

Addendum

(Lecture 13 $\frac{1}{2}$)

Postfix and Infix

Or

Why you should learn to stop worrying
and love the stack

Infix – the *fix you know

- You already know infix notation. Easy!
- In algebraic expression with two inputs, we **fix** the operator within the operands:

$$5 - 3 = 2$$

$$\langle \text{operand_1} \rangle \langle \text{operator} \rangle \langle \text{operand_2} \rangle$$

- Things can get ambiguous sometimes:

$$5 - 3 \times 2 = 4?$$
$$= -1?$$

- We use order-of-operations rules to resolve these

Postfix – the *fix you need

- Another notational method avoids the ambiguity
- Assume we always use binary operators (limited to two inputs)
- Write the operator after (or **post**) the operands; in other words, write the symbol after the numbers:

$$5\ 3\ -\ =\ 2$$

$$5\ 3\ 2\ *\ -\ =\ -1$$

Postfix – Stacks in the mix

- How does a stack play into this?
- In processing a postfix string, left-to-right
- Basic algorithm idea for a tokenized string:
 - Consider next token
 - If token is a number, push it onto stack
 - If token is an operator ...
 - Pop two items (numbers) from stack
 - Perform operation
 - Push result onto stack
 - Loop to consider next token

Postfix – Examples

1 2 + 3 - 4 + 5 6 * *

2 4 8 / * 16 *

10 15 20 + - *

In reverse, infix to postfix:

$((3 * 4) + 2) / 7$

(peel the onion)

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