

Seismic anomaly detection based on PSO-VMD separation of satellite electromagnetic signals

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Abstract

During the process of earthquake development, minute fluctuations in the Earth's geomagnetic field strength can be affected, thereby enabling the analysis of seismic anomalies through geomagnetic data. Since the variations in the geomagnetic field are relatively small compared to the overall field strength, it is essential to decompose the geomagnetic field before performing anomaly detection. In the analysis of the seismic event that occurred in the Nicaragua region on September 15, 2016, an enhanced signal decomposition technique based on Variational Mode Decomposition (VMD), specifically Particle Swarm Optimization-VMD (PSO-VMD), was employed to mitigate the interference of the electromagnetic dynamic field and investigate the association between electromagnetic data and earthquakes. Furthermore, the Empirical-Cumulative-distribution-based Outlier Detection (ECOD) method was utilized for anomaly clustering of orbital numbers.

Compared to the raw data, the methodology presented in this study shows that the accumulation of anomalies preceding the earthquake matches a slow-fast-slow pattern. We propose an anomaly detection method for seismic monitoring that shows a marked increase in anomaly occurrences during earthquake periods compared to non-earthquake periods. This suggests its potential effectiveness for earthquake-related anomaly identification. This finding compellingly substantiates a robust correlation between electromagnetic data and earthquakes.

Keywords: PSO-VMD, Seismic anomaly detection, ECOD

1. Introduction

The increasing number of global satellite launches has led to a vast accumulation of electromagnetic monitoring data. Abnormal earthquake detection now relies heavily on satellite

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signals, particularly from DEMETER (Detection of Electro-Magnetic Emissions Transmitted from Earthquake Regions) and the Swarm satellites as well as CSES (China Seismo-Electromagnetic Satellite)(Zhao et al., 2022). DEMETER, a French satellite launched on June 29, 2004, was specifically designed for detecting electromagnetic signals associated with earthquake precursors. It is equipped with electromagnetic sensors, low-energy particle detectors, and high-energy electron detectors, enabling it to observe environmental changes in the ionosphere and magnetic field. Its main objective was to identify electromagnetic signals related to earthquake precursors, enhancing earthquake prediction and early warning capabilities (Shi et al., 2023). DEMETER followed a sun-synchronous orbit, with nighttime observations during the upward half and daytime observations during the downward half.

Statistical analysis of the data obtained from the DEMETER satellite has demonstrated a certain correlation with earthquakes (Parrot, 2012). Xiong et al. (2020) utilized the Light-GBM method based on gradient descent to analyze DEMETER data and found that certain frequency ranges of low-frequency electric and magnetic fields were key features in identifying electromagnetic precursor disturbances. Akhoondzadeh and Marchetti (2022) proposed a Mamdani fuzzy inference system (FIS) for earthquake prediction using DEMETER data, finding that the highest number of anomalies appeared approximately one month before an earthquake. Additionally, studies by Nemec et al. (2008) and Molchanov et al. (2006) showed correlations between VLF electromagnetic wave intensity and major earthquakes, but these correlations were often weak and inconsistent. Zlotnicki et al. (2006) attempted multi-scale statistical analysis to identify pre-seismic anomalies, yet their methods were limited by the complexity and variability of the data.

The Swarm (Friis-Christensen et al., 2006) satellite mission, launched by the European Space Agency (ESA) on November 22, 2013 with the aim of collecting data on Earth's magnetic field, magnetic field variations, and geomagnetic activity, consists of three satellites: Swarm A, Swarm B, and Swarm C. Unlike DEMETER, Swarm satellites are not sun-synchronous, meaning their local time measurements vary with each pass, complicating the analysis of data due to time-dependent variations.

Marchetti et al. (2022) analyzed magnetic field and electron density signals from Swarm and found a statistical correlation with M5.5+ shallow earthquakes, proposing frequency as a criterion for anomaly detection. However, geomagnetic storms and other natural phenomena often interfere with these signals, making it challenging to isolate true seismic anomalies.

In the analysis of Swarm satellite data, De Santis et al. (2017) introduced the slow-fast-slow pattern, known as the "S-shape," explaining it as a critical system nearing a mainshock. However, it is important to note that there is currently no definitive research linking such anomalies directly to seismic events. As such, this study builds upon previous works, offering insights into the potential use of these indicators while recognizing the uncertainty surrounding their specific connection to earthquakes. Fan et al. (2022) further developed a signal decomposition method for Swarm data analysis. Our research builds on these foundational studies.

According to previous studies, this research utilizes vector information of electromagnetic data acquired by the Swarm satellite. The CIY4 model was first applied to eliminate the static field component from the geomagnetic vector data. Subsequently, a Variational Mode

Decomposition (VMD) approach optimized by Particle Swarm Optimization (PSO) was used to extract two intrinsic mode functions, aiming to reduce interference caused by geomagnetic disturbances. Finally, an unsupervised anomaly detection method Empirical Cumulative Distribution-based Outlier Detection (ECOD) was employed to cluster data points and assess cumulative anomalies over a defined time span. The study mainly contains the following contributions:

1. A combined method for seismic anomaly analysis based on signal decomposition and outlier detection. A PSO-optimized Variational Mode Decomposition (PSO-VMD) technique is used to process geomagnetic data, helping to reduce the influence of dynamic geomagnetic variations during analysis.
2. Application of ECOD for anomaly clustering. The study explores the use of the Empirical Cumulative Distribution-based Outlier Detection (ECOD) method in the context of satellite-derived orbital anomaly detection. This method enables unsupervised identification of cumulative anomaly patterns.
3. Demonstration of methodological potential in seismic anomaly detection. The results illustrate that the proposed combination of PSO-VMD and ECOD can extract patterns in the satellite electromagnetic data that may be relevant to pre-earthquake anomaly analysis. The methods and results may provide useful references for future research in seismic monitoring using satellite data.

2. Data and Methods

Based on the analysis of existing research, this paper initially acquired vector information of electromagnetic data through the Swarm satellite. The CIY4 (Sabaka et al., 2018) model was then utilized to remove the core and lithospheric magnetic fields from the geomagnetic vector data, which is derived from the Swarm Comprehensive Model (SCM). To eliminate the interference of geomagnetic activity, a Particle Swarm Optimization (PSO) (Wanpeng and Zhenhong, 2010) - optimized Variational Mode Decomposition (VMD) method was employed to extract two modal data, using the average sliding energy as a basis for eliminating the effects of geomagnetic activity. For anomaly extraction, an unsupervised outlier detection technique called Empirical Cumulative Distribution Function (ECOD) (Li et al., 2022) was used to cluster data points and assess accumulated anomalies within a certain time span. These accumulations were then fitted with a Boltzmann function at a given time scale to determine if they exhibited sharp increases before earthquakes and stabilized afterward. The work flow of the model is shown as Figure 1. By analyzing seismic events in the Nicaragua region, it was observed that the seismic anomalies exhibited a distinct gradual-steep-gradual characteristic. Building upon this observation, seismic events from random global locations were randomly selected, and a statistical analysis of the pre-earthquake cumulative anomaly growth trend for both non-seismic and seismic events was conducted. The results demonstrated the effectiveness of this method in extracting pre-earthquake anomaly features.

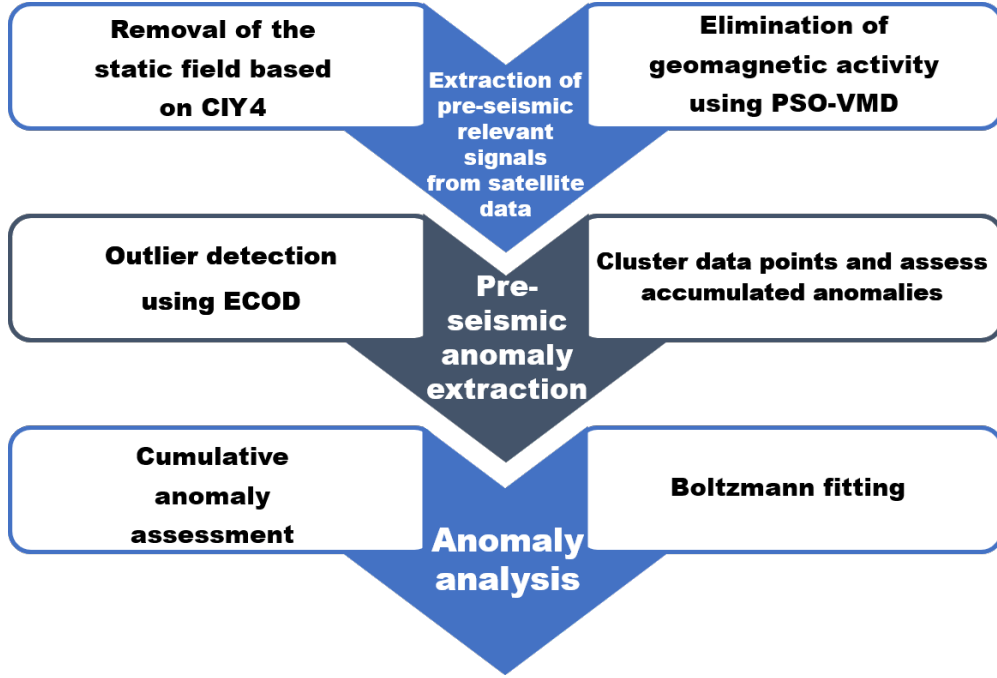


Figure 1: The workflow for pre-seismic anomaly detection based on Swarm satellite electromagnetic data

2.1. Data from Swarm

The Swarm satellite is equipped with multiple payloads to meet various observational requirements. These payloads include magnetometers, GPS receivers, star trackers, and a gravity gradient instrument, among others. The Level 1b data is a standardized format used to describe the measurement results from the Swarm satellite. The data can be obtained for free through <https://swarm-diss.eo.esa.int/>. The Level 1b data records the raw data from satellite observations, including satellite position, velocity, attitude, and Earth's magnetic field, as well as pre-processed and corrected measurements of the magnetic and gravity fields. Specifically, the data used in this study was sourced from the MAGX_LR product, which corresponds to the low-rate (1Hz) magnetic field data collected from all three Swarm satellites: Swarm A, Swarm B, and Swarm C. This multi-satellite approach ensures comprehensive data coverage and consistency across different regions and time periods. Specifically, the Level 1b data consists of the following components:

- **Timestamp:** Records the time and date of the data record.
- **Raw Data:** Includes satellite attitude, position, and velocity data, as well as raw data measured by various sensors.
- **Data Pre-processing:** Pre-processes and corrects the raw data to compensate for sensor errors and signal noise.
- **Earth's Magnetic Field:** Models and measures Earth's magnetic field to obtain more accurate magnetic field data.

- **Gravity Field:** Models and measures the gravity field to obtain more accurate gravity field data.
- **Correction Coefficients:** Includes various correction coefficients and correction factors to correct deviations and errors in the data.

The Level 1b data format of the Swarm satellite adopts the standard NetCDF format, facilitating data exchange and processing on different platforms. Data files in this format can be read, processed, and visualized using various scientific data processing software, greatly facilitating the analysis of magnetic field data. By utilizing data from all three Swarm satellites (A, B, and C), we ensure consistency across different satellite measurements and increase the reliability of the results obtained from the magnetic field data. All the data are sourced from MAGX_LR, X represents (A, B, C) for the three satellites.

In this study, data from all three Swarm satellites (A, B, and C) were used to enhance the reliability of the analysis. Given the variations in local time coverage and orbital parameters, cross-validation was performed to ensure the consistency of the data. Specifically, we compared the anomalies detected by each of the three satellites and assessed the consistency of their detection results. While each satellite provides unique time and spatial coverage, the consistency of the anomalies detected by Swarm A, B, and C supports the robustness of our findings. The data from different satellites were integrated by aligning their temporal and spatial data, ensuring the anomalies detected across satellites were comparable. Any discrepancies due to the varying local times and satellite coverage were carefully addressed through the pre-processing stage, where the data were normalized to a common reference frame.

2.2. CIY4 model

In order to remove the influence of the earth's main magnetic field, lithospheric magnetic field, external source field, geomagnetic activity, etc. from the electromagnetic information obtained by the swarm satellite, and extract the part of the electromagnetic signal directly affected by earthquakes, this study uses a joint model to remove the static field. For existing joint models, such as CM5, CIY4, CHAOS, etc., since CIY4 improves the possible magnetic anomaly areas in CM5 and enriches the ionospheric inversion data compared to CHAOS, this study uses the CIY4 model to analyze the static field to remove.

The inversion process of CIY4 mainly includes the following steps: first, preprocessing the geomagnetic vector data, including removing the influence of satellite attitude; then transforming the processed data into the geomagnetic field in spherical coordinates; next, decomposing the geomagnetic field into different levels and types of spherical harmonic terms using the spherical harmonic expansion method; calculating the analytical solution of the spherical harmonic coefficients; smoothing and predicting the spherical harmonic coefficients; finally, evaluating and validating the inversion results. In this study, we validated the CIY4 model's inversion accuracy by comparing data from multiple Swarm satellites, ensuring robust results even with potential inconsistencies between different satellite data.

For the anomaly detection and spatial localization, we focused on seismic events in the Nicaragua region as a case study. The region was selected due to its seismic activity, which

provides a rich dataset for studying pre-earthquake anomalies. The Swarm satellite data was analyzed for potential electromagnetic anomalies in this region, and the spatial localization was achieved by focusing on the geographic coordinates corresponding to seismic events. The anomalies were then extracted using the Empirical Cumulative Distribution Function (ECOD) method, which allowed us to identify and assess the presence of significant anomalies leading up to the earthquakes. By analyzing the data in this localized region, we were able to explore the unique characteristics of seismic anomalies and validate the method's effectiveness for anomaly detection in active seismic zones.

Table 1 presents the parameter values for the given models in the Swarm product. The model corresponding to the core field is MCO_SHA_2C, the ionospheric field is represented by the model MIO_SHA_2C, the lithospheric field is associated with the model MLI_SHA_2C, and the magnetospheric field corresponds to the model MMA_SHA_2C. In these models, N_{min} denotes the minimum degree of the spherical harmonic expansion, while N_{max} represents the maximum degree of the expansion. The degree of expansion determines the accuracy and spatial resolution of the model.

Table 1: Value of Swarm Model Parameters

Swarm Models	Description	Value
MCO_SHA_2C	core field	$N_{min} = 1, N_{max} = 18$
MIO_SHA_2C	ionospheric field	$N_{min} = 1, N_{max} = 60$
MLI_SHA_2C	lithospheric field	$N_{min} = 16, N_{max} = 120$
MMA_SHA_2C	magnetospheric field	$N_{min} = 1, N_{max} = 2$

The table is a table of the values of various swarm model parameters, where the first and second columns represent different swarm models and the corresponding magnetic fields. In the third column, N_{min} represents the minimum expansion order in the parameters, and N_{max} represents the maximum expansion order.

Figures 2(a)-(d) illustrate the core field data, ionospheric field data, lithospheric field data, and magnetospheric field data obtained from the CIY4 inversion model. Among them, Figure 2(e) displays the observational data from the Swarm satellites, while Figure 2(f) depicts the residuals between the observed data and the inversion results of the CIY4 model. Through careful examination, it is evident that the core field exhibits an exceptionally high correlation with the observed data, with a Pearson coefficient of 0.99982901. The very high value of the Pearson coefficient is probably based on periods without geomagnetic storms. Given the magnitude of the core field, reaching up to 10^4 nT, it is crucial to remove its influence from the raw observational data.

2.3. PSO-VMD method

VMD (Variational Mode Decomposition) (Dragomiretskiy and Zosso, 2014) is a signal decomposition method that adaptively extracts oscillatory modes from non-stationary signals. Unlike wavelet or Fourier transforms, it does not require stationarity assumptions.

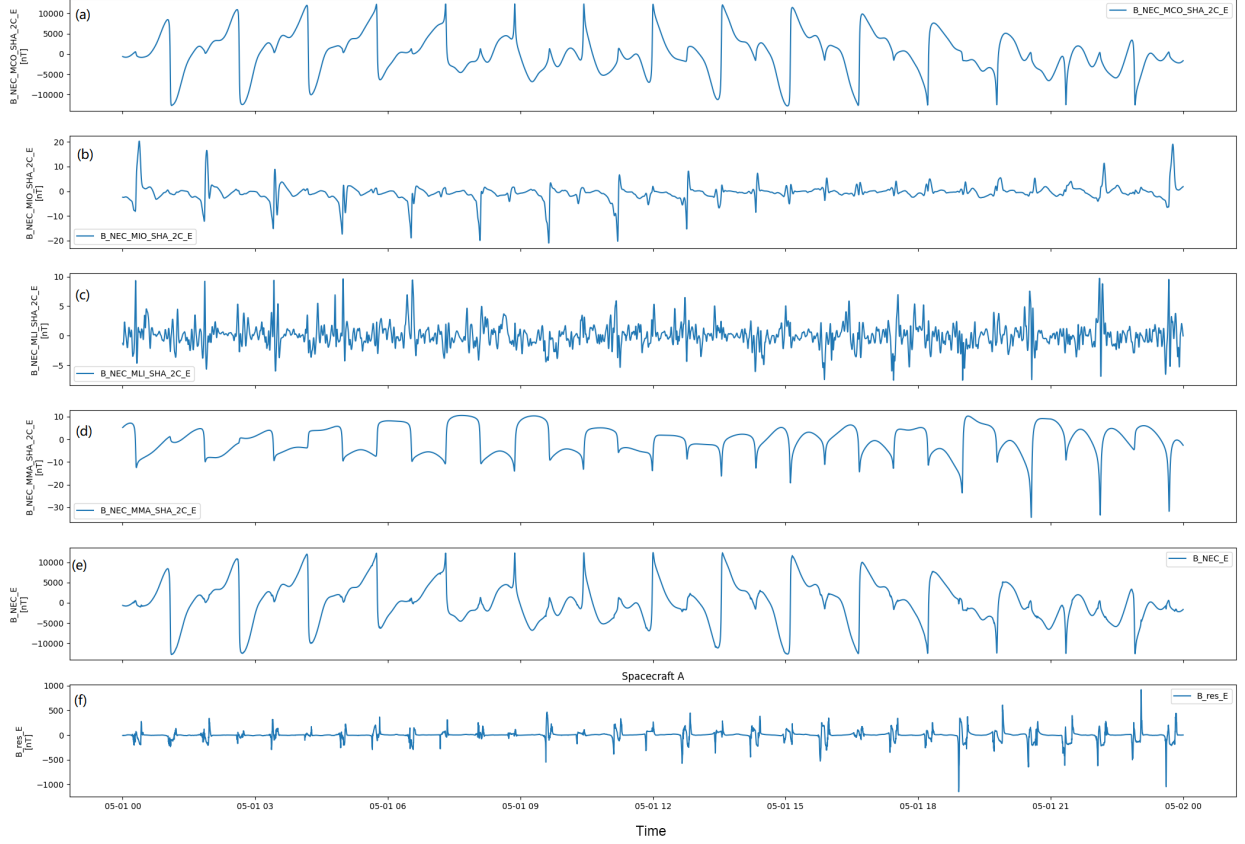


Figure 2: Data of CIY4 model. Each sub-figure represents the electromagnetic E component data and the electromagnetic E component residual graph, where (a) is the main magnetic field component data, (b) is the ionosphere magnetosphere component data, (c) is the lithosphere magnetic field component data, (d) is the magnetosphere magnetic field component data, (e) is the original observation data, and (f) is the residual of the observation data and the model inversion data.

However, its performance is sensitive to two parameters: the number of modes K and the penalty factor α .

In applying the PSO-VMD method to the Swarm satellite dataset, we first preprocess the electromagnetic signals from the Swarm satellites. The preprocessing includes noise filtering and signal normalization to ensure that the data is in a suitable format for VMD. We then use the PSO algorithm to search for optimal values of parameters α and K for the VMD process. The optimized parameters are used to decompose the signals into intrinsic modes, which are then further analyzed for anomaly detection. The effectiveness of the PSO-VMD method lies in its ability to adaptively determine the number of modes and bandwidth, improving the accuracy of signal decomposition, especially for the non-stationary nature of the satellite data.

However, before using the VMD algorithm, it is necessary to determine the penalty coefficient α and the number of modes K in advance. The selection of these two parameters directly affects the results of the VMD algorithm. If K is too large, it may lead to over-

decomposition, while if it is too small, it may result in under-decomposition. The value of α affects the bandwidth of each mode. A smaller α leads to larger bandwidth for each mode, which may cause overlapping passbands among the modes. On the other hand, a larger α leads to smaller bandwidth, which may result in the loss of signal information.

To determine appropriate values for α and K , this study adopts the Particle Swarm Optimization (PSO)-based VMD algorithm (referred to as PSO-VMD hereinafter). To avoid manual tuning, we employ Particle Swarm Optimization (PSO) to optimize α and K . Each particle represents a candidate solution, and the optimization minimizes the residual between the original signal and the reconstructed signal after VMD. The process terminates either when convergence is achieved (residual change < 0.001) or after 500 iterations.

The Particle Swarm Optimization (PSO) algorithm treats each solution as a particle in the entire solution space. Each particle is initialized with its initial position and velocity, and it moves in the solution space at a unit time according to the direction and step size determined by its own best local history and the best history of the collective particles. By starting from random positions in the solution space, multiple particles avoid the drawback of a single particle getting trapped in local optima.

The optimization process terminates when either of the following criteria are met:

- **Maximum iterations:** We set the maximum number of iterations to 500 to avoid excessive computational costs.
- **Convergence threshold:** If the change in the fitness function value (i.e., the residual error) is smaller than 0.001 between consecutive iterations, the optimization is considered to have converged.

The velocity and position updates follow standard PSO formulations, with each particle's performance evaluated by the L^2 norm of the decomposition residual. The update equations for the particle velocity and position are shown in Equation 1.

$$\begin{aligned} v_i^{t+1} &= wv_i^t + c_1r_1(pbest_i - x_i^t) + c_2r_2(gbest - x_i^t) \\ x_i^{t+1} &= x_i^t + v_i^{t+1} \end{aligned} \quad (1)$$

In the context of the VMD algorithm, K and α are treated as the position parameters of the particles. The loss error is calculated as the residual of the sum of all modes, as shown in Equation 2. The L^2 norm, denoted by $\|\cdot\|_2$, is used to measure the magnitude of the residual.

$$u_{error} = \left\| f(t) - \sum_k u_k(t) \right\|_2 \quad (2)$$

The inputs are the electromagnetic data $f(t)$ and the number of iterations $Iter$, and the output is the decomposed modal data u_k . In the algorithm, the particle swarm is constructed by setting the number of particles num and initializing their initial states. The parameters for the PSO algorithm are also set. In each iteration, the VMD decomposition u_k^j is computed for the current particle state (as shown in Equation 3). The particle states are updated by

calculating the residual (as shown in Equation 2) and recording the individual best solution $pbest_i$ as well as the global best solution $gbest$ (as shown in Equation 1). After each particle completes one iteration, the next iteration begins. Once all iterations are completed, the VMD decomposition values are computed based on $gbest$, and the modal data u_k is returned.

$$\begin{aligned} u_k^{n+1} &= \underset{u_k}{\operatorname{argmin}} \mathcal{L} (u_{i < k}^{n+1}, w_k^n, \lambda^n) \\ w_k^{n+1} &= \underset{w_k}{\operatorname{argmin}} \mathcal{L} (u_k^n, w_{i < k}^{n+1}, \lambda^n) \\ \lambda^{n+1} &= \lambda^n + \rho \left(f(t) - \sum_k u_k^{n+1}(t) \right) \end{aligned} \quad (3)$$

After completing all iterations, the VMD decomposition values are obtained based on the global best position $gbest$. The modal data u_k can then be extracted from the VMD decomposition.

The complete optimization procedure is summarized in Algorithm 1.

Algorithm 1 PSO-based-VMD

input: electromagnetic $f(t)$ and the number of iterations $Iter$

output: the decomposed mode data u_k

- 1: initializing the number of the particles num and specifying their initial states;
 - 2: **for** $i = 1, 2, \dots, Iter$ **do**
 - 3: **for** $j = 1, 2, \dots, num$ **do**
 - 4: Perform VMD decomposition u_k^j based on the current particle state
 - 5: Update the state of each point using the residual calculation
 - 6: Update the individual best solution $pbest_j$ and the global best solution $gbest$
 - 7: **end for**
 - 8: **end for**
 - 9: Calculate the VMD decomposition value based on $gbest$
 - 10: **return** u_k ;
-

The PSO-VMD approach offers several advantages: it automatically determines optimal parameters, reduces mode mixing, and suppresses periodic or spurious components in the signal. By decomposing the electromagnetic data into narrow-band intrinsic modes, it enhances background variation and facilitates anomaly detection.

One notable advantage of the PSO-VMD preprocessing method is its inherent capability to suppress periodic or spurious components within the original signal. Through the adaptive decomposition of signals into narrow-band intrinsic modes, the method effectively isolates and attenuates high-amplitude periodic outliers, which often manifest as artifacts in electromagnetic recordings. While we do not explicitly present side-by-side visual comparisons in this paper, this property of PSO-VMD contributes to the clearer expression of background variations in the residual magnetic field, which is critical for subsequent anomaly detection.

2.4. ECOD method

ECOD (Empirical Cumulative Outlier Detection) is an unsupervised outlier detection method that effectively detects outliers in data (Li et al., 2022). This method is based on the Empirical Cumulative Distribution Function (ECDF), which is a non-parametric empirical distribution function representing the proportion of data points in a dataset that are less than or equal to a given value. To ensure outlier detection in different directions, ECOD calculates the left-tail ECDF and right-tail ECDF of the data in the j -th dimension, as shown in Equation 4. Here, x_i^j represents the j -th dimensional value of the i -th sample, n is the total number of samples, and $1(\cdot)$ is the indicator function. $F_{left}^j(z)$ represents the proportion of samples in the j -th dimension that are less than or equal to z , i.e., the left-tail ECDF, while $F_{right}^j(z)$ represents the proportion of samples in the j -th dimension that are greater than or equal to z , i.e., the right-tail ECDF. By calculating the left-tail ECDF and right-tail ECDF in each dimension, ECOD constructs a multi-dimensional ECDF in the multi-dimensional space and utilizes it for outlier detection of multi-dimensional data.

$$\begin{aligned} F_{left}^j(z) &= \frac{1}{n} \sum_{i=1}^n 1(x_i^j \leq z) \\ F_{right}^j(z) &= \frac{1}{n} \sum_{i=1}^n 1(x_i^j \geq z) \end{aligned} \quad (4)$$

To calculate the skewness of the data in the j -th dimension, this paper uses the sample's third central moment as a measure of skewness, as shown in Equation 5. This skewness value will serve as a reference for the final outlier score. Here, SK represents the skewness, $E[\cdot]$ denotes the mathematical expectation, X represents a random variable, μ represents the mean, σ represents the standard deviation, x_i represents the i -th sample, \bar{x} represents the sample mean, and n represents the sample size.

$$\begin{aligned} SK &= E \left[\left(\frac{X - \mu}{\sigma} \right)^3 \right] \\ &= \frac{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^3}{\left(\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2 \right)^{\frac{3}{2}}} \end{aligned} \quad (5)$$

In ECOD, there are three components involved in calculating the outlier scores: left-only

value, right-only value, and auto value $O_{auto}(X_i)$, as shown in Equation 6.

$$\begin{aligned}
O_{left_only}(X_i) &= - \sum_{j=1}^d \log(F_{left}^j(X_i^j)) \\
O_{right_only}(X_i) &= - \sum_{j=1}^d \log(F_{right}^j(X_i^j)) \\
O_{auto}(X_i) &= - \sum_{j=1}^d [1(SK_j < 0) \log(F_{left}^j(X_i^j)) \\
&\quad + 1(SK_j \geq 0) \log(F_{right}^j(X_i^j))]
\end{aligned} \tag{6}$$

In the context of the Swarm dataset, after the signals are decomposed using PSO-VMD, the ECOD method is applied to detect anomalies within the decomposed modes. Each mode is evaluated using the ECDF approach, and outlier scores are computed based on the distribution of the data within that mode. The computed outlier scores allow us to identify data points that exhibit significant deviations from the expected behavior of the satellite signals. These anomalies are flagged for further analysis, aiding in the detection of unusual patterns or artifacts in the Swarm satellite data.

In outlier detection, the larger the value of $O(\cdot)$, the farther the data point is from the collective characteristics of the entire dataset, indicating a higher likelihood of being an outlier. $O_{left_only}(X_i)$ represents the distance of data point X_i from the left-tail outliers, while $O_{right_only}(X_i)$ represents the distance from the right-tail outliers. $O_{auto}(X_i)$ considers the skewness of each feature in X_i to determine which direction of outliers to consider.

Specifically, if the skewness of the j -th feature is less than 0, indicating a right-skewed distribution, the left-tail outliers are more likely, so the left-tail outliers are used. Conversely, if the skewness of the j -th feature is greater than or equal to 0, indicating a left-skewed distribution, the right-tail outliers are more likely, so the right-tail outliers are used. The maximum value among $O_{left_only}(X_i)$, $O_{right_only}(X_i)$, and $O_{auto}(X_i)$ is taken as the outlier score O_i for data point X_i , as shown in Equation 7.

$$O_i = \max \{O_{left_only}(X_i), O_{right_only}(X_i), O_{auto}(X_i)\} \tag{7}$$

This outlier score O_i helps identify the extent to which a data point deviates from the overall distribution of the dataset, thereby indicating its likelihood of being an outlier. To determine whether a data point is an outlier, we rank all samples based on their outlier scores O_i in descending order. Specifically, we consider a point to be anomalous if its outlier score lies within the top 1% of the entire dataset. This percentile-based threshold allows us to adaptively identify the most significant deviations while avoiding arbitrary fixed thresholds, thereby enhancing the robustness of the detection process.

3. Results and Discussion

3.1. Pre-earthquake Electromagnetic Data Anomaly Detection

In order to verify the effectiveness of the anomaly detection method proposed in this

study, this study selected an incident that occurred on September 15, 2016, 11 kilometers north-northeast of La Paz Centro urban area in Leon Province, Nicaragua (west longitude 86° , north latitude 12°) of a shallow earthquake of magnitude 5.7. After obtaining electromagnetic data from the swarm satellite in the time range from 6 months before the earthquake to 3 months after the earthquake, anomalies were detected within this interval. In our study, we selected a relatively long time window (approximately three months) to analyze anomaly patterns. This choice was based on empirical observations showing that pre-seismic anomalies tend to emerge gradually and are more reliably captured over extended periods. After obtaining the electromagnetic data, effective earthquake-related signals are obtained by removing the static field and dynamic field of the earth. On this basis, the data is segmented. The segmentation is based on the orbit number (OrbitNumber) of the Swarm satellite. For the Swarm A satellite, it is in a near-polar orbit at an altitude of 462-524 kilometers and an orbital inclination of 87.4° degrees. In this orbit, the Swarm A satellite takes approximately 91 minutes to orbit the Earth. Therefore, the data time span of each piece of data is 91 minutes.

Figure 3 presents the geographic distribution of earthquake epicenters with a magnitude greater than 5.0 in the Nicaragua region from 2000 to the present (March 4, 2023). In the Figure, the size of the blue dots represents the magnitude intensity of each earthquake. Furthermore, the red star in the figure indicates the location of the seismic event selected in this survey.

As shown in Figure 4, Figure 4a displays the cumulative results obtained by applying the ECOD method directly to the original data without utilizing the PSO-VMD method for preprocessing. On the other hand, Figure 4b represents the cumulative results obtained after applying the PSO-VMD method for preprocessing. Since the trend of the sigmoid function (Oksum et al., 2021) is gradual-steep-gradual, fitting the cumulative results with the sigmoid function allows for a better representation of the pre-earthquake anomaly trend. Consequently, the fitted Sigmoid function is utilized to discern the trend of the critical anomaly.

To determine whether anomalies are related to earthquakes, analysis can be conducted by calculating cumulative anomalies. If the cumulative anomalies show a linear increasing trend, it indicates a random process. Conversely, if the cumulative anomalies exhibit a sharp rise before the earthquake, especially with multiple sudden anomalies occurring in the period leading up to the earthquake, followed by a return to stability after the earthquake, it can be concluded that there is a strong correlation between the anomalies and the earthquake event. Since the trend of the sigmoid function (Equation 8) is gradual-steep-gradual, fitting the cumulative results with a sigmoid function can better characterize the trend of pre-earthquake anomalies, allowing the identification of critical anomaly trends. Compared with other sigmoid functions (such as Logistic function, Hill function, SWeibull function), the Boltzmann function has more adjustment parameters, so this study chose it as the fitting function. The adjusted sigmoid function is Boltzmann function like Equation 8, where A_1 controls the upper bound of the function, and the A_2 control the lower bound, x_0 controls

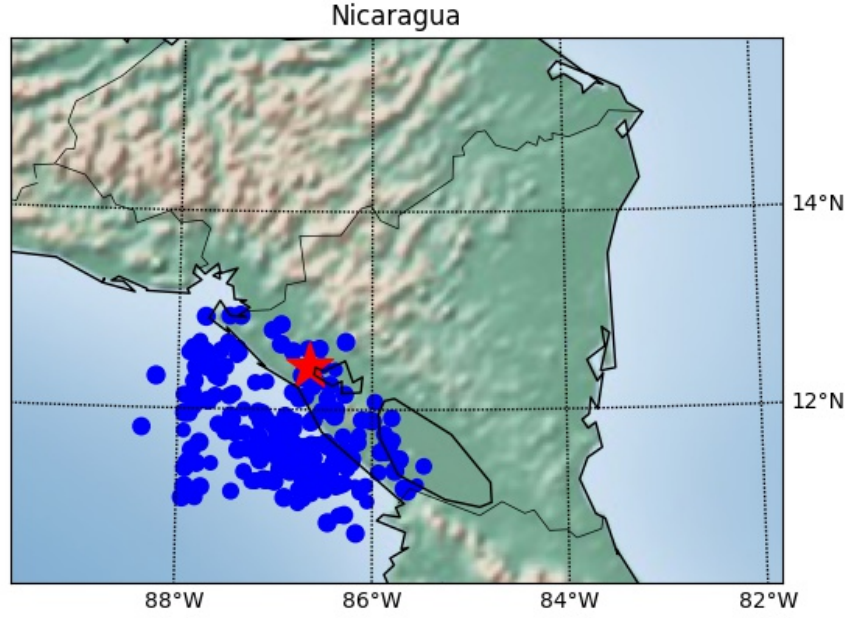
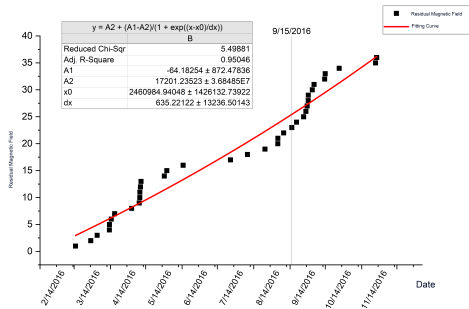
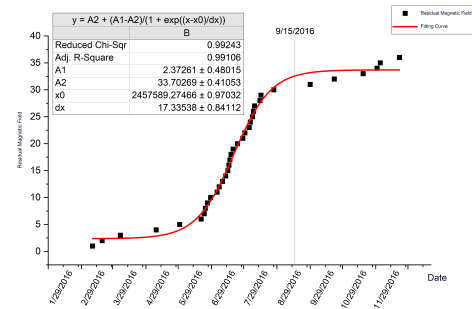


Figure 3: Nicaragua earthquake distribution map. Each point in the map represents the location of an earthquake with a magnitude greater than 5. The size of the blue point represents the magnitude intensity, and the red asterisk represents the earthquake selected in the experiment.



(a) Anomaly detection based on raw data



(b) Anomaly detection based on PSO-VMD

Figure 4: Pre-earthquake anomaly detection comparison of Nicaragua between raw data and preprocessed data with PSO-VMD.

the growth inflection point, and dx controls the growth slope.

$$f(x) = A_2 + \frac{A_1 - A_2}{1 + e^{-\frac{(x-x_0)}{dx}}} \quad (8)$$

To provide an initial assessment of the fitting results, this study utilizes the Adjusted R-Squared coefficient. The main purpose of Adjusted R-Squared is to measure the difference between the fitting results and the original data. Equation 9 represents the calculation method of Adjusted R-Squared, where RSS denotes the residual sum of squares of the regression model, TSS represents the total sum of squares of the data, n is the sample size and p is the number of independent variables. Compared to R-Squared, Adjusted R-Squared adjusts R-Squared based on the sample size and the number of independent variables to account for the influence of irrelevant dimensions on the fitting results. The use of Adjusted R-Square in this study can better reflect the correlation between the abnormal accumulation trend and the fitting function, so as to better study pre-earthquake anomalies.

$$\begin{cases} R^2 = 1 - \frac{RSS}{TSS} = 1 - \frac{\sum (y - \hat{y})^2}{\sum (y - \bar{y})^2} \\ R_{adj}^2 = 1 - \frac{(1 - R^2)(n - 1)}{n - p - 1} \end{cases} \quad (9)$$

3.2. Global Random Seismic Anomaly Analysis

In order to further study the generalization ability of this method, we randomly selected multiple earthquake events and non-earthquake events and applied this method to perform pre-earthquake anomaly detection. Within the year 2016, a random selection of events was made. The time range for the selected events was 180 days before and 90 days after the given earthquake occurrences. Among the selected events, there were a total of 6 earthquake events and 14 non-earthquake events (no earthquakes greater than magnitude 5 occurred within the given grid). The detailed information of the earthquake and non-earthquake events is presented in Tables 2 and Tables 3, respectively.

Table 2: random earthquake event

Index	Earthquake Occurrence Time	Latitude	Longitude	Magnitude Level
A	2016/3/18 16:11	43°	72°	5.6
B	2016/4/2 5:50	62°	-155°	5.9
C	2016/3/10 3:24	-55°	-66°	5.2
D	2016/5/28 9:46	-57.74°	-27.15°	7.2
E	2016/9/15 5:57	13°	-85.75°	5.7
F	2016/5/28 4:43	5°	-38°	5.2

The earthquake events and non-earthquake events have undergone data preprocessing, signal classification, and anomaly detection, and the results have been fitted. Figure 5 shows

Table 3: random non earthquake event

Index	Earthquake Time	Lat	Lon	Index	Earthquake Time	Lat	Lon
A	2016/5/27 19:32	-71°	-60°	H	2016/8/22 16:41	-24°	-49°
B	2016/8/13 2:18	54°	89°	I	2016/8/21 17:40	-15°	146°
C	2016/5/6 20:24	-45°	115°	J	2016/6/12 10:49	38°	11°
D	2016/4/10 21:59	36°	-103°	K	2016/7/25 3:31	34°	114°
E	2016/8/26 6:32	67°	-173°	L	2016/8/21 1:22	-63°	-71°
F	2016/6/8 20:35	-35°	15°	M	2016/5/20 9:51	68°	138°
G	2016/6/9 21:50	65°	46°	N	2016/4/21 14:11	18°	69°

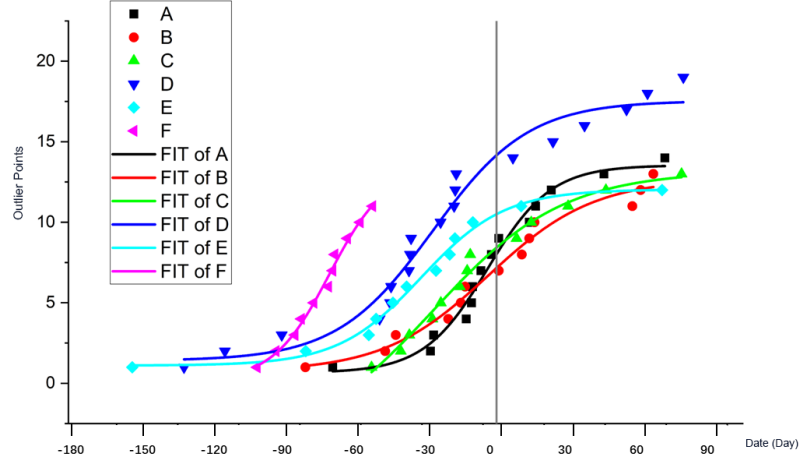
the final results. The time scale for all events is constrained between -180 days and 90 days. In the figure, the gray line represents the occurrence of earthquake events.

Figure 5a represents the results of anomaly detection for earthquake events. It is evident that there is a significant increase in the number of outlier points at the occurrence of earthquake events. Furthermore, these outlier points follow the trend of a Sigmoid function more closely. In contrast, the data during non-earthquake events, as shown in Figure 5b and Figure 5c, exhibit smaller increases in the fitted anomalies, which are closer to linear and thus more consistent with the probability of random event occurrences.

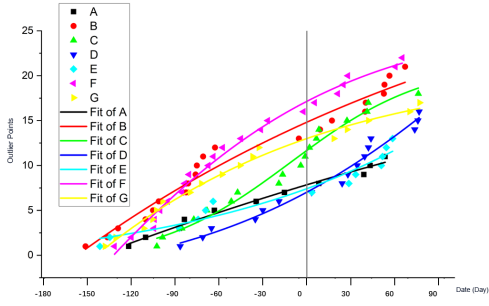
To qualitatively study the fitting quality, we will use the given R_{adj}^2 in Equation 9 as a criterion to compare the linear fitting and Boltzmann function fitting for earthquake and non-earthquake events. Additionally, we will use the ratio of the Boltzmann function-fitted R_{adj}^2 to the linear-fitted R_{adj}^2 , as shown in Equation 9, and take its logarithm as a basis. If this ratio is greater than 0, it indicates that the curve is closer to the Boltzmann function; if the ratio is less than 0, it indicates that the curve is closer to a linear function. Furthermore, we will use two parameters to assist in assessing the quality of the fitting results. x_0 , which represents the time difference between the Boltzmann function-fitted center value and the occurrence of earthquake events, will be used to determine if the fitting result detects anomalies within a reasonable time. The larger the absolute value of x_0 is, the greater the difference between the detected anomaly and the earthquake occurrence time is, and the weaker the correlation. dx will characterize the growth trend of the Boltzmann function and can indicate the magnitude of anomaly amplitudes.

$$R_{ratio} = \log\left(\frac{R_{Boltzmann}^2}{R_{linear}^2}\right) \times 100 \quad (10)$$

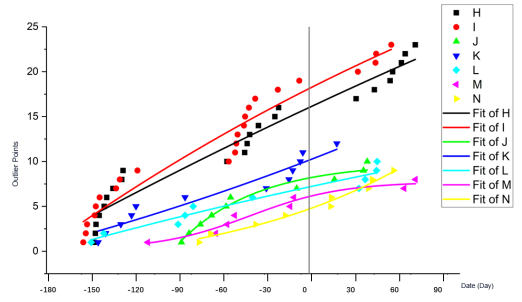
According to Table 4 and Table 5, x_0 represents the number of days relative to the occurrence of the earthquake, where negative values indicate pre-earthquake and positive values indicate post-earthquake. dx represents the rate of anomaly accumulation, and its value is converted to the ratio with the average value of all dx data. The closer the value is to 0, the more pronounced the rate of anomaly accumulation. Regarding earthquake events, we can observe from Table 4 that almost all x_0 values are close to the occurrence of the event, and R_{ratio} values are greater than 0, indicating that the trend of outlier points is



(a) Earthquake event



(b) Non-seismic events (part 1)



(c) Non-seismic events (part 2)

Figure 5: Random earthquake event analysis (a) is the anomaly detection result for earthquake events, (b) and (c) are the anomaly detection results for non-earthquake events.

closer to the Boltzmann function rather than linear growth. Additionally, the dx values are close to 0, indicating significant increases in anomaly rates occurring before the earthquake.

To further validate these observations, we performed independent two-sample t-tests to assess whether the differences in anomaly detection indicators between earthquake and non-earthquake events are statistically significant. The results show that the difference in dx is statistically significant ($p = 0.0027$), suggesting a distinct pattern of anomaly accumulation in earthquake events. The difference in R_{ratio} is marginally significant ($p = 0.0504$), indicating a potential difference in the fitting trend between the two groups. However, the difference in x_0 is not statistically significant ($p = 0.2503$), which may be due to the large variability in anomaly timing among non-earthquake events.

However, for the anomaly detection result indicators in the non-earthquake time period in Table 5, almost all values are unreasonable. For example, events A, E, H, I, J, and L are

closer to the fitting result of random events. For events B, G, K, and N, the inflection points are too far from the events, making them meaningless in practical terms. Although the data point M may seem reasonable, it is actually due to a small value of $|A_1 - A_2|$, which is 7. This means that although there is some level of anomaly, the perturbation is small and can be ignored.

Table 4: Earthquake Event Anomaly Detection Result Metrics

Index	R_{ratio}	x_0	dx
A	5.08392	-4	0.06
B	1.034487	-4	0.10
C	3.362188	-30	0.12
D	1.896997	-30	0.09
E	8.724399	-36	0.08
F	0.664581	-79	0.05

Table 5: Non Earthquake Event Anomaly Detection Result Metrics

Index	R_{ratio}	x_0	dx	Index	R_{ratio}	x_0	dx
A	-0.14521	-2282	2.65	H	-0.25267	-2873	4.58
B	0.053099	-1614	1.46	I	-0.12263	-1995	2.19
C	0.105649	-13	0.22	J	1.982042	-537	0.25
D	0.655548	169	0.46	K	-0.94167	2728	2.32
E	-0.016	1232	0.74	L	-1.04415	-2358	2.83
F	1.071618	-207	0.44	M	0.679202	-47	0.14
G	1.401158	-456	0.63	N	0.450923	785	0.59

By utilizing the three parameters, R_{ratio} , x_0 and dx , along with the examples of earthquake events, we can compare the proposed method with other methods as shown in Table 6 based on the average values of these parameters. It can be observed that all the methods are able to fit the Sigmoid function well in terms of the fitting aspect. Compared to the EEMD (Barman et al., 2016), EMD (Yang et al., 2023), SSA (Rasheed et al., 2023), and Kalman filtering (Kitahara et al., 2023) methods, the proposed method exhibits a noticeable rise in anomalies during the 30 days before the earthquake, while the other methods show an accumulation of anomalies that starts after a certain period following the earthquake. Even for the Kalman filtering and SSA methods, anomalies start accumulating after approximately 500 days post-earthquake, indicating that these two methods perform poorly in extracting pre-earthquake anomalies. Compared to the CEEMDAN (Chen et al., 2021) method, both the proposed method and the CEEMDAN method can detect anomalies within a certain period before the earthquake. However, only the proposed method can identify the most obvious process of anomaly accumulation. The other methods are also able to fit the Sigmoid function, but the accumulation of anomalies is less evident. Only the proposed method

and the CEEMDAN method show clear anomalies in the processed waveforms, and only the proposed method and the CEEMDAN method can observe the accumulation of anomalies before the earthquake.

Table 6: Comparative Experiment

	R_{ratio}	x_0	dx (10^5)
Proposed Method	3.46	-30.58	18.25
CEEMDAN(Chen et al., 2021)	6.78	-20.73	378.73
EEMD(Barman et al., 2016)	3.72	140.20	3280.62
EMD(Yang et al., 2023)	6.90	69.48	416.32
SSA(Rasheed et al., 2023)	1.45	492.15	1843.93
Kalman(Kitahara et al., 2023)	1.145	512.85	1854.91

4. Conclusion

The study explores the detection of seismic anomalies through the analysis of geomagnetic data, acknowledging fluctuations in Earth’s geomagnetic field strength reflected by processed Swarm data during earthquake development. Given the relative smallness of these variations compared to the overall field strength, it’s necessary to decompose the geomagnetic field before performing anomaly detection. This approach is applied in the analysis of a seismic event that occurred in the Nicaragua region on September 15, 2016.

The study employs an enhanced signal decomposition technique based on Variational Mode Decomposition (VMD), specifically Particle Swarm Optimization-VMD (PSO-VMD), to mitigate the interference of the electromagnetic dynamic field. This method assists in investigating the association between electromagnetic data and earthquakes. Then we further use the Empirical-Cumulative-distribution-based Outlier Detection (ECOD) method for anomaly clustering of orbital numbers.

The methods presented in this study identify a slow-fast-slow pattern in the accumulation of anomalies preceding the earthquake, a finding not easily discernable in the raw data. This research offers significant contributions to the field of seismic anomaly detection, demonstrating the potential of PSO-VMD and ECOD in unearthing valuable insights from satellite electromagnetic signals. However, its complexity may necessitate additional time and resources when applied to large satellite datasets. Future research should aim to streamline the methodology and explore computational optimization techniques to facilitate its widespread application in earthquake precursor analysis.

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6. Declaration of generative AI and AI-assisted technologies in the writing process

During the preparation of this work the author used ChatGPT in order to improve language and readability. After using this tool, the author reviewed and edited the content as needed and takes full responsibility for the content of the publication.

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