

## Problems

5. Pat builds a track for his model car out of solid wood as shown in Figure P12.5. The track is 5.00 cm wide, 1.00 m high, and 3.00 m long. The runway is cut so that it forms a parabola with the equation  $y = (x - 3)^2/9$ . Locate the horizontal coordinate of the center of gravity of this track.

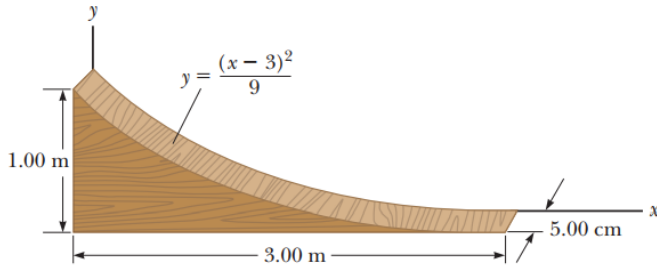


Figure P12.5

6. A circular pizza of radius  $R$  has a circular piece of radius  $R/2$  removed from one side as shown in Figure P12.6. The center of gravity has moved from  $C$  to  $C'$  along the  $x$ -axis. Show that the distance from  $C$  to  $C'$  is  $R/6$ . Assume the thickness and density of the pizza are uniform throughout.

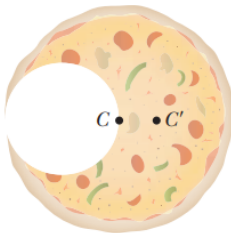


Figure P12.6

9. Find the mass  $m$  of the counterweight needed to balance a truck with mass  $M = 1500$  kg on an incline of  $\theta = 45^\circ$  (Fig. P12.9). Assume both pulleys are frictionless and massless.

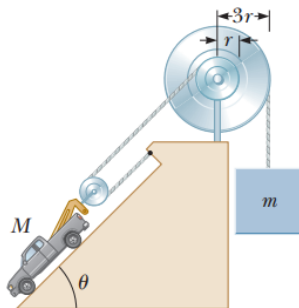


Figure P12.9

11. A uniform beam of length 7.60 m and weight  $4.50 \times 10^2$  N is carried by two workers, Sam and Joe, as shown in Figure P12.11. Determine the force that each person exerts on the beam.

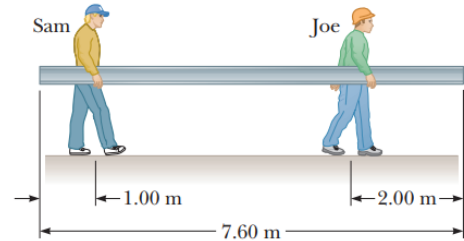


Figure P12.11

13. A 15.0-m uniform ladder weighing 500 N rests against a frictionless wall. The ladder makes a  $60.0^\circ$  angle with the horizontal. (a) Find the horizontal and vertical forces the ground exerts on the base of the ladder when an 800-N firefighter has climbed 4.00 m along the ladder from the bottom. (b) If the ladder is just on the verge of slipping when the firefighter is 9.00 m from the bottom, what is the coefficient of static friction between ladder and ground?

14. A uniform ladder of length  $L$  and mass  $m_1$  rests against a frictionless wall. The ladder makes an angle  $\theta$  with the horizontal. (a) Find the horizontal and vertical forces the ground exerts on the base of the ladder when a firefighter of mass  $m_2$  has climbed a distance  $x$  along the ladder from the bottom. (b) If the ladder is just on the verge of slipping when the firefighter is a distance  $d$  along the ladder from the bottom, what is the coefficient of static friction between ladder and ground?

16. A uniform beam of length  $L$  and mass  $m$  shown in Figure P12.16 is inclined at an angle  $\theta$  to the horizontal. Its upper end is connected to a wall by a rope, and its lower end rests on a rough, horizontal surface. The coefficient of static friction between the beam and surface is  $\mu_s$ . Assume the angle  $\theta$  is such that the static friction force is at its maximum value. (a) Draw a force diagram for the beam. (b) Using the condition of rotational equilibrium, find an expression for the tension  $T$  in the rope in terms of  $m$ ,  $g$ , and  $\theta$ . (c) Using the condition of translational equilibrium, find a second expression for  $T$  in terms of  $\mu_s$ ,  $m$ , and  $g$ . (d) Using the results from parts (a) through (c), obtain an expression for  $\mu_s$  involving only the angle  $\theta$ . (e) What happens if the ladder is lifted upward and its base is placed back on the ground slightly to the left of its position in Figure P12.16? Explain.

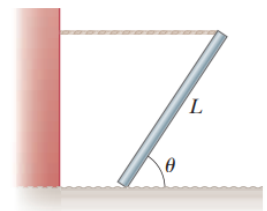


Figure P12.16

5) 0.75 m  
23) 2.81 m

9) 177 kg  
25) 501N, 672N & 384 N

11) 274 & 176 N

13) 1300 & 268 N, 0.324

16)  $T = mg\mu$ ,  $\mu = 0.5 \cot \theta$

23. One end of a uniform 4.00-m-long rod of weight  $F_g$  is supported by a cable at an angle of  $\theta = 37^\circ$  with the rod. The other end rests against the wall, where it is held by friction as shown in Figure P12.23. The coefficient of static friction between the wall and the rod is  $\mu_s = 0.500$ . Determine the minimum distance  $x$  from point A at which an additional object, also with the same weight  $F_g$ , can be hung without causing the rod to slip at point A.

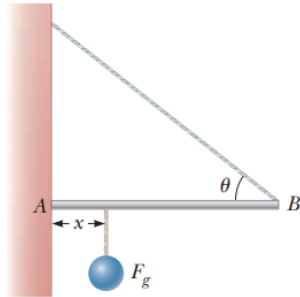


Figure P12.23

25. A uniform plank of length 2.00 m and mass 30.0 kg is supported by three ropes as indicated by the blue vectors in Figure P12.25. Find the tension in each rope when a 700-N person is  $d = 0.500$  m from the left end.

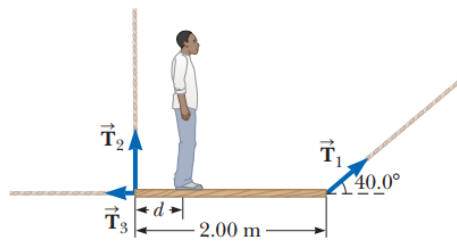


Figure P12.25