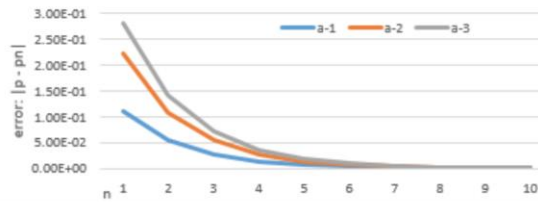


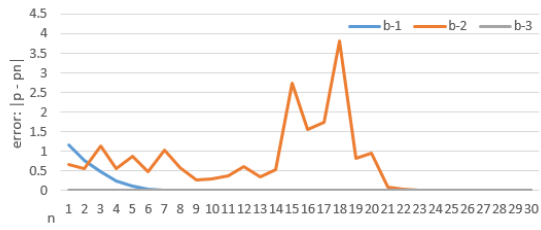
In this assignment, the purpose is to use Newton's Method, Modified Newton's Method, and Steffensen's method (notated as -1, -2 and -3 within the following charts) to find solutions of Exercise Set 2.4 Question 2 accurate to within $1e-5$.

These root finding methods, gotten from *Numerical analysis tenth edition*, written by RICHARD L. BURDEN, DOUGLAS J. FAIRES, ANNETTE M. BURDEN, (2014), the algorithm2.3 (page67) and algorithm2.6 (page88), were used to iterate values and find the approximated roots by following table.

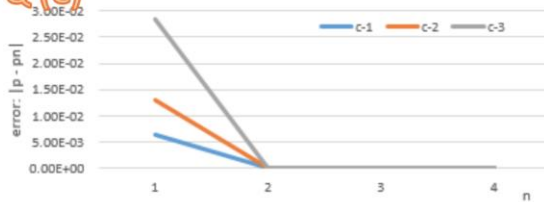
Q (A) errors of Newton's Method-1, Modified NM-2, and Stefensen's Method-3 in Question (a) vs n



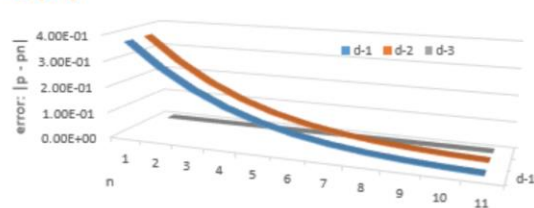
Q (B) error Q(b) vs n



Q (C) error Q(c) vs n



Q (D) error Q(d) vs n



Same question, but different root finding methods

Same question, but different root finding methods

	Number:	Q(a)	Q(b)	Q_	Q(d)
	Interval:	[0, 1]	[-3, -2]	[3, 4]	[3, 5]
solution	Newton's Method	0.73907	-1.3343	3.1416	3.7331
	Modified Newton's Method	0.73909	-1.3343	3.1416	3.7331
	Steffensen's Method	0.73910	-3.0000	3.1416	3.5000

The **stopping condition** for these iteration methods is when $|p_n - p| < \text{TOL}$ and $\text{TOL} = 1e-5$. For Steffensen's Method, adding an extra "x" in each side of each equation so that they were constructed as $g(x) = x$. Apparently, the roots of (b) which are **-1.3343** is out of interval $[-3, 2]$, so (b) is NOT convergence in this specific interval and (a), (c) and (d) are convergence from the charts above.

Q(a): Stefensen's Method is better, because it converges faster than other methods and it gets great solution.

Q(b): Since all the method that were used could not get the root within the specific interval, (b) will NOT be discussed in terms of these method.

Q©: Newton's Method is better, because this method requires **less work**, though all the method can cancel the error and get the solution at the exactly second step.

Q(d): Stefensen's Method is better. This method's error is always zero (or close to zero). Differently, the error of Newton's Method and Modified Newton's Method are exactly the same (> 0).