

# INVARIANT OBJECT RECOGNITION USING SPIKING NEURONS

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# Abstract

The human brain recognises a huge number of objects rapidly with ease even in cluttered and natural scenes. This robust object recognition of the biological system is invariant to the change of position, scale, viewing angle, etc. (known as transformation invariance). While the major stumbling problem of computer object recognition lies in the poor robustness to these transformations.

Exploring and mimicking invariant object recognition within the brain is a promising approach to tackling the computational difficulty; in turn it also contributes to understanding biological visual processing by means of mimicking neural activity in the visual system of the brain.

Thanks to its high-performance massively parallel processing, SpiNNaker makes it possible to simulate large-scale neural networks in real-time. Thus, to explore the visual pathway of primate brain, this work exploits a neuromorphic hardware system formed from a Dynamic Video Sensor (DVS) silicon retina in concert with SpiNNaker. As a first step in the exploration, a recognition system for dynamic hand postures is developed on the platform. Inspired by the behaviour of the primary visual cortex, Convolutional Neural Networks (CNNs) are modelled using both linear perceptrons and Leaky Integrate-and-Fire (LIF) neurons.

Future work is proposed to build an object recognition system with position, scale and view invariance by modelling the hierarchical visual pathway up to the inferotemporal (IT) cortex. The proposed system will be able to recognise 200 objects in real time exploiting LIF neurons.



# Chapter 1

## Introduction

Patterns or objects in two-dimensional images can be described with four properties [7]: position, geometry (i.e. size, area and shape), colour/texture, and trajectory. Appearance-based methods are the most direct approach to performing pattern recognition where the test image is compared with a set of templates to find the best match for an individual or combination of properties. However, the 2D projection of an object changes under different conditions including illumination, viewing angles, relative positions and distance, making it virtually impossible to represent all appearances of an object. To improve reliability, robustness and classification efficiency, approaches such as edge matching [8], divide-and-conquer [9], gradient matching [10] and feature based methods [11, 12] are used. In computer vision and image processing, features can be specific structures in the image such as points, edges or objects; and also may be a general neighborhood operation or feature detection applied to the image. Finding an appropriate feature for a specific object still remains an open question and there is no process as general, accurate, or energy-efficient as that demonstrated by the brain. It is not a new idea to turn to nature for inspiration. Riesenhuber et al. [13], for instance, presented a biologically-inspired model based on the organisation of the visual cortex which has the ability to represent relative position- and scale-invariant features. Integrating a rich set of visual features became possible using a feed-forward hierarchical pathway.

### 1.1 What Is Object Recognition?

Object recognition is the process of assigning labels to particular objects, ranging from precise labels ('identification') to coarse labels ('categorisation') [4]. This includes

the ability to accomplish these tasks under various identity-preserving transformations such as object position, scale, viewing angle, background clutter, etc.

The brain can accurately recognise and categorise objects remarkably quickly, for example object recognition time in monkeys is under 200 ms [14] and the images are presented sequentially in spikes less than 100 ms along the visual pathway [15]. This research focuses on this rapid and highly accurate object recognition, ‘core recognition’, which is defined by DiCarlo and Cox [16].

## **1.2 Why Is It Important?**

The human brain recognises huge amount of objects rapidly with ease even in cluttered and natural scenes. This robust object recognition of the biological system is invariant to the change of position, scale, viewing angle and etc. (known as transformation invariance). While the major stumbling problem of the computer object recognition lies in the poor robustness to the transformations. Each encounter of an object on the retina is unique because of differing illumination (lighting conditions), position (projection locations on the retina), scale (distances and sizes), pose (viewing angles), and clutter (visual contexts). In addition, a difficult specificity-invariance trade-off occurs in the categorisation tasks, since the recognition should be able to discriminate different object classes (intraclass variability) while at the same time remaining tolerant to image transformations.

Exploring and mimicking invariant object recognition within the brain is a promising approach to tackling the computational difficulty; in turn it also contributes to understanding biological visual processing by means of mimicking neural activity in the visual system of the brain. Moreover, energy-efficiency improvements following from the great energy efficiency of biological systems will help in building object recognition systems, e.g. posture recognition for human-machine interfaces in mobile devices.

## 1.3 How to Mimic The Brain

To explore how the brain may recognise objects, we have employed a biologically-inspired DVS silicon retina [17]. This is a good example of low-cost visual processing due to its event-driven and redundancy-reducing style of computation. A SpiNNaker machine [18] is also exploited as the back-end of the system, which is a massive parallel computing platform aimed at real-time simulation of Spiking Neural Networks (SNNs). Thanks to SpiNNaker's high-performance processing of large-scale neural networks, we explore biological approaches to visual processing by mimicking the functions of different layers along the visual pathway.

Building a real-time recognition system for dynamic hand postures is a first step of exploring visual processing in a biological fashion and is also a validation of the performance of the neuromorphic platform. To keep the task simple at first, the postures are of similar size and the goal is to recognise the shape of a hand with moving positions. This preliminary work achieved the first milestone of the research which aims at building a position-invariant object recognition system exploiting V1-like neurons (primary visual cortex: area V1) to classify five hand postures.

## 1.4 Report Structure

In Chapter 2, this report starts from the biological aspects of object recognition: the task is mainly processed along the ventral visual pathway with the untangling object representations at different levels of abstraction. This is followed by the introduction of spiking neural networks to illustrate the abilities of neural modelling from single neurons to populations. Further, a number of learning algorithms are also discussed together with recognition/classification tasks where they have been successfully applied. The final part of this chapter describes the details of the hardware neuromorphic system, including the silicon retina and the SpiNNaker platform.

In terms of preliminary work, convolutional neural network models exploiting V1-like neurons are defined and tested in Matlab, and model structures and experimental results are stated in Chapter 3. In Chapter 4, these rate-based models are converted into spiking neurons, and real-time live object recognition and recorded data experiments are carried out.

Finally, the contribution of this work is summarised and the future directions are outlined in Chapter 5.

# Chapter 2

## Background

This chapter provides the readers with detailed biology background of object recognition in the brain and the fundamental principles of neural modelling using spiking neural networks. This is followed by an introduction to the neuromorphic hardware platform specialised for neural simulations of visual processing.

### 2.1 How the Brain Represent Objects

The central visual system consists of several cortical areas responsible for visual processing, which are placed in a hierarchical pattern according to the anatomical experiments [19]. There are two basic streams locating in the visual area: a dorsal and a ventral pathway (Figure 2.1).

They differ in behavioural patterns according to the observation from brain lesions [20], and also in functions where the dorsal pathway targets on the ‘where’ tasks and the ventral on the ‘what’. The ventral visual stream holds the critical circuits for object recognition and stimulus identification, whereas the dorsal pathway pathway contributes to the processing of the spatial location of the stimulus [20, 21]. Another definition of the difference between these two pathways is a ‘perception/action’ dichotomy: the ventral (‘perception’) stream perceives the world by means of object recognition and memory, while the dorsal (‘action’) stream provides real-time visual guidance for motor actions such as eye movements and grasping objects [22].

This research mainly focuses on the ventral visual pathway, since it dominates the object recognition among the cortical areas. Thus, the dorsal pathway will be beyond the scope of this study.

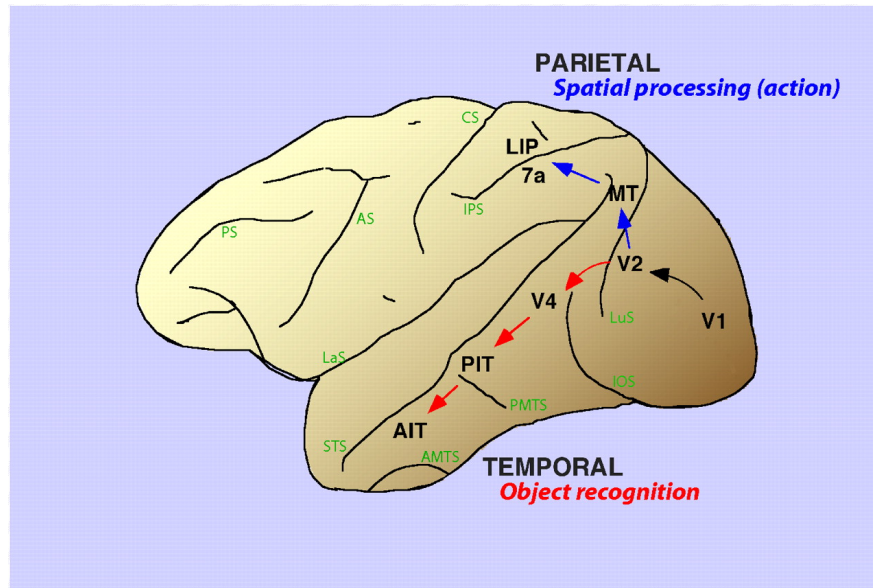


Figure 2.1: The dorsal and ventral pathway in the brain [1]. The dorsal stream (blue) arrives to the parietal lobe, whereas the ventral pathway (red) reaches the inferotemporal (IT) cortex in the temporal lobe.

### 2.1.1 Cortical Areas in The Ventral Visual Pathway

The ventral visual pathway starts from the primary visual cortex V1 in the occipital cortex through areas such as V2 and V4 to the Inferotemporal (IT) cortex. These cortex areas are divided based on the anatomical experiments and retinotopic maps. Accordingly, the IT complex is commonly parsed into sub areas such as TEO and TE [23, 24] or posterior IT (PIT), central IT (CIT), and anterior IT (AIT) [19].

#### Primary Visual Cortex: V1

As the simplest and earliest cortical area in the ventral stream, the primary visual cortex V1 is the best-studied since the well-known discovery of the orientation selectivity by Hubel and Wiesel [25] in 1958. The retinotopic map is well-defined to transform spatial information from retinal image to V1 [26]. In human and animals with a fovea in the retina, the central 10 degrees of the visual field occupies roughly half of V1. This distorted retinotopic map in V1 is a phenomenon known as cortical magnification.

In the spatial domain, V1 neurons are tuned to Gabor-like transforms applied to their small local receptive field. The retinotopic and orientation map on the surface of V1 of a tree shrew is shown in Figure 2.2. A black bar presented in the retinal image evokes a response in the corresponding grid square of V1 ( $6^\circ$ ,  $2^\circ$ ) depending on the

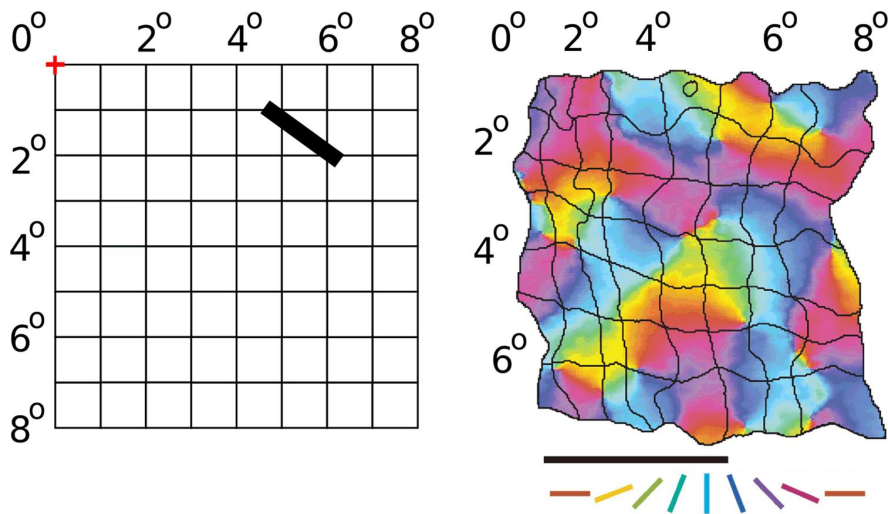


Figure 2.2: The retinotopic and orientation map on the surface of V1 of a tree shrew [2]. The visual field (left) with a fixation point marked as a red cross on the up-left corner can be divided into a regular grid. Each square represents a  $1^\circ \times 1^\circ$  area of visual space. In cortical area V1 of mammals, neurons are arranged into a retinotopic map (right) responding to the retinal visual space. As an example, the retinotopic map shows the orientation preference of the V1 neurons of a tree shrew for an  $8^\circ \times 7^\circ$  area of visual space (adapted from [3]; scale bar is 1 mm).

orientation of the stimulus. The coloured map on the right represents the preferred orientation of neurons in each location. Thus the black bar shown at left will activate V1 neurons coloured in purple in the specific square. In theory, these Gabor-like filters together can carry out neuronal processing of spatial frequency, orientation, motion, direction, speed, and many other spatiotemporal features. Similar maps could be plotted for this same area showing preference for other visual features.

### Prestriate Cortex: V2

Visual area V2, also called prestriate cortex [27], is the second major area located in the occipital lobe of the primate brain, and the first region within the visual association area [28]. It receives strong feed-forward connections from V1 and has many properties in common with V1.

The responses of V2 neurons are tuned to simple shapes such as orientation and sinusoidal gratings. Moreover, V2 neurons are able to represent variety of higher order shapes that are based on contours (e.g., angles and curves with multiple orientations at different subregions within a single receptive field) or grating patterns [29]. The responses of many V2 neurons are also modulated for complex properties: orientation

of illusory contours [30], binocular disparity [31], and whether the stimulus is part of the figure or the ground [32].

### **Visual Area V4**

Area V4 is the third cortical area in the ventral stream, receiving strong feedforward input from V2 and transmitting to the PIT. It also receives direct inputs from V1 which are mostly generated in the visual central space. V4 is the first area in the ventral stream to show strong attentional modulation. Most studies indicate that selective attention can change firing rates in V4 by about 20% [33]. This discovery found by Moran and Desimone [34] was the first report of attention effects anywhere in the visual cortex.

Although V4 is mainly modulated for colour recognition, it is also tuned for orientation and spatial frequency similar to V1. Comparing to V1, V4 responds to more complex object features with intermediate complexity but is not tuned for complex objects as areas in the inferotemporal cortex are [35].

### **Inferotemporal Cortex: IT**

Inferotemporal Cortex is only found in the temporal lobe in primates including humans. It is tuned to a range of object features complexity starting with simpler patterns in the PIT/TEO [36]; And the complexity increases along the ventral stream towards AIT/TE where objects are represented and recognised [37]. The high-order complex features includes the combinations of colour or texture with complicated shapes [36], and body parts such as faces and hands [38]. The distinguishing features of the IT cortex is that the neuronal responses are position and size invariant [39, 40], and also invariant to changes in luminance, texture, and relative motion [41, 42]. It is wide-accepted that the identity-preserving transformation invariance makes IT ideal for representing objects despite changes in the surrounding environment and retinal image.

In the next section, this report will explore the detailed mechanism of object representation in this cortical area.

#### **2.1.2 Object Representation in IT**

The neuronal representation in the cortical area of IT is considered to be the spatio-temporal pattern of spikes. The spiking activities of single neurons and populations are thought to hold the key to encode visual information. In Section 2.2, the report

will introduce single neuron models and spike coding mechanisms in computational spiking neural networks.

## Single neurons

Most studies have investigated the neural activities in the IT by means of firing rate or spike count. A typical histogram, Figure 2.3(A) [43], shows the spike count of a single neuron in time bins of 25 ms for a duration of 300 ms in total right after the presentation of a visual image. The highlighted time window, the so-called ‘decoding’ window, is adjusted to the latency of the conductance along the ventral stream. The spike count of the ‘decoding’ window is well modulated for object identity, position or size [44, 45], see example in Figure 2.3(B) where the left shows the spiking activities for clean figures and the right for natural scenes. The neural responses were sorted from high to low with the corresponding figures presented, where the red point

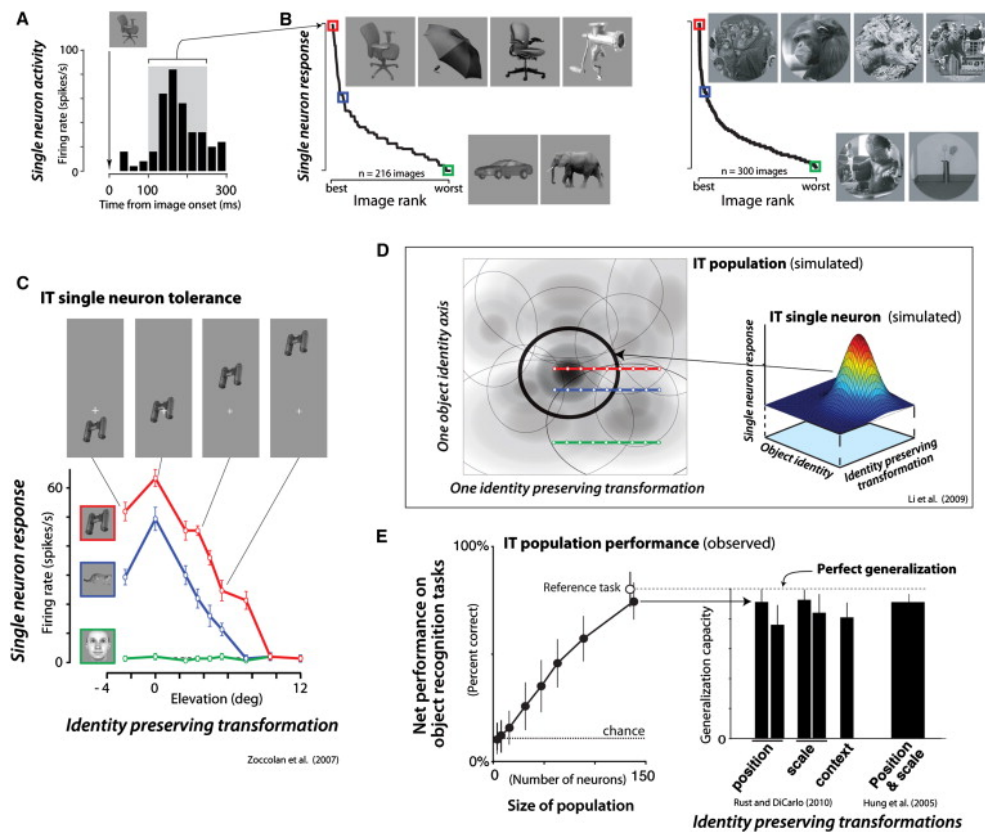


Figure 2.3: IT single-neuron properties and their relationship to population performance [4].



indicated the highest respond while the green the lowest and the blue the medium. Another example in Figure 2.3(C) shows the responses of an example IT neuron obtained by varying the position (elevation) of three objects with high (red), medium (blue), and low (green) activities. The object identity preference was maintained in the entire test range regardless of the position changes. These tuning curves are similar to the well-understood firing rate modulation in visual area V1 on the bar orientation.

Understanding IT single neuron responses has proven to be extremely challenging and even predicting the responses of an IT neuron to a new image remains impossible. Nevertheless, IT neurons are activated by complex combinations of visual features and that they are often able to maintain their relative object preference over small to moderate changes in object position, scale, pose [46], illumination [47] and clutter [48].

Although IT neurons are commonly described as narrowly selective object identifier, neurophysiological studies have shown a diverse selectivity of single neurons [44]. Most IT neurons are broadly tuned and the typical IT neuron responds to many different images and objects [43], also see Figure 2.3(B). As illustrated in Figure 2.3(D), a single neuron (right) is modulated to both object identities and variables of identity-preserving transformations. To explain the plot in 2.3(C), position is the variable here; thus the tuning curve for different identities on each position can be described as a slice in the 3-D plot which is Gaussian-like. As a result, the rank order of the three objects remains the same due to the Gaussian-like curve stays similar. If a population of such IT neurons tiles with the overlapping fashion, see left panel of Figure 2.3(D), a more accurate recognition result containing the transformation parameter can be carried out with population coding.

## **Population of neurons**

Spike timing variability in the ms resolution of spikes is consistent with a Poisson-like stochastic spike generation process. The underlying output rate of IT neurons is determined by each particular image. Despite the timing variability, the brain can reliably recognise the presented object by integrating the neural responses across IT population [49]. However, it still remains unclear whether the spike timing variability brings down the encoding/decoding accuracy or if it contributes to the population tuning for useful informations [50].

Although the first stage of the ventral stream, V1, is reasonably well studied, the visual processing in higher stages especially in V4 and IT remains poorly understood.

Nevertheless, as stated above IT is the main part of ventral stream to recognise and categorise the objects in real-time and is tolerant to identity-preserving transformations. Specifically, simple linear classifier built on the output rates of randomly selected population with only a few hundred neurons reveals a high-level of object recognition performance [51]; and the simple weighted summation explains a wide range of invariant object recognition behaviour sufficiently [52].

Figure 2.3(E) shows the direct tests of measuring the cross-validated population performance on categorisation tasks using linear classifiers. The recognition performance approaches ceiling level with only a few hundred neurons (left panel), and the same population shows a good generalization across moderate changes in position, scale, and context.

## **Decoding Window Matters**

The output spiking pattern of the ventral visual stream are well described by a firing rate code where the decoding window size is 50 ms [51]. Thus the visual representation in IT is usually found in the first 50 ms of neuronal response, although different time epochs relative to stimulus onset may encode different types of visual information [53] (see Figure 2.3(A), an appropriate decoding window can be 100-150 ms after image onset).

In sum, the output of the ventral stream is reflexively expressed in neuronal firing rates across a short interval of 50 ms and is an explicit object representation; and the rapid production of this representation is consistent with a largely feed-forward, non-linear processing of the visual input [4], which is described in the following section.

### **2.1.3 Hierarchical Feed-forward Organisation**

Figure 2.4(A) illustrates the ventral stream cortical area locations in the macaque monkey brain, and the flow of visual information from the retina. The corresponding hierarchical organisation is showed in Figure 2.4(B). Each area is plotted with the size proportional to its cortical surface size. Approximate total number of neurons of both hemispheres is shown in the corner of the cortical areas. The approximate number of projections is written above each block. In addition, the colour dedicates to processing the central 10° of the visual field. At last, approximate median response latency is listed on the right.

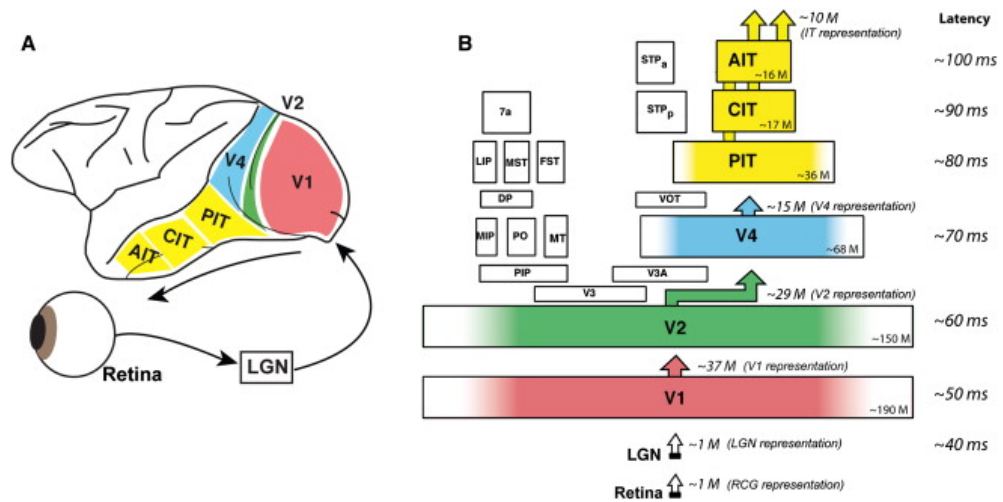


Figure 2.4: The ventral visual pathway and its hierarchical organization [4].

## Latency

Each cortical area along the ventral stream contributes a conductance latency of about 10 ms of the visual information [54]. Thus, just around 100 ms after images appeared in front of the retina, a first wave of object identity neuronal activity is present throughout much of IT (e.g., Figure 2.3(A)).

## Neurons and Connections

Because retinal and LGN receptive fields are point-wise spatial sensors, the object visual information conveyed to V1 are nearly as raw as the pixel representation (1 million pixels). As V1 carries out its visual process, the total object representation increases approximately 30-times [55] because of its non-linear filtering. This dimensionality expansion results in an overcomplete population re-representation [56] in which the object representation vectors have more dimensions than the LGN input. As a result, simulations show that a V1-like representation is clearly better than RGN-like/pixel-based representation, but still far below human performance for real-world recognition problems [16].

The output projections of each area decreases from V2 (about 29 million) to AIT which represents the object with 10 million dimensions. At the same time, the receptive field size of neurons increases to complete the object representation with a whole image and to perform invariant recognition.

## Tuned Features and Receptive Fields

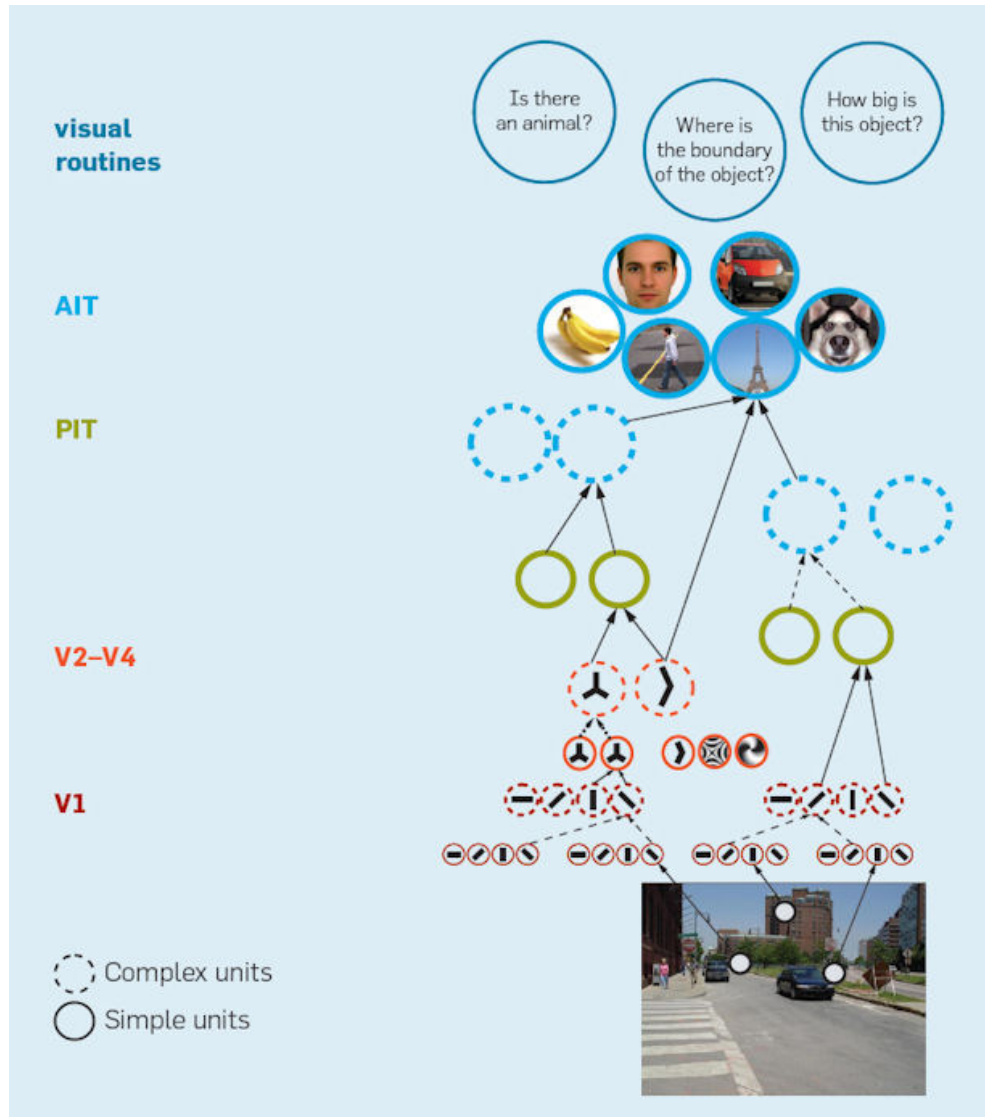


Figure 2.5: The hierarchical ventral stream and the corresponding tuned features for each layer [5].

As the visual information conducts along the ventral stream, neurons become selective for stimuli that are increasingly complex from simple oriented bars and edges in early visual area V1 to moderately complex features in intermediate areas: V2, V4 and PIT to complex objects and faces in AIT, see Figure 2.5. Along with this growing complexity of the preferred stimulus, the invariance properties of neurons also increase. Neurons become more and more tolerant with respect to the exact position and scale of the stimulus within their receptive fields. As a result, the receptive field

size of neurons increases from about one degree or less in V1 to several degrees in IT, see Figure 2.6.

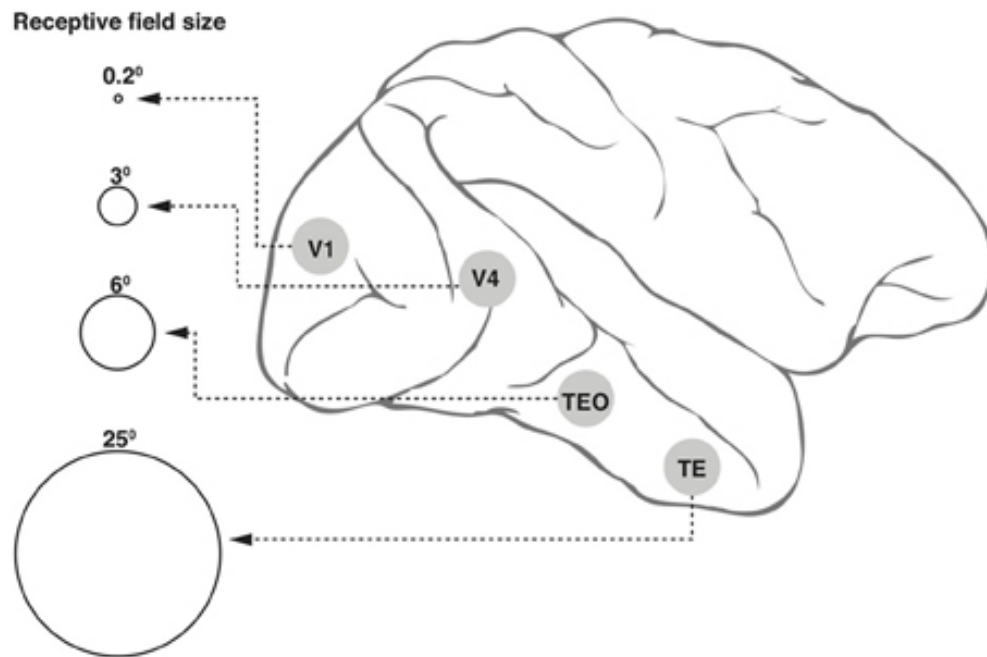


Figure 2.6: Receptive field (RF) sizes along the ventral cortical stream in the primate. While the degree of complexity of processing may increase, the RF size at any one eccentricity also increases dramatically along the various cortical areas from V1 into the temporal pole. The circles shown in the figure are not drawn to scale, but the numbers above the circles indicate approximate relative sizes of the RF diameters. [6].

## 2.2 Spiking Neural Network

The so-called third generation of neural networks [57] introduces a different set of functions and parameters to model neurons; it models the biological neurons more precisely and increases the computational power of neural networks when compared to the classical sigmoid functions. Such networks rely on the propagation of an all-or-none signal, the action potential, which asynchronously carries information to its connected units by means of its timing.

### **2.2.1 Neuronal Model**

Spiking neuron models can be divided into two major categories [58] based on their level of abstraction: The conductance models and the threshold models. The conductance models simulate a lower level on the ion channels, while the threshold models represent a higher level of neuron abstraction where the threshold voltage is fixed and the neuron fires once the membrane potential reaches it.

In general, Conductance-Based models have been derived from the Nobel prize winners (1963) Hodgkin and Huxley, based on the experiments that they performed on the giant axon squid [59]. Spikes arriving at a LIF neuron cause a temporary flow of current into (excitatory synapse) or out of (inhibitory synapse) the neuron, modelling the behaviour of synapses in biological neurons. The LIF neuron sums up this current over time, accumulating charge which gradually leaks away. If the membrane potential in the neuron reaches a certain threshold, it produces a spike and its charge is reset. LIF neurons have been extensively used in large spiking neural networks [60] because of their ease of implementation and the low computational cost.

### **2.2.2 Learning**

The influence each incoming spike has on a post-synaptic neuron is modelled by assigning a ‘weight’ to each synapse; tuning on the weight scales the impact of a spike arriving via that synapse. Many learning models simulate the changes in weights over long periods of time observed within the brain. The exact rules by which these weights are adjusted is the subject of much active research though most promising approaches attempt to learn from the relative timing [61] or rate [62] of spikes arriving at a neuron. As well as adjusting weights, some learning rules can also form entirely new connections between previously unconnected neurons [63].

### **2.2.3 Successful Applications**

Numerous applications using SNN-based vision processing have been successfully carried out in the past. A dual-layer SNN has been trained using Spike Time Dependent Plasticity (STDP) and employed for character recognition [64]. Lee et al. [65] have implemented direction selective filters in real time using spiking neurons, considered as a convolution layer in the model of a so called CNN [66]. Different features, such as Gabor filter features (scale, orientation and frequency) and shape can be modelled as layers of feature maps. The similar behaviours have been found in the primary visual

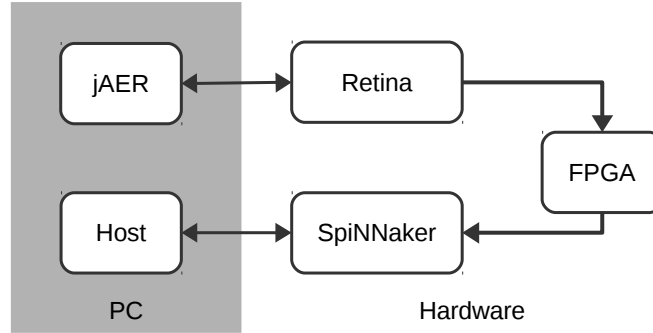
cortex (V1) in the visual pathway [67] as the foundation for higher level visual process e.g. object recognition. Rank order coding, as an alternative to conventional rate-based coding, treats the first spike as the most important and has been successfully applied to an orientation detection training process [68]. Nengo [69] is a graphical and scripting based software package for simulating large-scale neural systems and has been used to build the world's largest functional brain model, Spaun [70]. An FPGA implementation of a Nengo model for digit recognition has been reported [71]. Deep Belief Networks (DBNs), the 4th generation of artificial neural network, have shown great success in solving classification problems. Recent study [72] in this area has mapped an offline-trained DBN onto an efficient event-driven spiking neural network for digit recognition tasks with resounding success.

## 2.3 Platforms

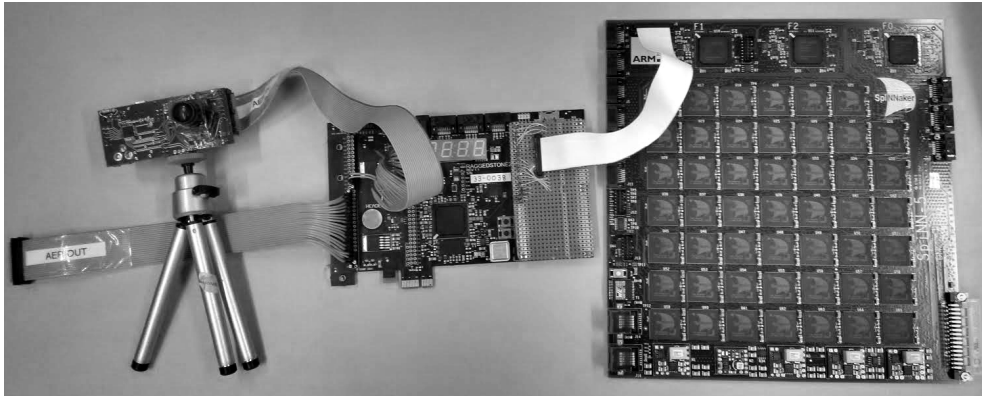
The outline of the platform is illustrated in Figure 2.7a, where the hardware system is configured, controlled and monitored by the PC. The jAER [73] event-based processing software on the PC configures the retina and displays the output spikes through a USB link. The host communicates to the SpiNNaker board via Ethernet to set up its runtime parameters and to download the neural network model off-line. It visualises [74] the spiking activity of the network in real-time. The photograph of the hardware platform, Figure 2.7b, shows that the silicon retina connects to the SpiNNaker 48-node system via a Spartan-6 FPGA board [75].

### 2.3.1 Vision Processing Front-ends

The visual input is captured by a DVS silicon retina, which is quite different from conventional video cameras. Each pixel generates spikes when its change in brightness reaches a defined threshold. Thus, instead of buffering video into frames, the activity of pixels is sent out and processed continuously with time. The communication bandwidth is therefore optimised by sending activity only, which is encoded as pixel events using Address-Event Representation (AER [76]) protocol. The level of activity depends on the contrast change; pixels generate spikes faster and more frequently when they are subject to more active change. The sensor is capable of capturing very fast moving objects (e.g., up to 10 K rotations per second), which is equivalent to 100 K conventional frames per second [17].



(a) Outline of the platform.



(b) Picture of the hardware platform. From left to right: a silicon retina, a FPGA board, and a 48-node SpiNNaker system.

Figure 2.7: System overview of the dynamic hand posture recognition platform.

### 2.3.2 SNNs Back-ends

The SpiNNaker project’s architecture mimics the human brain’s biological structure and functionality. This offers the possibility of utilizing massive parallelism and redundancy, as the brain, to provide resilience in an environment of unreliability and failure of individual components.

In the human brain, communication between its computing elements, or neurons, is achieved by the transmission of electrical ‘spikes’ along connecting axons. The biological processing of the neuron can be modelled by a digital processor and the axon connectivity can be represented by messages, or information packets, transmitted between a large number of processors which emulate the parallel operation of the billions of neurons comprising the brain.

The engineering of the SpiNNaker concept is illustrated in Figure 2.8 where the hierarchy of components can be identified. Each element of the toroidal interconnection



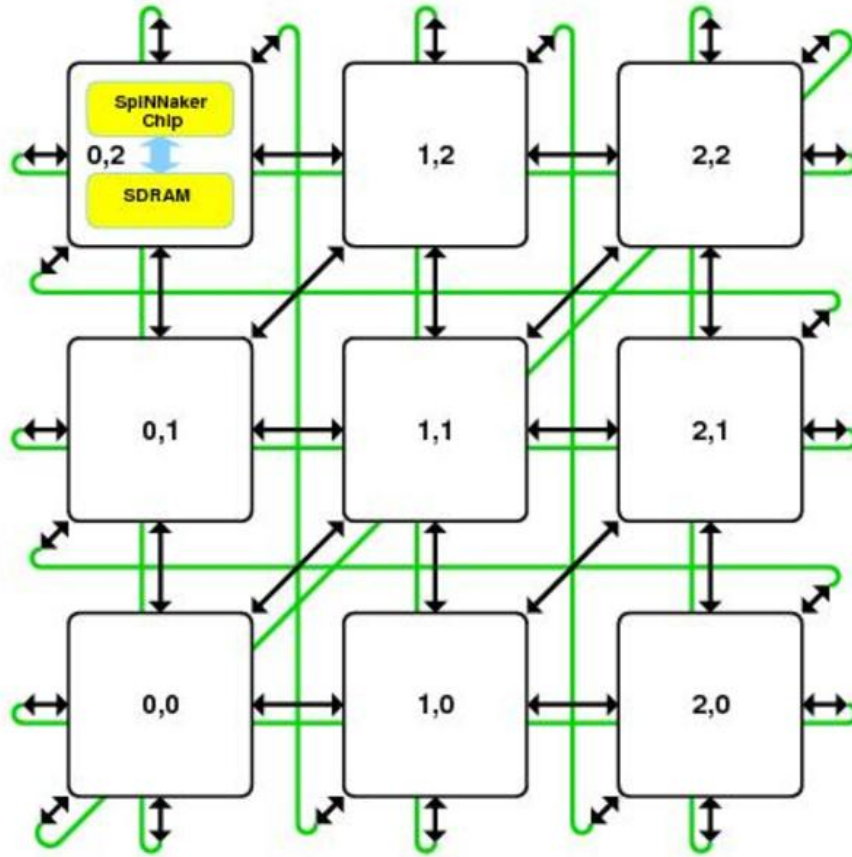


Figure 2.8: SpiNNaker system diagram. Each element represents one chip with local memory. Every chip connects to its neighbours through the six bi-directional on-board links.

mesh is a multi-core processor known as the ‘SpiNNaker Chip’ comprising 18 processing cores. Each core is a complete processing sub-system with local memory. It is connected to its local peers via a Network-on-Chip (NoC) which provides high bandwidth on-chip communication and to other SpiNNaker chips via links between them. In this way massive parallelism extending to thousands or millions of processors is possible.

The ‘103 machine’ is the name given to the 48-node board which we use for the hand posture recognition system, see Figure ???. It has 864 ARM processor cores, typically deployed as 768 application, 48 monitor and 48 spare cores. The boards can be connected together to form larger systems using high-speed serial interfaces.

### 2.3.3 SpiNNaker distinguishing features

Spikes from the silicon retina are injected directly into SpiNNaker via a SPARTAN-6 FPGA board that translates them into a SpiNNaker compatible AER format [77].

From a neural modelling point of view, interfacing the silicon retina is performed using pyNN [78]. The retina is configured as a spike source population that resides on a virtual SpiNNaker chip, to which an AER sensor's spikes are directed, thus abstracting away the hardware details from the user[75]. Besides the retina, we have successfully connected an AER based silicon cochlea [79] to SpiNNaker for a sound localisation task [80], see Figure 2.9.

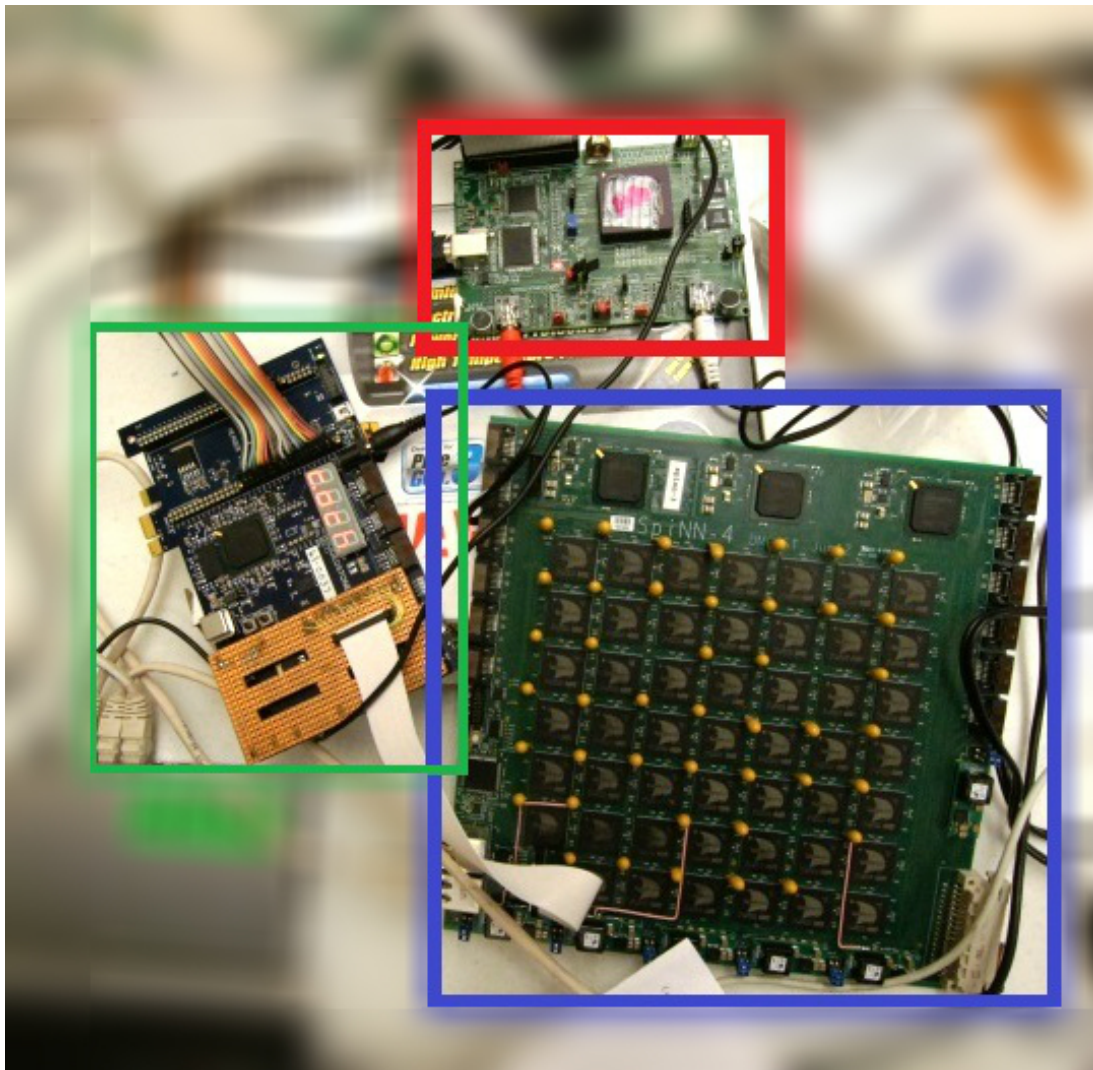


Figure 2.9: Neuromorphic platform for sound localisation: a silicon cochlea connects to a 48-node SpiNNaker board via a FPGA.

## Chapter 3

# Convolutional Neural Networks

The convolutional network is well-known as an example of a biologically-inspired model. Figure 3.1 shows a typical convolutional connection between two layers of neurons. The repeated convolutional kernels are overlapped in the receptive fields of the input neurons.

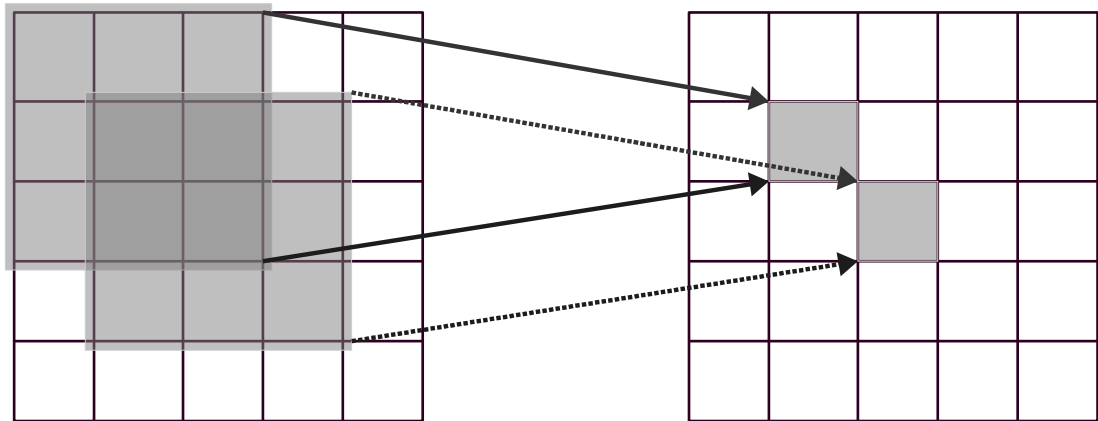


Figure 3.1: Each individual neuron in the convolution layer (right matrix) connects to its receptive field using the same kernel. The value of the kernel is represented by the synaptic weights between the connected neurons.

### 3.1 Model Description

There are two CNNs proposed to accomplish the dynamic hand posture recognition task. A straight forward method of template matching is employed at first, followed by a network of multi-layer perceptrons (MLP) trained to improve the recognition performance.

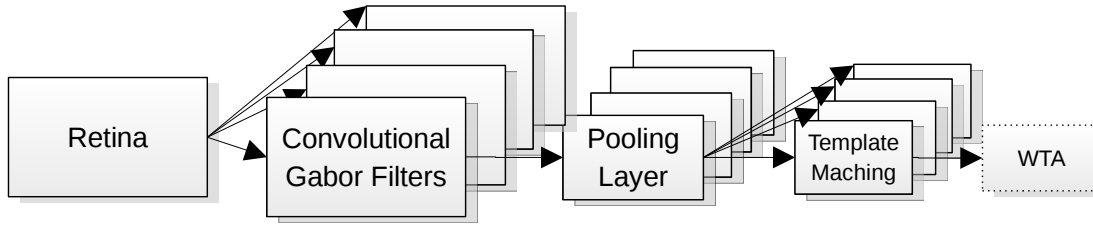


Figure 3.2: Model 1. The retina input is convolved with Gabor filters in the second layer, and then shrinks the sizes in the pooling layer. The templates are considered as convolution kernels in the last layer. The WTA circuit can be used as an option to show the template matching result more clearly.

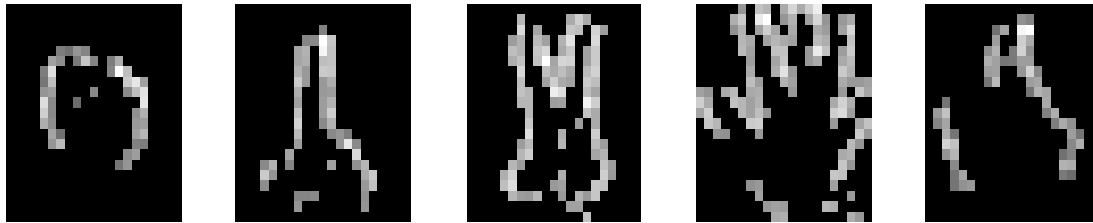


Figure 3.3: Templates of the five postures: ‘Fist’, ‘Index Finger’, ‘Victory Sign’, ‘Full Hand’ and ‘Thumb up’.

Model 1: Template Matching. Shown in Figure 3.2 the first layer is the retina input, followed by the convolutional layer, where the kernels are Gabor filters responding to edges of four orientations. The third layer is the pooling layer where the size of the populations shrinks. This down-sampling enables robust classification due to its tolerance to variations in the precise shape of the input. The fourth layer is another convolution layer where the output from the pooling layer is convolved with the templates. The optional layer of Winner-Take-All (WTA) neurons enables a clearer classification result due to the inhibition between the neurons. In the Matlab simulation, the retina input spikes are buffered into 30 ms frames, and the neurons are simple linear perceptrons. The templates are chosen by sampling the output of the pooling layer when given some reference stimulus, see Figure 3.3.

The Gabor filter is well-known as a linear filter for edge detection in image processing. A Gabor filter is a 2D convolution of a Gaussian kernel function and a sinusoidal

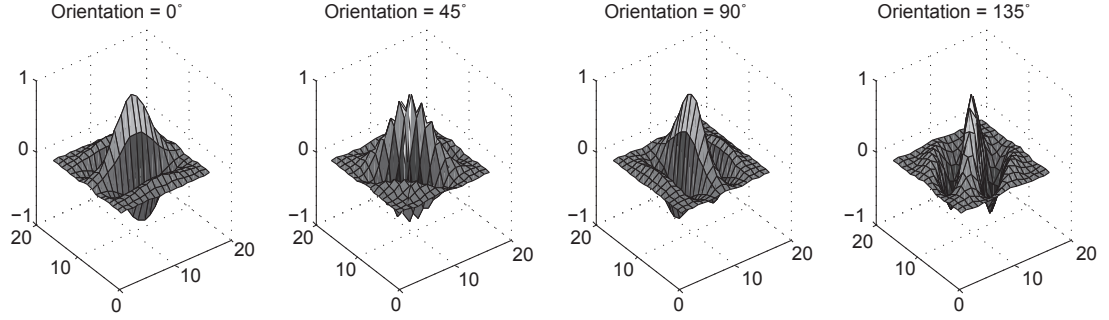


Figure 3.4: Real parts of the Gabor filters orienting four directions.

plane wave; see Equation 3.1.

$$\text{RealParts} = \exp\left(\frac{-x'^2 + y'^2}{2\sigma^2}\right) \cos\left(2\pi \frac{x'}{\lambda}\right)$$

$$\text{ImaginaryParts} = \exp\left(\frac{-x'^2 + y'^2}{2\sigma^2}\right) \sin\left(2\pi \frac{x'}{\lambda}\right)$$

(3.1)

where :

$$x' = x \cos(\theta) + y \sin(\theta)$$

$$y' = -x \sin(\theta) + y \cos(\theta)$$

$\theta$  represents the orientation of the filter,  $\lambda$  is the wavelength of the sine wave, and  $\sigma$  is the standard deviation of the Gaussian envelope. The frequency and orientation features are similar to the responses of V1 neurons in the human visual system. Only the real parts of the Gabor filters (see Figure 3.4) are used as the convolutional kernels to configure the weights between the input layer and the Gabor filter layer.

The output score of a convolution is determined by the matching degree between the input and the kernel. Regarding the template matching layer, each neuron in a population responds to how closely its receptive field matches the specific template. The position of moving gesture is also naturally encoded in the address of template matching neuron. Thus, there are five populations of template matching neurons, one for each hand posture listed.

**Model 2: Trained MLP.** Inspired by the research of Lecun [81], we designed a combined network model with MLP and CNN (Figure 3.5). The first three layers are

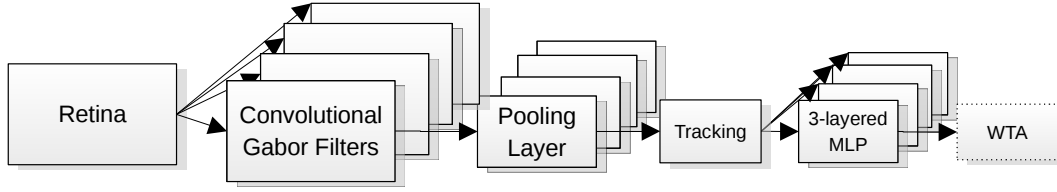


Figure 3.5: Model 2. The retina input convolves with Gabor filters in the second layer, and then shrinks the sizes in the pooling layer. The following tracking layer finds the most active area of some fixed size, moves the posture to the centre and pushes the image to the trained MLP. The winner-take-all (WTA) layer can be used as an option to show the template matching result more clearly.

exactly the same as the previous model. The training images for the 3-layered MLP are of same size and the posture is centred in the images. Therefore, a tracking layer plays an important role to find the most active region and forward the centred image to the next layer.

## 3.2 Experimental Set-up

In order to evaluate the cost and performance trade-offs in optimizing the number of neural components, both the convolutional models described above are tested at different scales. Five videos of every posture are captured from the silicon retina in AER format, all of similar size and moving clock-wise in front of the retina. The videos are cut into frames (30 ms per frame) and presented to the convolutional networks. The configurations of the networks are listed in Table 3.1. The integration layer is not necessary in a convolutional network, but is used here to decrease the number of synaptic connections.

## 3.3 Experimental Results

In Figure 3.6 the first two plots refer to Model 1, using template matching. Each colour represents one of the recognition populations. Each point in the plot is the highest neuronal response in the recognition population during the time of one frame (30 ms). The neuronal response, ‘the spiking rate’, is normalised to  $[-1, 1]$ . It can be seen that the higher resolution input makes the boundaries between the classes clearer. On the other hand, recognition only happens when the test image and template are similar enough. The templates are only selected from the frames where the gestures

Table 3.1: Sizes of the convolutional neural networks.

(a) Model 1: Template matching

	<b>Full Resolution <math>128 \times 128</math></b>		<b>Sub-sampled Resolution <math>32 \times 32</math></b>	
	Population Size	Connections per Neuron	Population Size	Connections per Neuron
<b>Retinal Input</b>	$128 \times 128$	1	$32 \times 32$	$4 \times 4$
<b>Gabor Filter</b>	$112 \times 112 \times 4$	$17 \times 17$	$28 \times 28 \times 4$	$5 \times 5$
<b>Pooling Layer</b>	$36 \times 36 \times 4$	$5 \times 5$	null	null
<b>Integration Layer</b>	$36 \times 36$	4	$28 \times 28$	4
<b>Template Matching</b>	$16 \times 16 \times 5$	$21 \times 21$	$14 \times 14 \times 5$	$15 \times 15$
<b>Total</b>	74,320	15,216,512	5,925	318,420

(b) Model 2: Trained MLP

	<b>Full Resolution <math>128 \times 128</math></b>		<b>Sub-sampled Resolution <math>32 \times 32</math></b>	
	Population Size	Connections per Neuron	Population Size	Connections per Neuron
<b>Tracked Input</b>	$21 \times 21$	null	$15 \times 15$	null
<b>Hidden Layer</b>	10	$21 \times 21 \times 10$	10	$15 \times 15 \times 10$
<b>Recognition Layer</b>	5	$5 \times 10$	5	$5 \times 10$
<b>Total</b>	456	4,460	240	2,300

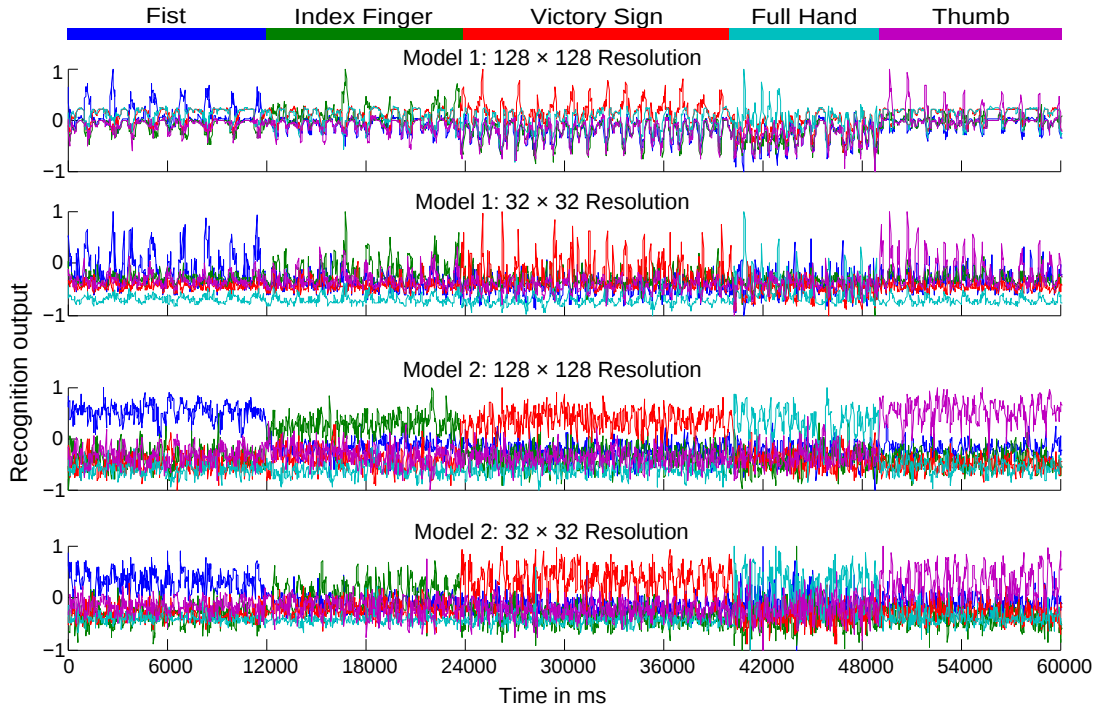


Figure 3.6: Neural responses with time of four experiments to the same recorded moving postures. The recognition output is normalised to  $[-1, 1]$ . Every point represents the highest response in a specific population (different colour) for a 30 ms frame. The 1st plot refers to Model 1 with the full input resolution, and the 2nd plot Model 1 with the sub-sampled input resolution; and the 3rd and fourth plots both refer to Model 2, and with high and low input resolution respectively.

are moving towards the right, and the gestures are moving clockwise in the videos, thus, all the peaks in plot 1 correspond with moments when the gesture moves towards right. It is notable that the higher resolution causes the recogniser to be more sensitive to the differences between the test data and the template, while the smaller neural network can recognize more generalized patterns. Therefore, a threshold is required to differentiate between data that is close enough and that which is not. Since the gestures are moving in four different directions during the clockwise movement, a rejection rate (i.e. none of the template is matched) of 75% is to be expected.

The latter two plots of Figure 3.6 refer to Model 2. The three-layer MLP network significantly improves the recognition rate and can generalise the pattern. There is no rejection rate for Model 2, since the MLP is trained with all the moving directions of the postures.

Detailed results are listed in Table 3.2. The correct recognition rate is calculated



Table 3.2: Recognition results using linear perceptrons in %

		Model 1		Model 2	
		High Resolution	Low Resolution	High Resolution	Low Resolution
<b>Fist</b> (399 Frames)	Correct	99.11	99.23	96.24	84.21
	Reject	71.93	67.42	Null	Null
<b>Index Finger</b> (392 Frames)	Correct	92.98	80.00	94.39	71.69
	Reject	70.92	75.77	Null	Null
<b>Victory Sign</b> (551 Frames)	Correct	96.56	93.07	95.64	87.66
	Reject	73.68	81.67	Null	Null
<b>Full Hand</b> (293 Frames)	Correct	95.65	72.41	93.52	72.01
	Reject	92.15	90.10	Null	Null
<b>Thumb up</b> (391 Frames)	Correct	89.61	84.44	96.68	74.68
	Reject	80.31	76.98	Null	Null
<b>Average</b>	Correct	94.78	85.83	95.29	78.05
	Reject	77.80	78.39	Null	Null

from the non-rejected frames. The lower resolution of the  $32 \times 32$  retina input is adequate (85.83%) for this gesture recognition task. The smaller network uses only 1/10th the number of neurons and 1/50th the number of synaptic connections compared with the full resolution network, while the recognition rate drops only around by 9.0% with Model 1 and 17.2% with Model 2.

# Chapter 4

## Recognition on SpiNNaker

### 4.1 Moving from Perceptrons to Spiking Neurons

It remains a challenge to transform traditional artificial neural networks into spiking ones. There are attempts [82] [83] to estimate the output firing rate of the LIF neurons (Equation 4.1) under certain conditions.

$$\frac{dV(t)}{dt} = -\frac{V(t) - V_{rest}}{\tau_m} + \frac{I(t)}{C_m} \quad (4.1)$$

The membrane potential  $V$  changes in response to input current  $I$ , starting at the resting membrane potential  $V_{rest}$ , where the membrane time constant is  $\tau_m = R_m C_m$ ,  $R_m$  is the membrane resistance and  $C_m$  is the membrane capacitance.

Given a constant current injection  $I$ , the response function, i.e. firing rate, of the LIF neuron is

$$\lambda_{out} = \left[ t_{ref} - \tau_m \ln \left( 1 - \frac{V_{th} - V_{rest}}{IR_m} \right) \right]^{-1} \quad (4.2)$$

when  $IR_m > V_{th} - V_{rest}$ , otherwise the membrane potential cannot reach the threshold  $V_{th}$  and the output firing rate is zero. The absolute refractory period  $t_{ref}$  is included, where all input during this period is invalid. In a more realistic scenario, the post-synaptic potentials (PSPs) are triggered by the spikes generated from the neuron's pre-synaptic neurons other than a constant current. Assume that the synaptic inputs are Poisson spike trains, the membrane potential of the LIF neuron is considered as a diffusion process. Equation 4.1 can be modelled as a stochastic differential equation

referring to Ornstein-Uhlenbeck process,

$$\tau_m \frac{dV(t)}{dt} = -[V(t) - V_{rest}] + \mu + \sigma \sqrt{2\tau_m} \xi(t) \quad (4.3)$$

where

$$\mu = \tau_m (\mathbf{w}_E \cdot \lambda_E - \mathbf{w}_I \cdot \lambda_I) \quad (4.4)$$

$$\sigma^2 = \frac{\tau_m}{2} (\mathbf{w}_E^2 \cdot \lambda_E + \mathbf{w}_I^2 \cdot \lambda_I)$$

are the conditional mean and variance of the membrane potential. The delta-correlated process  $\xi(t)$  is Gaussian white noise with zero mean,  $\mathbf{w}_E$  and  $\mathbf{w}_I$  stand for the weight vectors of the excitatory and the inhibitory synapses, and  $\lambda$  represents the vector of the input firing rate. The response function of the LIF neuron with Poisson input spike trains is given by the Siegert function [84],

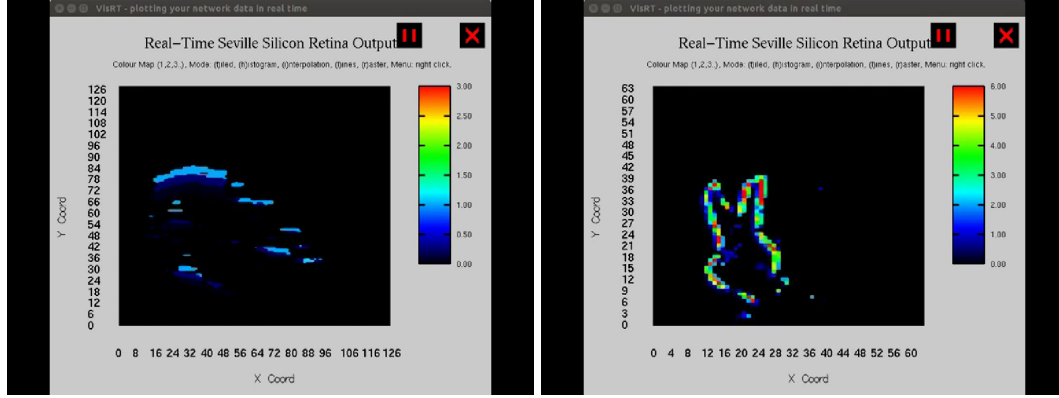
$$\lambda_{out} = \left( \tau_{ref} + \frac{\tau_Q}{\sigma_Q} \sqrt{\frac{\pi}{2}} \int_{V_{rest}}^{V_{th}} du \exp \left( \frac{u - \mu_Q}{\sqrt{2}\sigma_Q} \right)^2 \left[ 1 + \operatorname{erf} \left( \frac{u - \mu_Q}{\sqrt{2}\sigma_Q} \right) \right] \right)^{-1} \quad (4.5)$$

where  $\tau_Q, \mu_Q, \sigma_Q$  are identical to  $\tau_m, \mu, \sigma$  in Equation 4.4, and erf is the error function.

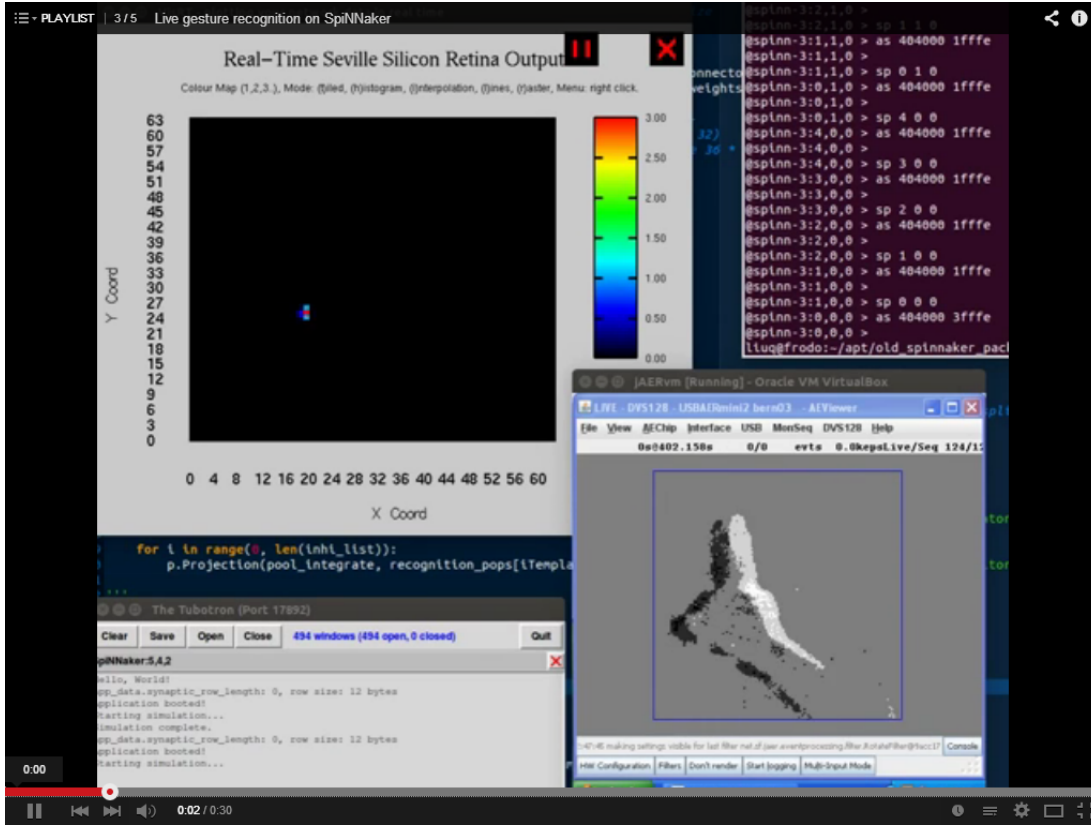
Still there are some limitations on the response function. For the diffusion process, only small amplitude (weight) of the PostSynaptic Potentials (PSPs) generated by a large amount of input spikes (high spiking rate) work under this circumstance; plus, the delta function is required, i.e. the synaptic time constant is considered to be zero. Thus only a rough approximation of the output spike rate has been determined. Secondly, given different input spike rate to each pre-synaptic neurons, the parameters of the LIF neuron and the output spiking rate, how to tune every single corresponding synaptic weight remains a difficult task.

## 4.2 Live Recognition

We implemented the prototype of the dynamic posture recognition system on SpiN-Naker using LIF neurons. The input retina layer consists of  $128 \times 128$  neurons; each Gabor filter has  $112 \times 112$  valid neurons, since the kernel size is  $17 \times 17$ ; each pooling layer is as big as  $36 \times 36$ , convolving with five template kernels ( $21 \times 21$ ); thus, the recognition populations are  $16 \times 16$  neurons each. Altogether 74,320 neurons and



(a) Neural responses of the Gabor filter layer orienting to the horizontal direction [85] (b) Neural responses of the integrate layer [86]



(c) Snapshot of the neuron responses of the template matching layer [87]

Figure 4.1: Snapshots of the real-time dynamic posture recognition system on SpiNNaker.

15,216,512 synapses, use up to 19 chips (290 cores) on a 48-node board, see Table 3.1a. Regarding the lower resolution of  $32 \times 32$  retinal input, the network (Table 3.1b) consists of 5,925 neurons and 318,420 synapses taking up only two chips (31 cores) of the board.

Figure 4.1 shows snapshots of neural responses of some populations during real-time recognition. Figure 4.1a is a snapshot of the Gabor population which prefers the horizontal direction, given the input posture of a 'Fist'; and Figure 4.1b shows the activity of the neurons in the integration layer, given a 'Victory Sign'. And the active neurons in the visualiser in Figure 4.1c are pointing out the position of the recognised pattern the 'Index finger'. All the supporting demonstrative videos can be found on YouTube [85, 86, 87].

### 4.3 Recognition of Recorded Data

To compare with the results of the experiments carried out with Matlab (in Section 3.3), the same recorded retinal data is conducted into SpiNNaker. Only Model 1 is tested on the neuromorphic hardware platform, since tracking is still need to investigate using SNN (for Model 2) in the future. The recorded data is presented as spike source array in the system with  $128 \times 128$  input (see Figure 4.3a) while the data is forwarded to a sub-sampling layer of  $32 \times 32$  resolution in the system of the smaller network (see Figure 4.4a). The output spikes generated from the recognition populations with time are shown in Figures 4.3 and 4.4 for full resolution and lower systems respectively. More spikes are generated during the period when the preferred input posture is shown.

Correspondingly, the spiking rates of each recognition population is sampled into frames (Figure 4.2) to make a comparison with the Matlab simulation. Each colour represents one recognition population, and the spike activity goes higher when the input posture matches the template. Firstly, the spike rates are sampled into 30 ms frames which is in accordance with the Matlab experiments. In the Matlab simulation, the templates are trained with cut frames and so the test images are also fixed to the same length frames. Otherwise, the recogniser will not work properly because of the replications of the moving posture. Contrasting this, the spiking rates can be sampled to various frame lengths. Thus, the other two plots in the figure illustrate the classification in a wider window of 300 ms. From Table 4.1, the recognition and rejection rates are quantified as percentages.

Comparing with the results of Matlab simulation (Table 3.2), the recognition rate is about 7.6% lower at both high and low resolutions, and the rejection rate remains the same slightly above 75%. However, by changing the frame length to 300 ms recognition rates reach (93.0% for the larger network) or exceed (86.4% for smaller network) the Matlab simulation, meanwhile the rejection rates also drop dramatically by 26.0%

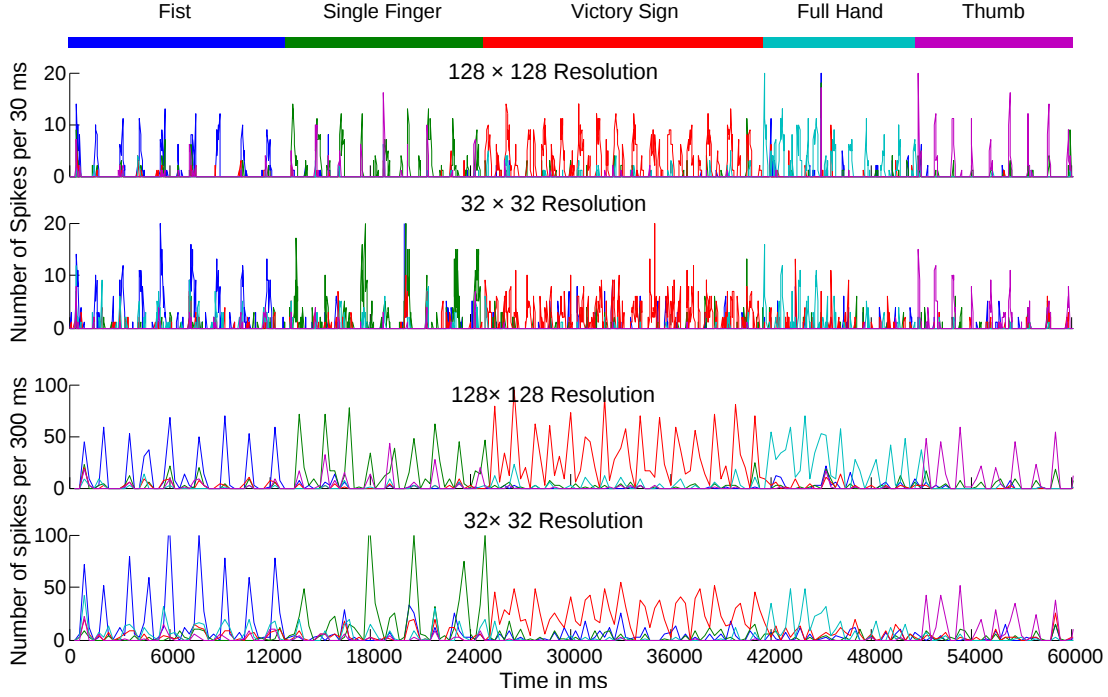
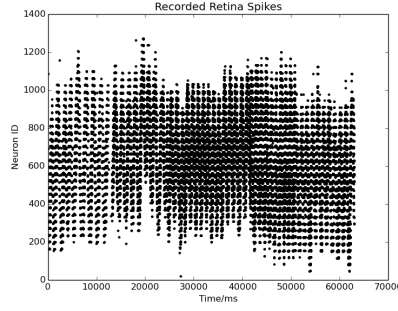
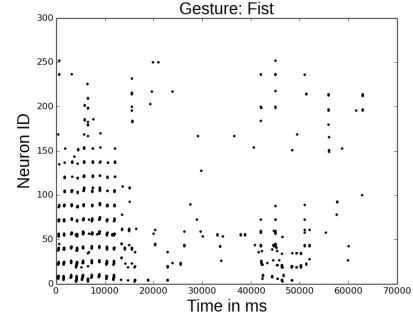


Figure 4.2: Real-time neural responses of two experiments on SpiNNaker with time to the same recorded postures. These two experiments only differ in input resolution. The result of the high input resolution test is plotted the first with a sample frame of 30 ms; while the 3rd plot shows the same result with a sample frame of 300 ms. The other two plots refer to the smaller input resolution. Every point represents the over all number of spikes of a specific population (different colour) in a ‘frame’.

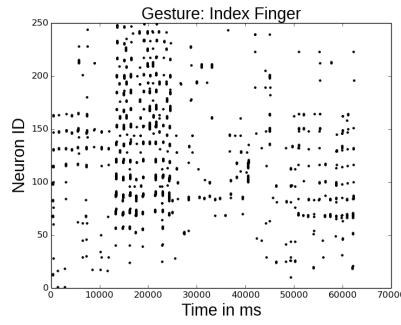
and 22.4%. This is in accordance with natural visual responses, which means, the longer an object shows, the more accurate the recognition will be. Between the two network scales there is also a smaller gap in recognition rates as the window length grows, i.e. 8.9% and 6.6% respectively.



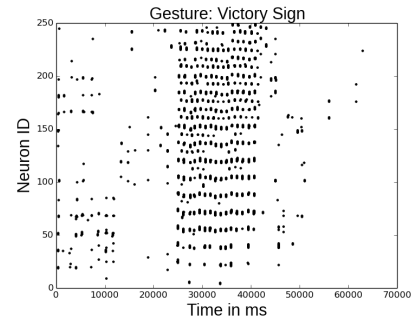
(a) Retinal input population



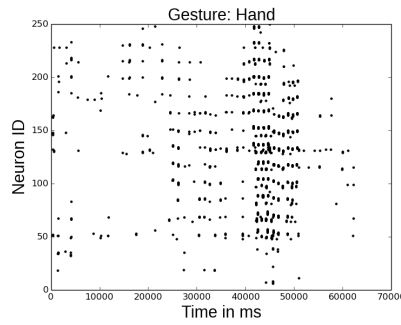
(b) Template matching population, 'Fist'



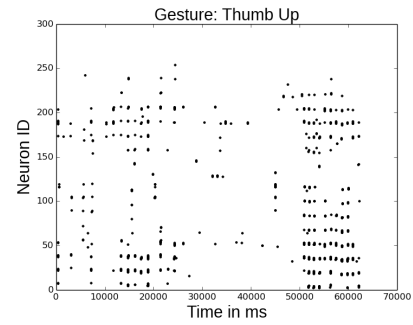
(c) Template matching population, 'Index Finger'



(d) Template matching population, 'Victory Sign'

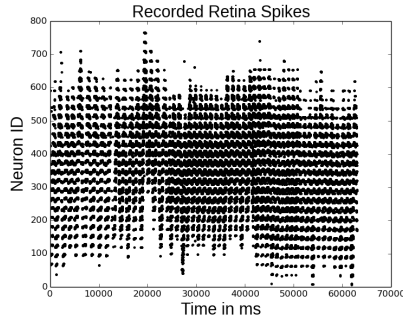


(e) Template matching population, 'Full Hand'

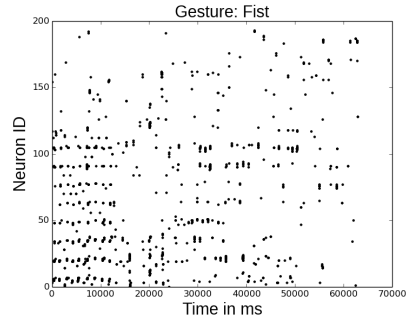


(f) Template matching population, 'Thumb Up'

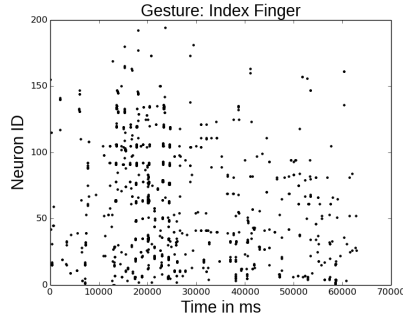
Figure 4.3: Spikes captured during the live recognition of the recorded retinal input with the resolution of  $128 \times 128$ .



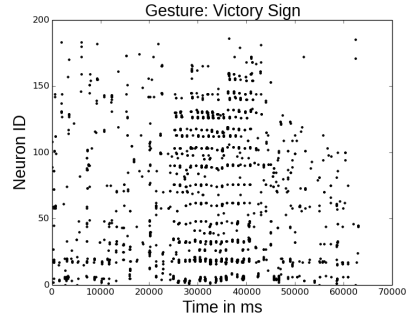
(a) Retinal input population



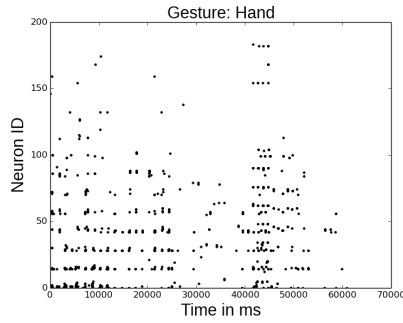
(b) Template matching population, 'Fist'



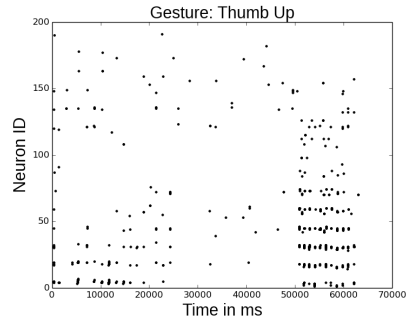
(c) Template matching population, 'Index Finger'



(d) Template matching population, 'Victory Sign'



(e) Template matching population, 'Full Hand'



(f) Template matching population, 'Thumb Up'

Figure 4.4: Spikes captured during the live recognition of the recorded retinal input with the resolution of  $32 \times 32$ .



Table 4.1: Real-time recognition results on SpiNNaker in %

		<b>30 ms per frame</b>		<b>300 ms per frame</b>	
		High Resolution	Low Resolution	High Resolution	Low Resolution
<b>Fist</b>	Correct	91.78	78.02	100	92.31
	Reject	82.78	78.54	70.73	68.29
<b>Index Finger</b>	Correct	78.25	78.25	88.24	72.22
	Reject	80.46	73.56	57.50	55.00
<b>Victory Sign</b>	Correct	96.48	86.27	95.00	92.50
	Reject	64.46	72.68	28.57	28.57
<b>Full Hand</b>	Correct	85.29	60.78	90.00	75.00
	Reject	67.31	83.65	35.48	61.29
<b>Thumb up</b>	Correct	84.09	88.10	91.67	100
	Reject	87.54	73.81	66.67	66.67
<b>Average</b>	Correct	87.18	78.28	92.98	86.41
	Reject	76.51	76.45	51.79	55.96

# Chapter 5

## Contributions and Research Plan

### 5.1 Contributions

To explore how brain may recognise objects in its general, accurate, invariant and energy-efficient manner, this work proposes the use of a neuromorphic hardware system which includes a DVS retina connected to SpiNNaker, a real-time SNN simulator. Building a hand gesture recognition system based on this bespoke hardware for dynamic hand postures is a first step in the study of the ventral visual pathway in the brain. Inspired by the structures of the primary visual cortex, convolutional neural networks are modelled, and the V1-like neurons are simulated with both linear perceptrons and LIF neurons. This model is position invariant to recognise five hand postures.

The detailed contributions are listed below:

- Modelling a convolutional neural network which can recognise moving postures (position invariant) with V1-like neurons.
- Translation of conventional artificial neural networks of perceptrons to spiking neural networks of LIF neurons using the Siegert function.
- Configuring the SpiNNaker neuromorphic platform to communicate with the silicon retina to perform real-time posture recognition using spiking neurons.
- Maintaining software to make SpiNNaker receive correct recorded spikes and compare performance with perceptrons and also visualise the live neural activity in real time.

## **5.2 Achievements**

### **5.2.1 Publications**

- Q. Liu and S. Furber, “Real-time recognition of dynamic hand posture on a neuromorphic system.” Artificial Neural Networks ICANN 2015. Springer Berlin Heidelberg. (Under review)
- Q. Liu, X. Lagorce, E. Stamatias, D. Emmanouilidou, R. Benosman, S. Furber and S. Liu, “A large-scale, real-time sound localization on a neuromorphic platform.” Neuromorphic Engineering. (Under proof reading of co-authors)
- Q. Liu, C. Patterson, S. Furber, Z. Huang, Y. Hou, and H. Zhang, “Modeling populations of spiking neurons for fine timing sound localization.” in Neural Networks (IJCNN), The 2013 International Joint Conference on, pp.1-8, Aug 2013.

### **5.2.2 Workshops**

- The 2014 CapoCaccia Cognitive Neuromorphic Engineering Workshop, 28/04/2014 - 10/05/2014 Alghero, Sardinia, Italy
- From Maps to Circuits: Models and Mechanisms for Generating Neural Connections, 28/07/2014 - 29/07/2014, Edinburgh UK

## **5.3 Future Work**

The proposed research plan is illustrated in Figure 5.1, where the scope of the research is estimated in three dimensions. To build a biologically-plausible object recognition system using spiking neurons, this work will be completed in three stages:

1. Year 1, building a position-invariant object recognition system exploiting V1-like neurons to classify five hand postures.
2. Year 1.5, combining scale- with position-invariance on the object recognition system, and building the hierarchy ventral pathway to the V2/V4 layer to recognise 50 simple combined features such as gratings and contours.

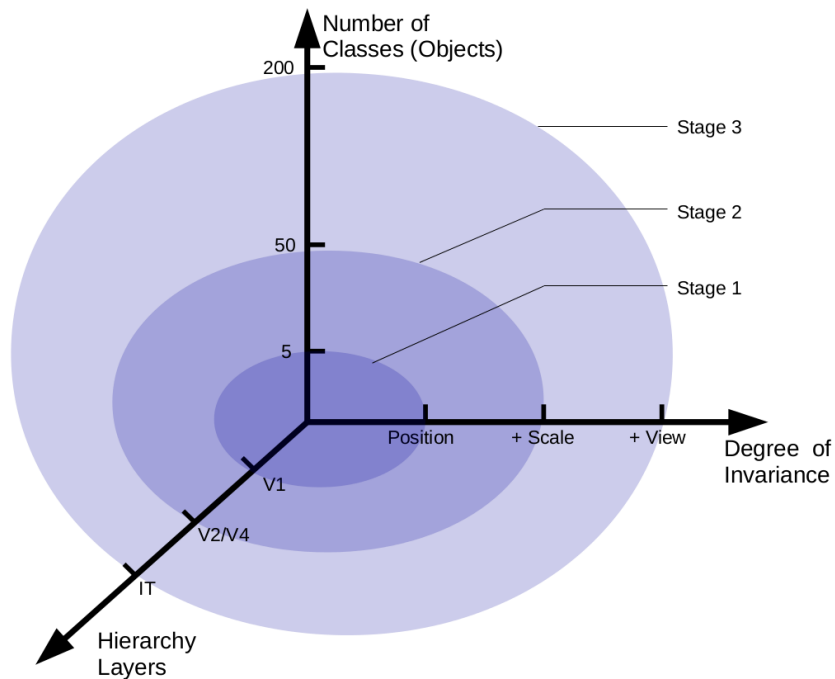


Figure 5.1: 3D representation of the research plan on the transformation-invariant object recognition system. Three milestones are pointed out indicating the expected targets of the object recognition networks.

3. Year 2.5. integrating position-, scale- and view-invariance by modelling the hierarchical visual pathway up to the IT cortex and equipping the system with the ability to recognise 200 objects in real time.

This work will contribute to the understanding of biological visual processing by means of mimicking the neural activities in the ventral stream. More importantly, the research will apply the accurate, rapid and robust approaches to artificial systems by exploring the brain's invariant object recognition. The performance of the real-time recognition system will be tested on each milestone to validate the success of the models. The neural activities and recognition rate will also be compared with biological data.

The key research steps are listed in Figure 5.2. Since the incremental work flow is hard to present in Gantt charts, only the work for the first milestone is shown. The subsequent sections will outline the key research stages.

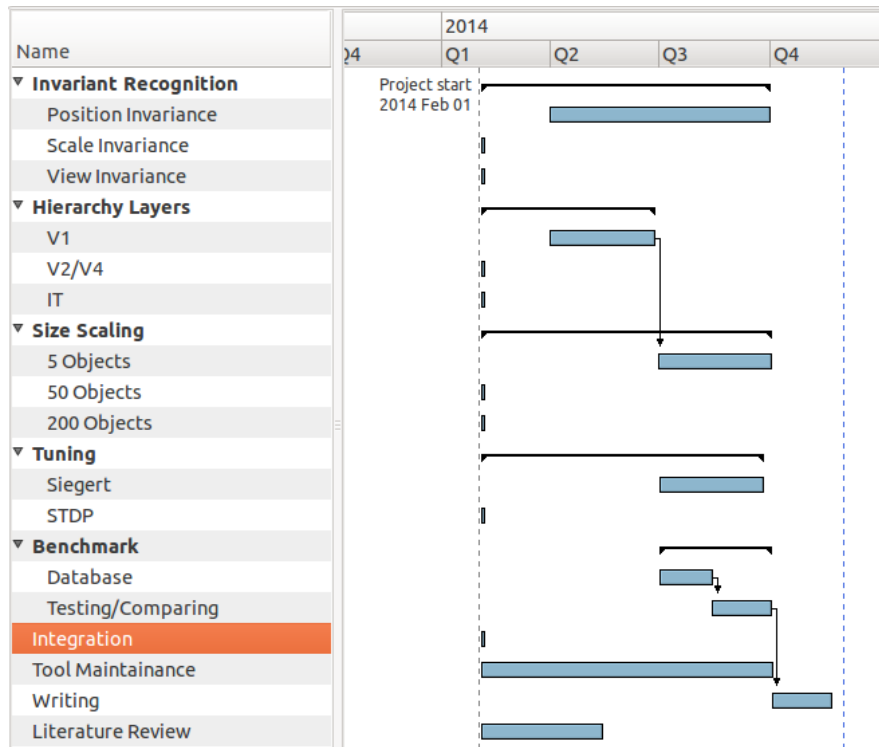


Figure 5.2: Gantt chart of the work flow for the first milestone. The main research works are listed on the left.

### 5.3.1 Invariant Object Recognition

As stated previously the brain recognises huge number of objects rapidly with ease even in noisy natural scenes. We will explore the invariant object recognition in three features: position, scale and viewing angle.

#### Position Invariance

Position invariance in the lower level of V1-like neurons has been achieved in the preliminary work by convolving receptive fields with Gabor kernels. The following work in accordance with Figure 5.1 will focus on expanding the position invariance to higher hierarchical levels of the ventral stream.

#### Scale Invariance

Similar to orientation detection, V1 provides overcomplete population re-representations of visual image on the features of scale, frequency and orientation. It forms the basis of scale invariant object recognitions. Likewise, integrating the features into the higher

abstraction of layered network to recognise more complex figures will require a tense work on tuning.

### **View Invariance**

A difficult specificity-invariance trade-off occurs in view invariant recognition tasks, since the recogniser should be able to discriminate different objects while at the same time also tolerating to viewing angle transformations. Learning will play a very important role in this work, where objects observed with multiple view points can be recognised even if only single view point is presented during training.

### **5.3.2 Modelling the Ventral Visual Pathway**

As the visual information propagates through the ventral stream (via visual area V1, V2/V4 and IT), neurons become selective for increasingly complex features. Along with this growing complexity of the preferred stimulus, neurons become more and more tolerant to the position and scale of the stimulus within their receptive fields. Inspired from the functional behaviour of the biological data (many have been mentioned in Section 2.1), this work will mimic the neural activity of each hierarchy layer by LIF neurons.

### **5.3.3 Size Scaling**

The milestones set for the dimension of number of classes/objects is in accordance with experimental data from the study of neuroscience. In work by [88], the classical receptive field of the V2 cell consists of 48 grating stimuli and 80 contour stimuli; while Zoccolan et al. [43] tested and recorded the activity of the IT neurons of monkeys with 213 grayscale pictures of isolated real-world objects.

Thanks to the massively-parallel neural simulations possible in the SpiNNaker system, implementing real-time invariant object recognition becomes possible. However, it also requires the supporting software development to support larger neural networks than currently possible.

### **5.3.4 Integration**

To reach the milestone of building an object recognition system with position, scale and view invariance, integration of these separate models will be a challenge. It not

only requires placing the models physically together but also merging their functions. As illustrated in Section 2.1.2, single neurons are tuned to different features and object identities. This work requires further investigation into population coding and learning.

### **5.3.5 Tuning**

Tuning is the key to make the object recognition system a success. In preliminary work, Siegert transformation functions are used to adjust perceptual weights for spiking LIF neurons. This is a strong indicator of the feasibility of the work. However, learning algorithms such as STDP in spiking neural networks are must be employed to make the system more biologically plausible. It is hoped that, this work will provoke further study of learning algorithms on SpiNNaker.

### **5.3.6 Benchmarking Performance**

The performance of the real-time recognition system will be evaluated of each milestone to validate the success of the models. The neural activities and recognition rate will be compared with biological data which will act as a benchmark.

#### **Building a Dataset**

Building a well-labelled retinal output dataset is essential in spike-based object recognition study. Unified benchmarks with AER format will be ideal for SNN study, because of its non-frame, event-based fashion. These benchmark datasets will also make it possible for other researchers to test their SNN model without a silicon retina present. It is hoped that this would boost communication, comparison and collaboration within the community. This work also requires lively discussion and cooperation with neuroscientists, where data can be derived and tested.

#### **Testing/Comparing**

The testing and comparing on the dataset will verify the reliability of the models. The neural responses of single or populated neurons to the same dataset will be analysed in firing rate and response time. By comparing with the biological data, the model can be rectified and improved. The more data it compares with, the closer it could untangle the object representation.

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