$\overline{\textbf{Algorithm 1} \ hybrid \ key - switching}$

Input:
$$P = \{P_{\mathcal{A}_i}\}_{0 \leq i < dnum'}$$

 $\mathbf{evk_0} = \{\mathbf{evk_0}_i\}_{0 \leq i < dnum'}$

Output:
$$res0_A, res1_A$$

1: for
$$i \leftarrow 0$$
: $dnum' - 1$ do

 $\mathbf{evk}_1 = \{\mathbf{evk}_{1i}\}_{0 \le i < dnum'}$

2:
$$P_{\mathcal{A}_i} = intt(P_{\mathcal{A}_i})$$

3:
$$P_{\mathcal{C}/\mathcal{A}_i} = Bconv(P_{\mathcal{A}_i}, \mathcal{C}/\mathcal{A}_i)$$

4:
$$P_{\mathcal{C}} = ntt(P_{\mathcal{C}/\mathcal{A}_i}) \cup P_{\mathcal{A}_i}$$

5:
$$res0_{\mathcal{C}} = res0_{\mathcal{C}} + PMult(\mathbf{evk}_{0_i}, P_{\mathcal{C}})$$

6:
$$res1_{\mathcal{C}} = res1_{\mathcal{C}} + PMult(\mathbf{evk}_{1i}, P_{\mathcal{C}})$$

7: for
$$i \leftarrow 0:1$$
 do

8:
$$resi_{\mathcal{B}} = intt(resi_{\mathcal{B}})$$

9:
$$tmpi_{\mathcal{A}} = Bconc(\mathcal{B}, \mathcal{A})$$

10:
$$resi_{\mathcal{A}} = resi_{\mathcal{A}} - ntt(tmpi_{\mathcal{A}})$$

Algorithm 2 hmult

Input:
$$ct0 = (ct_{00}, ct_{01})_{\mathcal{A}}, ct1 = (ct_{10}, ct_{11})_{\mathcal{A}}$$

Output: res =
$$(res_0, res_1)_A$$

1:
$$x = ct_{00} * ct_{10}$$

2:
$$y = ct_{00} * ct_{11} + ct_{01} * ct_{10}$$

3:
$$z = ct_{01} * ct_{11}$$

4:
$$\mathbf{w} = keyswitch(z, evk)$$

5:
$$res_0 = x + \mathbf{w}_0$$

6:
$$res_1 = y + \mathbf{w}_1$$