

**Name:** \_\_\_\_\_

**Date:** \_\_\_\_\_

1. Consider the polynomial function below.

$$f(x) = 9x^6 - 9x^5 + 7x^3 - 5x^2$$

Multiple choice: describe the end behavior.

- (a) Down-down: when  $x \rightarrow -\infty$  then  $f(x) \rightarrow -\infty$  and when  $x \rightarrow \infty$  then  $f(x) \rightarrow -\infty$ .
- (b) Up-down: when  $x \rightarrow -\infty$  then  $f(x) \rightarrow \infty$  and when  $x \rightarrow \infty$  then  $f(x) \rightarrow -\infty$ .
- (c) Down-up: when  $x \rightarrow -\infty$  then  $f(x) \rightarrow -\infty$  and when  $x \rightarrow \infty$  then  $f(x) \rightarrow \infty$ .
- (d) Up-up: when  $x \rightarrow -\infty$  then  $f(x) \rightarrow \infty$  and when  $x \rightarrow \infty$  then  $f(x) \rightarrow \infty$ .

2. Consider the polynomial function below.

$$f(x) = -2x^5 - 8x^4 + 7x^3$$

How many roots, including complex roots and counting multiplicity, does the polynomial have?

Or, in other words, based on the degree of the polynomial, what is the most number of possible real roots?

3. **Draw** the polynomial function  $f(x)$  shown in factored and expanded forms. Be sure to indicate the roots, where the function is positive or negative, and end behavior.

$$f(x) = -(x - 4)(x + 2)$$

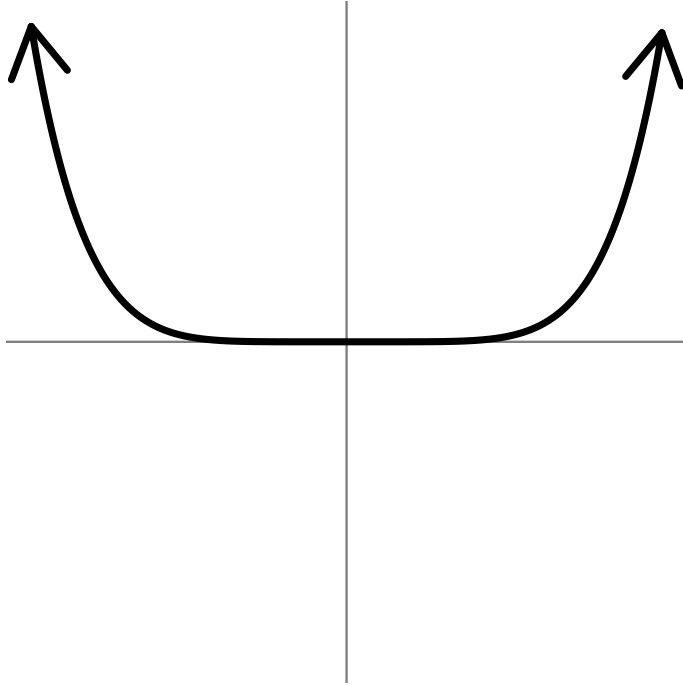
$$f(x) = -x^2 + 2x + 8$$

4. Factor the polynomial function  $f(x)$  to determine the roots.

$$f(x) = -x^3 - x^2 - 15x + 17$$

1. The degree of the polynomial is 6, which is even. The highest-degree term's coefficient is positive.

Thus the end behavior is up-up: when  $x \rightarrow -\infty$  then  $f(x) \rightarrow \infty$  and when  $x \rightarrow \infty$  then  $f(x) \rightarrow \infty$ .

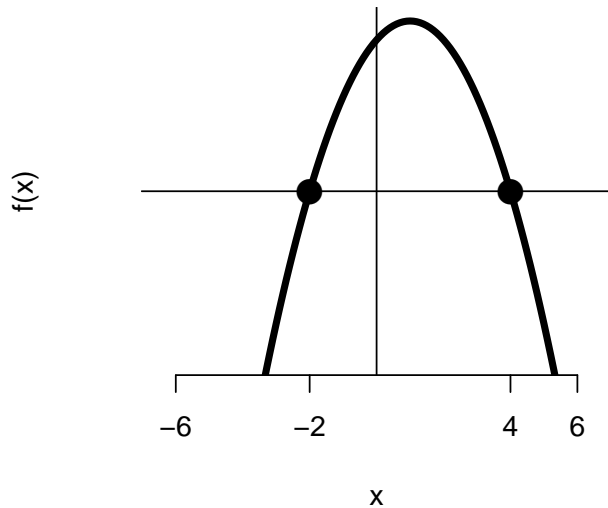


2. 5

The Fundamental Theorem of Algebra tells us that the number of complex roots, when counting for multiplicity, is equal to the degree of the polynomial.

The degree of the polynomial is just the largest exponent, 5.

3. You need to consider the roots and end behavior. If a root has even multiplicity, you need to bounce the curve off the x-axis there.



4. Factor.

$$f(x) = -(x - 1)(x + 1 - 4i)(x + 1 + 4i)$$

The roots:

$$x|_{f(x)=0} = [1, -1 - 4i, -1 + 4i]$$