneVsRestClassifier
   # Gaussian Kernel
369
   clf = OneVsRestClassifier(SVC(C=15,kernel='rbf')).fit(X train, y train)
   y pred = clf.predict(X train)
   train_accuracy = accuracy_score(y_train,y_pred)*100
   print("train accuracy: " , train_accuracy)
373
374
   c_matrix = confusion_matrix(y_train, y_pred)
376
   afig, ax = plot_confusion_matrix(conf_mat=c_matrix,figsize=(7,7),
377
                                      cmap=plt.cm.RdBu)
378
   ax.set(title = "Confusion Matrix for train data")
379
   y_pred = clf.predict(X_val)
380
   val accuracy = accuracy score(y val,y pred)*100
381
   print("validation accuracy: " , val_accuracy)
382
383
   y_pred = clf.predict(X_test)
384
   test accuracy = accuracy score(y test,y pred)*100
385
   print("test accuracy: " , test_accuracy)
386
387
   c_matrix = confusion_matrix(y test, y pred)
388
389
   afig, ax = plot confusion matrix(conf mat=c matrix,figsize=(7,7),
390
                                     cmap=plt.cm.RdBu)
391
   ax.set(title = "Confusion Matrix for test data")
```