

Homework 0

*Release Date: January 12, 2023**Due Date: January 20, 2023***Name:** Qihang Dai**PennKey:** ahgdyyc**PennID:** 78803164

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1 Written Questions

A1

1. False.
2. False.
3. False. $(AB)^T = B^T A^T$
4. True.

A2

1. rank = 2
2. min span is $[1, 2, 3]$ $[0, -3, -2]$

A3

1. $\det(A - \lambda I) = 0$ $\lambda_1 = 6$ $v_1 = [1, 1, 1]$, and two more eigenvalues
2. No. it have negative eigenvalue
3. $\lambda_1 = 6a + 1$ $v_1 = [1, 1, 1]$
4. $\lambda^2 = 36$

A4

1. w
2. $-2(y - w^T x) * w$
3. $-y * w * (\exp(-yw^T x)/(1 + \exp(-yw^T x)))$
4. $2Ax$

A5

1. $b = 0$
2. $\text{distance} = \frac{|w^T x_0 + b|}{|w|}$

A6

1. true
2. true
3. false
4. true

A7

1. No. the hessian is not positive semi-definite
2. x_1, x_2 and x_3 all equals to 0, or $x_1 = 0$ $x_2 = \pm\sqrt{\frac{1}{2}}$
3. zero

A8 solved by Bayes rule

$$P(\text{sunny}/\text{forecastSunny}) = \frac{P(\text{forecastSunny}/\text{sunny}) * P(\text{sunny})}{P(\text{forecastSunny})}$$

$$P(\text{sunny}) = 0.1, P(-\text{sunny}) = 0.9$$

$$P(-\text{for}/\text{sunny}) = 0.15, P(\text{for}/\text{sunny}) = 1 - P(-\text{for}/\text{sunny}) = 0.85, P(\text{for}/-s) = 0.05$$

$$P(\text{for}) = P(\text{for}/s) * P(s) + P(\text{for}/-s) * P(-s) = 0.85 * 0.1 + 0.05 * 0.9 = 0.13$$

$$P(\text{sunny}/\text{for}) = \frac{P(\text{for}/s) * P(s)}{P(\text{for})} = \frac{0.85 * 0.1}{0.13} = 0.65$$

A9

1. $a = \frac{1}{\sigma}$ $b = -\frac{\mu}{\sigma}$
2. $E[z^2] = \text{var}(z) + (E[z])^2 = \sigma^2 + \mu^2$
3. $N(\mu + \bar{\mu}, \sigma^2 + \bar{\sigma}^2)$

A10

1. $1/p$
2. independent event, so also p