model output

xj2249 12/15/2019

Data cleaning

```
# import
df = read_csv("Lawsuit.csv") %>%
  janitor::clean_names() %>%
  mutate(dept = factor(dept, levels = c(1:6), labels = c("Biochemistry/Molecular Biology", "Physiology
         gender = factor(gender, levels = c(0, 1), labels = c("Female", "Male")),
         clin = factor(clin, levels = c(1, 0), labels = c("Clinical", "Research")),
         cert = factor(cert, levels = c(1, 0), labels = c("Certified", "Not certified")),
         rank = factor(rank, levels = c(1, 2, 3), labels = c("Assistant", "Associate", "Full professor"
         sal = (sal94 + sal95)/2)
## Parsed with column specification:
## cols(
##
     ID = col_double(),
##
    Dept = col_double(),
     Gender = col_double(),
##
     Clin = col_double(),
##
    Cert = col_double(),
##
##
    Prate = col_double(),
##
    Exper = col_double(),
    Rank = col_double(),
##
    Sal94 = col_double(),
##
##
     Sal95 = col_double()
## )
# consider log mean sal only
df_sal = df %>%
  mutate(log_sal = log(sal)) %>%
  dplyr::select(-sal95, -id, -sal94, -sal)
```

interaction term (not sure whether to test)

```
## general test

# no prate
fit_conf = lm(log_sal ~gender+dept+clin+cert+exper+rank, data = df_sal)
summary(fit_conf)
```

Call: $lm(formula = log_sal \sim gender + dept + clin + cert + exper + rank, data = df_sal)$ Residuals: Min 1Q Median 3Q Max -0.34605 -0.07696 -0.01873 0.07596 0.90393 Coefficients: Estimate Std. Error t value $\Pr(>|t|)$ (Intercept) 11.373862 0.034398 330.651 < 2e-16 genderMale~0.025763~0.019624~1.313~0.19 deptPhysiology~0.175749~0.029122~6.035~5.73e-09 deptGenetics 0.185970 0.036501 5.095 6.90e-07 deptPediatrics~0.203345~0.035712~5.694~3.48e-08 deptMedicine 0.539304 0.029515 18.272 < 2e-16 deptSurgery~0.933820~0.035533~26.280 < 2e-16 clinResearch~0.208340 0.021885~9.520 < 2e-16 certNot~certified~0.189749~0.021244~8.932 < 2e-16 exper 0.017726 0.001812 9.783 < 2e-16 rankAssociate~0.134663~0.023557~5.716~3.10e-08 rankFull professor 0.222214 0.026249 8.466 2.22e-15 *** — Signif. codes: 0 '' 0.001 " 0.01 " 0.05 " 0.1 "

Residual standard error: 0.1337 on 249 degrees of freedom Multiple R-squared: 0.9339, Adjusted R-squared: 0.931 F-statistic: 319.7 on 11 and 249 DF, p-value: < 2.2e-16

```
fit_int = lm(log_sal ~gender+dept+clin+cert+exper+ gender*rank +gender*exper, data = df_sal)
```

Interaction term *gender* * *exper* is significant, thus we may conside it in our model.

stratified regression

dept	n	coef	p
Biochemistry/Molecular Biology	50	-0.0187106	0.6600235
Physiology	40	-0.0052950	0.9224663
Genetics	21	0.0754572	0.2339215
Pediatrics	30	0.0115277	0.8453661
Medicine	80	0.0366927	0.3660339
Surgery	40	0.0416427	0.4947262

```
stratified_clin = df_sal %>%
  group_by(clin) %>%
summarize(
    n = n(),
    coef = lm(log_sal ~ gender + dept + cert + exper +
    rank)$coef["genderMale"],
    p = summary(lm(log_sal ~ gender + dept + cert + exper +
    rank))$coefficients["genderMale",4]
    )
stratified_clin %>%
  knitr::kable()
```

clin	n	coef	p
Clinical	160	0.0083165	0.7108663
Research	101	0.0465115	0.2948187

```
stratified_cert = df_sal %>%
  group_by(cert) %>%
summarize(
    n = n(),
    coef = lm(log_sal ~ gender + dept + clin + exper +
    rank)$coef["genderMale"],
    p = summary(lm(log_sal ~ gender + dept + clin + exper +
    rank))$coefficients["genderMale",4]
    )
stratified_cert %>%
    knitr::kable()
```

cert	n	coef	p
Certified	188	0.0126811	0.5584154
Not certified	73	0.0265111	0.5547041

```
stratified_rank = df_sal %>%
  group_by(rank) %>%
  summarize(
    n = n(),
    coef = lm(log_sal ~ gender + dept + clin + cert + exper)$coef["genderMale"],
    p = summary(lm(log_sal ~ gender + dept + clin + cert + exper))$coefficients["genderMale",4]
    )
  stratified_rank %>%
  knitr::kable()
```

rank	n	coef	p
Assistant	112	0.0826555	0.0213160
Associate	64	-0.0132771	0.6702516
Full professor	85	-0.0404129	0.2680458

```
summarize(
    n = n(),
    coef = lm(log_sal ~ gender + dept + clin + cert + rank)$coef["genderMale"],
    p = summary(lm(log_sal ~ gender + dept + clin + cert + rank))$coefficients["genderMale",4]
         )
stratified_exper %>%
    knitr::kable()
```

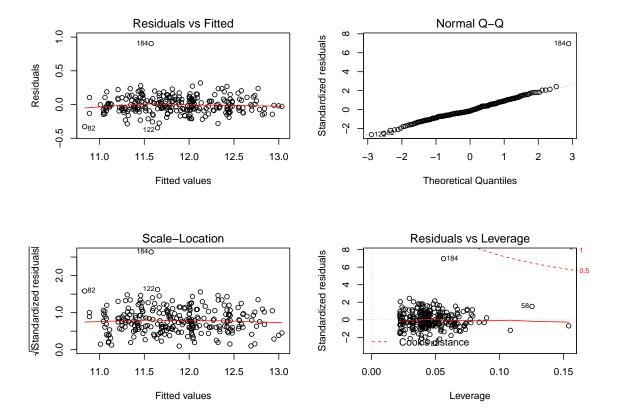
exper	n	coef	p
0	64	0.1257741	0.0238410
1	57	0.0340942	0.2757676
2	74	-0.0005508	0.9876466
3	66	-0.0034961	0.9439975

```
df_exper %>%
  group_by(exper, rank) %>%
  summarize(
    n = n())
```

```
## # A tibble: 11 x 3
## # Groups: exper [4]
##
     exper rank
     <fct> <fct>
                     <int>
## 1 0
       Assistant
                       59
## 2 0
        Associate
                         5
## 3 1
        Assistant
                        36
## 4 1
       Associate
                         15
## 5 1
        Full professor
                        6
## 6 2 Assistant
                        12
## 7 2
        Associate
                         31
## 8 2 Full professor
                        31
## 93 Assistant
                         5
## 10 3
        Associate
                         13
## 11 3
        Full professor
                        48
```

Model diagnostics

```
final_model = lm(log_sal ~gender+dept+clin+cert+exper+rank, data = df_sal)
par(mfrow = c(2,2))
plot(final_model)
```



Outliers/influential points

```
stu_res<-rstandard(final_model)</pre>
stu_res[abs(stu_res)>2.5]
##
          82
                    122
                              184
## -2.507753 -2.640742
                         6.960085
influence.measures(final_model) %>%
  summary()
## Potentially influential observations of
##
     lm(formula = log_sal ~ gender + dept + clin + cert + exper +
                                                                           rank, data = df_sal) :
##
##
       dfb.1_ dfb.gndM dfb.dptPh dfb.dptG dfb.dptPd dfb.dptM dfb.dptS
        0.08 -0.01
                         0.04
                                    0.04
                                             0.00
                                                        0.03
                                                                 0.03
## 19
##
  82
        0.01
               0.07
                        -0.31
                                    0.00
                                            -0.05
                                                       -0.08
                                                                -0.11
##
  91
        0.04
              -0.01
                        -0.01
                                   -0.08
                                            -0.02
                                                       -0.02
                                                                -0.01
        0.00
              -0.02
                         0.00
                                   0.05
                                                        0.01
                                                                 0.01
## 109
                                             0.00
## 122 -0.14
               0.07
                         0.03
                                    0.04
                                            -0.27
                                                        0.08
                                                                 0.06
## 184 -0.62
               0.75
                         0.22
                                   0.16
                                             0.53
                                                        1.00
                                                                 0.53
## 208
       0.06 -0.19
                        -0.01
                                   -0.01
                                            -0.04
                                                        0.11
                                                                -0.02
##
       dfb.clnR dfb.crNc dfb.expr dfb.rnkA dfb.rnFp dffit
                                                               cov.r
                                                                        cook.d
## 19
       -0.01
                -0.09
                          -0.26
                                     0.05
                                              0.17
                                                       -0.30
                                                                1.21_*
                                                                        0.01
                                                                0.81_* 0.02
## 82 -0.13
                -0.18
                           0.08
                                     0.12
                                              0.07
                                                       -0.54
```

```
## 91 -0.04
                  0.03
                           -0.04
                                      0.02
                                               0.01
                                                        -0.10
                                                                  1.15_*
                                                                           0.00
                            0.00
                                      0.03
                                               0.00
                                                         0.07
                                                                          0.00
## 109
        0.02
                 -0.03
                                                                  1.15 *
                  0.02
                            0.02
                                      0.10
                                               0.05
                                                        -0.54
                                                                  0.78 *
                                                                          0.02
  122
        0.11
  184
        0.94
                  0.84
                           -0.36
                                    -0.51
                                              -0.26
                                                         1.89_*
                                                                  0.08_*
                                                                          0.24
##
##
   208 -0.06
                 -0.04
                            0.21
                                    -0.14
                                              -0.18
                                                         0.43
                                                                  0.81_*
                                                                         0.02
##
       hat
## 19
        0.15 *
## 82
        0.04
## 91
        0.09
## 109
        0.09
  122
##
        0.04
   184
        0.06
##
## 208
        0.03
```

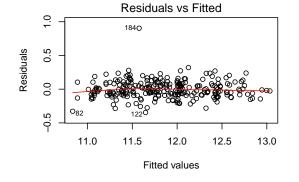
df [184,]

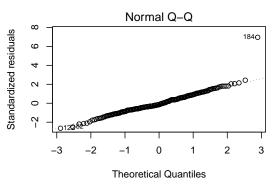
```
## # A tibble: 1 x 11
##
        id dept
                   gender clin
                                  cert
                                          prate exper rank
                                                              sal94
                                                                      sa195
                                                                               sal
##
     <dbl> <fct>
                   <fct>
                          <fct>
                                 <fct>
                                          <dbl> <dbl> <fct>
                                                              <dbl>
                                                                      <dbl>
                          Resea~ Not ce~
                                            5.1
                                                     2 Assi~ 250000 276163 2.63e5
       184 Medic~ Male
```

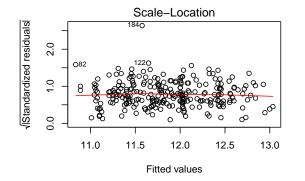
Using studentized residuals, id 184 is an outlier in Y. using leverage values, 19 and 216 are outliers in X. Using DFFIT, 8, 184 and 216 are influential points. Using main effects only, 184 is influential.

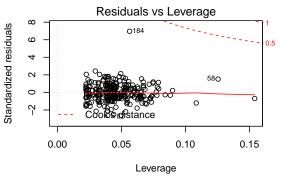
```
# consider the data without influential points
df_sal_noinflu = df_sal[-184, ]

par(mfrow = c(2,2))
plot(final_model)
```









```
temp = lm(log_sal ~gender+dept+clin+cert+exper+gender*rank+gender*exper, data = df_sal_noinflu)
summary(temp)
##
## Call:
## lm(formula = log_sal ~ gender + dept + clin + cert + exper +
     gender * rank + gender * exper, data = df_sal_noinflu)
##
## Residuals:
##
      Min
              1Q
                 Median
                            3Q
                                  Max
## -0.32895 -0.07173 -0.01277 0.08089 0.28179
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        ## genderMale
## deptPhysiology
                         ## deptGenetics
                         0.520522 0.026654 19.529 < 2e-16 ***
0.922849 0.031852 28 070
## deptPediatrics
## deptMedicine
## deptSurgery
## clinResearch
                        ## certNot certified
                      ## exper
                         ## rankAssociate
## rankFull professor
                         ## genderMale:rankAssociate
                         -0.011198 0.043888 -0.255 0.79882
## genderMale:rankFull professor 0.002157 0.054723 0.039 0.96858
                         ## genderMale:exper
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1188 on 245 degrees of freedom
## Multiple R-squared: 0.9483, Adjusted R-squared: 0.9454
## F-statistic: 321.2 on 14 and 245 DF, p-value: < 2.2e-16
df_exper_noinflu = df_sal_noinflu %>%
 mutate(exper_fct = case_when(
    exper < 6 ~ "0",
    exper >= 6 \& exper < 9 ~ "1",
    exper \geq 9 \& exper < 14 ~ "2",
    exper >= 14 ~ "3",
    TRUE ~ ""
 )) %>%
   mutate(exper = factor(exper_fct)) %>%
   dplyr::select(-exper_fct)
stratified_exper_noinflu = df_exper_noinflu %>%
 group_by(exper) %>%
 summarize(
    n = n(),
    coef = lm(log sal ~ gender + dept + clin + cert + rank)$coef["genderMale"],
    p = summary(lm(log_sal ~ gender + dept + clin + cert + rank))$coefficients["genderMale",4]
```

```
)
stratified_exper_noinflu %>%
knitr::kable()
```

exper	n	coef	p
0	63	0.0577437	0.2066119
1	57	0.0340942	0.2757676
2	74	-0.0005508	0.9876466
3	66	-0.0034961	0.9439975

```
stratified_rank_noinflu = df_sal_noinflu %>%
group_by(rank) %>%
summarize(
    n = n(),
    coef = lm(log_sal ~ gender + dept + clin + cert + exper)$coef["genderMale"],
    p = summary(lm(log_sal ~ gender + dept + clin + cert + exper))$coefficients["genderMale",4]
    )
stratified_rank_noinflu %>%
knitr::kable()
```

rank	n	coef	p
Assistant Associate	111 64	0.0390298 -0.0132771	$0.2009195 \\ 0.6702516$
Full professor	85	-0.0404129	0.2680458

Not significant now, -184 usinf main effects model or -216, -184, -8 using interaction model.

model output

% Table created by stargazer v.5.2.2 by Marek Hlavac, Harvard University. E-mail: hlavac at fas.harvard.edu

% Date and time: , 12 16, 2019 - 13 27 29

Table 8:

	Dependent variable:		
	Main effect model	Log Salary Final model with interaction	Final model without 184
	(1)	(2)	(3)
Male	0.026	0.133***	0.101***
	(0.020)	(0.038)	(0.035)
Physiology	-0.176***	-0.166***	-0.172^{***}
	(0.029)	(0.029)	(0.026)
Genetics	0.186***	0.188***	0.184***
	(0.037)	(0.036)	(0.032)
Pediatrics	0.203***	0.220***	0.200***
	(0.036)	(0.036)	(0.032)
Medicine	0.539***	0.548***	0.521***
	(0.030)	(0.029)	(0.027)
Surgery	0.934***	0.939***	0.923***
	(0.036)	(0.035)	(0.032)
Research emphasis	-0.208***	-0.205***	-0.226***
	(0.022)	(0.022)	(0.020)
Not board certified	-0.190^{***}	-0.181***	-0.198***
	(0.021)	(0.022)	(0.020)
Experience	0.018***	0.027***	0.027***
	(0.002)	(0.004)	(0.004)
Associate	0.135***	0.141***	0.138***
	(0.024)	(0.037)	(0.033)
Full professor	0.222***	0.217***	0.214***
	(0.026)	(0.049)	(0.044)
Male:Associate		-0.040	-0.011
		(0.048)	(0.044)
Male:Full professor		-0.019	0.002
		(0.060)	(0.055)
Male:Experience		-0.010**	-0.010**
		(0.005)	(0.004)
Constant	11.374***	11.293***	11.324***
	(0.034)	(0.043)	(0.039)
Observations	261	261	260
\mathbb{R}^2	0.934	0.937	0.948
Adjusted R ²	0.931	0.933	0.945
Residual Std. Error F Statistic	0.134 (df = 249) $319.746^{***} \text{ (df} = 11; 249)$	9 $0.131 \text{ (df} = 246)$ $260.501^{***} \text{ (df} = 14; 246)$	0.119 (df = 245) $321.180^{***} (df = 14; 245)$
Note:	013.140 (u1 — 11, 249)	, , ,	521.100 (df = 14, 245) $6p < 0.1; **p < 0.05; ***p < 0.01$

Note:

*p<0.1; **p<0.05; ***p<0.01