

# CSCI 3110

## Fun with Algorithms

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Dalhousie University  
Fall 2015



# Stable Matching: An Introductory Example

## Given:

- $n$  women  $w_1, w_2, \dots, w_n$
- $n$  men  $m_1, m_2, \dots, m_n$
- A preference list for each

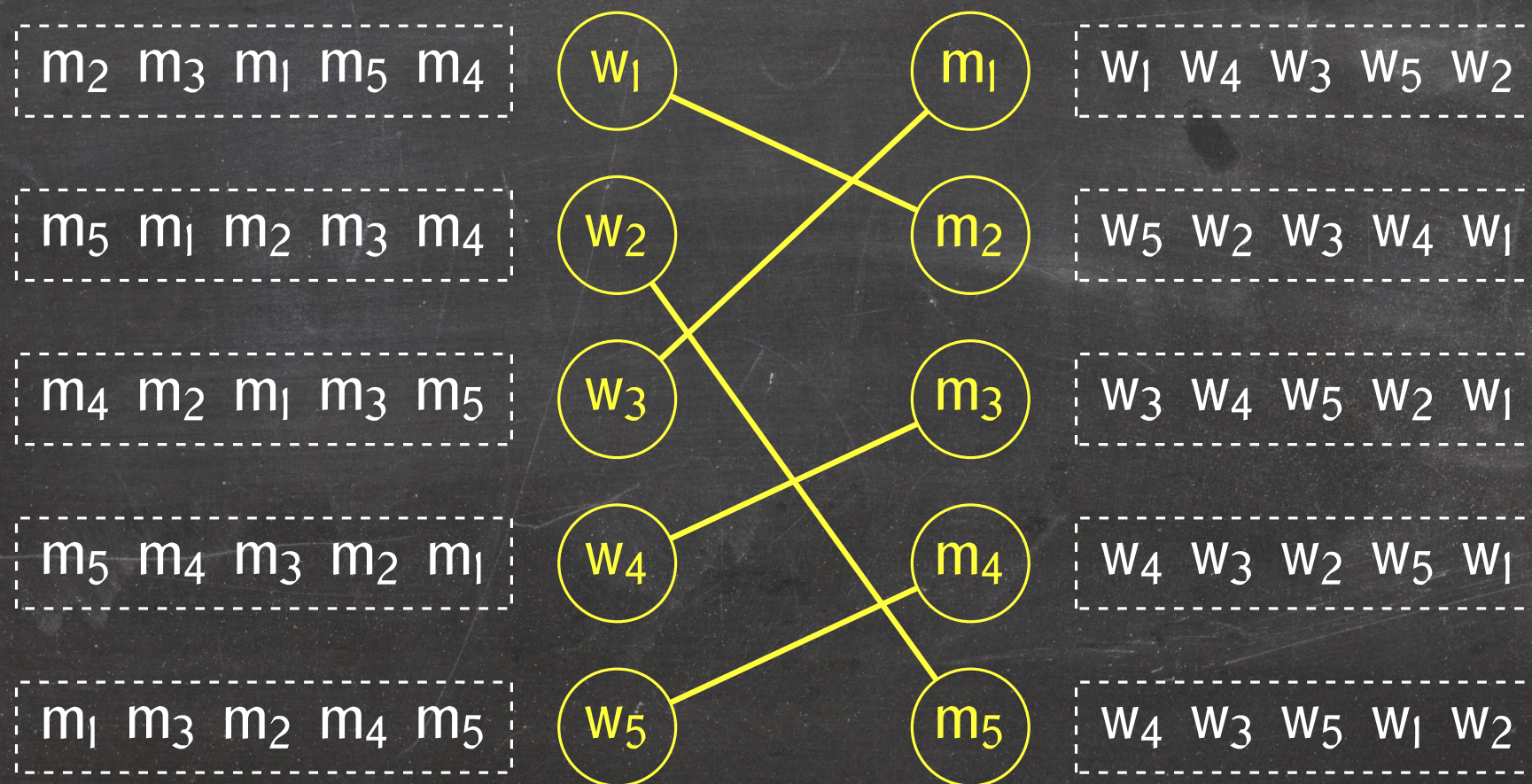
$m_2 \ m_3 \ m_1 \ m_5 \ m_4$	$w_1$	$m_1$	$w_1 \ w_4 \ w_3 \ w_5 \ w_2$
$m_5 \ m_1 \ m_2 \ m_3 \ m_4$	$w_2$	$m_2$	$w_5 \ w_2 \ w_3 \ w_4 \ w_1$
$m_4 \ m_2 \ m_1 \ m_3 \ m_5$	$w_3$	$m_3$	$w_3 \ w_4 \ w_5 \ w_2 \ w_1$
$m_5 \ m_4 \ m_3 \ m_2 \ m_1$	$w_4$	$m_4$	$w_4 \ w_3 \ w_2 \ w_5 \ w_1$
$m_1 \ m_3 \ m_2 \ m_4 \ m_5$	$w_5$	$m_5$	$w_4 \ w_3 \ w_5 \ w_1 \ w_2$



# Stable Matching: An Introductory Example

## Output:

- A set of  $n$  marriages  $\{(w_{i_1}, m_{j_1}), (w_{i_2}, m_{j_2}), \dots, (w_{i_n}, m_{j_n})\}$
- Every man is married
- Every woman is married
- The marriages are **stable**

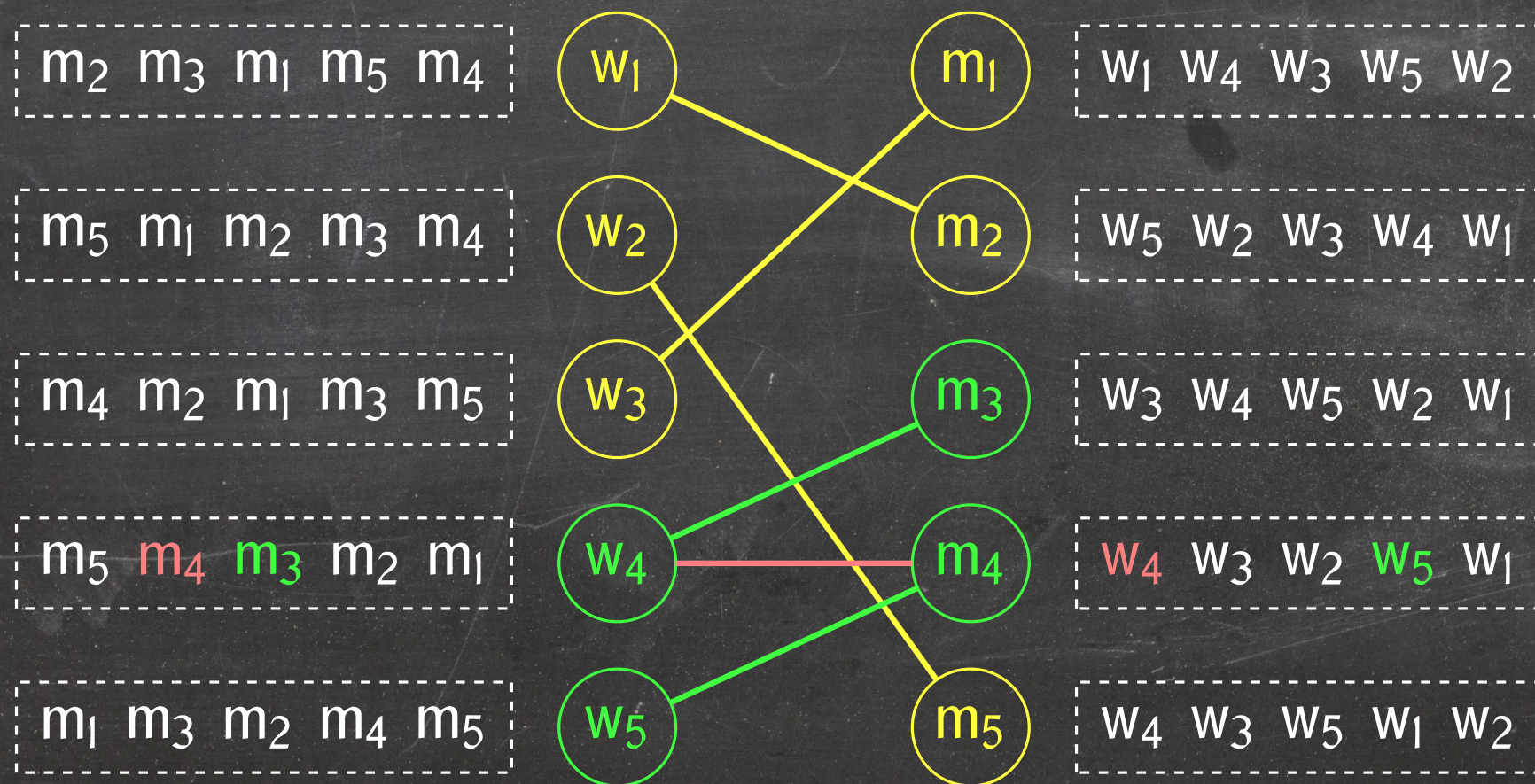




# Stable Matching: An Introductory Example

A pair of marriages  $(m, w)$  and  $(m', w')$  is **unstable** if

- $w$  prefers  $m'$  over  $m$  ( $m' \prec_w m$ )
- $m'$  prefers  $w$  over  $w'$  ( $w \prec_{m'} w'$ )

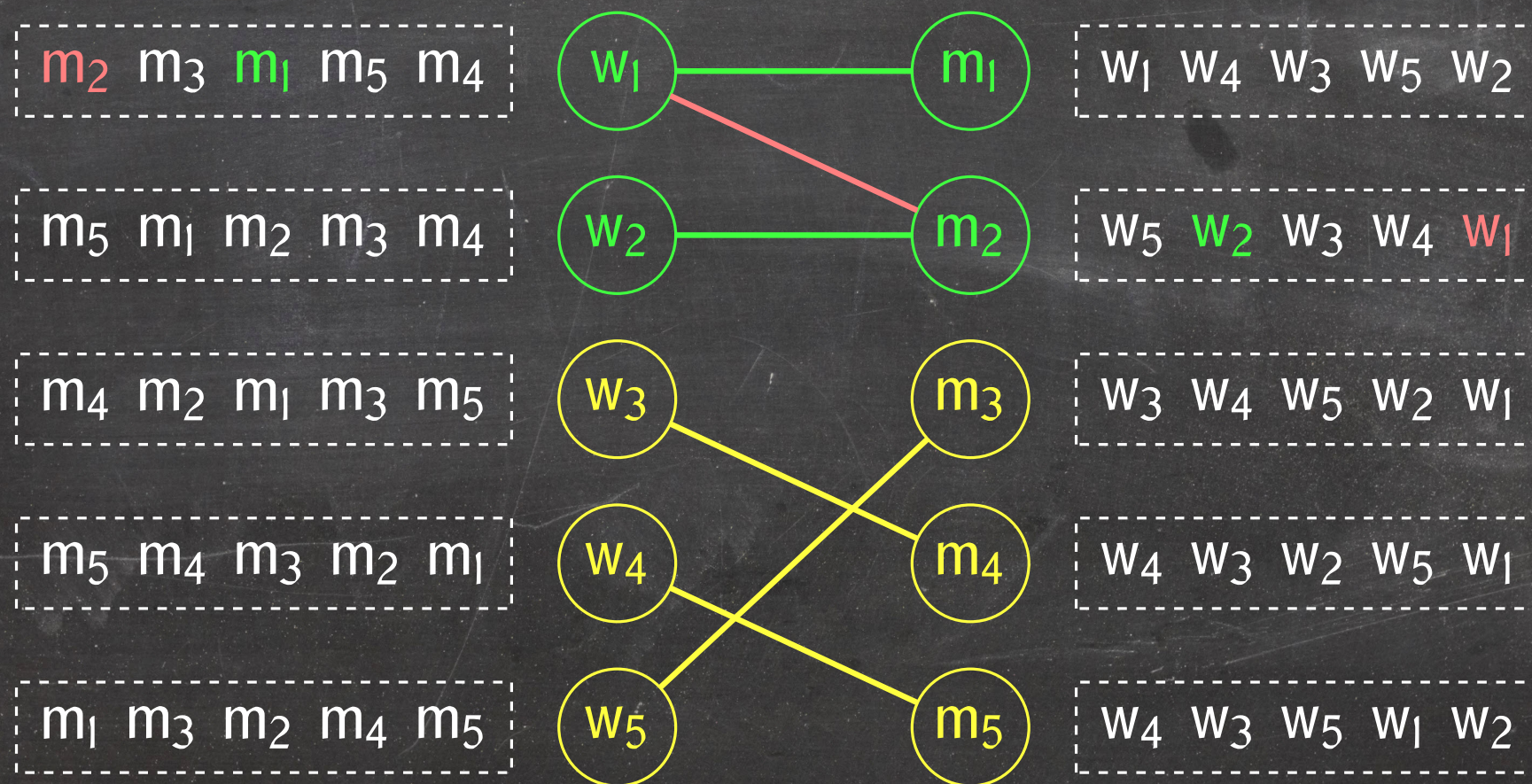




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# Stable Matching: A Solution Inspired By Real Life

## StableMatching(M, W)

```
1  while there exists an unmarried man m
2      do m proposes to the most preferable woman w he has not proposed to yet
3          if w is unmarried or likes m better than her current partner m'
4              then if w is married
5                  then w divorces m'
6                  w marries m
```



# Stable Matching: A Solution Inspired By Real Life

## StableMatching(M, W)

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## Questions we can and should ask about the algorithm:

- Is there always a stable matching?
- Does the algorithm always terminate?
- Does the algorithm always produce a stable matching?
- How efficient is the algorithm? Can we bound its running time?



# Course Outline

- Correctness proofs
- Analysis of resource consumption
- Algorithm design techniques
  - Graph exploration
  - Greedy algorithms
  - Divide and conquer
  - Dynamic programming
  - Data structuring
  - Randomization
- NP-completeness and intractability



# General Information

Instructor: Norbert Zeh

Office: Goldberg 313

Office hours: Mon, Wed 1:30–3:00

Email: [nzeh@cs.dal.ca](mailto:nzeh@cs.dal.ca)

Textbook: Cormen, Leiserson, Rivest, Stein. **Introduction to Algorithms.**  
3rd edition, MIT Press, 2009.

Zeh. **Data Structures.**  
CSCI 3110 Lecture Notes, 2005.

Website: <http://www.cs.dal.ca/~nzeh/Teaching/3110>

TAs: David Samuel  
Mengdu Li  
Habibeh Naderi

Midterm: Oct 30



# Grading

- 10 Assignments (A)

The best 8 count. Each carries equal weight.

- Midterm (M)
- Final (F)

$$\text{Final grade} = \max \begin{pmatrix} F \\ 60\% \cdot F + 40\% \cdot M \\ 60\% \cdot F + 40\% \cdot A \\ 40\% \cdot F + 20\% \cdot M + 40\% \cdot A \end{pmatrix}$$



# Collaboration, Plagiarism, Late Assignments

## Collaboration

- Groups of up to three people are allowed to collaborate on assignments.
- Every group hands in one set of solutions; every group member gets the same marks.
- Collaboration between groups is not allowed!

## Plagiarism

- Plagiarism will not be tolerated.
- Collaboration between groups is a form of plagiarism.

## Late assignments

... will not be accepted without a doctor's note.

Please see course website for a detailed discussion of these rules.



# Things I Expect You To Know

- Basic rules concerning logarithms
- Basic rules concerning limits
- Basic derivatives
- Propositional logic
- Elementary combinatorics (counting permutations, combinations, ...)
- Elementary probability theory (linearity of expectation, ...)
- Elementary data structures (arrays, lists, stacks, queues, ...)
- Standard sorting algorithms (insertion sort, quick sort, merge sort)
- Binary heaps