

Problems

27. A large, flat, horizontal sheet of charge has a charge per unit area of $9.00 \mu\text{C}/\text{m}^2$. Find the electric field just above the middle of the sheet.

33. Consider a long, cylindrical charge distribution of radius R with a uniform charge density ρ . Find the electric field at distance r from the axis, where $r < R$.

34. A cylindrical shell of radius 7.00 cm and length 2.40 m has its charge uniformly distributed on its curved surface. The magnitude of the electric field at a point 19.0 cm radially outward from its axis (measured from the midpoint of the shell) is 36.0 kN/C . Find (a) the net charge on the shell and (b) the electric field at a point 4.00 cm from the axis, measured radially outward from the midpoint of the shell.

37. A long, straight metal rod has a radius of 5.00 cm and a charge per unit length of 30.0 nC/m . Find the electric field (a) 3.00 cm , (b) 10.0 cm , and (c) 100 cm from the axis of the rod, where distances are measured perpendicular to the rod's axis.

38. Why is the following situation impossible? A solid copper sphere of radius 15.0 cm is in electrostatic equilibrium and carries a charge of 40.0 nC . Figure P24.38 shows the magnitude of the electric field as a function of radial position r measured from the center of the sphere.

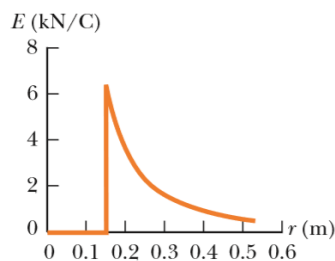


Figure P24.38

50. A hollow, metallic, spherical shell has exterior radius 0.750 m , carries no net charge, and is supported on an insulating stand. The electric field everywhere just outside its surface is 890 N/C radially toward the center of the sphere. Explain what you can conclude about (a) the amount of charge on the exterior surface of the sphere and the distribution of this charge, (b) the amount of charge on the interior surface of the sphere and its distribution, and (c) the amount of charge inside the shell and its distribution.

54. A solid, insulating sphere of radius a has a uniform charge density throughout its volume and a total charge Q . Concentric with this sphere is an uncharged, conducting, hollow sphere whose inner and outer radii are b and c as shown in Figure P24.54 (page 744). We wish to

understand completely the charges and electric fields at all locations. (a) Find the charge contained within a sphere of radius $r < a$. (b) From this value, find the magnitude of the electric field for $r < a$. (c) What charge is contained within a sphere of radius r when $a < r < b$? (d) From this value, find the magnitude of the electric field for r when $a < r < b$. (e) Now consider r when $b < r < c$. What is the magnitude of the electric field for this range of values of r ? (f) From this value, what must be the charge on the inner surface of the hollow sphere? (g) From part (f), what must be the charge on the outer surface of the hollow sphere? (h) Consider the three spherical surfaces of radii a , b , and c . Which of these surfaces has the largest magnitude of surface charge density?

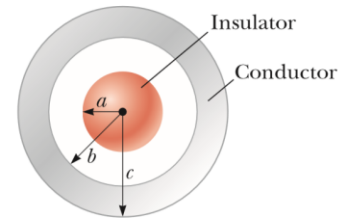


Figure P24.54

Problems 54, 55, and 57.

55. A solid insulating sphere of radius $a = 5.00 \text{ cm}$ carries a net positive charge of $Q = 3.00 \mu\text{C}$ uniformly distributed throughout its volume. Concentric with this sphere is a conducting spherical shell with inner radius $b = 10.0 \text{ cm}$ and outer radius $c = 15.0 \text{ cm}$ as shown in Figure P24.54, having net charge $q = -1.00 \mu\text{C}$. Prepare a graph of the magnitude of the electric field due to this configuration versus r for $0 < r < 25.0 \text{ cm}$.

56. Two infinite, nonconducting sheets of charge are parallel to each other as shown in Figure P24.56. The sheet on the left has a uniform surface charge density σ , and the one on the right has a uniform charge density $-\sigma$. Calculate the electric field at points (a) to the left of, (b) in between, and (c) to the right of the two sheets. (d) **What If?** Find the electric fields in all three regions if both sheets have positive uniform surface charge densities of value σ .

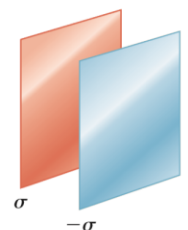
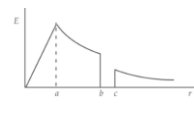


Figure P24.56

57. For the configuration shown in Figure P24.54, suppose $a = 5.00 \text{ cm}$, $b = 20.0 \text{ cm}$, and $c = 25.0 \text{ cm}$. Furthermore, suppose the electric field at a point 10.0 cm from the center is measured to be $3.60 \times 10^3 \text{ N/C}$ radially inward and the electric field at a point 50.0 cm from the center is of magnitude 200 N/C and points radially outward. From this information, find (a) the charge on the insulating sphere, (b) the net charge on the hollow conducting sphere, (c) the charge on the inner surface of the hollow conducting sphere, and (d) the charge on the outer surface of the hollow conducting sphere.

27) $5.08 \times 10^5 \text{ N/C}$ 33) $E = \frac{\rho r}{2\epsilon_0}$ 34) $9.13 \times 10^{-7} \text{ C}, 0$ 37) $0, 5400 \text{ N/C}, 540 \text{ N/C}$ 38) 50) $+, - 5.57 \times 10^{-8} \text{ C}$

54) $Qr^3/a^3, kQr/a^3, Q, kQ/r^2, 0, \text{ in } -Q, \text{ out } +Q, a > b > c$ 55)



57) $-4.0 \text{ nC}, 9.56 \text{ nC}, 4.0 \text{ nC}, 5.56 \text{ nC}$

56) $0, E = \frac{\sigma}{\epsilon_0}, 0, -\frac{\sigma}{\epsilon_0}, 0, \frac{\sigma}{\epsilon_0}$