

- '15.1 (a) Taking to the right as positive, the spring force acting on the block at the instant of release is

$$F_s = -kx_i = -(130 \text{ N/m})(+0.13 \text{ m}) \\ = -17 \text{ N} \text{ or } \boxed{17 \text{ N to the left}}$$

- (b) At this instant, the acceleration is

$$a = \frac{F_s}{m} = \frac{-17 \text{ N}}{0.60 \text{ kg}} = -28 \text{ m/s}^2$$

or $\boxed{a = 28 \text{ m/s}^2 \text{ to the left}}$

- '15.4 (a) The equation for the piston's position is given as

$$x = (5.00 \text{ cm}) \cos\left(2t + \frac{\pi}{6}\right)$$

At $t = 0$,

$$x = (5.00 \text{ cm}) \cos\left(\frac{\pi}{6}\right) = \boxed{4.33 \text{ cm}}$$

- (b) Differentiating the equation for position with respect to time gives us the piston's velocity:

$$v = \frac{dx}{dt} = -(10.0 \text{ cm/s}) \sin\left(2t + \frac{\pi}{6}\right)$$

At $t = 0$, $v = \boxed{-5.00 \text{ cm/s}}$

- (c) Differentiating again gives its acceleration:

$$a = \frac{dv}{dt} = -(20.0 \text{ cm/s}^2) \cos\left(2t + \frac{\pi}{6}\right)$$

At $t = 0$, $a = \boxed{-17.3 \text{ cm/s}^2}$

- (d) The period of motion is

$$T = \frac{2\pi}{\omega} = \frac{2\pi}{2} = \boxed{3.14 \text{ s}}$$

- (e) We read the amplitude directly from the equation for x :

$$A = \boxed{5.00 \text{ cm}}$$

- '15.5 $x = (4.00 \text{ m})\cos(3.00\pi t + \pi)$; compare this with $x = A \cos(\omega t + \phi)$ to find

(a) $\omega = 2\pi f = 3.00\pi$ or $\boxed{f = 1.50 \text{ Hz}}$

(b) $T = \frac{1}{f} = \boxed{0.667 \text{ s}}$

(c) $A = \boxed{4.00 \text{ m}}$

(d) $\phi = \boxed{\pi \text{ rad}}$

(e) $x(t = 0.250 \text{ s}) = (4.00 \text{ m}) \cos(1.75\pi) = \boxed{2.83 \text{ m}}$

- 15.17 (a) The distance traveled in one cycle is four times the amplitude of motion, or $\boxed{20.0 \text{ cm}}$.

(b) $v_{\max} = \omega A = 2\pi f A = 2\pi(3.00 \text{ Hz})(5.00 \text{ cm}) = \boxed{94.2 \text{ cm/s}}$

This occurs as the particle passes through equilibrium.

(c) $a_{\max} = \omega^2 A = (2\pi f)^2 A = [2\pi(3.00 \text{ Hz})]^2 (0.05 \text{ m}) = \boxed{17.8 \text{ m/s}^2}$

This occurs at maximum excursion from equilibrium.

- 15.19 $\omega = \sqrt{\frac{k}{m}} = \sqrt{\frac{8.00 \text{ N/m}}{0.500 \text{ kg}}} = 4.00 \text{ s}^{-1}$. Assuming the position of the object is at the origin at $t = 0$, position is given by $x = 10.0 \sin(4.00t)$, where x is in cm. From this, we find that $v = 40.0 \cos(4.00t)$, where v is in cm/s, and $a = -160 \sin(4.00t)$, where a is in cm/s².

(a) $v_{\max} = \omega A = (4.00 \text{ rad/s})(10.0 \text{ cm}) = \boxed{40.0 \text{ cm/s}}$

(b) $a_{\max} = \omega^2 A = (4.00 \text{ rad/s})^2 (10.0 \text{ cm}) = \boxed{160 \text{ cm/s}^2}$

From our assumed expression for x , we solve for the time t :

$$t = \left(\frac{1}{4.00 \text{ Hz}} \right) \sin^{-1} \left(\frac{x}{10.0 \text{ cm}} \right)$$

When $x = 6.00 \text{ cm}$, $t = \left(\frac{1}{4.00 \text{ Hz}} \right) \sin^{-1} \left(\frac{6.00 \text{ cm}}{10.0 \text{ cm}} \right) = 0.161 \text{ s}$.

We find then that at that time:

(c) $v = (40.0 \text{ cm/s}) \cos [(4.00 \text{ Hz})(0.161 \text{ s})] = \boxed{32.0 \text{ cm/s}}$ and

(d) $a = -(160 \text{ cm/s}^2) \sin [(4.00 \text{ Hz})(0.161 \text{ s})] = \boxed{-96.0 \text{ cm/s}^2}$

(e) Using $t = \left(\frac{1}{4.00 \text{ Hz}} \right) \sin^{-1} \left(\frac{x}{10.0 \text{ cm}} \right)$ we find that when $x = 0$, $t = 0$, and when $x = 8.00 \text{ cm}$, $t = 0.232 \text{ s}$. Therefore, $\Delta t = \boxed{0.232 \text{ s}}$.

15.33 (a) The motion is simple harmonic because the tire is rotating with constant angular velocity and you see the projection of the motion of the bump in a plane perpendicular to the tire.

(b) Since the car is moving with speed $v = 3.00 \text{ m/s}$, and its radius is 0.300 m , we have

$$\omega = \frac{3.00 \text{ m/s}}{0.300 \text{ m}} = 10.0 \text{ rad/s}$$

Therefore, the period of the motion is

$$T = \frac{2\pi}{\omega} = \frac{2\pi}{(10.0 \text{ rad/s})} = \boxed{0.628 \text{ s}}$$