

problem 1.(1)

```
function binomialNumber(n, m)
    binoNum[n+1][n+1] = {0}
    binoNum[0][0] = 1
    for i from 1 to n :
        for j from 0 to i :
            binoNum[i][j] = binoNum[i-1][j] + binoNum[i-1][j+1]
        end for
    end for
    return binoNum[n][m]
```

problem 1.(2)

```
function catalanNumber(n)
    count[n+1][n+1] = {0}
    count[0][0] = 0
    for i from 1 to n :
        for j from 1 to n :
            count[i][j] = count[i-1][j] + count[i][j-1]
        end for
    end for
    return count[n][n]
```

problem 1.(3)

by the definition of "H(n, g)", we can build the table

groups	1	2	3	4	5	6	7
number							
1	1						
2	1	1					
3	1	1	1				
4	1	2	1	1			
5	1	2	2	1	1		
6	1	3	3	2	1	1	
7	1	3	4	3	2	1	1

=====

```
function partitionNumber(n)
    partNum[n+1][n+1]
    partNum[1][1] = partNum[2][1] = partNum[2][2] = 1
    for num = 3 to n :
        for group = 1 to num :
            partNum[num][group] = sum of (partNum[num-group][1] to partNum[num-
group][group])
```

```

        end for
    end for
    return sum of (partNum[n][1] to partNum[n][n])

```

problem 2.(1)

see problem 2.(2)

problem 2.(2)

set $f(n)$ to be the number of hidden code of HH-code :

$f(n) =$

- (a). 1, if length = 0
- (b). 2, if length = 1
- (c). $f(n-1) \times 2 - f(\text{the previous place same element going to add})$

===== code :

```

function findHidden(code)
    hiddenNum[length+1]
    for pos = 1 to max_length :
        if pos == 1 :
            hiddenNum[pos] = 1
        else
            for pre = pos-1 to 1 :
                if code[pre] == code[pos] :
                    break
                end if
            end for
            hiddenNum[pos] = hiddenNum[pos-1]*2 - hiddenNum[pre-1]
        end if
    end for
    return hiddenNum[length]-1

```

problem 2.(3)

K		0	1	2	3	4
N						
0	null	0	0	0	0	0
1	1	0	1	0	0	0
2	0	0	2	1	0	0
3	1	0	2	3	1	0
4	1	0	2	3	3	1

problem 3.(1).1

Each multiplication of element need $\mathbf{O}(m)$ time :

ex: $[a \ b; \ c \ d] * [a \ b; \ c \ d]$

$(a*a + b*c) \Rightarrow m = 2$, need to add m times

And we have m^2 elements $\Rightarrow \mathbf{O}(m^3)$

Last, we compute A^n by dividing it into half again and again

$$\begin{aligned}\text{ex: } A^n &= A^{n/2} \times A^{n/2} \\ &= (A^{n/4} \times A^{n/4}) \times A^{n/2} \\ &= \dots\end{aligned}$$

So, we need $\Rightarrow \mathbf{O}(m^3 \log_2 n)$ time to calculate A^n

problem 3.(1).2