CSCI 2110

Data Structures and Algorithms Practice Set for Test No. 1

1. Derive the big O complexities for each of the following running times: a. $25n^4 + 45n - 256$

a.
$$25n^4 + 45n - 256$$

b.
$$n^2 + 3000n + 500 n^2 log n + 1000$$

c.
$$(3\log n + 5)(n^3 + 2)$$

d.
$$(n^3 + 2n^2 + 3)/n^2$$

e.
$$(1+2+3+...+n)(1+2+3+...+n)$$

f.
$$(1^2+2^2+3^2+....+n^2)/(1+3+5+...+2n-1)$$

g.
$$\log n^3 + n \log n^4 + n \log n^2$$

- 2. Arrange the following growth functions in <u>increasing order</u> of growth rates. (Reduce the growth functions wherever necessary).
 - a. The growth functions that you derived in Question 1 above.
 - b. $10000n, 100n^2, \sqrt{n}, 10n^3, 2^n, \sqrt{n} * logn, nlogn, nlogn^n$
- 3. a) What does it mean for a function to be O(1)?
 - b) Which has the larger time complexity O(1) or O(1/n)? Why?
- 4. An algorithm with complexity $O(n^2)$ takes 5 ms to process 50 data items.
 - a) Estimate how long it will take to process 5000 data items.
 - b) Estimate how much data can be processed in 500 ms.
- 5. An algorithm with complexity O(nlog₂n) takes 1 ms to process 1024 data items.
 - a) Estimate how long it will take to process 512 data items.
 - b) Estimate how long it will take to process 1024*1024 data items.
- 6. Three software packages A, B and C are being used to determine DNA patterns. Software package A takes exactly $T_A = K_A * n + 100$ seconds, B takes exactly $T_B = K_B * n + \log_2 n$ seconds and C takes $T_C = K_C * n^2$ seconds to finish the task for a problem of size n. During an experiment, it was observed that A takes 1700 seconds, B takes 100 seconds, and C takes 256 seconds to complete to process n = 16 data items.
 - Which package would be the best for processing n = 1024 data items?
 - Which package would be the worst for the same?
 - Which two packages would have the same Big O complexity?

7. Give one example each of an algorithm or operation that has the following time complexity

Complexity	Algorithm / Operation
O(1)	
O(n)	
$O(n^2)$	
O(log n)	
$O(n^3)$	
$O(2^n)$	

8. Derive the number of iterations for each of the following code segments, the big O complexity of each and the overall complexity of the full code.

```
for (int i = 1; i <= n; i++)
     sum++;
for (int i = 1; i <= n; i++)
      for (int j = 1; j <=n; j++)
           sum++;
if (x==10)
     for (int i = 1; i <= n; i++)
           sum++;
else
{
     for(int i=1;i<=n;i++)</pre>
           for(int j=1; j<=n;j++)</pre>
                 for(int k=1;k<=n;k++)</pre>
                       sum++;
}
for (int j = 1; j < n; j=2*j)
           sum++;
for (int i = 1; i <= n; i++)
      for (int j = 1; j <= i; j++)
                 sum++;
```

9. There is a highway with n exits numbered 1 to n. You are given a list of the distances between them. For instance:

Exits: 0 1 2 3 4 5 6 Distances: 0 5 3 4 2 8 7

The distance from exit0 to exit1 is 5, from exit1 to exit2 is 3, from exit2 to exit3 is 4, and so on.

Design an algorithm (in pseudocode) that would calculate the distance between a given pair of exits:

For example, Distance(exit4, exit6) is 8+7 = 15 As a second example, Distance(exit0, exit5) is 5+3+4+2+8= 22

Remember, n can be any number. You may use any appropriate storage structure.

Note: A pseudocode is just an outline of the program written in a form that can be easily converted to a program. Syntax is not important in a pseudocode.

What is the worst case complexity of your algorithm?

What is the best case complexity of your algorithm?

What is the average case complexity of your algorithm?

10. Two people compare their favourite playlists for matching songs. Both playlists have n songs each. Each playlist is stored in an array, in no particular order.

Design an algorithm in pseudocode to find the common songs in these lists. The algorithm should search the two playlists and put all the common songs into a third array.

What is the worst-case complexity of the algorithm?

11. The Node<T> class has been defined and is given on the Reference sheet.

The LinkedList<T> class has the following structure.

```
public class LinkedList<T>
{
    private Node<T> front;
    private int count;

    public LinkedList()
    {
        front = null;
        count=0;
    }
```

Add the following methods to the above code

- a. Add a given item to the end of the list.
- b. Print the data contained in every second item in the linked list.
- c. Remove the last node from the linked list (if it exists).
- d. Remove the second last node from the linked list (if it exists).

12. Short Snappers

- 1. The class in java from which all classes directly or indirectly inherit from is the ______ class.
- 2. The operator that can be used to determine whether a reference variable references an object of a particular class is the operator.
- 3. If ClassB extends ClassA, and ClassC is a superclass of ClassA, and the following declaration has been made:

```
ClassA ref;
which of the following are valid?
    ref = new ClassA();
    ref = new ClassB();
    ref = new ClassC();
```

4. ClassB extends ClassA, and ClassC extends ClassB, and ClassD extends ClassC. The following is a part of the code in a program:

```
ClassB ref;
ref = new ClassC();
```

What will each of the following statements return?

```
if (ref instanceof ClassA)
if (ref instanceof ClassB)
if (ref instanceof ClassC)
if (ref instanceof ClassD)
```

13. Write a class called Point that has two attributes (xpos and ypos), a constructor that sets xpos and ypos, set methods for xpos and ypos, get methods for xpos and ypos, and a toString method that returns the values.

The class must be written as a generic class, which means that it should work for any type of object, say Integer, or Double, or String.

14. You are given the methods in the Unordered List class on the reference sheet. *Using these methods*, implement the following methods. You may declare any necessary variables inside the methods.

```
//create a new list that has list1 concatenated with
// list2.Order doesn't matter
public List concatenate(List<T> list1, List<T> list2)
{
```

15. An application program class PokemonList uses the Unordered List class. Another class Pokemon defines the Pokemon object items that will be used by the PokemonList class. The first few lines of the program are given. Some lines are missing or some parameters in each line may be missing. Write the missing pieces.

REFERENCE SHEET

Useful properties of logarithms:

```
\begin{split} log_b(xy) &= log_b x + log_b y \\ log_b\left(x/y\right) &= log_b x - log_b y \\ log_b x^a &= alog_b x \\ log_x a/log_x b = log_b a \end{split}
```

Useful properties of exponentials:

```
\overline{a^{(b+c)}} = \overline{a^b a^c}

a^{bc} = (a^b)^c

a^b / a^c = a^{(b-c)}
```

Useful series:

}

```
Sum of first n integers: 1+2+3 + ... + n = n(n+1)/2
```

Sum of first n odd positive integers: $1 + 3 + 5 + ... (2n-1) = n^2$

Sum of squares of first n integers: $1^2 + 2^2 + 3^2 + \dots + n^2 = n*(n+1)*(2n+1)/6$

```
//Class Node<T>
public class Node<T>
{
    private T data;
    private Node<T> next;
    public Node (T data, Node<T> next)
    {
        this.data = data;
        this.next = next;
    }
    public T getData()
    {
        return data;
    }
    public Node<T> getNext()
    {
        return this.next;
    }
    public void setData(T data)
    {
        this.data = data;
    }
    public void setNext(Node<T> next)
    {
        this.next = next;
}
```

Unordered List Class Reference Sheet

Constructors

List <t>()</t>	Constructs an empty unordered list
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Methods

Name	What it does	Header
size	returns size of the list	int sime()
size	returns size of the list	int size()
isEmpty	returns true if list is empty	boolean isEmpty()
clear	clears the list	void clear()
add	adds an item to the front of the list	void add(T item)
first	gets the first entry	T first ()
next	gets the next entry	T next()
enumerate	scans the list and prints it	void enumerate()
contains	searches for a given item and returns true or false	boolean contains(T item)
remove	remove an item (first occurrence) from the list.	void remove(T item)
removeAll	remove all occurrences of a specified item from the list.	void removeAll(T item)