

**CONFIDENTIAL**

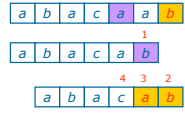
# C Programming Basic – week 13

*String Pattern Matching*

**Lecturers :**  
**Cao Tuan Dung**  
**Le Duc Trung**  
**Dept of Software Engineering**  
**Hanoi University of Technology**

## Topics of this week

- String pattern matching algorithms
  - Naive algorithm
  - Knuth-Morris-Pratt algorithm
  - Boyer-Moore algorithm
- Exercises



2

## String matching problem

- Let  $P$  be a string of size  $m$ 
  - A substring  $P[i..j]$  of  $P$  is the subsequence of  $P$  consisting of the characters with ranks between  $i$  and  $j$
  - A prefix of  $P$  is a substring of the type  $P[0..i]$
  - A suffix of  $P$  is a substring of the type  $P[i..m-1]$
- Given strings  $T$  (text) and  $P$  (pattern), the pattern matching problem consists of finding a substring of  $T$  equal to  $P$
- Applications:
  - Text editors, Search engines, Biological research

3

## Brute Force Matching

- The brute-force pattern matching algorithm compares the pattern  $P$  with the text  $T$  for each possible shift of  $P$  relative to  $T$ , until either
  - a match is found, or
  - all placements of the pattern have been tried
- Brute-force pattern matching runs in time  $O(nm)$
- Example of worst case:
  - $T = \text{aaa} \dots \text{ah}$
  - $P = \text{aaah}$
  - may occur in images and DNA sequences
  - unlikely in English text

4

## Algorithm

```

Algorithm BruteForceMatch(T, P)
// Input text T of size n and pattern P of size m
// Output starting index of a substring of T equal to P or -1
if no such substring exists
  for i ← 0 to n - m {
    test shift i of the pattern
  }
  j ← 0
  while j < m ∧ T[i + j] = P[j]
    j ← j + 1
  if j = m
    return i {match at i}
  else
    break while loop {mismatch}
return -1 {no match anywhere}
  
```

5

## Exercise 13.1

- Make a random string that has about 2000 characters consisting of a set of characters..
- For example:
  - set of characters: abcdef
  - string: abcadacaeeeffaadbfcadddcedfbecca...
- Write the program that searches the pattern, for example "aadbfc", from the string.
- Note: use Simple searching string Algorithm

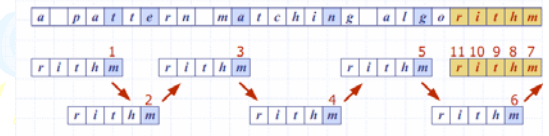
6

## Boyer-Moore Heuristics

- The Boyer-Moore's pattern matching algorithm is based on two heuristics
- Looking-glass heuristic: Compare P with a subsequence of T
- moving backwards
- Character-jump heuristic: When a mismatch occurs at  $T[i] = c$ 
  - If P contains c, shift P to align the last occurrence of c in P with  $T[i]$
  - Else, shift P to align  $P[0]$  with  $T[i + 1]$

7

## Example



8

## Last-Occurrence Function

- Boyer-Moore's algorithm preprocesses the pattern P and the alphabet  $\Sigma$  to build the last-occurrence function L mapping  $\Sigma$  to integers, where  $L(c)$  is defined as
  - the largest index i such that  $P[i] = c$  or
  - 1 if no such index exists
- Example:
  - $\Sigma = \{a, b, c, d\}$
  - $P = abacab$
- The last-occurrence function can be represented by an array indexed by the numeric codes of the characters
- The last-occurrence function can be computed in time  $O(m + s)$ , where m is the size of P and s is the size of  $\Sigma$

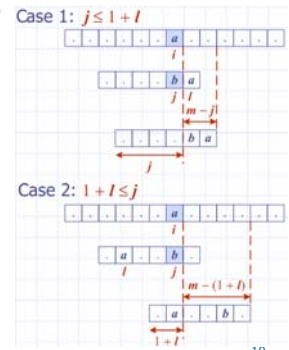
	c	a	b	c	d
L(c)	4	5	3	-1	

9

## Algorithm Boyer Moore

```

Algorithm BoyerMooreMatch(T, P,  $\Sigma$ )
  L  $\leftarrow$  lastOccurrenceFunction(P,  $\Sigma$ )
  i  $\leftarrow$  m - 1
  j  $\leftarrow$  m - 1
  repeat
    if T[i] = P[j]
      if j = 0
        return i { match at i }
      else
        i  $\leftarrow$  i - 1
        j  $\leftarrow$  j - 1
    else
      { character-jump }
      l  $\leftarrow$  L[T[i]]
      i  $\leftarrow$  i + m - min(j, l + 1)
      j  $\leftarrow$  m - 1
  until i > n - 1
  return -1 { no match }
    
```



10

## Exercise 13.2: Searching string by Boyer-Moore

- Make a random string that has about 2000 characters consisting of a set of characters.
- set of characters: abcdef
- string:
   
abcaadacaeeeffaadbfbacddedcedfbeccae...
- Write the program that search the pattern, for example "aadbfb", from the string.
- Note: use Boyer-Moore Algorithm

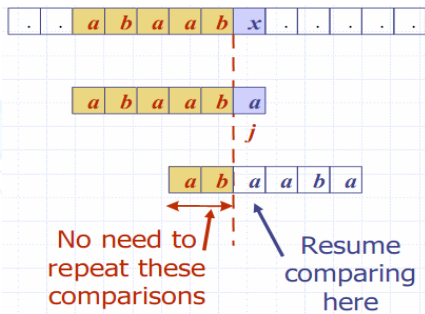
11

## KMP string matching

- Knuth-Morris-Pratt's algorithm compares the pattern to the text in left-to-right, but shifts the pattern more intelligently than the brute-force algorithm.
- When a mismatch occurs, what is the most we can shift the pattern so as to avoid redundant comparisons?
- Answer: the largest prefix of  $P[0..j]$  that is a suffix of  $P[1..j]$

12

## Example



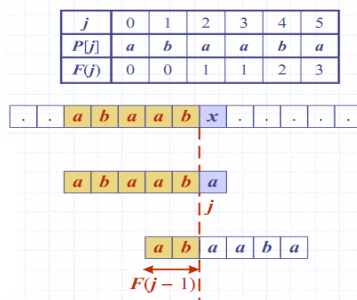
13

## KMP Failure Function

- Knuth-Morris-Pratt's algorithm preprocesses the pattern to find matches of prefixes of the pattern with the pattern itself
- The failure function  $F(j)$  is defined as the size of the largest prefix of  $P[0..j]$  that is also a suffix of  $P[1..j]$
- Knuth-Morris-Pratt's algorithm modifies the brute-force algorithm so that if a mismatch occurs at  $P[j] \neq T[i]$  we set  $j \leftarrow F(j - 1)$

14

## Example



15

### Algorithm failureFunction(P)

```

F[0] ← 0
i ← 1
j ← 0
while i < m
  if P[i] = P[j]
    {we have matched j + 1 chars}
    F[i] ← j + 1
    i ← i + 1
    j ← j + 1
  else if j > 0 then
    {use failure function to shift P}
    j ← F[j - 1]
  else
    F[i] ← 0 { no match }
    i ← i + 1

```

16

## Exercise 13.3

- Repeat the exercise 13.2 using the KMP algorithm.
- Calculate the number of comparisons.

17

## The KMP algorithm

- The failure function can be represented by an array and can be computed in  $O(m)$  time
- At each iteration of the while-loop, either
  - $i$  increases by one, or
  - the shift amount  $i - j$  increases by at least one (observe that  $F(j - 1) < j$ )
- Hence, there are no more than  $2n$  iterations of the while-loop
- Thus, KMP's algorithm runs in optimal time  $O(m + n)$

18

Algorithm KMPMatch(T, P)

$F \leftarrow \text{failureFunction}(P)$

$i \leftarrow 0$

$j \leftarrow 0$

while  $i < n$

if  $T[i] = P[j]$

if  $j = m - 1$

return  $i - j$  { match }

else

$i \leftarrow i + 1$

$j \leftarrow j + 1$

else

if  $j > 0$

$j \leftarrow F[j - 1]$

else

$i \leftarrow i + 1$

return  $-1$  { no match }

19

## Example

a b a c a a b a c a b a c a a b a a b b

1 2 3 4 5 6  
a b a c a b

7  
a b a c a b

8 9 10 11 12  
a b a c a b

13  
a b a c a b

14 15 16 17 18 19  
a b a c a b

j	0	1	2	3	4	5
P[j]	a	b	a	c	a	b
F[j]	0	0	1	0	1	2

20