Assignment 3: Calibration

Please edit the cell below to include your name and student ID #

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1. Parameterizing 3D Rotations

In order to optimize over the camera rotation during calibration, we need a way to parameterize the space of 3D rotations. There are many different ways to do this and each comes with different tradeoffs, but for our purposes we will adopt a simple approach of building a rotation by a sequence of rotations around the X, Y and Z axes (so called *Tait-Bryan angles*, see https://en.wikipedia.org/wiki/Euler_angles) for more discussion)

1.1 Implement

Write a function **makerotation** which takes as input three angles **rx,ry,rz** and returns a rotation matrix corresponding to rotating by **rx** degrees around the x-axis, followed by a rotation of **ry** degrees around the y-axis, followed by a rotation of **rz** degrees around the z-axis.

```
In [1]: import numpy as np
   import matplotlib.pyplot as plt
   import scipy.optimize
   import matplotlib.patches as patches
   from mpl_toolkits.mplot3d import Axes3D
   import visutils
    *matplotlib inline
```

```
In [2]:
        def makerotation(rx,ry,rz):
            Generate a rotation matrix
            Parameters
            rx,ry,rz : floats
                Amount to rotate around x, y and z axes in degrees
            Returns
            R: 2D numpy.array (dtype=float)
                 Rotation matrix of shape (3,3)
            xangle=np.radians(rx)
            yangle=np.radians(ry)
            zangle=np.radians(rz)
            rz_matrix= np.array([[np.cos(zangle), - np.sin(zangle),0],[(np.sin(
            ry_matrix= np.array([[np.cos(yangle),0, np.sin(yangle)],[0,1,0],[(
            rx_matrix= np.array([[1,0,0],[0,np.cos(xangle),- np.sin(xangle)],
            r_matrix= rx_matrix.dot(ry_matrix)
            r_matrix= r_matrix.dot(rz_matrix)
            return r_matrix
```

1.2 Test

Work out by hand what a 90 degree rotation should look like. Then execute the test examples below and verify/convince yourself that the output of your code matches.

Find a way to achieve the same rotation as **makerotation(90,90,0)** but without using rotation around the x-axis. That is, determine some angles so that **makerotation(0,?,?)** == makerotation(90,90,0)

```
[[ 1.
        0.
            0.]
 [ 0.
        0. -1.1
            0.]]
   0.
        1.
            1.1
[[ 0.
        0.
        1.
            0.1
 [ 0.
            0.11
 [-1.
        0.
[[0. -1.
            0.]
   1.
        0.
            0.]
            1.]]
   0.
        0.
            1.]
[[ 0.
        0.
   1.
        0. -0.1
            0.11
 [-0.
        1.
[ [ 0. -0. ]
            1.1
 [ 1.
        0.
            0.]
 [-0.
        1.
            0.11
```

2. Reprojection Error

We will now specify a function which computes the reprojection error. This is the function that we will later optimize when calibrating the camera extrinsic parameters. Take a look at the documentation for **scipy.optimize.leastsq**. The optimizer expects that our function should take a vector of parameters and return a vector of residuals which it will square and sum up to get the total error. For this reason, we will structure our code in the following way.

First, write a member function for the Camera class called **update_extrinsics** which takes a vector of 6 parameters (rx,ry,rz,tx,ty,tz). The function should keep the same intrinsic parameters (f,c) but update the extrinsic parameters (R,t) based on the entries in the parameter vector.

Second, implement a function named **residuals** which computes the difference between a provided set of 2D point coordinates and the projection of 3D point coordinates by specified camera. The residuals function takes as input the 3D points, the target 2D points, a camera with specified intrinsic parameters, and an extrinsic parameter vector. You should use **update_extrinsics** to update the extrinsic parameters, compute the projection of the 3D points with the updated camera and return a 1D vector containing the differences of all the x and y coordinates.

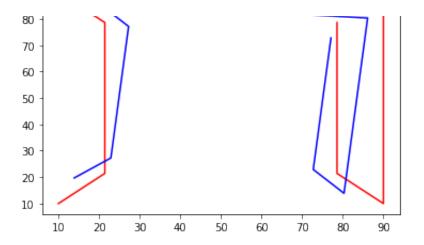
```
In [4]:
        class Camera:
            A simple data structure describing camera parameters
            The parameters describing the camera
            cam.f : float     --- camera focal length (in units of pixels)
            cam.c: 2x1 vector --- offset of principle point
            cam.R: 3x3 matrix --- camera rotation
            cam.t: 3x1 vector --- camera translation
            .....
            def __init__(self,f,c,R,t):
                self.f = f
                self.c = c
                self_R = R
                self.t = t
            def str (self):
                return f'Camera : \n f={self.f} \n c={self.c.T} \n R={self.R}
            def project(self,pts3):
                Project the given 3D points in world coordinates into the spec
```

```
Parameters
    pts3 : 2D numpy.array (dtype=float)
        Coordinates of N points stored in a array of shape (3,N)
    Returns
    pts2 : 2D numpy.array (dtype=float)
        Image coordinates of N points stored in an array of shape
    assert(pts3.shape[0]==3)
    temp=pts3.copy()
      print(self.t.reshape((3,1)))
    temp=np.subtract(temp,self.t)
    rr=np.linalg.inv(self.R)
    r=np.dot(rr,temp)
    r[0,:]=np.divide(r[0,:],r[2,:])
    r[1,:]=np.divide(r[1,:],r[2,:])
    r= r*self.f
    pts2=r[0:2,:]
    pts2=pts2+self.c
    assert(pts2.shape[1]==pts3.shape[1])
    assert(pts2.shape[0]==2)
    return pts2
def update_extrinsics(self,params):
    Given a vector of extrinsic parameters, update the camera
    to use the provided parameters.
    Parameters
    params: 1D numpy.array of shape (6,) (dtype=float)
        Camera parameters we are optimizing over stored in a vector
        params[:3] are the rotation angles, params[3:] are the tra
    .....
    self.t=params[3:].reshape(3,1)
    self.R=makerotation(params[0],params[1],params[2])
```

```
Parameters
    pts3 : 2D numpy.array (dtype=float)
        Coordinates of N points stored in a array of shape (3,N)
    pts2 : 2D numpy.array (dtype=float)
        Coordinates of N points stored in a array of shape (2,N)
    params : 1D numpy.array (dtype=float)
        Camera parameters we are optimizing stored in a vector of share
    Returns
    residual : 1D numpy.array (dtype=float)
        Vector of residual 2D projection errors of size 2*N
#
      print("residuals",pts2.size,pts3.size)
    z= np.zeros((1,pts2[0].size))
    cam.update_extrinsics(params)
    pts2_d=cam.project(pts3)
    z=pts2-pts2_d
    zz=np.reshape(z,pts2.size, order='F')
    return zz
#
      def fun x(a,b):
#
          return arg min(sum(((a-b)**2,axis=0))
#
      for i in range(pts2.shape[1]):
          temp= np.dstack((pts2[:,i],pts2_d[:,i]))
#
#
          temp= temp.reshape(2,2)
            print(temp)
#
          print(cam.t)
#
#
          y=pts2[:,i]-pts2_d[:,i]
          x = arg min(sum(fun_x(y)**2,axis=0))
          ztemp = scipy.optimize.leastsq(x, z)
#
            z[0,i]=ztemp[0][0]
            z[1,i] = ztemp[0][1]
            z[i] = (pts2[0,i]-pts2_d[0,i])**2
# #
            z[i+1] = (pts2[1,i]-pts2_d[1,i])**2
# #
            i+=1
    return z
```

```
In [6]: #
# Test the residual function to make sure it is doing the right thing.
#
```

```
# create two cameras with same intrinsic but slightly different extrin
camA = Camera(f=200, c=np.array([[50,50]]).T, t=np.array([[0,0,0]]).T, f
camB = Camera(f=200, c=np.array([[50,50]]).T, t=np.array([[0,0,0]]).T, f
paramsA = np.array([0,0,0,0.5,0.5,-2.5])
paramsB = np.array([0,0,5,0.5,0.5,-3])
camA.update_extrinsics(paramsA)
camB.update_extrinsics(paramsB)
print(camA)
print(camB)
# create a test object (corners of a 3D cube)
pts3 = np.array([[0,0,0],[0,0,1],[0,1,1],[0,1,0],[1,1,0],[1,0,0],[1,0,0]
# print(pts3)
# visualize the two projections
pts2A = camA.project(pts3)
pts2B = camB.project(pts3)
plt.plot(pts2A[0,:],pts2A[1,:],'r')
plt.plot(pts2B[0,:],pts2B[1,:],'b')
plt.show()
# double check that the residuals are the same as the difference in the
print("\n residuals of camB relative to camA")
print(residuals(pts3,pts2A,camB,paramsB))
print(pts2A-pts2B)
print("\n residuals of camA relative to camB")
print(residuals(pts3,pts2B,camA,paramsA))
print(pts2B-pts2A)
Camera:
 f=200
 c = [[50 50]]
R=[[1. 0. 0.]
 [0. 1. 0.]
 [0. 0. 1.]]
 t = [[ 0.5  0.5 -2.5]]
Camera:
 f = 200
 c=[[50 50]]
R = [[0.9962 - 0.0872 0.
 [ 0.0872 0.9962 0.
                         11
 [ 0.
           0.
                   1.
 t = [[ 0.5  0.5 -3. ]]
```



```
residuals of camB relative to camA
[-3.8883 -9.6987 -1.4877 -5.8455 -5.8455 1.4877 -9.6987 3.8883
883
         9.6987 -3.8883
                         5.8455 -1.4877
  9.6987
                                         1.4877
                                                 5.8455]
[[-3.8883 -1.4877 -5.8455 -9.6987
                                 3.8883 9.6987
                                                  5.8455
                                                          1.48771
 [-9.6987 - 5.8455]
                 1.4877
                          3.8883
                                 9.6987 -3.8883 -1.4877
                                                          5.8455]]
residuals of camA relative to camB
[ 3.8883
         9.6987
                1.4877
                        5.8455
                                 5.8455 -1.4877 9.6987 -3.8883 -3.8
883
-9.6987 -9.6987
                 3.8883 -5.8455
                                 1.4877 -1.4877 -5.84551
[[ 3.8883
          1.4877
                  5.8455 9.6987 -3.8883 -9.6987 -5.8455 -1.4877]
 9,6987 5,8455 -1,4877 -3,8883 -9,6987 3,8883
                                                 1.4877 -5.8455]]
```

3. Camera Pose Estimation

We are now ready to estimate camera pose using optimize. Implement a function calibratePose which takes as input the 3D coordinates of a calibration object, the observed 2D coordinates in the image, and an initial guess of the camera. Your function should use scipy.optimize.leastsq to optimize the extrinsic parameters in order to minimize the reprojection error. Since the residuals function takes additional arguments and leastsq expects a function which only takes the parameter vector as input, you should use Python's lambda function to wrap residuals, subistituting in the parameters that are fixed during the optimization. Once you have determined the optimum parameters, update the extrinsic parameters to the optimum and return the resulting camera.

3.1 Implementation

```
In [7]:
        def calibratePose(pts3,pts2,cam,params_init):
            Calibrate the provided camera by updating R,t so that pts3 project
            as close as possible to pts2
            Parameters
            pts3 : 2D numpy.array (dtype=float)
                Coordinates of N points stored in a array of shape (3,N)
            pts2 : 2D numpy.array (dtype=float)
                Coordinates of N points stored in a array of shape (2,N)
            cam : Camera
                Initial estimate of camera
            params_init : 1D numpy.array (dtype=float)
                Initial estimate of camera extrinsic parameters ()
                params[0:2] are the rotation angles, params[2:5] are the trans
            Returns
            cam : Camera
                Refined estimate of camera with updated R,t parameters
            x = lambda params init,pts3=pts3,pts2=pts2,cam=cam: residuals(pts3
            input_int = [pts3,pts2,cam,params_init]
            ex= scipy.optimize.leastsq(x,params_init)
            cam.update_extrinsics(ex[0])
            return cam
```

3.2 Synthetic Test Example and Failure Cases

Use the code below to check that your calibrate function works. Add some code to also visualize the point locations in 3D and the location and orientation of the camera (i.e., using the 3D plotting functions from Assignment 2)

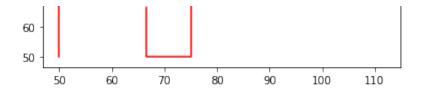
Once you are confident that your calibration function is behaving correctly, you should experiment with changing the initial parameters. Find a set of initial parameters which yields a **wrong** solution (i.e. where the Final Camera is not similar to the True Camera). In the text box below indicate what bad initialization you used and the resulting set of camera parameters after the optimization. Give a brief explanation of where this bad camera is located and what direction it is oriented in.

```
In [8]: # 3D calibration object
        pts3 = np.array([[0,0,0],[0,0,1],[0,1,1],[0,1,0],[1,1,0],[1,0,0],[1,0,0])
        # true camera
        cam_true = Camera(f=50, c=np.array([[50,50]]).T, <math>t=np.array([[-1,-1,-2]]
        print("\n True Camera")
        print(cam_true)
        # image of calibration object with some simulated noise in the 2D lock
        pts2 = cam true.project(pts3)
        noiselevel = 0.5
        pts2 = pts2 + noiselevel*np.random.randn(pts2.shape[0],pts2.shape[1])
        # initial guess of camera params
        cam = Camera(f=50, c=np.array([[50,50]]).T, t=np.array([[0,0,0]]).T, R=n
        params_init = np.array([0,0,0,0,0,-2])
        cam.update_extrinsics(params_init)
        print("\n Initial Camera")
        print(cam)
        pts2init = cam.project(pts3)
        # now run calibration
        cam = calibratePose(pts3,pts2,cam,params_init)
        print("\n Final Camera")
        print(cam)
        pts2final = cam.project(pts3)
        # Plot the true, initial and final reprojections
```

```
# The final reprojection should be on top of the true image
#
plt.plot(pts2[0,:],pts2[1,:],'bo')
plt.plot(pts2init[0,:],pts2init[1,:],'r')
plt.plot(pts2final[0,:],pts2final[1,:],'k')
plt.show()

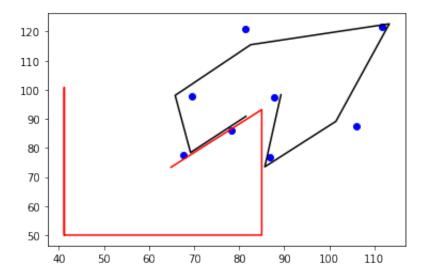
#
# Add some additional visualization here to show the points in 3D and if
# of cam_true and cam. You can either use a 3D plot or show multiple
# and side views)
#
```

```
True Camera
Camera:
 f=50
 c=[[50 50]]
R = [[1.]
               0.
                        0.
 [ 0.
            0.9848 - 0.1736
            0.1736 0.9848]]
 t = [[-1 -1 -2]]
 Initial Camera
Camera:
 f=50
 c=[[50 50]]
R=[[1. 0. 0.]]
 [0. 1. 0.]
 [0. 0. 1.]]
 t = [[0 \ 0 \ -2]]
Final Camera
Camera:
 f=50
 c=[[50 50]]
R=[[0.9999 0.0158 0.0017]
 [-0.0153 \quad 0.9841 \quad -0.177]
 [-0.0044 0.1769 0.9842]]
 t = [[-1.0441 - 0.9642 - 1.9988]]
120
110
100
 90
 80
 70
```



```
In [9]:
        # Now repeat the calibration but with a setting for params_init that i
        # in the optimization finding a poor solution (a bad local minima)
        #np.array([0,10,0,1,1,2])
        params_init = np.array([0,10,0,1,1,2])
        cam = Camera(f=50, c=np.array([[50,50]]).T, t=np.array([[0,0,0]]).T, R=n
        cam.update extrinsics(params init)
        print("\n Initial Camera")
        print(cam)
        pts2init = cam.project(pts3)
        # now run calibration
        cam = calibratePose(pts3,pts2,cam,params_init)
        print("\n Final Camera")
        print(cam)
        pts2final = cam.project(pts3)
        # Plot the true, initial and final reprojections
        # The final reprojection should be on top of the true image
        plt.plot(pts2[0,:],pts2[1,:],'bo')
        plt.plot(pts2init[0,:],pts2init[1,:],'r')
        plt.plot(pts2final[0,:],pts2final[1,:],'k')
        plt.show()
        #
        # Visualize the resulting bad solution.
                              atad at [1 1 ]] and ratata 10 dagrace
```

```
f=50
c=[[50 50]]
R=[[-0.5454 0.577 0.608]
[ 0.4535 -0.4069 0.793]
[ 0.7049 0.7082 -0.0397]]
t = [[2.1578 2.1879 2.8821]]
```



The camera located at [1,1,2] and rotate 10 degrees around the y axis

describe the failure mode here... how is the camera located and oriented for the bad local minima?

4. Calibration from real images

There is a provided set of calibration images (images of a planar checkerboard) along with stereo pair depicting an object. In order to calibrate the intrinsic camera parameters we will use the OpenCV library which includes functionality for automatically detecting corners of the checkerboard and estimating intrinsic parameters. To install OpenCV python libraries in your Anaconda environment. You can do this from the terminal via the command **conda install opency** or via the Anconda Navigator gui.

I have provide a standalone script **calibrate.py** which uses OpenCV to carry out calibration of the camera intrinsic parameters for a series of checkerboard images. Read through the provided script to understand the code and modify file paths as necessary in order to compute the intrinsic camera parameters from the set of provided calibration images.

4.1 Implementation

Fill in the code snippet below to carry out the following steps.

- 0. Run the **calibrate.py** script to estimate the intrinsic camera parameters.
- 1. Load in the intrinsic parameter calibration data saved by the script in *calibration.pickle*. Since our camera model assumes that the focal length is the same in the x and y axes, you can set your f to be the average of the two estimated by the script.
- Load in the test images Left.jpg and Right.jpg and use the cv2.findChessboardCorners function in order to automatically get the 2D coordinates of the corners in the image.
- 3. Specify the true 3D coordinates of the 6x8 grid of checkerboard corners. The squares are 2.8cm x 2.8cm.
- 4. Use your calibratePose function to estimate the R,t for each camera. You will likely need to experiment with selecting the initial parameters in order to get a good solution (e.g., translate so the cameras have positive z coordinates and rotate so they are looking down on the checkerboard).
- 5. Finally, as a consistency check, once you have the calibrated pose for each camera, you can use your triangulate function to estimate the 3D coordinates of the checkerboard corners based on the 2D points in the left and right camera. The re-triangulated points should be close to the specified true 3D coordinates.

In [10]: def triangulate(pts2L,camL,pts2R,camR):

Triangulate the set of points seen at location pts2L / pts2R in the corresponding pair of cameras. Return the 3D coordinates relative to the global coordinate system

```
Parameters
    pts2L : 2D numpy.array (dtype=float)
        Coordinates of N points stored in a array of shape (2,N) seen
    pts2R : 2D numpy.array (dtype=float)
        Coordinates of N points stored in a array of shape (2,N) seen
    camL : Camera
        The first "left" camera view
    camR : Camera
        The second "right" camera view
    Returns
    pts3 : 2D numpy.array (dtype=float)
        (3,N) array containing 3D coordinates of the points in global
    .....
    # Your code goes here. I recommend adding assert statements to cl
    # sizes of the inputs and outputs to make sure they are correct
\#qL, and qR
    a= pts2L.copy()
    a= a-camL.c
    a= np.divide(a,camL.f)
    b= pts2R.copy()
    b= b-camR.c
    b= np.divide(b,camR.f)
    one=np.ones((1,pts2L.shape[1]))
    qL= np.concatenate((a,one))
    qR= np.concatenate((b,one))
\#Ax=t
    A0=np.dot(camL.R,qL)
    A1=-np.dot(camR.R,qR)
    t=camR.t-camL.t
    z= np.zeros((2,pts2L[0].size))
      print(A0,A1)
    for i in range(A0.shape[1]):
        temp= np.dstack((A0[:,i],A1[:,i]))
        temp= temp.reshape(3,2)
```

```
# print(temp)
ztemp =np.linalg.lstsq(temp,t)
z[0,i]=ztemp[0][0]
z[1,i]=ztemp[0][1]
print(ztemp[0])

pL= z[0,:]*qL
pR=z[1,:]*qR

ptsL =np.dot(camL.R,pL)+ camL.t
ptsR=np.dot(camR.R,pR)+ camR.t
pts3=(ptsL+ptsR)/2
print(pts3[0:3,0])
return pts3
```

In [11]: import cv2 import pickle # import calibrate.py # calibrate # load in the intrinsic camera parameters from 'calibration.pickle' intrinsic_param = pickle.load(open('/Users/ooo/Documents/CS117/Assignm # print(intrinsic_param) fc= (intrinsic param['fx']+intrinsic param['fy'])/2 # create Camera objects representing the left and right cameras # use the known intrinsic parameters you loaded in. camL = Camera(f=fc,c=np.array([[intrinsic_param['cx'],intrinsic param] t=np.array([[0,0,0]]).T, R=makerotation(0,0,0))camR = Camera(f=fc,c=np.array([[intrinsic_param['cx'],intrinsic_param] t=np.array([[1,0,0]]).T, R=makerotation(0,0,0))# load in the left and right images and find the coordinates of # the chessboard corners using OpenCV imgL = plt.imread('calib1/Left.jpg') ret, cornersL = cv2.findChessboardCorners(imgL, (8,6), None) pts2L = cornersL.squeeze().T imgR = plt.imread('calib1/Right.jpg') ret, cornersR = cv2.findChessboardCorners(imgR, (8,6), None) pts2R = cornersR.squeeze().T # generate the known 3D point coordinates of points on the checkerboar pts3 = np.zeros((3,6*8))yy,xx = np.meshgrid(np.arange(8),np.arange(6))pts3[0,:] = 2.8*xx.reshape(1,-1)pts3[1,:] = 2.8*yy.reshape(1,-1)# Now use your calibratePose function to get the extrinsic parameters

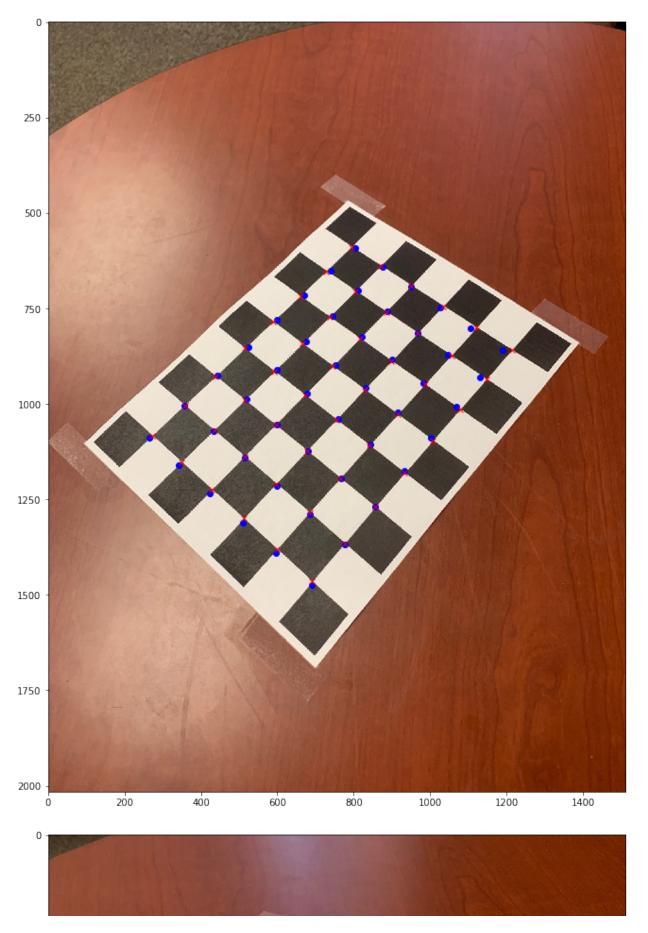
for the two images. You may need to experiment with the initializat

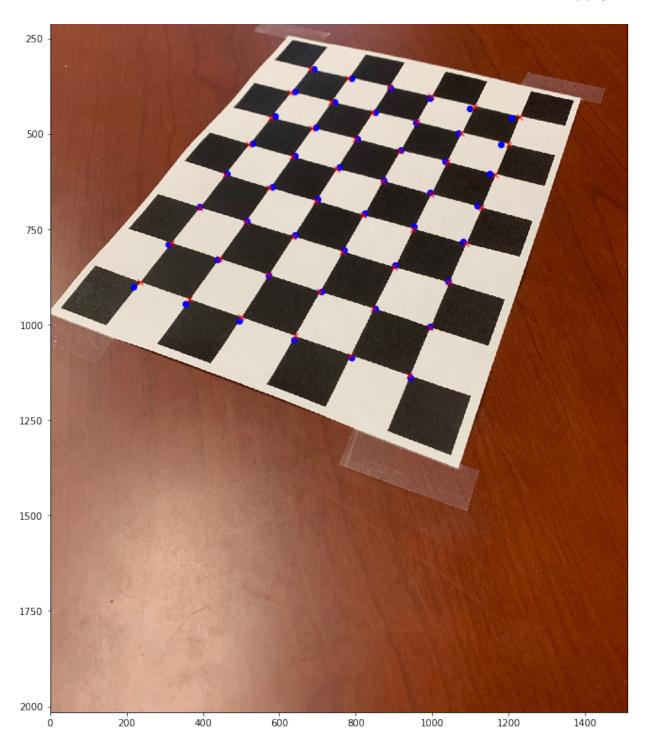
```
# IOI LHE LWO IMAGES. TOU MAY HEEU LO EXPERIMENT WITH THE INTITALIZAC
# in order to get a good result
params_init = np.array([0,0,0,0,0,-2])
camL = calibratePose(pts3,pts2L,camL,params init)
camR = calibratePose(pts3,pts2R,camR,params init)
print(camL)
print(camR)
# As a final test, triangulate the corners of the checkerboard to get
pts3r = triangulate(pts2L,camL,pts2R,camR)
# Display the reprojected points overlayed on the images to make
# sure they line up
plt.rcParams['figure.figsize']=[15,15]
pts2Lp = camL.project(pts3)
plt.imshow(imgL)
plt.plot(pts2Lp[0,:],pts2Lp[1,:],'bo')
plt.plot(pts2L[0,:],pts2L[1,:],'rx')
plt.show()
pts2Rp = camR.project(pts3)
plt.imshow(imgR)
plt.plot(pts2Rp[0,:],pts2Rp[1,:],'bo')
plt.plot(pts2R[0,:],pts2R[1,:],'rx')
plt.show()
Camera:
 f=1561.0139694324007
 c=[[1021.1465 755.8365]]
R = [[0.7928 \ 0.5479 \ -0.2671]
 0.6058 -0.66
                   0.44431
 [0.0671 - 0.514 - 0.8552]
 t = [[20.2533 - 0.3845 37.7861]]
Camera:
 f=1561.0139694324007
 c=[[1021.1465 755.8365]]
R = [[0.9506 \ 0.271 \ -0.1511]]
 [ 0.3029 -0.7042 0.6421]
 [ 0.0676 -0.6562 -0.7516]]
t = [[17.4715 -11.9475 24.0513]]
```

/Users/ooo/opt/anaconda3/lib/python3.7/site-packages/ipykernel_launch er.py:58: FutureWarning: `rcond` parameter will change to the default of machine precision times ``max(M, N)`` where M and N are the input matrix dimensions.

To use the future default and silence this warning we advise to pass `rcond=None`, to keep using the old, explicitly pass `rcond=-1`.

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The code below provides a visualization of the estimate camera positions relative to the checkerboard.

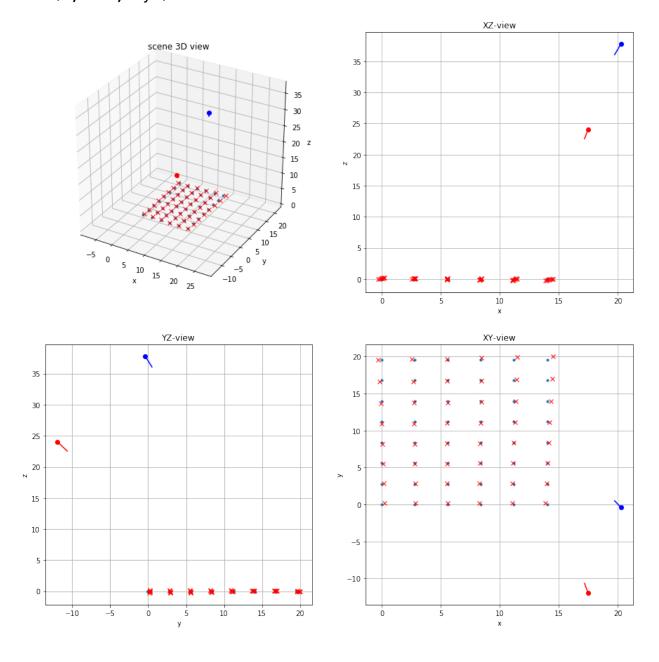
```
In [12]: # generate coordinates of a line segment running from the center
# of the camera to 3 units in front of the camera

lookL = np.hstack((camL.t,camL.t+camL.R @ np.array([[0,0,2]]).T))
lookR = np.hstack((camR.t,camR.t+camR.R @ np.array([[0,0,2]]).T))
```

```
# visualize the left and right image overlaid
fig = plt.figure()
ax = fig.add_subplot(2,2,1,projection='3d')
ax.plot(pts3[0,:],pts3[1,:],pts3[2,:],'.')
ax.plot(pts3r[0,:],pts3r[1,:],pts3r[2,:],'rx')
ax.plot(camR.t[0],camR.t[1],camR.t[2],'ro')
ax.plot(camL.t[0],camL.t[1],camL.t[2],'bo')
ax.plot(lookL[0,:],lookL[1,:],lookL[2,:],'b')
ax.plot(lookR[0,:],lookR[1,:],lookR[2,:],'r')
visutils.set_axes_equal_3d(ax)
visutils.label axes(ax)
plt.title('scene 3D view')
ax = fig.add_subplot(2,2,2)
ax.plot(pts3[0,:],pts3[2,:],'.')
ax.plot(pts3r[0,:],pts3r[2,:],'rx')
ax.plot(camR.t[0],camR.t[2],'ro')
ax.plot(camL.t[0],camL.t[2],'bo')
ax.plot(lookL[0,:],lookL[2,:],'b')
ax.plot(lookR[0,:],lookR[2,:],'r')
plt.title('XZ-view')
plt.grid()
plt.xlabel('x')
plt.ylabel('z')
ax = fig.add_subplot(2,2,3)
ax.plot(pts3[1,:],pts3[2,:],'.')
ax.plot(pts3r[1,:],pts3r[2,:],'rx')
ax.plot(camR.t[1],camR.t[2],'ro')
ax.plot(camL.t[1],camL.t[2],'bo')
ax.plot(lookL[1,:],lookL[2,:],'b')
ax.plot(lookR[1,:],lookR[2,:],'r')
plt.title('YZ-view')
plt.grid()
plt.xlabel('y')
plt.ylabel('z')
ax = fig.add_subplot(2,2,4)
ax.plot(pts3[0,:],pts3[1,:],'.')
ax.plot(pts3r[0,:],pts3r[1,:],'rx')
ax.plot(camR.t[0],camR.t[1],'ro')
ax.plot(camL.t[0],camL.t[1],'bo')
ax.plot(lookL[0,:],lookL[1,:],'b')
ax.plot(lookR[0,:],lookR[1,:],'r')
plt.title('XY-view')
plt.grid()
plt.xlabel('x')
plt.ylabel('y')
```

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Out[12]: Text(0, 0.5, 'y')



4.2 Recovered Pose

Using the provided calibration images, what are the recovered parameters for the left and right cameras? How far apart are the camera centers in centimeters (i.e. what is the baseline)?

18.168235

```
print("Transpose of two camera: ",camL.t,camR.t)
In [13]:
         print("Rotation of two camera: ",camL.R,camR.R)
         x=(camL_t-camR_t)**2
         print("The distance between two camera centers in centimeters is: ",ng
         # dis=np.linalg.lstsg(camL.t[:2]-camR.t[:2])
         # print(dis)
         Transpose of two camera:
                                   [[20.2533]
          [-0.3845]
          [37.7861]] [[ 17.4715]
          [-11.9475]
          [ 24.0513]]
         Rotation of two camera: [[ 0.7928  0.5479 -0.2671]
          [ 0.6058 - 0.66 ]
                            0.4443]
          [0.0671 - 0.514 - 0.8552] [[0.9506 0.271 - 0.1511]
          [ 0.3029 -0.7042 0.6421]
          [ 0.0676 -0.6562 -0.7516]]
```

The distance between two camera centers in centimeters is:

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4.3 Reconstruction Accuracy

Using the estimated camL and camR and the 2D point locations, triangulate to get 3D locations. What is the average error (in cm) for your recovered 3D locations of the grid corner points relative to their true coordinates? Where might this error be coming from?

The average error for recovered 3D locations of the grid corner point s is: 0.2375567703633784
This error may come from finding the local minimum or Triangulation.

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4.4 Focal Length

The checkerboard photos were taken with an iPhone Xs. Teardowns of this device reveal that the sensor is 5.6mm wide. Based on this and your recovered value for f, what was the focal length in millimeters? Explain how you computed this. Is the result you get a reasonable match to the published focal length of of 4.25mm?

In [15]:

print("The rate between the image and actual camera is: ",2016/5.6)
print("The focal length in millimeters is: ",camR.f/360)
print("The result is a reasonable match to the published focal length

The rate between the image and actual camera is: 360.0 The focal length in millimeters is: 4.336149915090002 The result is a reasonable match to the published focal length of 4.2 5mm since the different is 0.08 mm

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