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# Digital Components

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# Outline

## ■ Decoders, Multiplexers

## ■ Registers + Common sense design strategies

- ☐ Register with Parallel Load

- ☐ Shift Registers

- ☐ Bidirectional Shift Register with Parallel Load

## ■ Binary Counters

- ☐ Binary Counter with Parallel Load

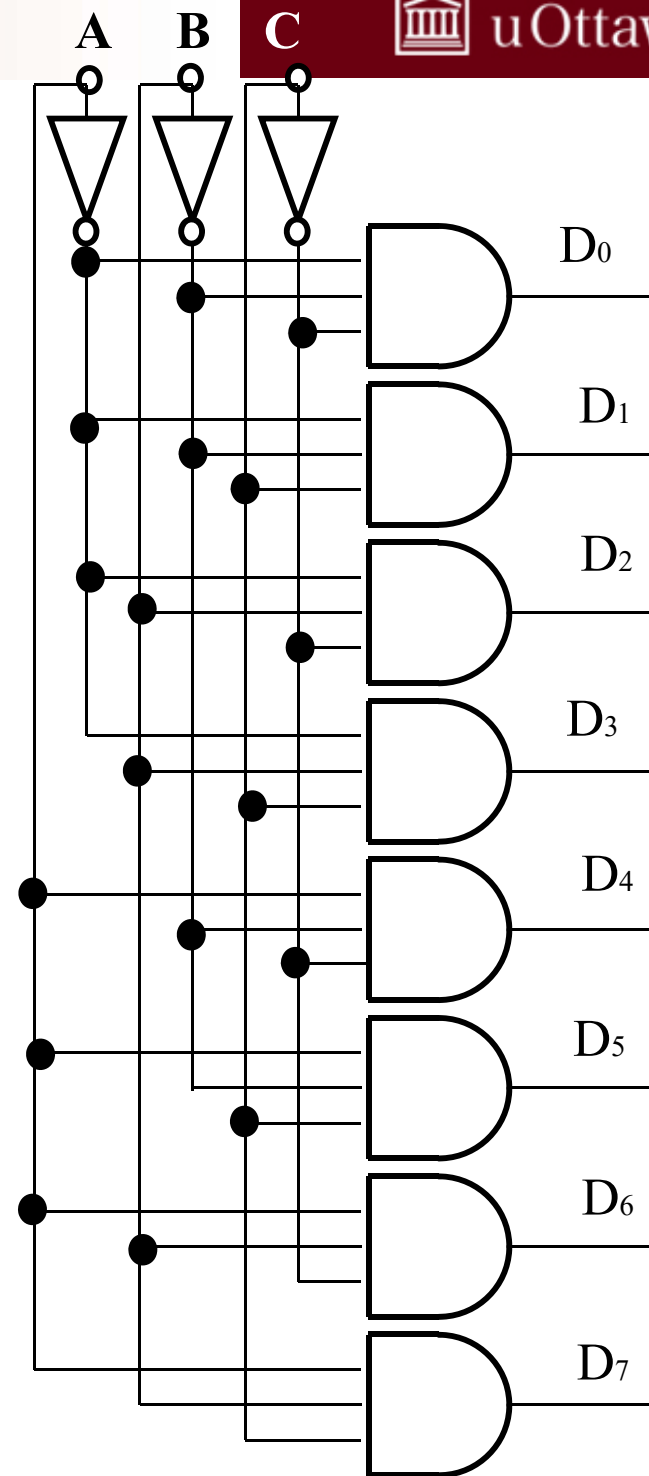
## ■ Multi-function Registers



## 3-to-8 Line Decoder

- A decoder is a combinational circuit that converts binary information from an  $n$ -bit input to a maximum of  $2^n$ -bit output.
- An  $n$ -input  $m$ -output decoder is called an  $n$ -to- $m$  line decoder, where  $m \leq 2^n$ .

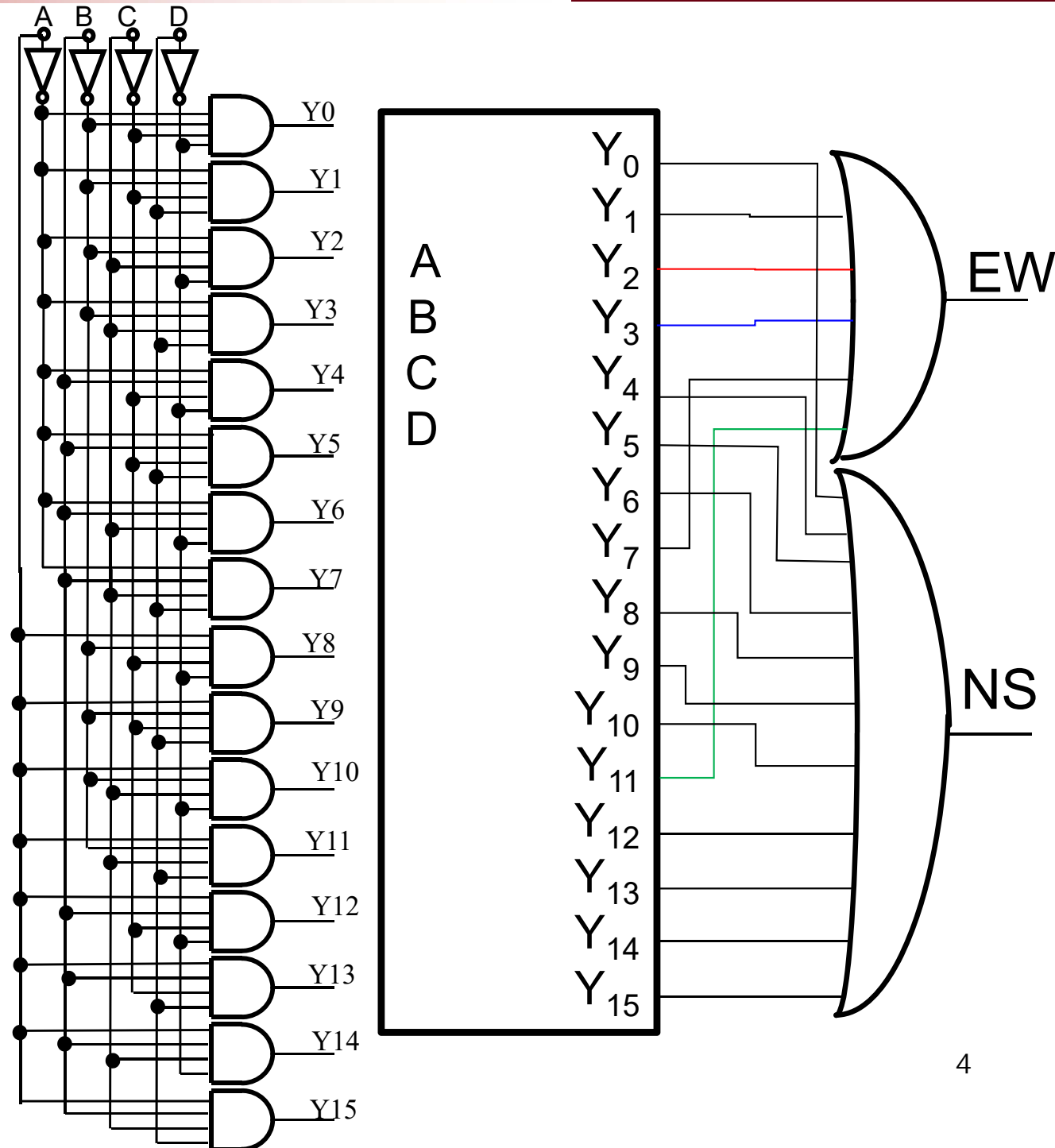
|     | A | B | C | D <sub>0</sub> | D <sub>1</sub> | D <sub>2</sub> | D <sub>3</sub> | D <sub>4</sub> | D <sub>5</sub> | D <sub>6</sub> | D <sub>7</sub> |
|-----|---|---|---|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
| (0) | 0 | 0 | 0 | 1              | 0              | 0              | 0              | 0              | 0              | 0              | 0              |
| (1) | 0 | 0 | 1 | 0              | 1              | 0              | 0              | 0              | 0              | 0              | 0              |
| (2) | 0 | 1 | 0 | 0              | 0              | 1              | 0              | 0              | 0              | 0              | 0              |
| (3) | 0 | 1 | 1 | 0              | 0              | 0              | 1              | 0              | 0              | 0              | 0              |
| (4) | 1 | 0 | 0 | 0              | 0              | 0              | 0              | 1              | 0              | 0              | 0              |
| (5) | 1 | 0 | 1 | 0              | 0              | 0              | 0              | 0              | 1              | 0              | 0              |
| (6) | 1 | 1 | 0 | 0              | 0              | 0              | 0              | 0              | 0              | 1              | 0              |
| (7) | 1 | 1 | 1 | 0              | 0              | 0              | 0              | 0              | 0              | 0              | 1              |



Implement the following functions using a decoder and OR gates:

$$EW = \Sigma (1, 2, 3, 7, 11)$$

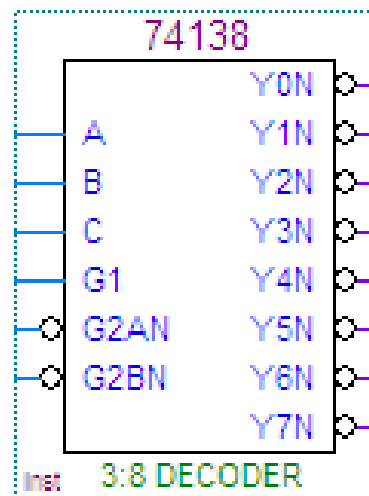
$$NS = \Sigma (0, 4, 5, 6, 9, 10, 12, 13, 14, 15)$$



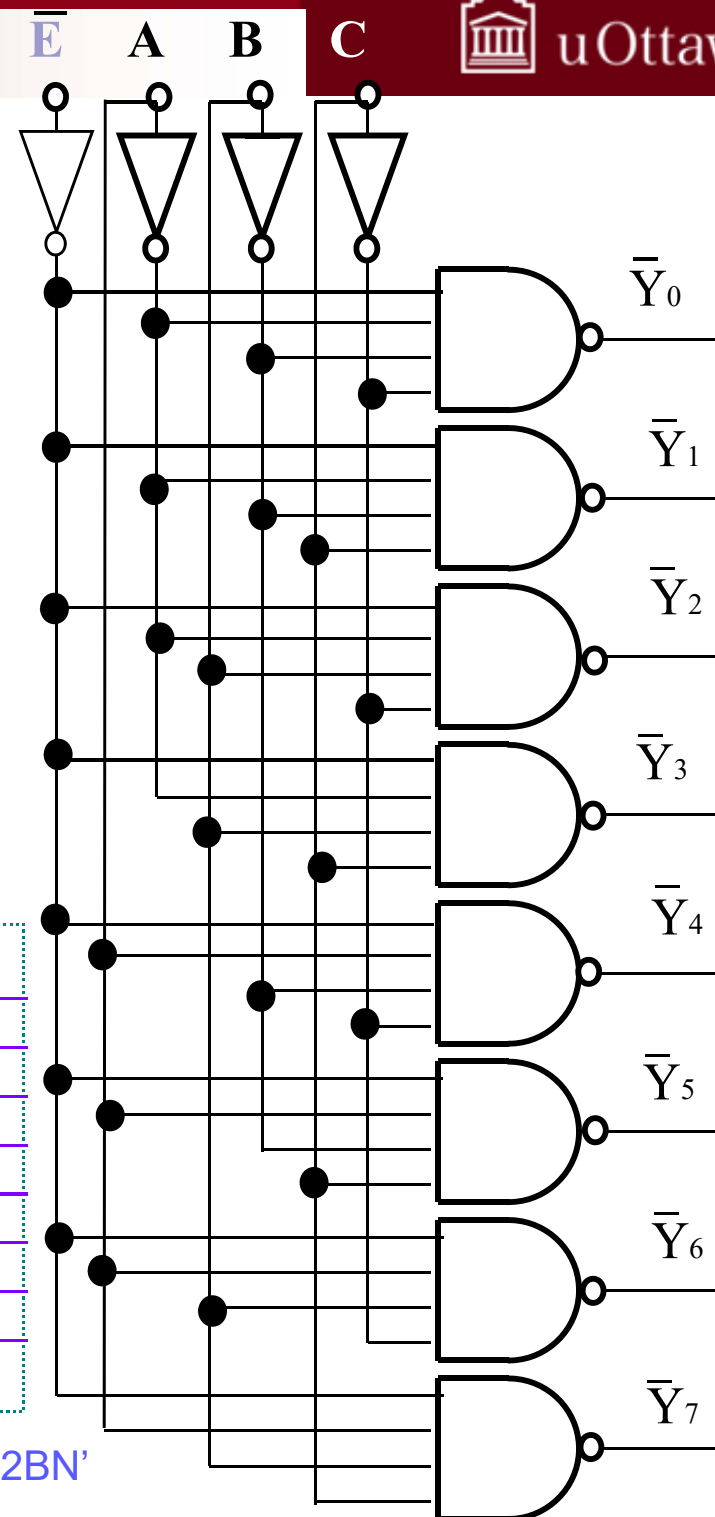
# ★ 3-to-8 Decoder (74 138)

- The Enable bit, E, enables (when  $E = 1$ , i.e.  $\bar{E}=0$ ) or disables (when  $E = 0$ , i.e.  $\bar{E}=1$ ) the functionality of the decoder.
- When the decoder is disabled ( $E = 0$ ), all the output pins of the decoder are reset to 0:

|     | A | B | C | $\bar{E}$ | $\bar{Y}_0$ | $\bar{Y}_1$ | $\bar{Y}_2$ | $\bar{Y}_3$ | $\bar{Y}_4$ | $\bar{Y}_5$ | $\bar{Y}_6$ | $\bar{Y}_7$ |
|-----|---|---|---|-----------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
|     | x | x | x | 1         | 1           | 1           | 1           | 1           | 1           | 1           | 1           | 1           |
| (0) | 0 | 0 | 0 | 0         | 0           | 1           | 1           | 1           | 1           | 1           | 1           | 1           |
| (1) | 0 | 0 | 1 | 0         | 1           | 0           | 1           | 1           | 1           | 1           | 1           | 1           |
| (2) | 0 | 1 | 0 | 0         | 1           | 1           | 0           | 1           | 1           | 1           | 1           | 1           |
| (3) | 0 | 1 | 1 | 0         | 1           | 1           | 1           | 0           | 1           | 1           | 1           | 1           |
| (4) | 1 | 0 | 0 | 0         | 1           | 1           | 1           | 1           | 0           | 1           | 1           | 1           |
| (5) | 1 | 0 | 1 | 0         | 1           | 1           | 1           | 1           | 1           | 0           | 1           | 1           |
| (6) | 1 | 1 | 0 | 0         | 1           | 1           | 1           | 1           | 1           | 1           | 0           | 1           |
| (7) | 1 | 1 | 1 | 0         | 1           | 1           | 1           | 1           | 1           | 1           | 1           | 0           |



$$E = G1 \cdot G2AN' \cdot G2BN'$$



# Encoders

- An **encoder** is a combinational circuit that performs the opposite operation of a decoder.
- A  $2^n$  -bit input  $n$ -bit output encoder generates the binary code corresponding to the input value.

| Inputs                            | Outputs       |
|-----------------------------------|---------------|
| $D_7 D_6 D_5 D_4 D_3 D_2 D_1 D_0$ | $A_2 A_1 A_0$ |
| 0 0 0 0 0 0 0 1                   | 0 0 0         |
| 0 0 0 0 0 0 1 0                   | 0 0 1         |
| 0 0 0 0 0 1 0 0                   | 0 1 0         |
| 0 0 0 0 1 0 0 0                   | 0 1 1         |
| 0 0 0 1 0 0 0 0                   | 1 0 0         |
| 0 0 1 0 0 0 0 0                   | 1 0 1         |
| 0 1 0 0 0 0 0 0                   | 1 1 0         |
| 1 0 0 0 0 0 0 0                   | 1 1 1         |

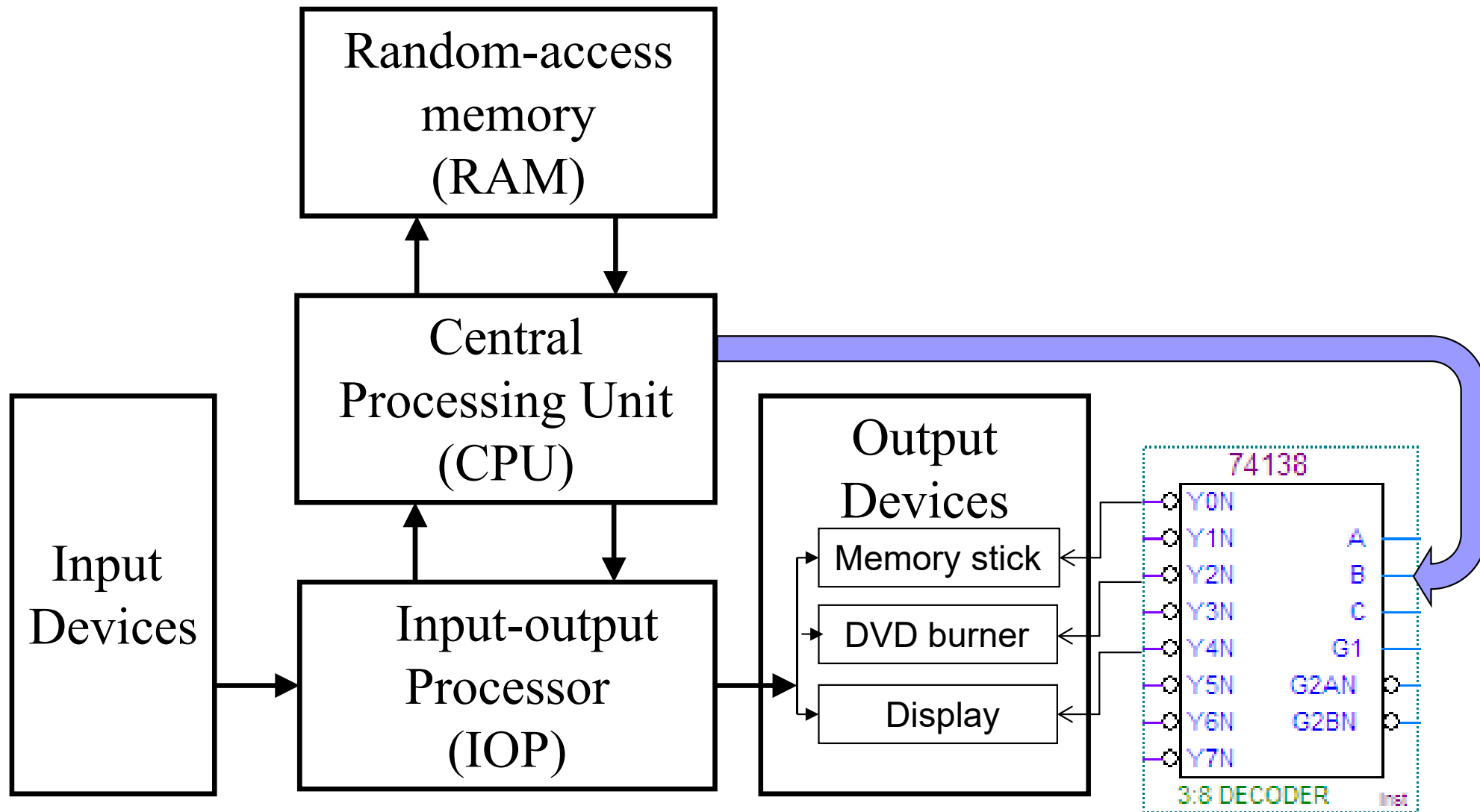
Truth Table for 8-to-3 Encoder

When all inputs are 0's but  $D_3 = 1$ , for instance, the output =  $A_2 A_1 A_0 = 011$ , which is the binary code for 3.

$$A_0 = D_1 + D_3 + D_5 + D_7$$

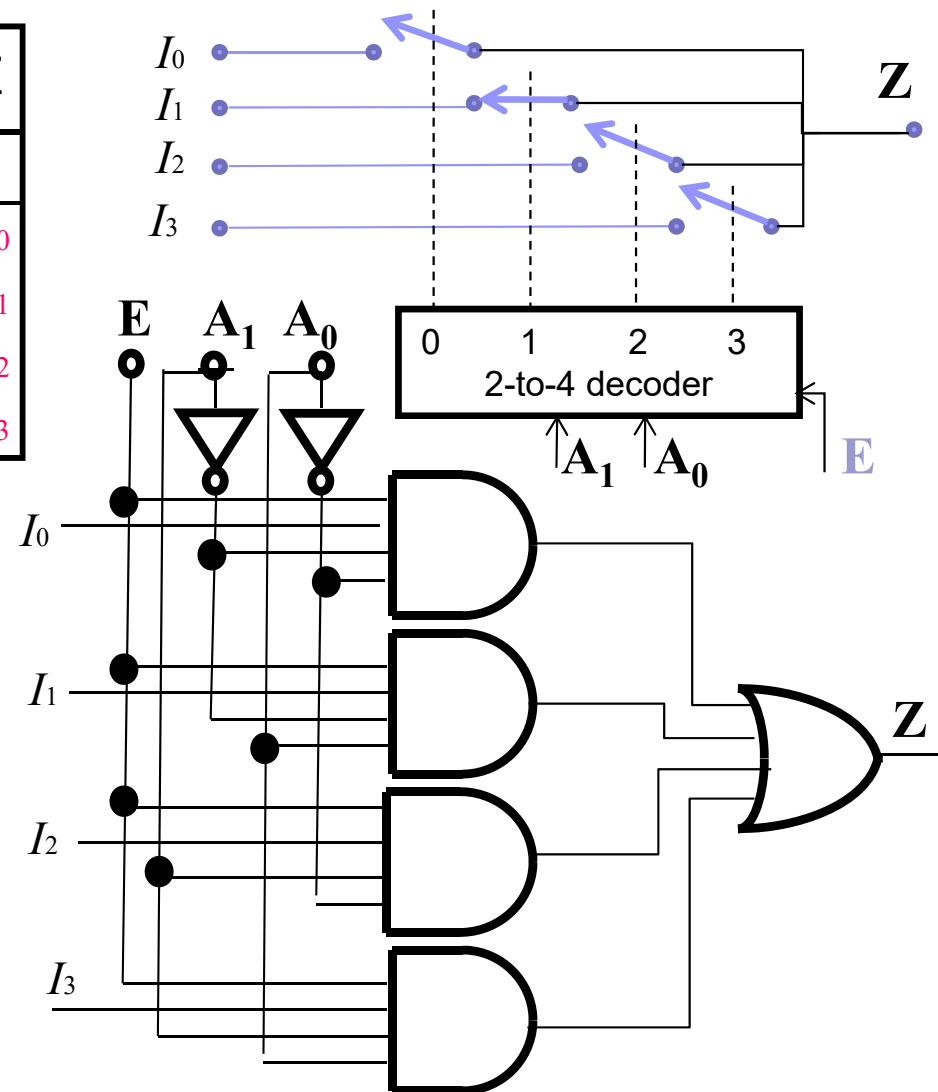
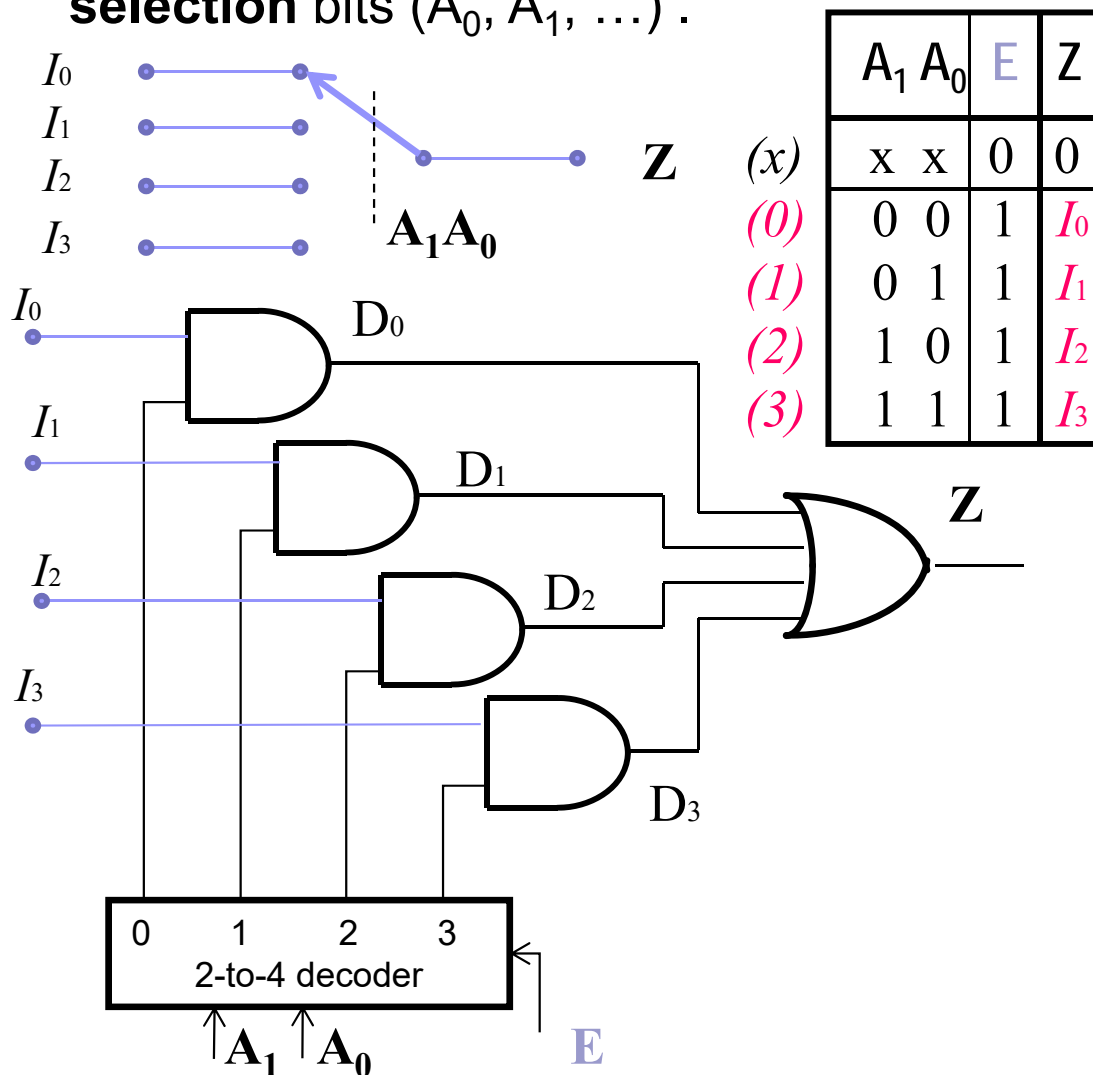
$$A_1 = D_2 + D_3 + D_6 + D_7$$

$$A_2 = D_4 + D_5 + D_6 + D_7$$

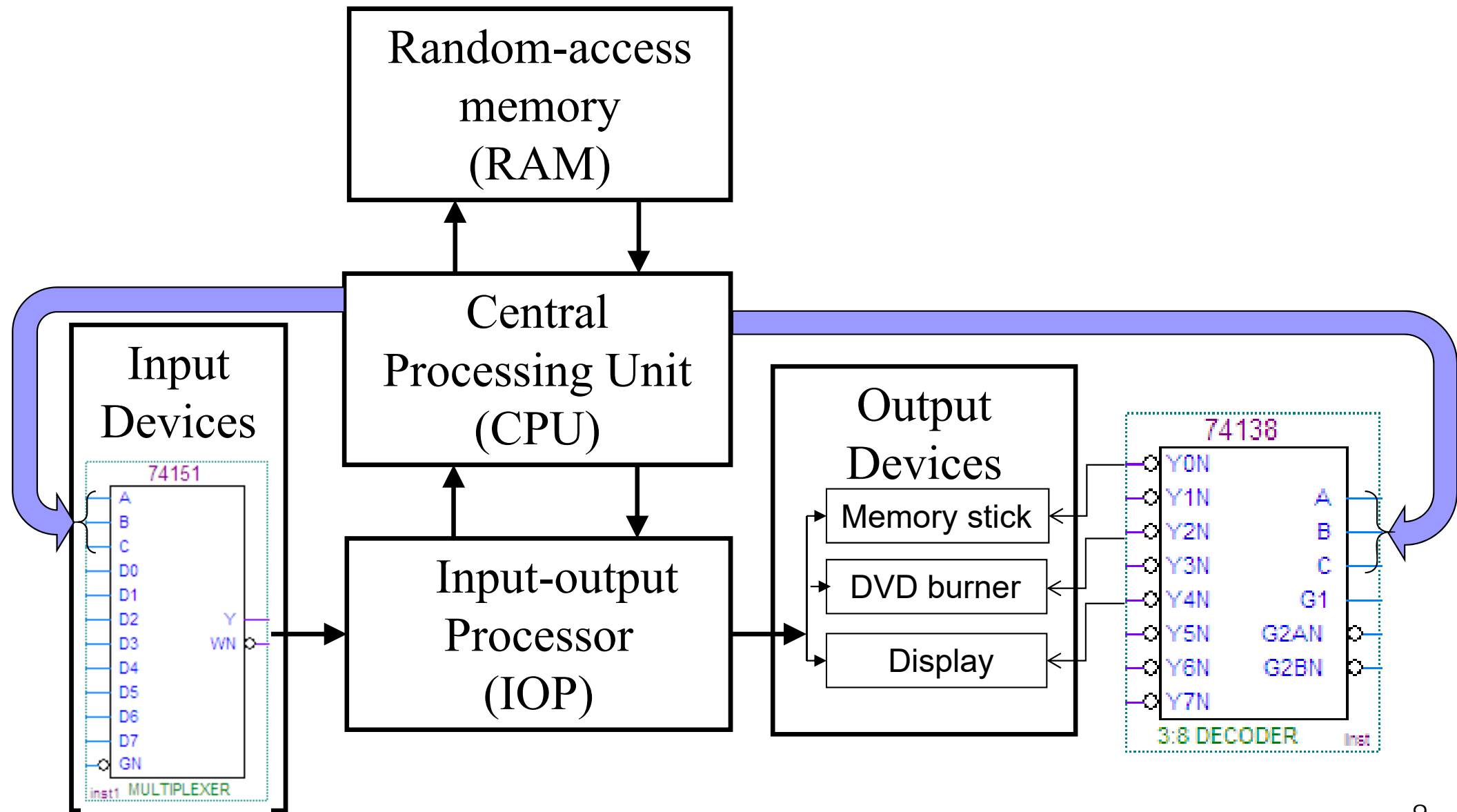


# 4-to-1-Line Multiplexer

- A **multiplexer** is a combinational circuit that receives binary information from one of the  $2^n$  input data bits ( $I_0, I_1, \dots$ ) and directs it to a single output line ( $Z$ ).
- The selection of a particular input data bit is determined by a set of  $n$  input **selection** bits ( $A_0, A_1, \dots$ ).







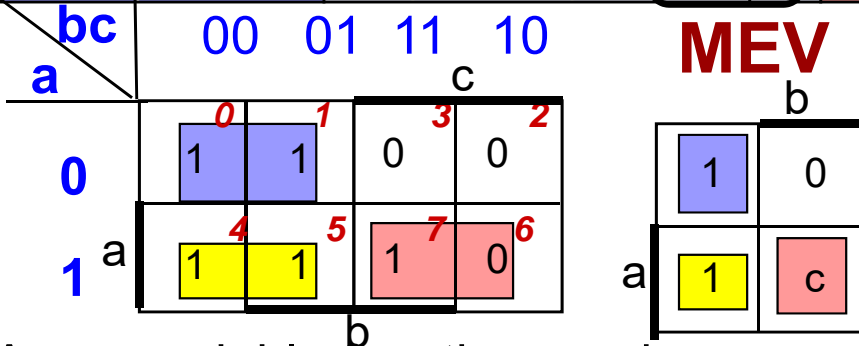
# Logic Function Implementation with MUX

## Map-Entered Variables (MEV)

Implement  $F = \Sigma (0,1, 4, 5, 7)$  with MUX

| Decimal | minterm  | Binary variables |   |         | Output |
|---------|----------|------------------|---|---------|--------|
| MEV     | Standard | a                | b | c (MEV) | F      |
| 0       | 0        | 0                | 0 | 0       | 1      |
| 0       | 1        | 0                | 0 | 1       | 1      |
| 1       | 2        | 0                | 1 | 0       | 0      |
| 1       | 3        | 0                | 1 | 1       | 0      |
| 2       | 4        | 1                | 0 | 0       | 1      |
| 2       | 5        | 1                | 0 | 1       | 1      |
| 3       | 6        | 1                | 1 | 0       | 0      |
| 3       | 7        | 1                | 1 | 1       | 1      |

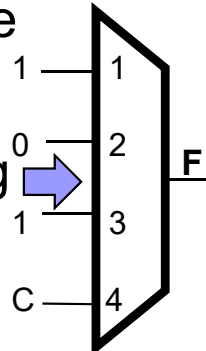
- 1.If the output variable is 0 for both standard minterms covered by a MEV square, then a 0 is written in that MEV map square.
- 2.If the output variable is a 1 for both standard minterms covered by a MEV map square, then a 1 is written in that MEV square.
- 3.If, for minterms covered by a MEV map square, the output variable (F) has the same value as the MEV, then the MEV is written into MEV map square.



- 4.If, for standard minterms covered by a MEV map square, the output and ME variables are complements, write the MEV complement into the MEV map square.
- 5.If, for standard minterms covered by a MEV map square, the output variable is a don't care term, write "x" into the MEV map square.
- 6.If, for standard minterms covered by a MEV map square, the output variable is a don't care term in one case and a 0 in the other, write 0 in the appropriate square.

Any  $n$  variable function can be implemented with

1.  $(2^n)$ -to-1 MUX directly;
2.  $(2^{n-1})$ -to-1 MUX by applying MEV;
3.  $(2^{n-k})$ -to-1 MUX + gates by using func. decomposition



# MEV K-maps Minimization

Use K-maps to minimize

$$F = \Sigma (3,7,11,12,13,14,15,16,18) + d(24,25,26,27,28,29,30,31).$$

To find the simplified function from a MEV K-map, follow these steps:

1. Determine the **EPI's** consisting of only 1's along with any *don't care* terms that may exist (i.e., cover the 1's in the K-map).
2. Consider the 1's as don't care terms once step 1 is completed, because all of the 1's have been previously covered.
3. Group all identical **MEV** terms with 1's or don't care terms to maximize the MEV EPI size, i.e., sequentially take only one MEV = 1 at a time, why all the others are considered 0, and derive the sum of product terms that cover that MEV=1. Determine the MEV EPI's by reading the K-map in the normal fashion. Then AND the MEV variable or expression with the remaining map variables.

$$F = bc + a'de + ac'e'$$

| MEV | m  | a | b | c | d | e | F | MEV | m  | a | b | c | d | e | F |
|-----|----|---|---|---|---|---|---|-----|----|---|---|---|---|---|---|
| 0   | 0  | 0 | 0 | 0 | 0 | 0 | 0 | 8   | 16 | 1 | 0 | 0 | 0 | 0 | 1 |
|     | 1  | 0 | 0 | 0 | 0 | 1 | 0 |     | 17 | 1 | 0 | 0 | 0 | 1 | 0 |
| 1   | 2  | 0 | 0 | 0 | 1 | 0 | 0 | 9   | 18 | 1 | 0 | 0 | 1 | 0 | 1 |
|     | 3  | 0 | 0 | 0 | 1 | 1 | 1 |     | 19 | 1 | 0 | 0 | 1 | 1 | 0 |
| 2   | 4  | 0 | 0 | 1 | 0 | 0 | 0 | 10  | 20 | 1 | 0 | 1 | 0 | 0 | 0 |
|     | 5  | 0 | 0 | 1 | 0 | 1 | 0 |     | 21 | 1 | 0 | 1 | 0 | 1 | 0 |
| 3   | 6  | 0 | 0 | 1 | 1 | 0 | 0 | 11  | 22 | 1 | 0 | 1 | 1 | 0 | 0 |
|     | 7  | 0 | 0 | 1 | 1 | 1 | 1 |     | 23 | 1 | 0 | 1 | 1 | 1 | 0 |
| 4   | 8  | 0 | 1 | 0 | 0 | 0 | 0 | 12  | 24 | 1 | 1 | 0 | 0 | 0 | x |
|     | 9  | 0 | 1 | 0 | 0 | 1 | 0 |     | 25 | 1 | 1 | 0 | 0 | 1 | x |
| 5   | 10 | 0 | 1 | 0 | 1 | 0 | 0 | 13  | 26 | 1 | 1 | 0 | 1 | 0 | x |
|     | 11 | 0 | 1 | 0 | 1 | 1 | 1 |     | 27 | 1 | 1 | 0 | 1 | 1 | x |
| 6   | 12 | 0 | 1 | 1 | 0 | 0 | 1 | 14  | 28 | 1 | 1 | 1 | 0 | 0 | x |
|     | 13 | 0 | 1 | 1 | 0 | 1 | 1 |     | 29 | 1 | 1 | 1 | 0 | 1 | x |
| 7   | 14 | 0 | 1 | 1 | 1 | 0 | 1 | 15  | 30 | 1 | 1 | 1 | 1 | 0 | x |
|     | 15 | 0 | 1 | 1 | 1 | 1 | 1 |     | 31 | 1 | 1 | 1 | 1 | 1 | x |

| cd \ ab | 00              | 01              | 11              | 10              |
|---------|-----------------|-----------------|-----------------|-----------------|
| 00      | 0 <sup>0</sup>  | e <sup>1</sup>  | e <sup>3</sup>  | 0 <sup>2</sup>  |
| 01      | 0 <sup>4</sup>  | e <sup>5</sup>  | 1* <sup>7</sup> | 1* <sup>6</sup> |
| 11      | x <sup>12</sup> | x <sup>13</sup> | x <sup>15</sup> | x <sup>14</sup> |
| 10      | e' <sup>8</sup> | e' <sup>9</sup> | 0 <sup>11</sup> | 0 <sup>10</sup> |

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- Decoders, Multiplexers
- **Registers + Common sense design strategies**
  - **Register with Parallel Load**
  - Shift Registers
  - Bidirectional Shift Register with Parallel Load
- Binary Counters
  - Binary Counter with Parallel Load
- Multi-function Registers

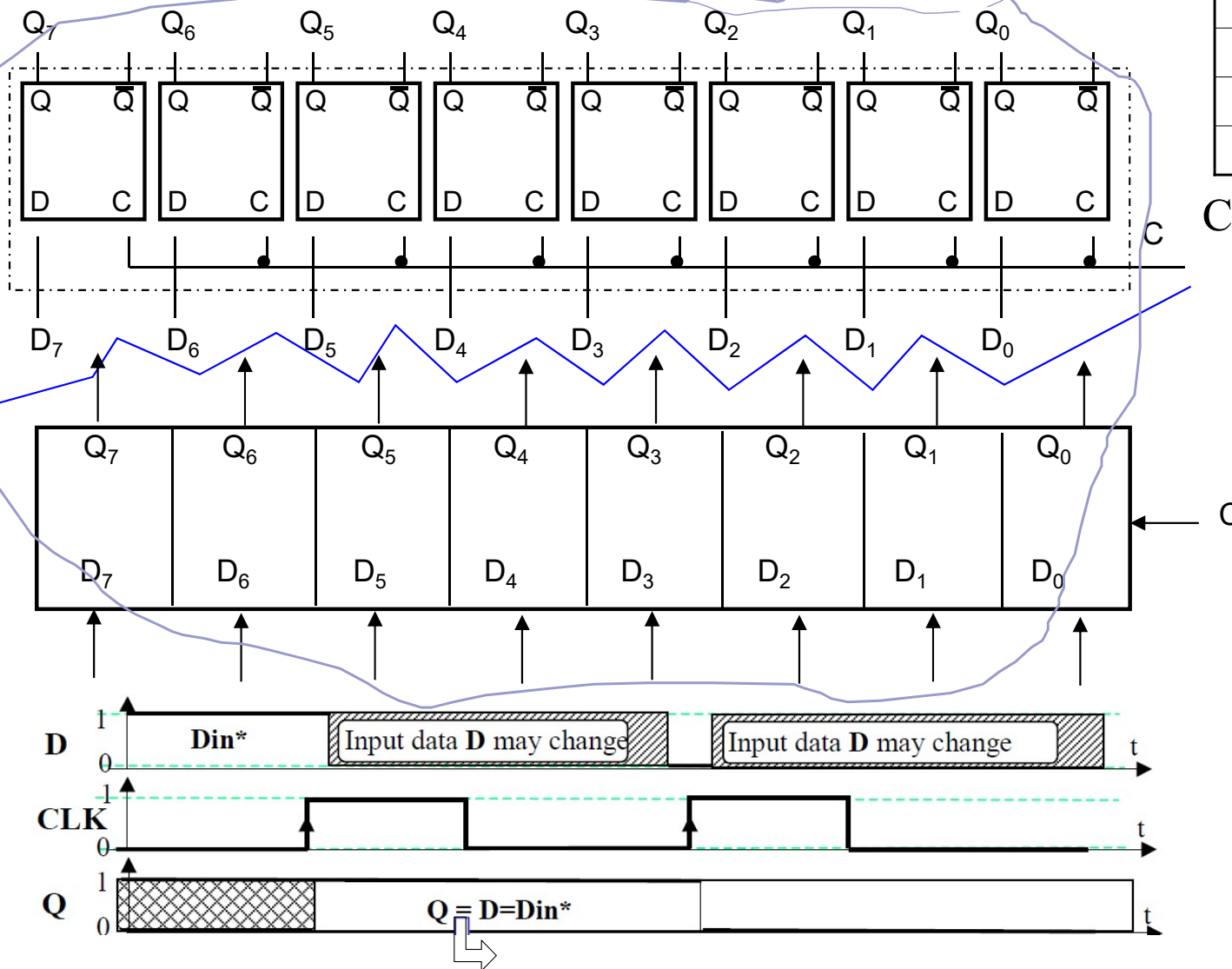
# Registers

Positive-Edge  
-Triggered  
D Flip-Flop

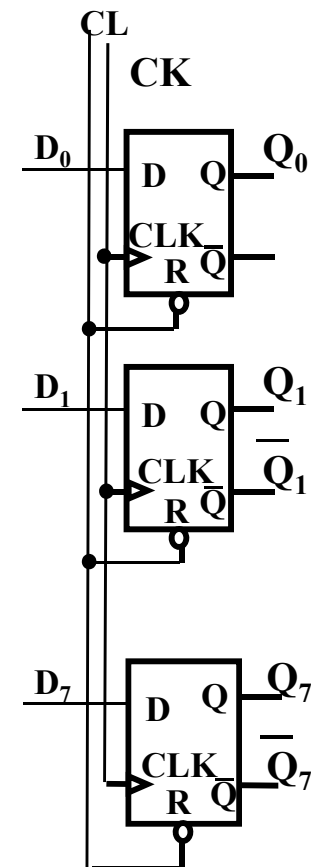
Characteristic Equation:  
 $Q_{n+1} = D_n$

| $D_n$ | $Q_n$ | $Q_{n+1}$ |
|-------|-------|-----------|
| 0     | 0     | 0         |
| 0     | 1     | 0         |
| 1     | 0     | 1         |
| 1     | 1     | 1         |

Characteristic Table



The state of the flip-flop's output Q copies input D when the positive edge of the clock CLK occurs

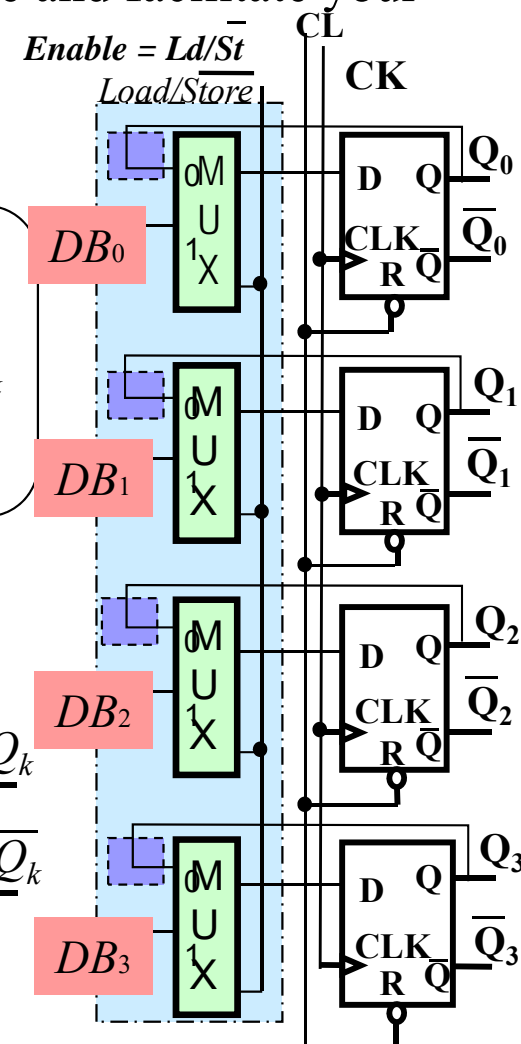
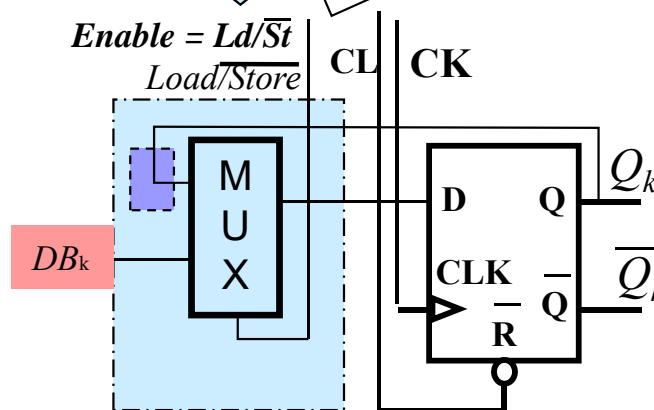
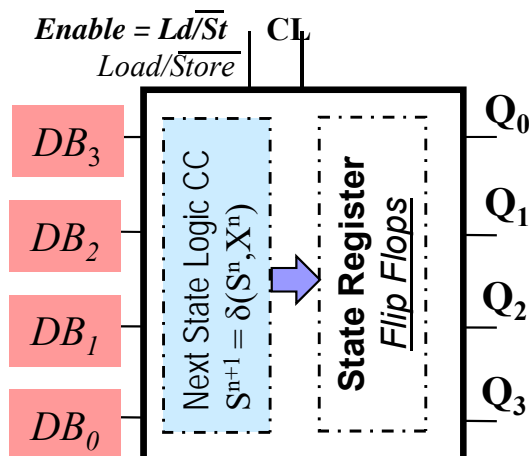
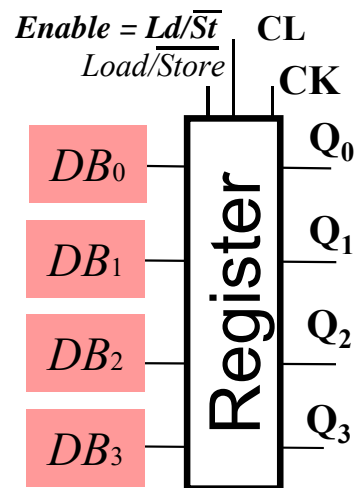
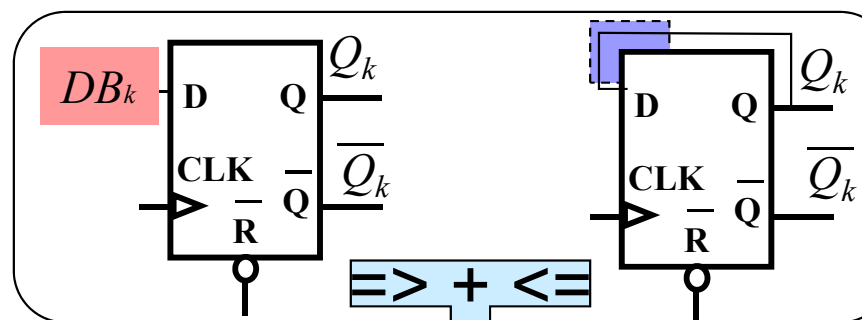


# Common sense design strategies

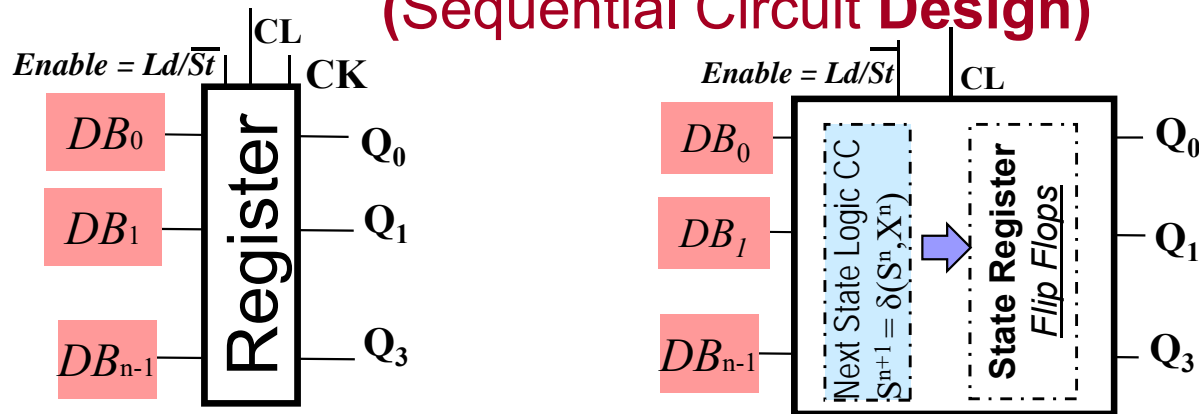
- Focus on one bit first. In many cases the rest would have a similar pattern.
- Try to reason with your own words. Do the computation with “words” first.
- See if you can define the “rules” governing the logic circuit, and put them in your own words.
- The above design strategies may save you a significant amount of time and facilitate your task as a designer. However, they may not be trivial in all the cases.

## Register with Parallel Load

| <i>Enable</i> | $Q_k^{n+1}$ | <i>Function</i> |
|---------------|-------------|-----------------|
| 0             | $Q_k^n$     | Store           |
| 1             | $DB_k$      | Load            |



## Register with Parallel Load (Sequential Circuit Design)



- When the load input  $Ld / \overline{St} = 1$ , at the **positive clock pulse transition time**, the data in the four input bits  $DB_0$  is transferred into the register; otherwise
- when load input  $Ld / \overline{St} = 0$ , the register output bits maintain their values.

### Steps 1,2

State / Transition Table  
(MEV format)

$$Enable = Ld / \overline{St}$$

| $Enable$              | $Q_k^{n+1}$ | $Function$ |
|-----------------------|-------------|------------|
| 0 ( $\overline{St}$ ) | $Q_k^n$     | Store      |
| 1 ( $Ld$ )            | $DB_k$      | Load       |

The transition function ( $\delta$ ) of the Parallel Register:

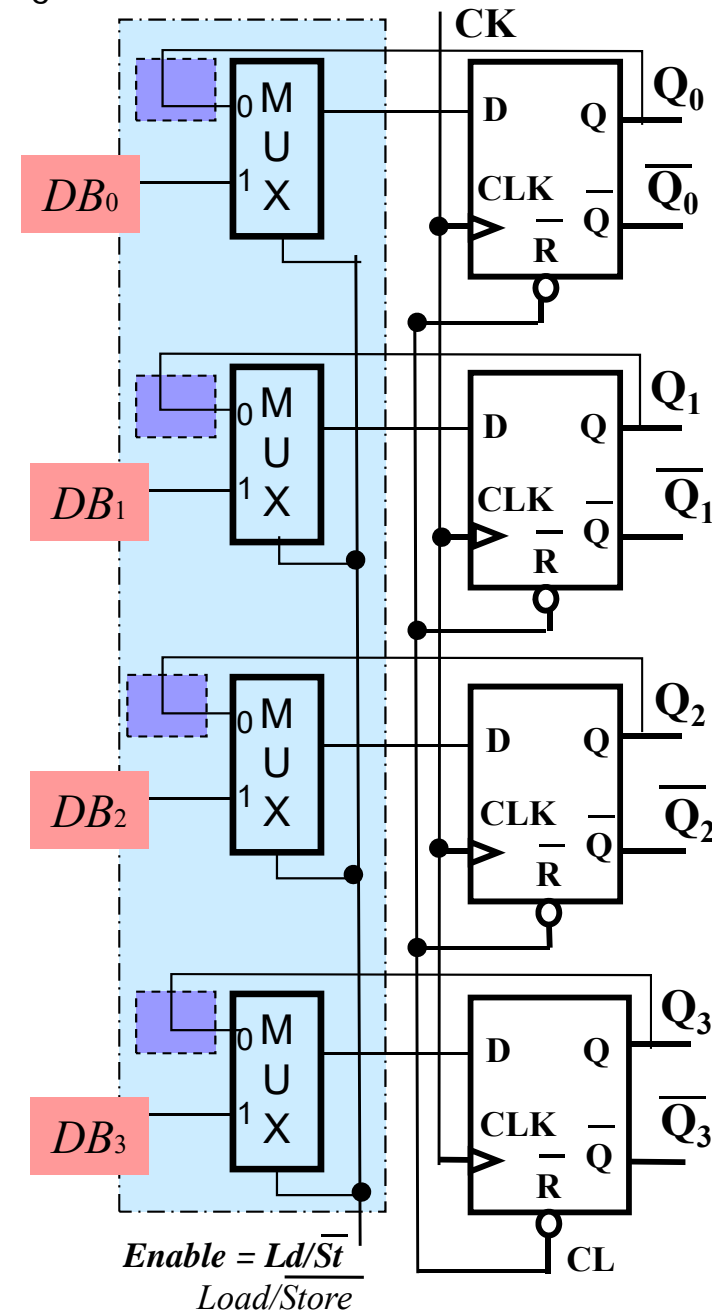
$$Q_k(n+1) = Ld DB_k + \overline{St} Q_k(n); k = \{0, 1, 2, 3\}$$

$$= Enable DB_k + \overline{Enable} Q_k$$

**Step 3** If the Parallel Register is implemented with D-FF's, its excitation equation gives:  $D(n) = Q_k(n+1)$

**Step 4**  $\Rightarrow D_k = Enable DB_k + \overline{Enable} Q_k; k = \{0, 1, 2, 3\}$

**Step 5** Equations  $D_k$  can be implemented with gates or MUX-es as shown below:



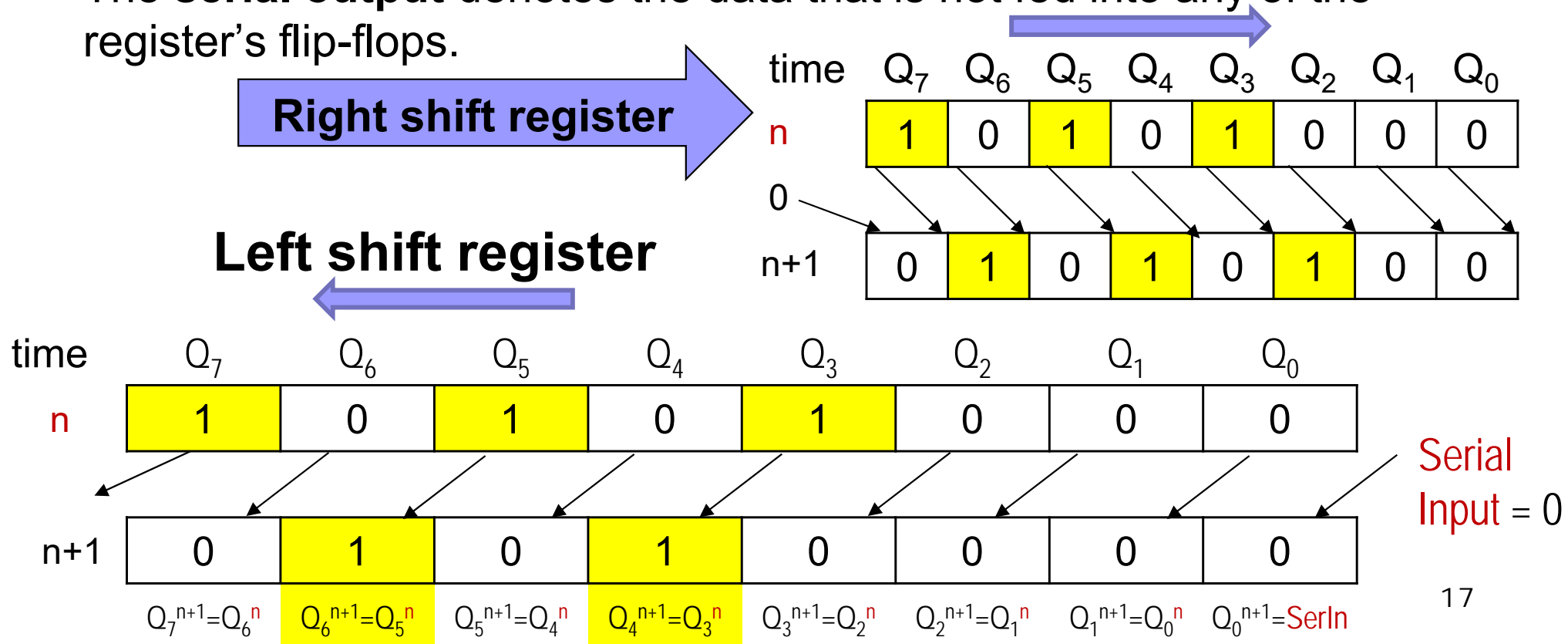
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  - ☐ **Shift Registers**
  - ☐ Bidirectional Shift Register with Parallel Load
- Binary Counters
  - ☐ Binary Counter with Parallel Load



# Shift Registers

- A **shift register** is a register that is capable of shifting its binary information in one or both directions.
- The logical configuration of a shift register consists of a chain of cascaded flip-flops.
- The **serial input** denotes the external input fed into the shift register.
- The **serial output** denotes the data that is not fed into any of the register's flip-flops.

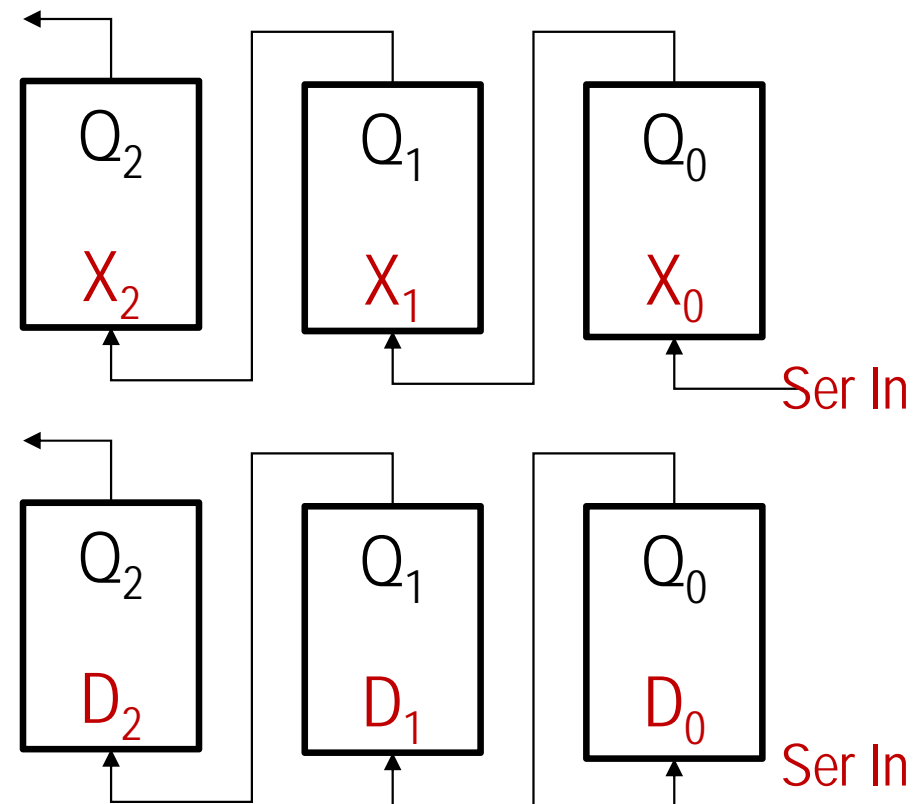
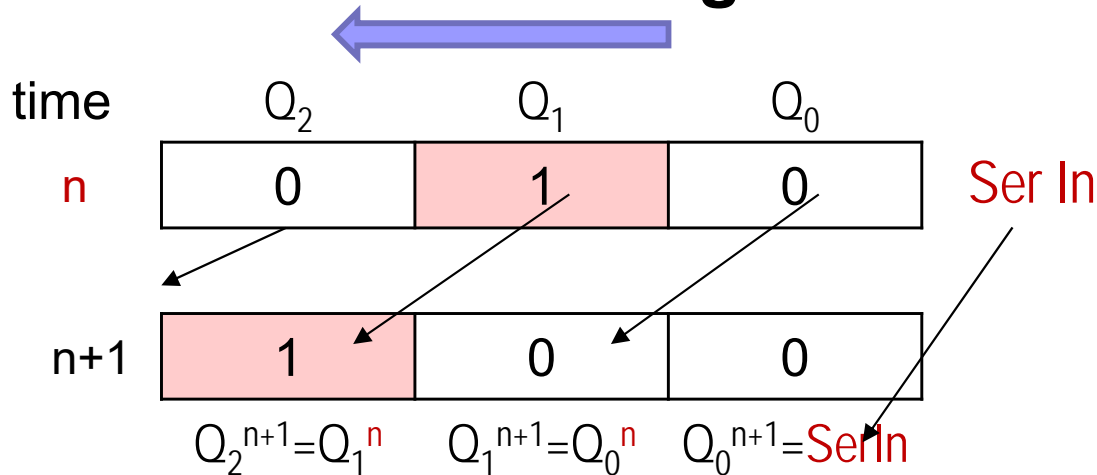


# Left Shift Register

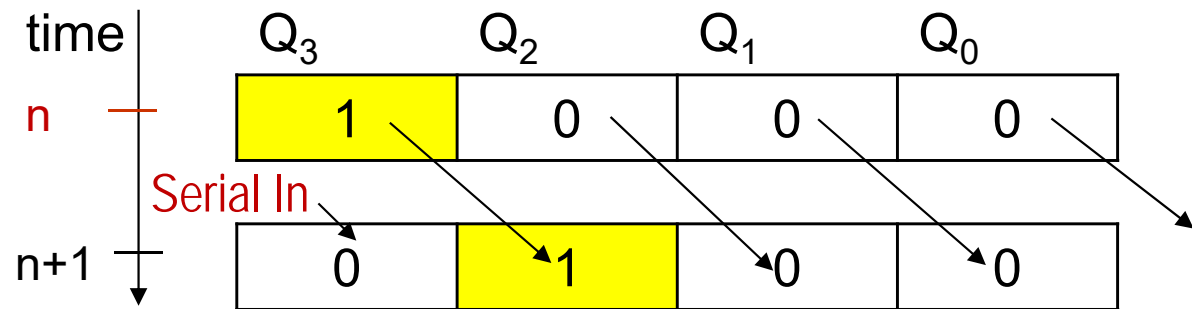
The Next State ( $S^{n+1}$ ) of a sequential circuit is a function ( $\delta$ ) of its **input** ( $X$ ) and of its present state ( $S^n$ ):  $S^{n+1} = \delta(X, S^n)$ .

For left shift, the **input**  $X_i$  of each  $FF_i$  is connected to the  $FF_{i-1}$  output from its right  $X_i = Q_{i-1} \Rightarrow Q_i^{n+1} = \delta(Q_{i-1}^n, Q_i^n); i = \{0, 1, 2, 3\}$

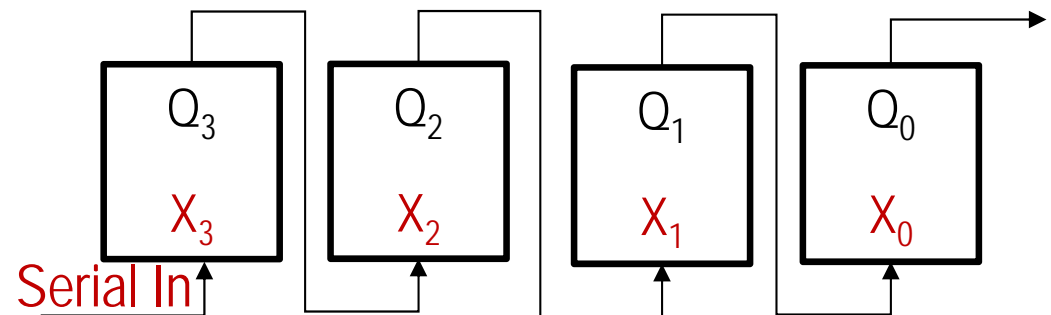
## Left shift register



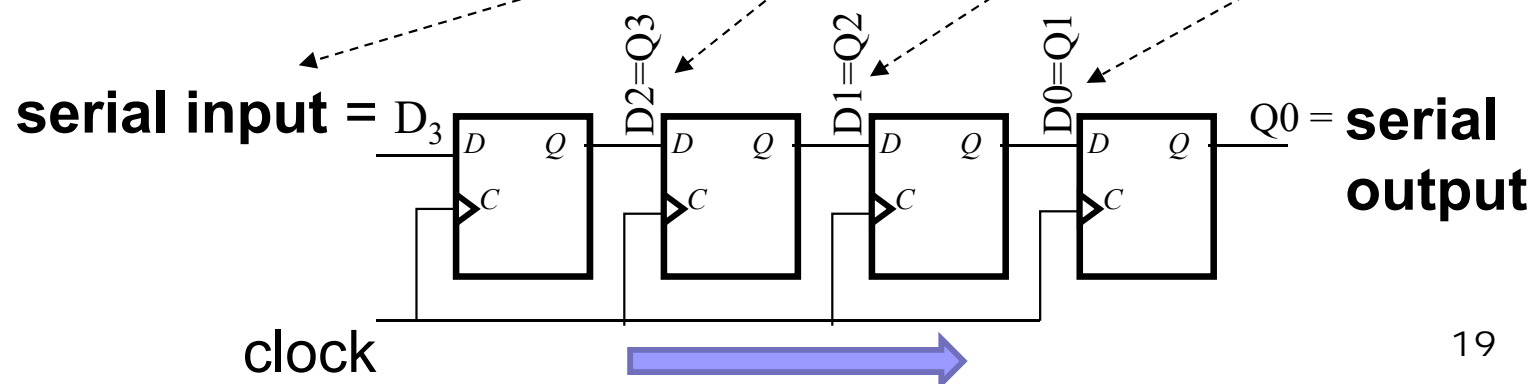
# Right Shift Register



$$Q_3^{n+1} = \text{SerIn} \quad Q_2^{n+1} = Q_3^n \quad Q_1^{n+1} = Q_2^n \quad Q_0^{n+1} = Q_1^n$$



$$X_3 = \text{SerIn} \quad X_2 = Q_3 \quad X_1 = Q_2 \quad X_0 = Q_1$$



- When implementing with D FF's:  $Q^{n+1} = D$
- So, the output Q of each flip-flop is connected to the input D of the next flip-flop

## Right Shift Register

Serial Input = 0

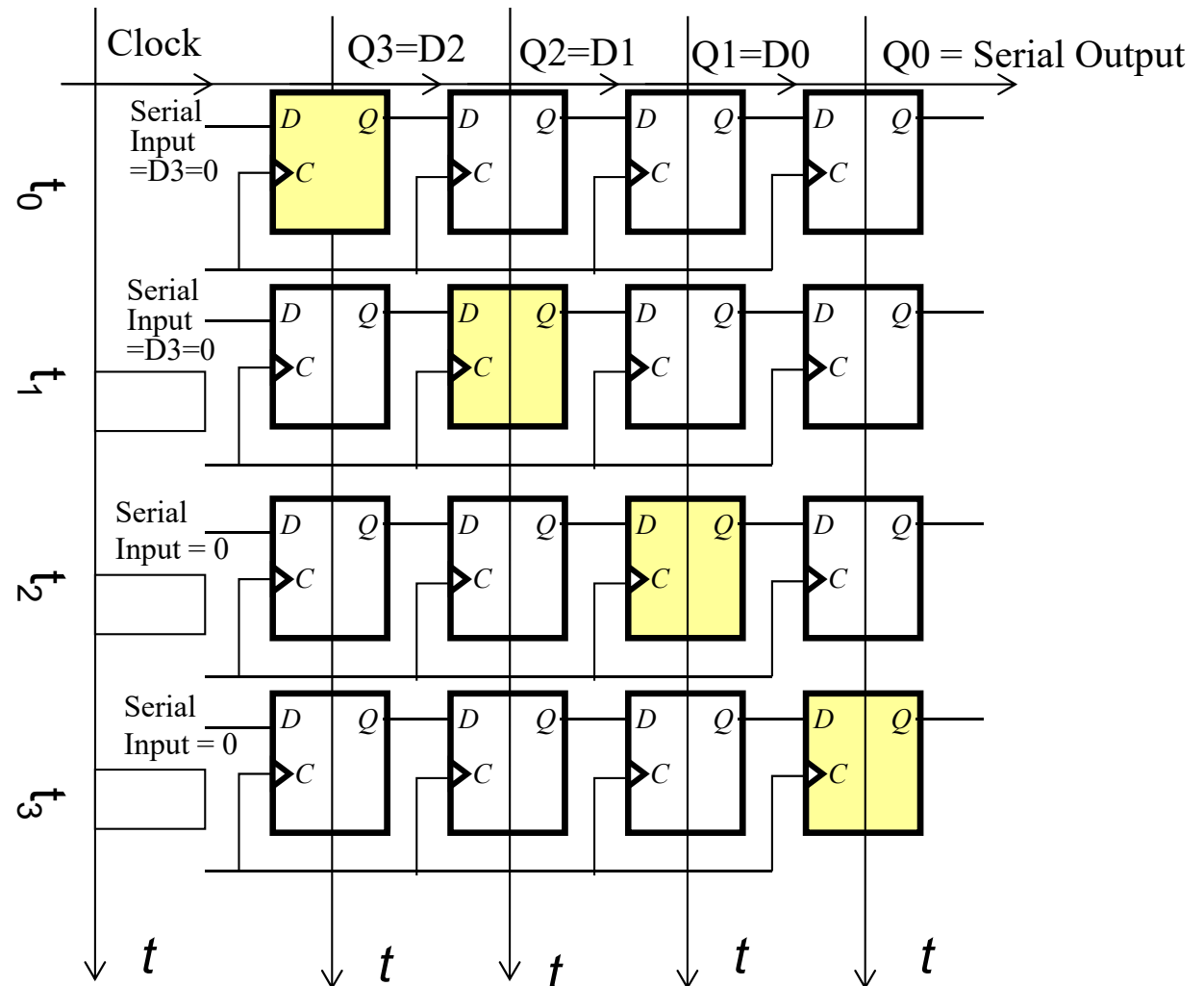
Initial State:

$t_0 : Q_3 Q_2 Q_1 Q_0 = 1000$

$t_1 : Q_3 Q_2 Q_1 Q_0 = 0100$

$t_2 : Q_3 Q_2 Q_1 Q_0 = 0010$

$t_3 : Q_3 Q_2 Q_1 Q_0 = 0001$



# Right Shift Register

Serial Input = 1

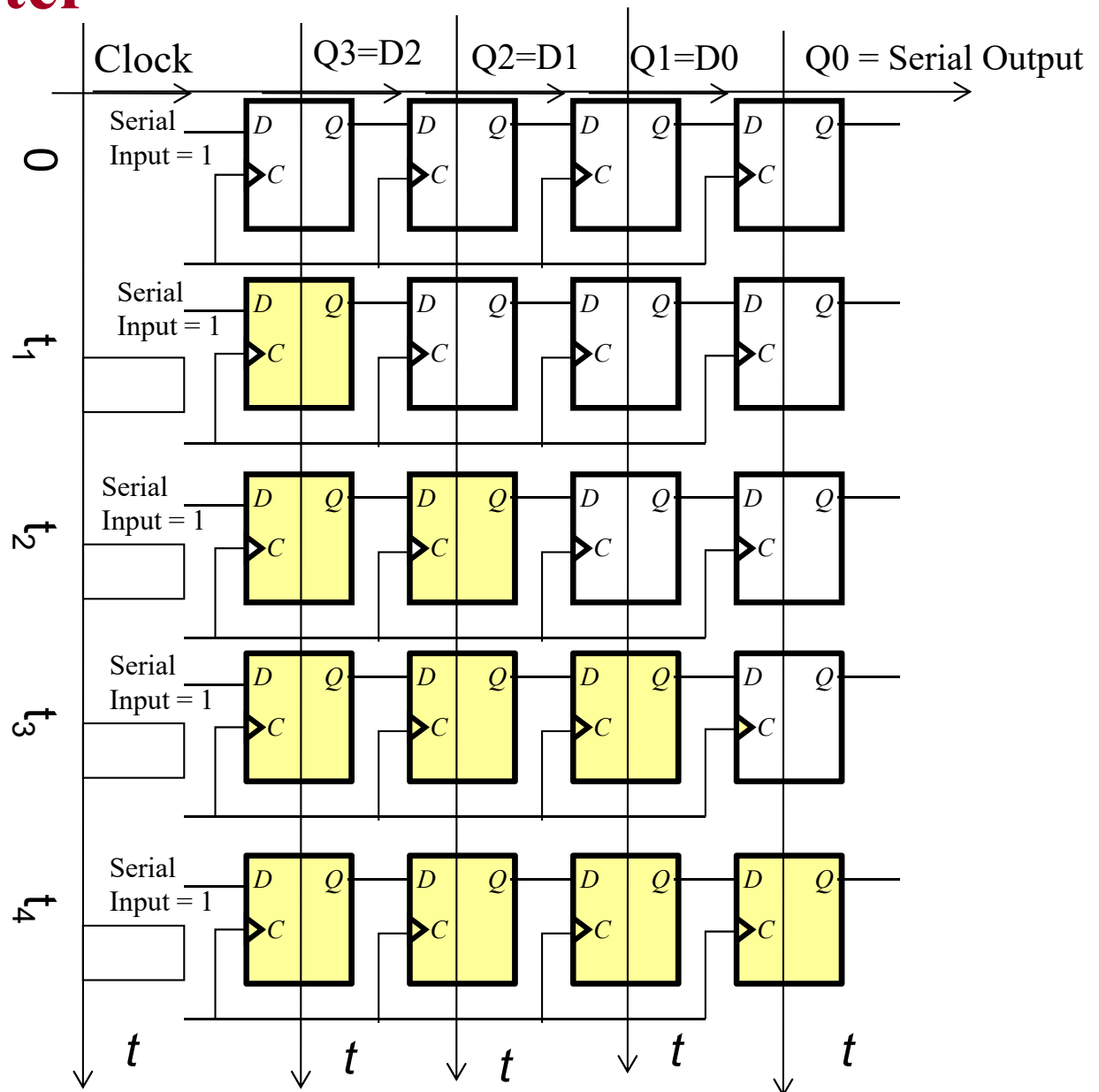
Initial State: 0000

$t_1 : Q_3 Q_2 Q_1 Q_0 = 1000$

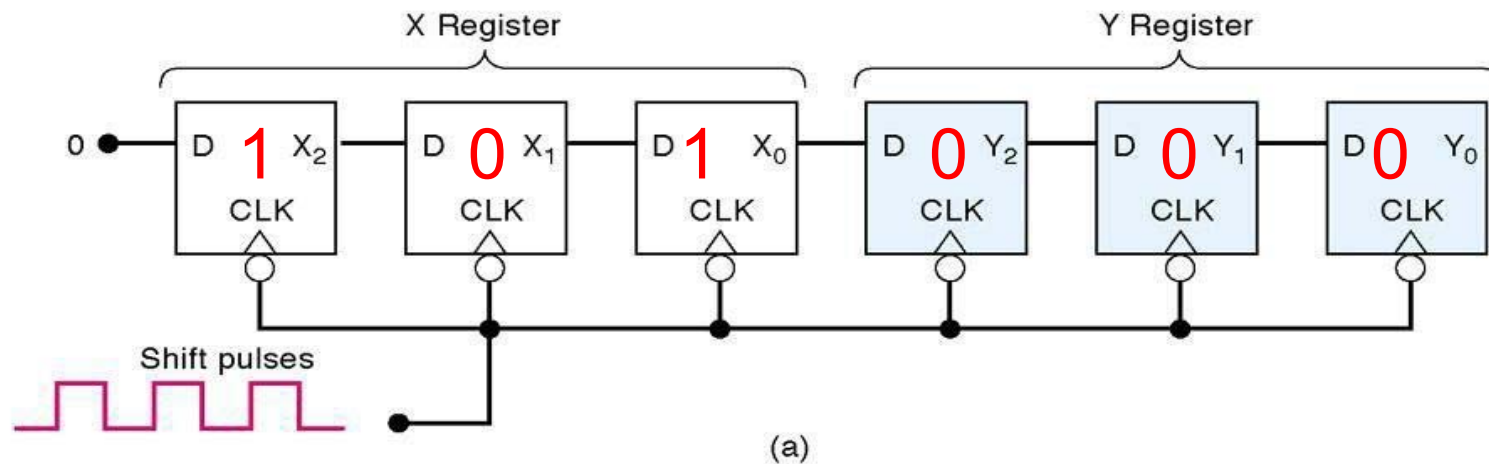
$t_2 : Q_3 Q_2 Q_1 Q_0 = 1100$

$t_3 : Q_3 Q_2 Q_1 Q_0 = 1110$

$t_4 : Q_3 Q_2 Q_1 Q_0 = 1111$



## Serial transfer from register X to register Y



| $X_2$ | $X_1$ | $X_0$ | $Y_2$ | $Y_1$ | $Y_0$ |                       |
|-------|-------|-------|-------|-------|-------|-----------------------|
| 1     | 0     | 1     | 0     | 0     | 0     | Before pulses applied |
| 0     | 1     | 0     | 1     | 0     | 0     | After first pulse     |
| 0     | 0     | 1     | 0     | 1     | 0     | After second pulse    |
| 0     | 0     | 0     | 1     | 0     | 1     | After third pulse     |

Diagram (b) shows the state of the registers after each shift pulse. The values in the X Register shift right, and the values in the Y Register shift right. The final state after three pulses is  $X_2=0$ ,  $X_1=0$ ,  $X_0=0$  and  $Y_2=1$ ,  $Y_1=0$ ,  $Y_0=1$ .

# FPGA Programmable Logic Element (LE)

## Truth Table

| ABC   | f(A,B,C) |
|-------|----------|
| 0 0 0 | f(0,0,0) |
| 0 0 1 | f(0,0,1) |
| 0 1 0 | f(0,1,0) |
| 0 1 1 | f(0,1,1) |
| 1 0 0 | f(1,0,0) |
| 1 0 1 | f(1,0,1) |
| 1 1 0 | f(1,1,0) |
| 1 1 1 | f(1,1,1) |

## Programmable Logic Element Memory

| ABC |                           |
|-----|---------------------------|
|     | f(0,0,0) = M <sub>0</sub> |
| 1   | f(0,0,1) = M <sub>1</sub> |
| 2   | f(0,1,0) = M <sub>2</sub> |
| 3   | f(0,1,1) = M <sub>3</sub> |
| 4   | f(1,0,0) = M <sub>4</sub> |
| 5   | f(1,0,1) = M <sub>5</sub> |
| 6   | f(1,1,0) = M <sub>6</sub> |
| 7   | f(1,1,1) = M <sub>7</sub> |

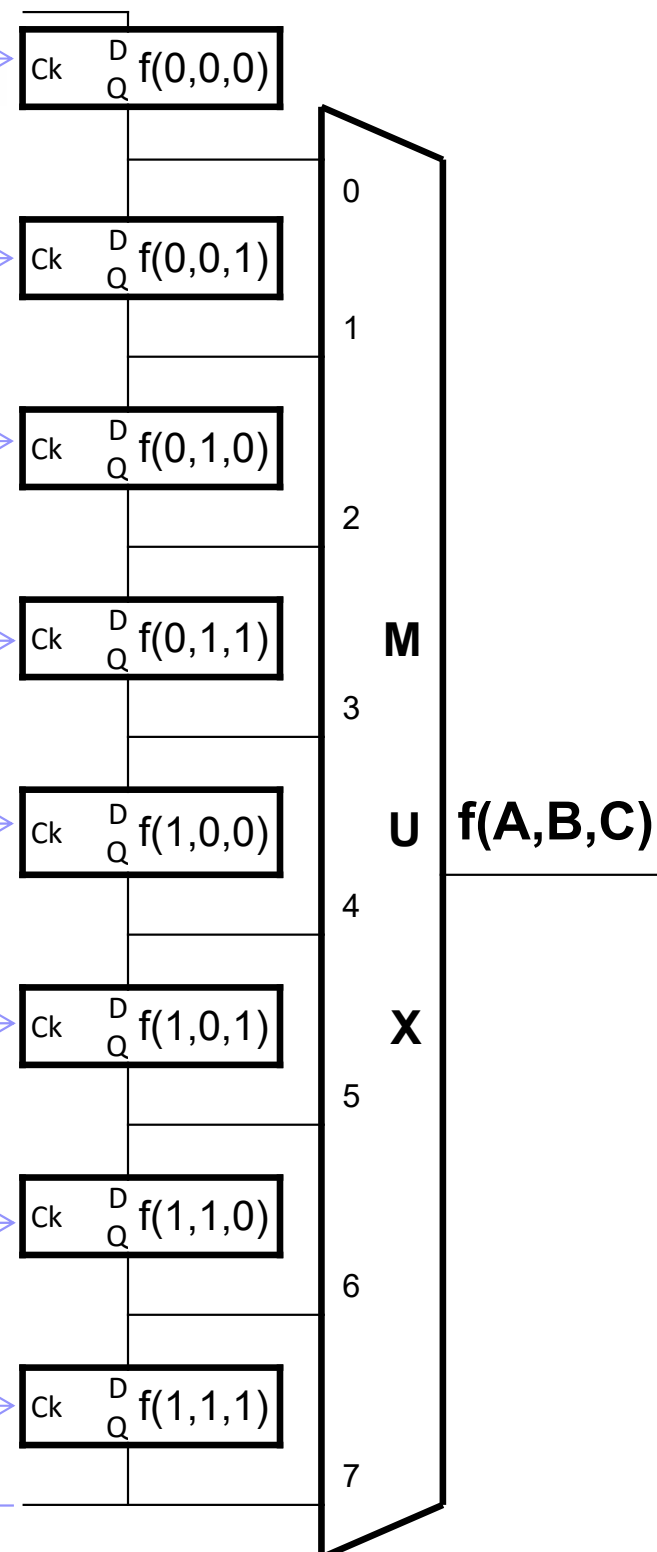
Programmable  
Inverter

f(A,B,C)

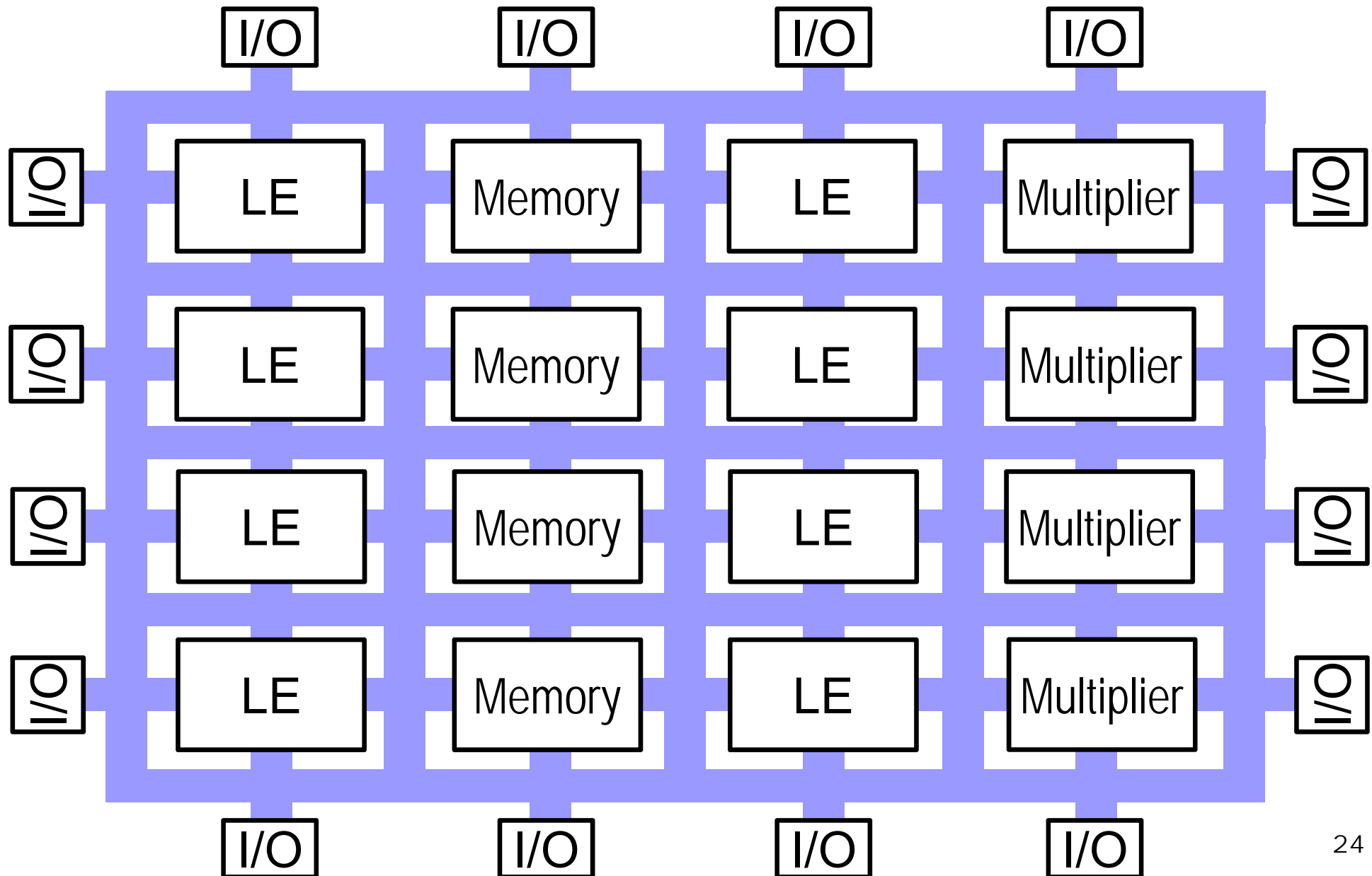
Clk · Prog

TDO

TDI



# FPGA





# Outline

- Decoders, Multiplexers
- Registers + Common sense design strategies
  - ☐ Register with Parallel Load
  - ☐ Shift Registers
  - ☐ **Bidirectional Shift Register with Parallel Load**
- Binary Counters
  - ☐ Binary Counter with Parallel Load

# Multi-function Registers

The most general register (Bidirectional Shift Register and Parallel Load) has the following capabilities:

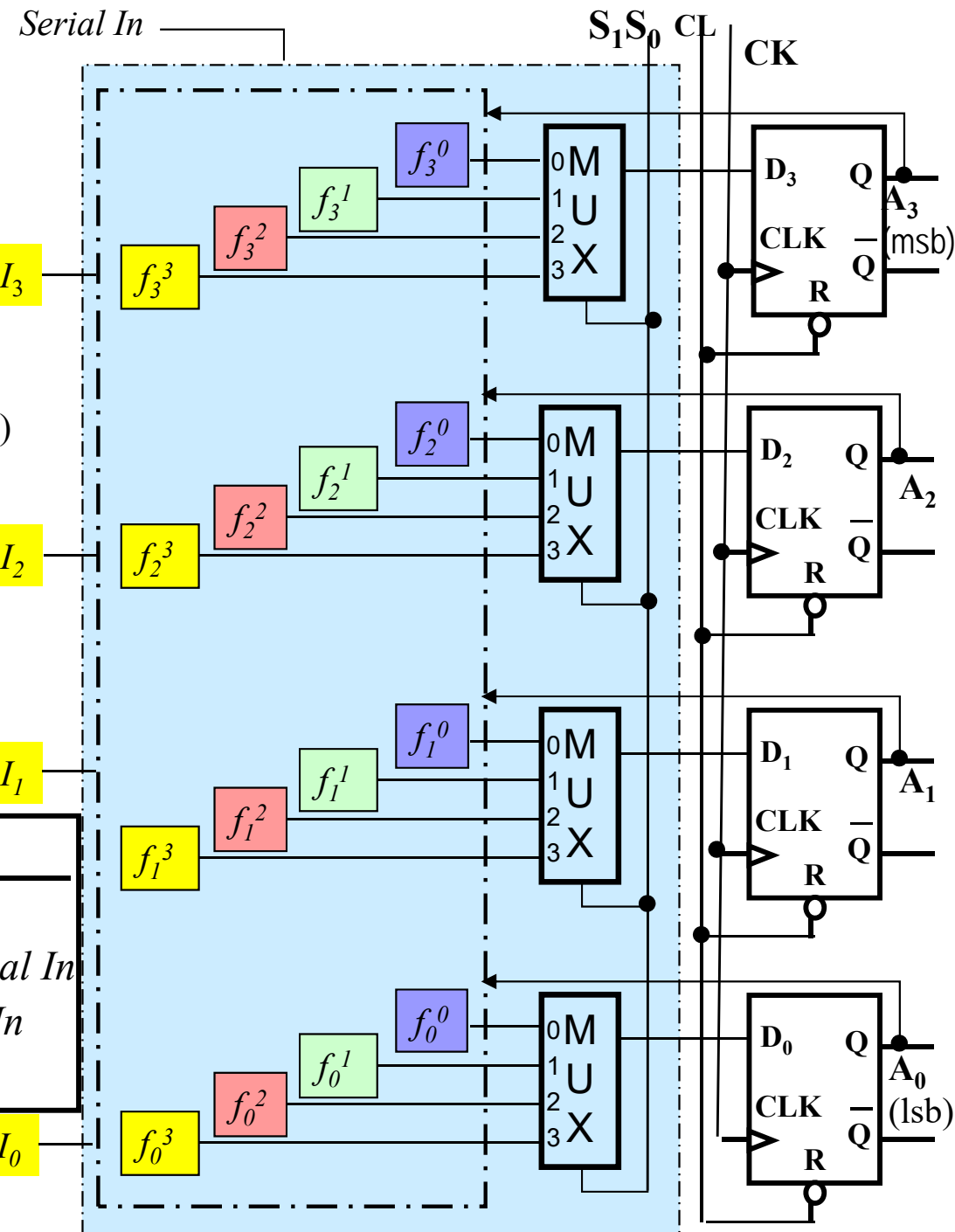
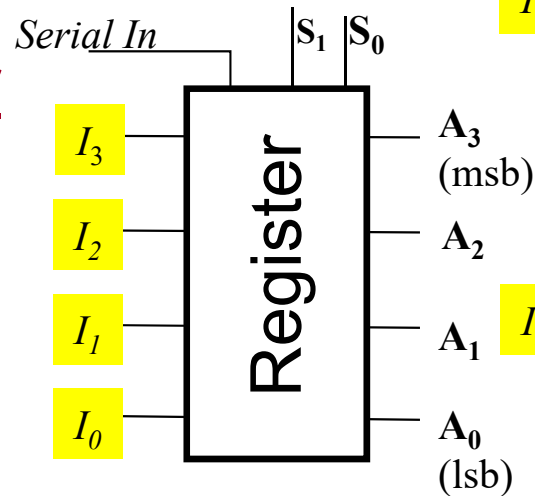
1. A clock pulse input to synchronize all operations.
2. A shift right operation and a serial input line associated to it.
3. A shift left operation and a serial input line associated to it.
4. A parallel load operation and  $n$  input lines associated to it.
5.  $n$  parallel output lines
6. A “no change” control state to leave the  $n$  parallel output lines unchanged for the next clock pulse.

Mode Control

| $S_1 S_0$ | Register operation                              |
|-----------|---|
| 00        | No change                                       |
| 01        | Shift right (msb $\rightarrow \rightarrow$ lsb) |
| 10        | Shift left (lsb $\rightarrow \rightarrow$ msb)  |
| 11        | Parallel load                                   |

# Top-down design

## Bidirectional Shift Register and Parallel Load with D Flip Flops

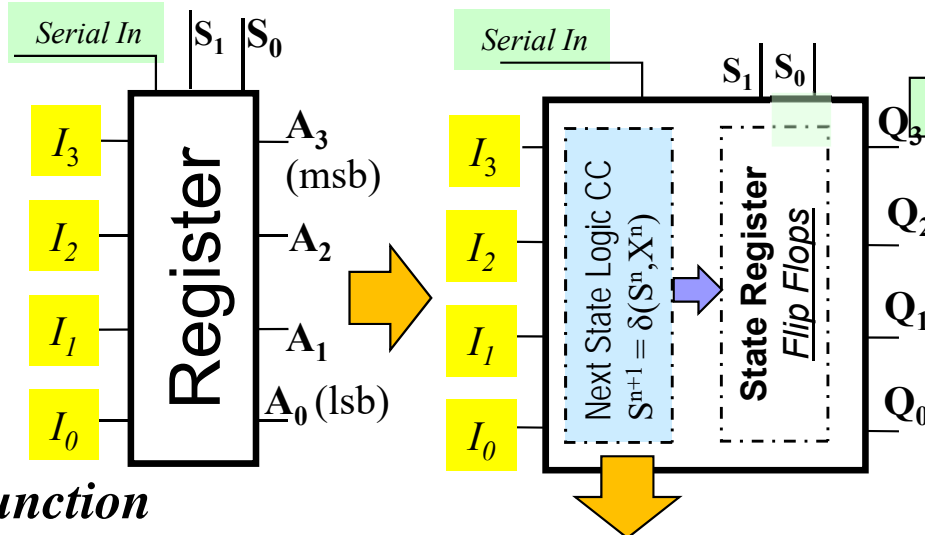


|         | $S_1$ | $S_0$ | Function                                       |
|---------|-------|-------|--|
| $(f^0)$ | 0     | 0     | No Change=Store                                |
| $(f^1)$ | 0     | 1     | Shift Right =down: msb->lsb & $D_3$ =Serial In |
| $(f^2)$ | 1     | 0     | Shift Left =up: msb->lsb & $D_0$ =Serial In    |
| $(f^3)$ | 1     | 1     | Parallel Load DB                               |

## Top-down design

### Bidirectional Shift Register and Parallel Load with D Flip Flops

#### Steps 1,2



|         | $S_1$ | $S_0$ | $A_k^{n+1}$ | Function   |
|---------|-------|-------|-------------|--|
| $(f^0)$ | 0     | 0     | $A_k^n$     | No Change=Store ( $k=\{0,1,2,3\}$ )  |
| $(f^1)$ | 0     | 1     | $A_{k+1}^n$ | Shift Right ( $k=\{0,1,2\}$ : $msb \rightarrow lsb$ & $D_3 = \text{Serial In}$ ) |
| $(f^2)$ | 1     | 0     | $A_{k-1}^n$ | Shift Left ( $k=\{1,2,3\}$ : $lsb \Rightarrow msb$ & $D_0 = \text{Serial In}$ )  |
| $(f^3)$ | 1     | 1     | $I_k$       | Parallel Load ( $k=\{0,1,2,3\}$ )  |

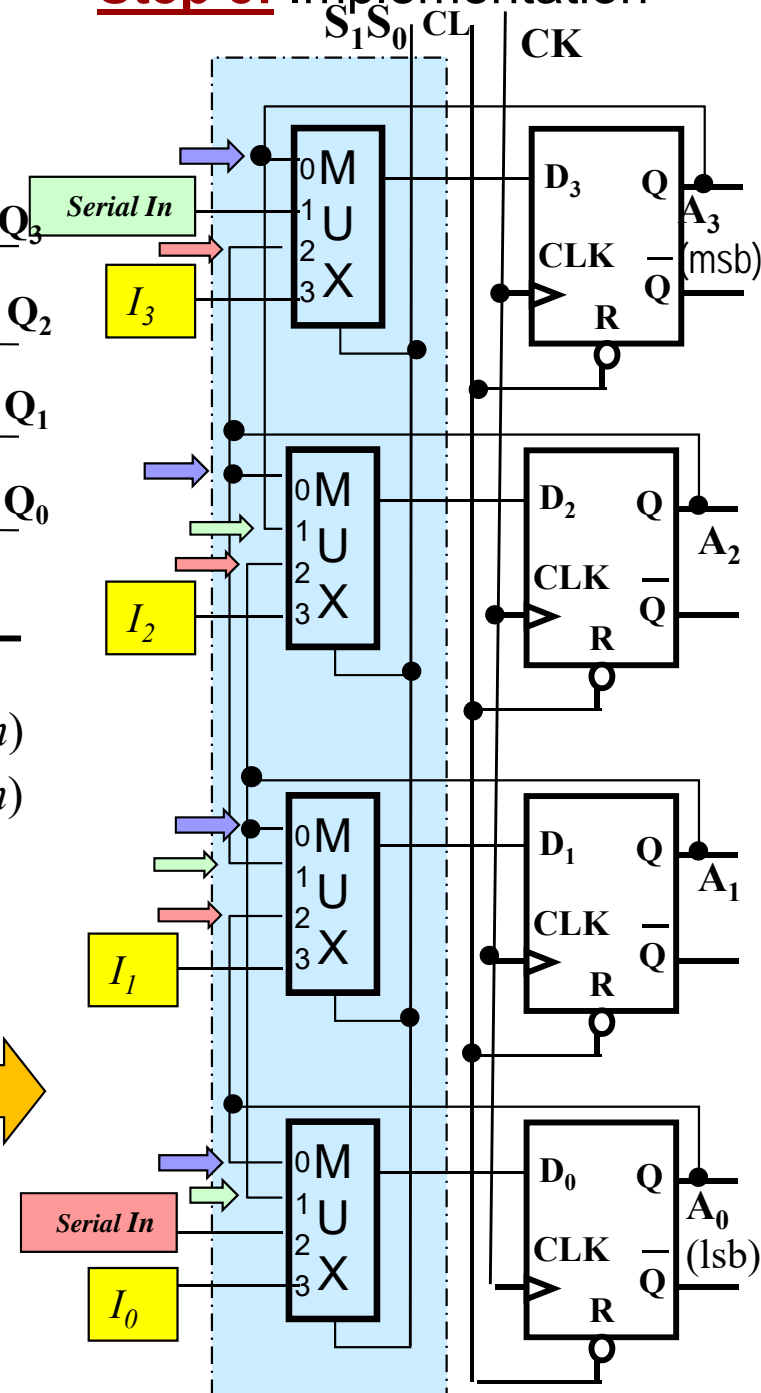
State / Transition Table (MEV format)

#### Steps 3,4

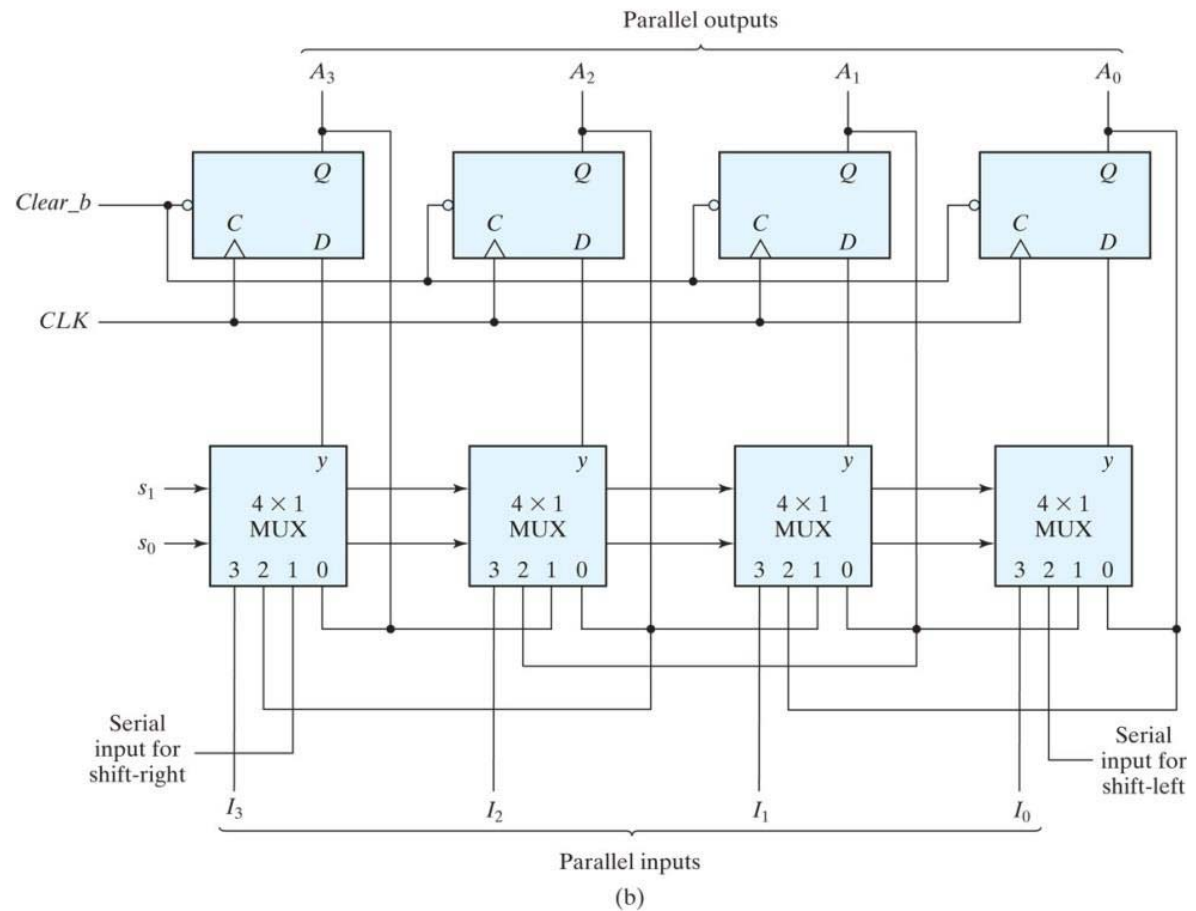
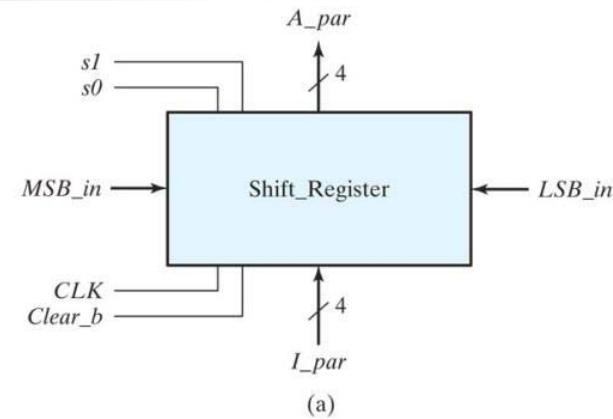
D-FF's excitation equations

|         | $S_1$ | $S_0$ | $D_k = A_k^{n+1}$   |
|---------|-------|-------|---|
| $(f^0)$ | 0     | 0     | $D_k = A_k$ ; $k=\{0,1,2,3\}$                               |
| $(f^1)$ | 0     | 1     | $D_k = A_{k+1}$ ; $k=\{0,1,2\}$<br>$D_3 = \text{Serial In}$ |
| $(f^2)$ | 1     | 0     | $D_k = A_{k-1}$ ; $k=\{1,2,3\}$<br>$D_0 = \text{Serial In}$ |
| $(f^3)$ | 1     | 1     | $D_k = I_k$ ; $k=\{0,1,2,3\}$                               |

#### Step 5: Implementation



# Four-bit universal shift register

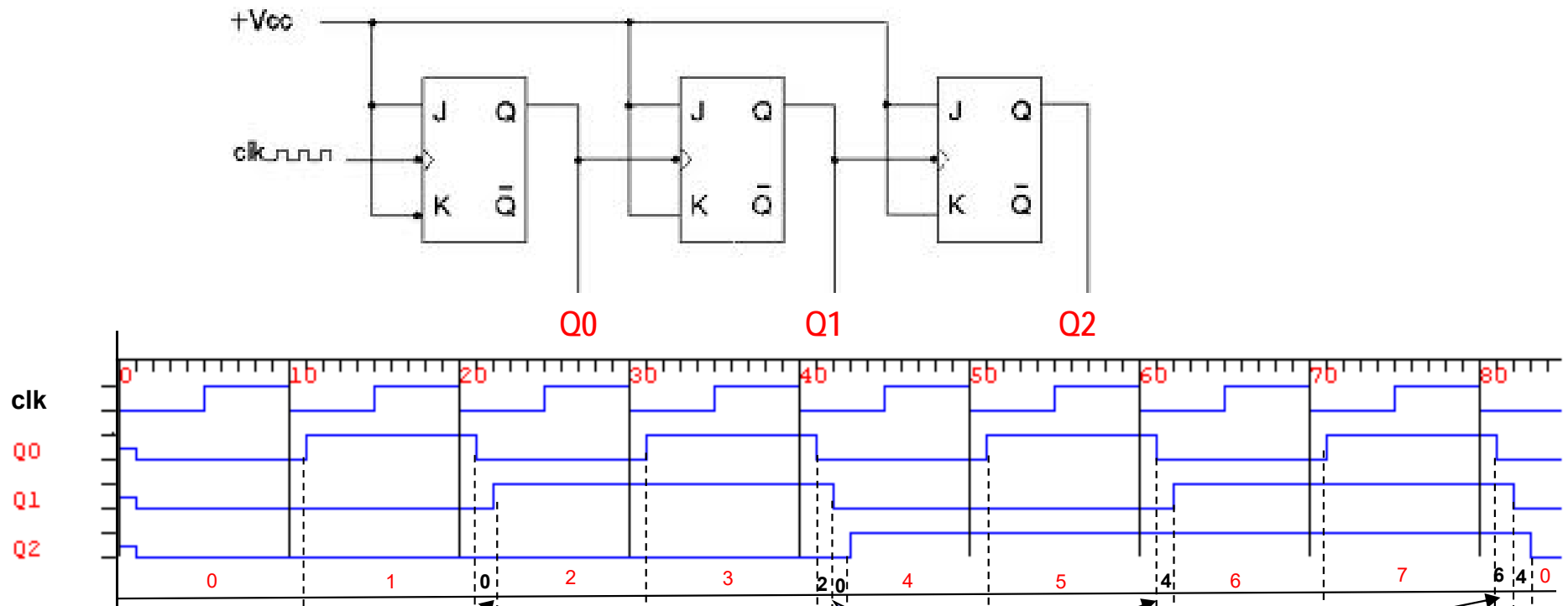



# Outline

- Decoders, Multiplexers
- Registers + Common sense design strategies
  - Register with Parallel Load
  - Shift Registers
  - Bidirectional Shift Register with Parallel Load
- **Binary Counters**
  - Binary Counter with Parallel Load

# Counters

- = Register that goes through a prescribed series of states
- There are two main types of counters:
  1. Asynchronous counters: also known as Ripple counters - Flip flop's output's serve as clock for triggering connected flip flops

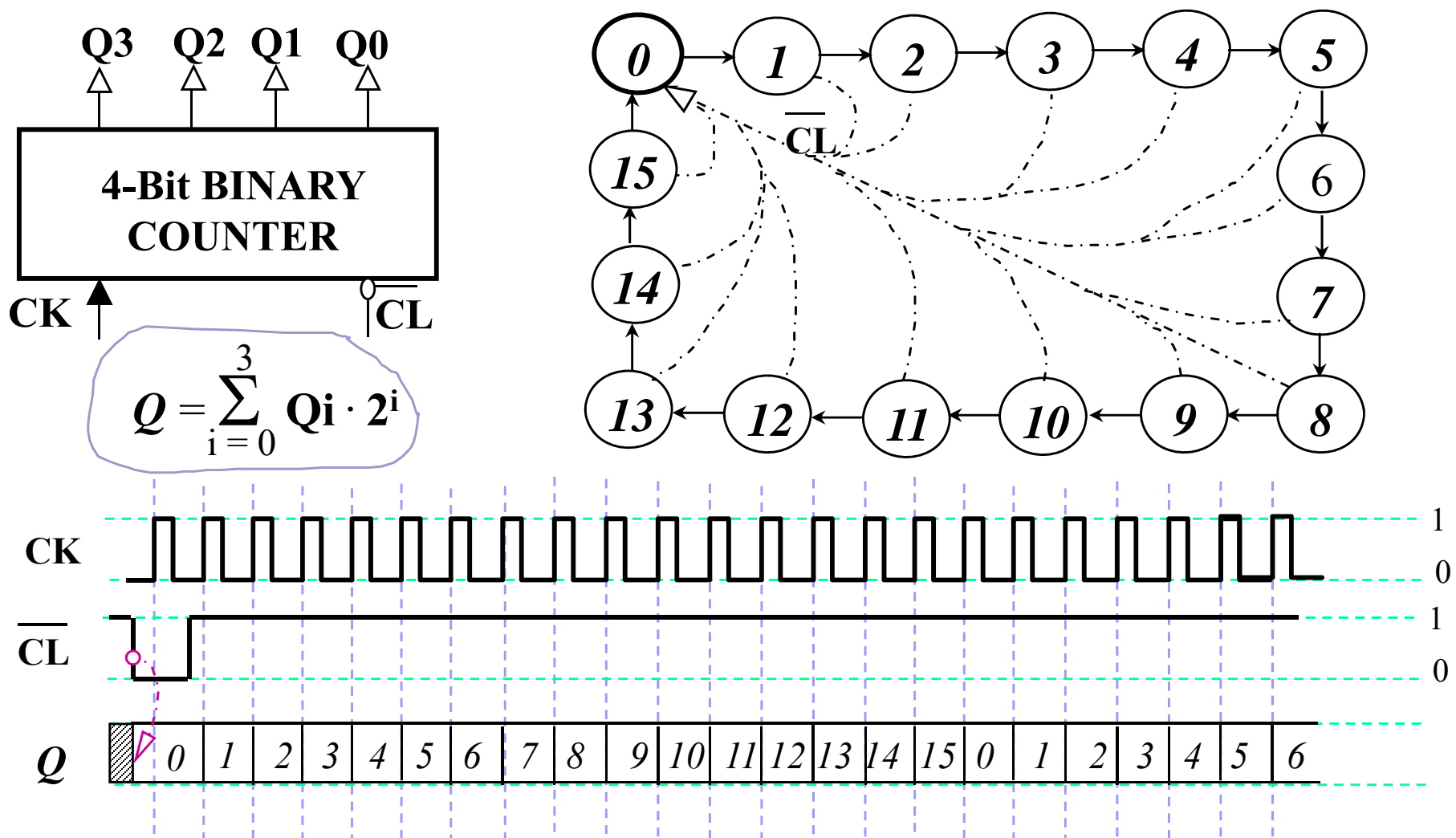


- ## 2. Synchronous counters
- All flip flops are triggered by a clock signal at the same time
- 



# Modulo 16 Synchronous Counter using *D* Flip-Flops

The number of unique states that a counter may go through before the count sequence repeats itself is the **modulus** (or MOD) of the counter.





## Modulo 16 Synchronous Counter

Using D flip-flops has the distinct advantage of a straightforward definition of the **flip-flop inputs**: the current state of these inputs is the next state of the counter  $Q_{n+1} = D_n$ . The logic equations for all four flip-flop inputs **D3**, **D2**,

**D1**, and **D0** are derived from this truth table as functions of the current states of the counter's flip-flops: **Q3**, **Q2**, **Q1**, and **Q0**. Karnaugh maps can be used to simplify these equations.

| DECIMAL STATE<br><i>Q</i> | Present STATE OF THE COUNTER |    |    |    | The next state = FLIP FLOP INPUTS |    |    |    |
|---------------------------|------------------------------|----|----|----|-----------------------------------|----|----|----|
|                           | Q3                           | Q2 | Q1 | Q0 | D3                                | D2 | D1 | D0 |
| 0                         | 0                            | 0  | 0  | 0  | 0                                 | 0  | 0  | 1  |
| 1                         | 0                            | 0  | 0  | 1  | 0                                 | 0  | 1  | 0  |
| 2                         | 0                            | 0  | 1  | 0  | 0                                 | 0  | 1  | 1  |
| 3                         | 0                            | 0  | 1  | 1  | 0                                 | 1  | 0  | 0  |
| 4                         | 0                            | 1  | 0  | 0  | 0                                 | 1  | 0  | 1  |
| 5                         | 0                            | 1  | 0  | 1  | 0                                 | 1  | 1  | 0  |
| 6                         | 0                            | 1  | 1  | 0  | 0                                 | 1  | 1  | 1  |
| 7                         | 0                            | 1  | 1  | 1  | 1                                 | 0  | 0  | 0  |
| 8                         | 1                            | 0  | 0  | 0  | 1                                 | 0  | 0  | 1  |
| 9                         | 1                            | 0  | 0  | 1  | 1                                 | 0  | 1  | 0  |
| 10                        | 1                            | 0  | 1  | 0  | 1                                 | 0  | 1  | 1  |
| 11                        | 1                            | 0  | 1  | 1  | 1                                 | 1  | 0  | 0  |
| 12                        | 1                            | 1  | 0  | 0  | 1                                 | 1  | 0  | 1  |
| 13                        | 1                            | 1  | 0  | 1  | 1                                 | 1  | 1  | 0  |
| 14                        | 1                            | 1  | 1  | 0  | 1                                 | 1  | 1  | 1  |
| 15                        | 1                            | 1  | 1  | 1  | 0                                 | 0  | 0  | 0  |

| Q3 Q2 |    |    |    |    |    |
|-------|----|----|----|----|----|
| Q1    | Q0 | 00 | 01 | 11 | 10 |
|       |    | 0  | 4  | 12 | 8  |
| 00    |    |    |    |    |    |
| 01    |    | 1  | 5  | 13 | 9  |
| 11    |    | 3  | 7  | 15 | 11 |
| 10    |    | 2  | 6  | 14 | 10 |

| Q3 Q2 |    | D3 |    |    |    |
|-------|----|----|----|----|----|
| Q1    | Q0 | 00 | 01 | 11 | 10 |
|       |    | 0  | 0  | 1  | 1  |
| 00    |    |    |    |    |    |
| 01    |    | 0  | 0  | 1  | 1  |
| 11    |    | 0  | 1  | 0  | 1  |
| 10    |    | 0  | 0  | 1  | 1  |

| Q3 Q2 |    | D2 |    |    |    |
|-------|----|----|----|----|----|
| Q1    | Q0 | 00 | 01 | 11 | 10 |
|       |    | 0  | 1  | 1  | 0  |
| 00    |    |    |    |    |    |
| 01    |    | 0  | 1  | 1  | 0  |
| 11    |    | 1  | 0  | 0  | 1  |
| 10    |    | 0  | 1  | 1  | 0  |

| Q3 Q2 |    | D1 |    |    |    |
|-------|----|----|----|----|----|
| Q1    | Q0 | 00 | 01 | 11 | 10 |
|       |    | 0  | 0  | 0  | 0  |
| 00    |    |    |    |    |    |
| 01    |    | 1  | 1  | 1  | 1  |
| 11    |    | 0  | 0  | 0  | 0  |
| 10    |    | 1  | 1  | 1  | 1  |

| Q3 Q2 |    | D0 |    |    |    |
|-------|----|----|----|----|----|
| Q1    | Q0 | 00 | 01 | 11 | 10 |
|       |    | 1  | 1  | 1  | 1  |
| 00    |    |    |    |    |    |
| 01    |    | 0  | 0  | 0  | 0  |
| 11    |    | 0  | 0  | 0  | 0  |
| 10    |    | 1  | 1  | 1  | 1  |

# ◆ Modulo 16 Synchronous Counter Excitation Equations

$$D^n = Q^{n+1}$$

**D3**

| Q3 Q2 \ Q1 Q0 | 00 | 01 | 11 | 10 |
|---------------|----|----|----|----|
| 00            | 0  | 0  | 1  | 1  |
| 01            | 0  | 0  | 1  | 1  |
| 11            | 0  | 1  | 0  | 1  |
| 10            | 0  | 0  | 1  | 1  |

$$D3 = Q3 \cdot \overline{Q2} + Q3 \cdot \overline{Q1} + Q3 \cdot \overline{Q0} + \overline{Q3} \cdot Q2 \cdot Q1 \cdot Q0$$

**D2**

| Q3 Q2 \ Q1 Q0 | 00 | 01 | 11 | 10 |
|---------------|----|----|----|----|
| 00            | 0  | 1  | 1  | 0  |
| 01            | 0  | 1  | 1  | 0  |
| 11            | 1  | 0  | 0  | 1  |
| 10            | 0  | 1  | 1  | 0  |

$$D2 = Q2 \cdot \overline{Q0} + Q2 \cdot \overline{Q1} + \overline{Q2} \cdot Q1 \cdot Q0$$

**D1**

| Q3 Q2 \ Q1 Q0 | 00 | 01 | 11 | 10 |
|---------------|----|----|----|----|
| 00            | 0  | 0  | 0  | 0  |
| 01            | 1  | 1  | 1  | 1  |
| 11            | 0  | 0  | 0  | 0  |
| 10            | 1  | 1  | 1  | 1  |

$$D1 = \overline{Q1} \cdot Q0 + Q1 \cdot \overline{Q0}$$

**D0**

| Q3 Q2 \ Q1 Q0 | 00 | 01 | 11 | 10 |
|---------------|----|----|----|----|
| 00            | 1  | 1  | 1  | 1  |
| 01            | 0  | 0  | 0  | 0  |
| 11            | 0  | 0  | 0  | 0  |
| 10            | 1  | 1  | 1  | 1  |

$$D0 = \overline{Q0}$$

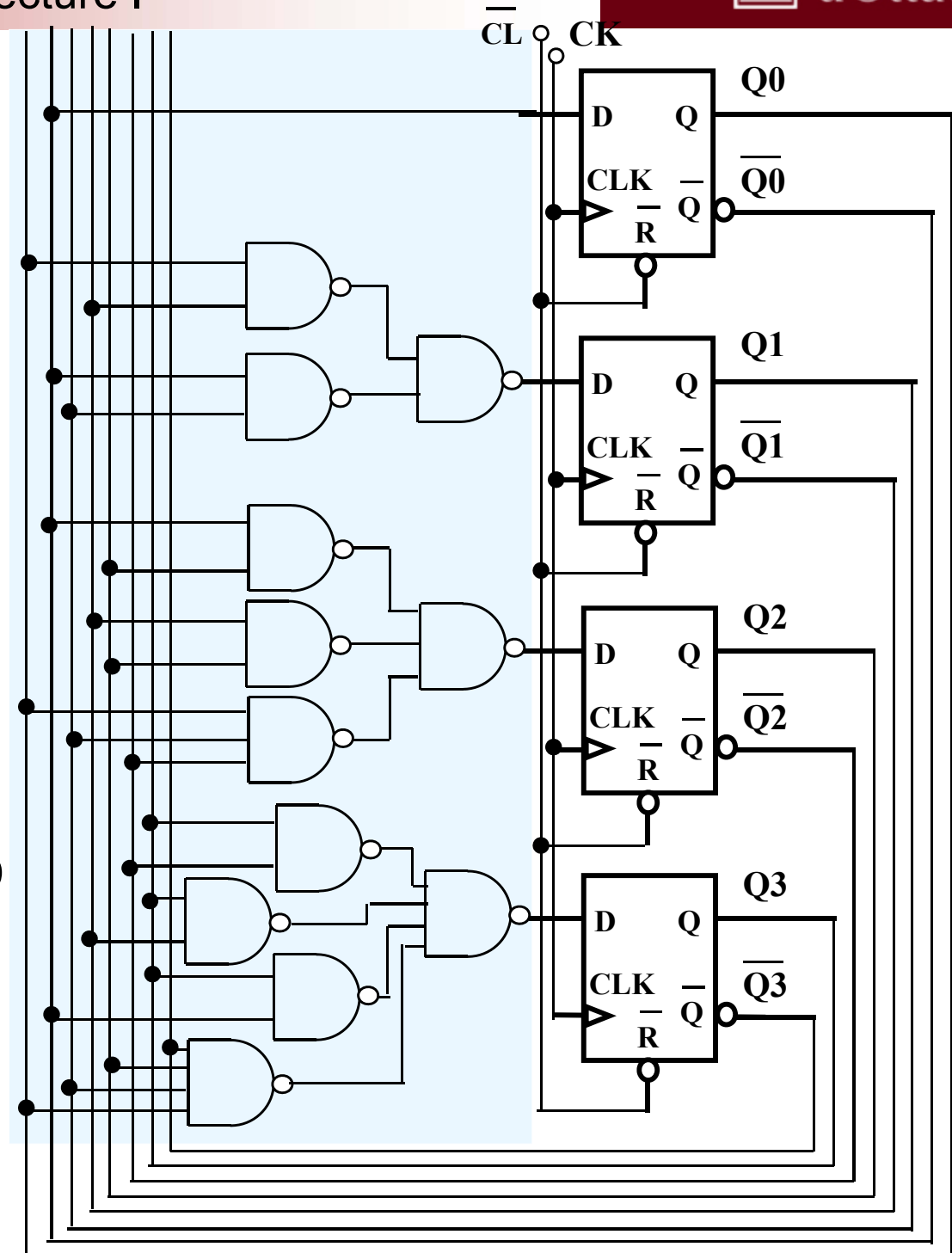
$$D^n = Q^{n+1}$$

$$\mathbf{D0} = \overline{\mathbf{Q0}}$$

$$\mathbf{D1} = \overline{\mathbf{Q1}} \cdot \mathbf{Q0} + \mathbf{Q1} \cdot \overline{\mathbf{Q0}}$$

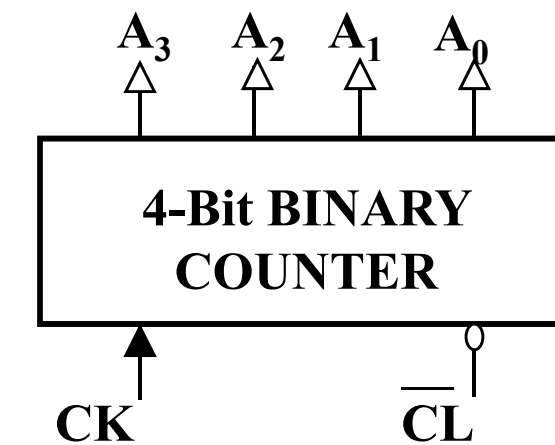
$$\mathbf{D2} = Q2 \cdot \overline{Q0} + Q2 \cdot \overline{Q1} + \overline{Q2} \cdot Q1 \cdot Q0$$

$$\mathbf{D3} = \mathbf{Q3} \cdot \overline{\mathbf{Q2}} + \mathbf{Q3} \cdot \overline{\mathbf{Q1}} + \mathbf{Q3} \cdot \overline{\mathbf{Q0}} + \overline{\mathbf{Q3}} \cdot \mathbf{Q2} \cdot \mathbf{Q1} \cdot \mathbf{Q0}$$

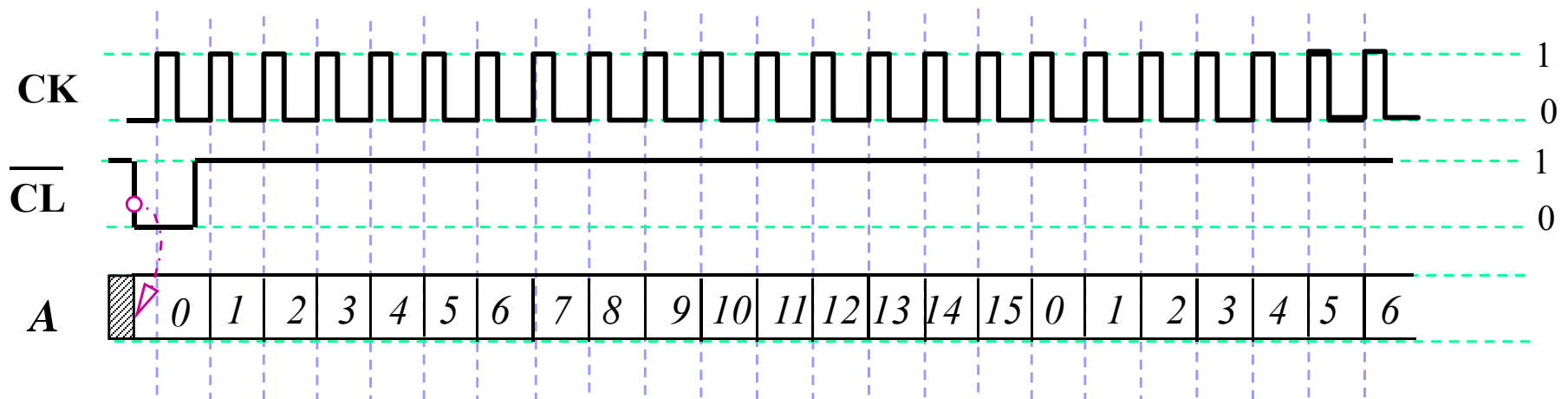
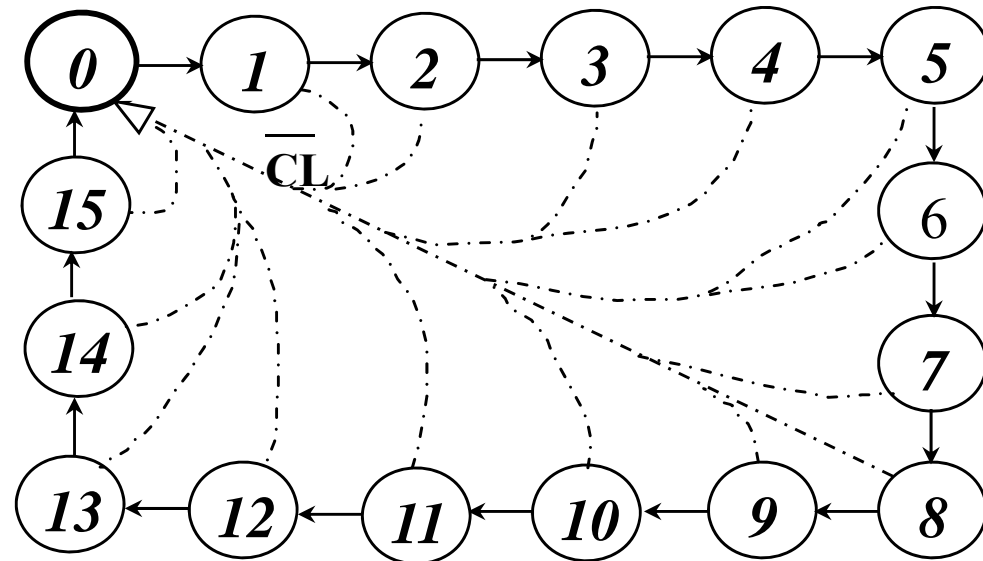


# Binary Counter

## Modulo 16 Synchronous Counter using JK Flip-Flops



$$A = \sum_{i=0}^3 A_i \cdot 2^i$$



| Present state<br>$S^n$ |       |       |       |       | Next state<br>$S^{n+1}$ |         |         |         |
|------------------------|-------|-------|-------|-------|-------------------------|---------|---------|---------|
| A                      | $A_3$ | $A_2$ | $A_1$ | $A_0$ | $A_3^+$                 | $A_2^+$ | $A_1^+$ | $A_0^+$ |
| 0                      | 0     | 0     | 0     | 0     | 0                       | 0       | 0       | 1       |
| 1                      | 0     | 0     | 0     | 1     | 0                       | 0       | 1       | 0       |
| 2                      | 0     | 0     | 1     | 0     | 0                       | 0       | 1       | 1       |
| 3                      | 0     | 0     | 1     | 1     | 0                       | 1       | 0       | 0       |
| 4                      | 0     | 1     | 0     | 0     | 0                       | 1       | 0       | 1       |
| 5                      | 0     | 1     | 0     | 1     | 0                       | 1       | 1       | 0       |
| 6                      | 0     | 1     | 1     | 0     | 0                       | 1       | 1       | 1       |
| 7                      | 0     | 1     | 1     | 1     | 1                       | 0       | 0       | 0       |
| 8                      | 1     | 0     | 0     | 0     | 1                       | 0       | 0       | 1       |
| 9                      | 1     | 0     | 0     | 1     | 1                       | 0       | 1       | 0       |
| 10                     | 1     | 0     | 1     | 0     | 1                       | 0       | 1       | 1       |
| 11                     | 1     | 0     | 1     | 1     | 1                       | 1       | 0       | 0       |
| 12                     | 1     | 1     | 0     | 0     | 1                       | 1       | 0       | 1       |
| 13                     | 1     | 1     | 0     | 1     | 1                       | 1       | 1       | 0       |
| 14                     | 1     | 1     | 1     | 0     | 1                       | 1       | 1       | 1       |
| 15                     | 1     | 1     | 1     | 1     | 0                       | 0       | 0       | 0       |

## “Common sense” design approach

We can notice from the State Table that:

- $A_0$  toggles its value at each clock pulse  
 $\Rightarrow J_0 = 1 ; K_0 = 1.$
- $A_1$  toggles its value at time  $T$  only if at time  $(T - 1)$   $A_0$  is 1.

| Present State |              |              | Next State      | Flip-Flop Inputs |       |
|---------------|--------------|--------------|-----------------|------------------|-------|
| $A_2(T - 1)$  | $A_1(T - 1)$ | $A_0(T - 1)$ | $A_1(T)$        | $J_1$            | $K_1$ |
| x             | x            | 0            | $A_1(t - 1)$    | 0                | 0     |
| x             | x            | 1            | $(A_1(t - 1))'$ | 1                | 1     |

$$J_1 = K_1 = A_0(T - 1)$$

- $A_2$  toggles its value at time  $T$  only if at time  $(T - 1)$   $A_1 = 1$  and  $A_0 = 1$

| Present State |              |              | Next State      | Flip-Flop Inputs |
|---------------|--------------|--------------|-----------------|------------------|
| $A_2(T - 1)$  | $A_1(T - 1)$ | $A_0(T - 1)$ | $A_2(T)$        | $J_2 K_2$        |
| x             | 0            | 0            | $A_2(t - 1)$    | 0 0              |
| x             | 0            | 1            | $A_2(t - 1)$    | 0 0              |
| x             | 1            | 0            | $A_2(t - 1)$    | 0 0              |
| x             | 1            | 1            | $(A_2(t - 1))'$ | 1 1              |

$$J_2 = K_2 = A_1(T - 1) A_0(T - 1)$$



Or use the “the  
receipe”

| Present state $S^n$ |       |       |       |       | Next state $S^{n+1}$ |         |         |         | $A_3$ input |       | $A_2$ input |       | $A_1$ input |       | $A_0$ input |       |
|---------------------|-------|-------|-------|-------|----------------------|---------|---------|---------|-------------|-------|-------------|-------|-------------|-------|-------------|-------|
| A                   | $A_3$ | $A_2$ | $A_1$ | $A_0$ | $A_3^+$              | $A_2^+$ | $A_1^+$ | $A_0^+$ | $J_3$       | $K_3$ | $J_2$       | $K_2$ | $J_1$       | $K_1$ | $J_0$       | $K_0$ |
| 0                   | 0     | 0     | 0     | 0     | 0                    | 0       | 0       | 1       | 0           | x     |             |       |             |       |             |       |
| 1                   | 0     | 0     | 0     | 1     | 0                    | 0       | 1       | 0       | 0           | x     |             |       |             |       |             |       |
| 2                   | 0     | 0     | 1     | 0     | 0                    | 0       | 1       | 1       | 0           | x     |             |       |             |       |             |       |
| 3                   | 0     | 0     | 1     | 1     | 0                    | 1       | 0       | 0       | 0           | x     |             |       |             |       |             |       |
| 4                   | 0     | 1     | 0     | 0     | 0                    | 1       | 0       | 1       | 0           | x     |             |       |             |       |             |       |
| 5                   | 0     | 1     | 0     | 1     | 0                    | 1       | 1       | 0       | 0           | x     |             |       |             |       |             |       |
| 6                   | 0     | 1     | 1     | 0     | 0                    | 1       | 1       | 1       | 0           | x     |             |       |             |       |             |       |
| 7                   | 0     | 1     | 1     | 1     | 1                    | 0       | 0       | 0       | 1           | x     |             |       |             |       |             |       |
| 8                   | 1     | 0     | 0     | 0     | 1                    | 0       | 0       | 1       | x           | 0     |             |       |             |       |             |       |
| 9                   | 1     | 0     | 0     | 1     | 1                    | 0       | 1       | 0       | x           | 0     |             |       |             |       |             |       |
| 10                  | 1     | 0     | 1     | 0     | 1                    | 0       | 1       | 1       | x           | 0     |             |       |             |       |             |       |
| 11                  | 1     | 0     | 1     | 1     | 1                    | 1       | 0       | 0       | x           | 0     |             |       |             |       |             |       |
| 12                  | 1     | 1     | 0     | 0     | 1                    | 1       | 0       | 1       | x           | 0     |             |       |             |       |             |       |
| 13                  | 1     | 1     | 0     | 1     | 1                    | 1       | 1       | 0       | x           | 0     |             |       |             |       |             |       |
| 14                  | 1     | 1     | 1     | 0     | 1                    | 1       | 1       | 1       | x           | 0     |             |       |             |       |             |       |
| 15                  | 1     | 1     | 1     | 1     | 0                    | 0       | 0       | 0       | x           | 1     |             |       |             |       |             |       |

Or use the “the  
recepte”

| Present state $S^n$ |       |       |       |       | Next state $S^{n+1}$ |         |         |         | $A_3$ input |       | $A_2$ input |       | $A_1$ input |       | $A_0$ input |       |
|---------------------|-------|-------|-------|-------|----------------------|---------|---------|---------|-------------|-------|-------------|-------|-------------|-------|-------------|-------|
| A                   | $A_3$ | $A_2$ | $A_1$ | $A_0$ | $A_3^+$              | $A_2^+$ | $A_1^+$ | $A_0^+$ | $J_3$       | $K_3$ | $J_2$       | $K_2$ | $J_1$       | $K_1$ | $J_0$       | $K_0$ |
| 0                   | 0     | 0     | 0     | 0     | 0                    | 0       | 0       | 1       | 0           | x     | 0           | x     |             |       |             |       |
| 1                   | 0     | 0     | 0     | 1     | 0                    | 0       | 1       | 0       | 0           | x     | 0           | x     |             |       |             |       |
| 2                   | 0     | 0     | 1     | 0     | 0                    | 0       | 1       | 1       | 0           | x     | 0           | x     |             |       |             |       |
| 3                   | 0     | 0     | 1     | 1     | 0                    | 1       | 0       | 0       | 0           | x     | 1           | x     |             |       |             |       |
| 4                   | 0     | 1     | 0     | 0     | 0                    | 1       | 0       | 1       | 0           | x     | x           | 0     |             |       |             |       |
| 5                   | 0     | 1     | 0     | 1     | 0                    | 1       | 1       | 0       | 0           | x     | x           | 0     |             |       |             |       |
| 6                   | 0     | 1     | 1     | 0     | 0                    | 1       | 1       | 1       | 0           | x     | x           | 0     |             |       |             |       |
| 7                   | 0     | 1     | 1     | 1     | 1                    | 0       | 0       | 0       | 1           | x     | x           | 1     |             |       |             |       |
| 8                   | 1     | 0     | 0     | 0     | 1                    | 0       | 0       | 1       | x           | 0     | 0           | x     |             |       |             |       |
| 9                   | 1     | 0     | 0     | 1     | 1                    | 0       | 1       | 0       | x           | 0     | 0           | x     |             |       |             |       |
| 10                  | 1     | 0     | 1     | 0     | 1                    | 0       | 1       | 1       | x           | 0     | 0           | x     |             |       |             |       |
| 11                  | 1     | 0     | 1     | 1     | 1                    | 1       | 0       | 0       | x           | 0     | 1           | x     |             |       |             |       |
| 12                  | 1     | 1     | 0     | 0     | 1                    | 1       | 0       | 1       | x           | 0     | x           | 0     |             |       |             |       |
| 13                  | 1     | 1     | 0     | 1     | 1                    | 1       | 1       | 0       | x           | 0     | x           | 0     |             |       |             |       |
| 14                  | 1     | 1     | 1     | 0     | 1                    | 1       | 1       | 1       | x           | 0     | x           | 0     |             |       |             |       |
| 15                  | 1     | 1     | 1     | 1     | 0                    | 0       | 0       | 0       | x           | 1     | x           | 1     |             |       |             |       |



Or use the “the  
recepte”

| Present state $S^n$ |       |       |       |       | Next state $S^{n+1}$ |         |         |         | $A_3$ input |       | $A_2$ input |       | $A_1$ input |       | $A_0$ input |       |
|---------------------|-------|-------|-------|-------|----------------------|---------|---------|---------|-------------|-------|-------------|-------|-------------|-------|-------------|-------|
| A                   | $A_3$ | $A_2$ | $A_1$ | $A_0$ | $A_3^+$              | $A_2^+$ | $A_1^+$ | $A_0^+$ | $J_3$       | $K_3$ | $J_2$       | $K_2$ | $J_1$       | $K_1$ | $J_0$       | $K_0$ |
| 0                   | 0     | 0     | 0     | 0     | 0                    | 0       | 0       | 1       | 0           | x     | 0           | x     | 0           | x     |             |       |
| 1                   | 0     | 0     | 0     | 1     | 0                    | 0       | 1       | 0       | 0           | x     | 0           | x     | 1           | x     |             |       |
| 2                   | 0     | 0     | 1     | 0     | 0                    | 0       | 1       | 1       | 0           | x     | 0           | x     | x           | 0     |             |       |
| 3                   | 0     | 0     | 1     | 1     | 0                    | 1       | 0       | 0       | 0           | x     | 1           | x     | x           | 1     |             |       |
| 4                   | 0     | 1     | 0     | 0     | 0                    | 1       | 0       | 1       | 0           | x     | x           | 0     | 0           | x     |             |       |
| 5                   | 0     | 1     | 0     | 1     | 0                    | 1       | 1       | 0       | 0           | x     | x           | 0     | 1           | x     |             |       |
| 6                   | 0     | 1     | 1     | 0     | 0                    | 1       | 1       | 1       | 0           | x     | x           | 0     | x           | 0     |             |       |
| 7                   | 0     | 1     | 1     | 1     | 1                    | 0       | 0       | 0       | 1           | x     | x           | 1     | x           | 1     |             |       |
| 8                   | 1     | 0     | 0     | 0     | 1                    | 0       | 0       | 1       | x           | 0     | 0           | x     | 0           | x     |             |       |
| 9                   | 1     | 0     | 0     | 1     | 1                    | 0       | 1       | 0       | x           | 0     | 0           | x     | 1           | x     |             |       |
| 10                  | 1     | 0     | 1     | 0     | 1                    | 0       | 1       | 1       | x           | 0     | 0           | x     | x           | 0     |             |       |
| 11                  | 1     | 0     | 1     | 1     | 1                    | 1       | 0       | 0       | x           | 0     | 1           | x     | x           | 1     |             |       |
| 12                  | 1     | 1     | 0     | 0     | 1                    | 1       | 0       | 1       | x           | 0     | x           | 0     | 0           | x     |             |       |
| 13                  | 1     | 1     | 0     | 1     | 1                    | 1       | 1       | 0       | x           | 0     | x           | 0     | 1           | x     |             |       |
| 14                  | 1     | 1     | 1     | 0     | 1                    | 1       | 1       | 1       | x           | 0     | x           | 0     | x           | 0     |             |       |
| 15                  | 1     | 1     | 1     | 1     | 0                    | 0       | 0       | 0       | x           | 1     | x           | 1     | x           | 1     |             |       |

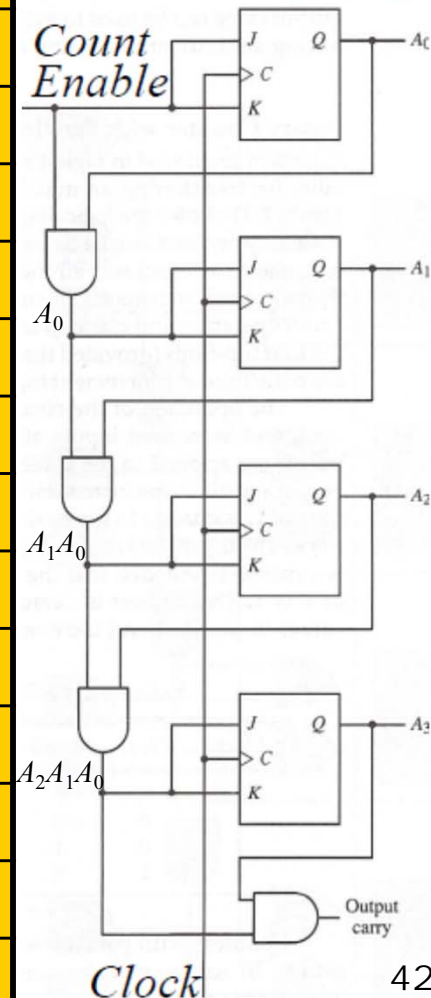
| Present state $S^n$ |       |       |       |       | Next state $S^{n+1}$ |         |         |         | $A_3$ input |       | $A_2$ input |       | $A_1$ input |       | $A_0$ input |       |
|---------------------|-------|-------|-------|-------|----------------------|---------|---------|---------|-------------|-------|-------------|-------|-------------|-------|-------------|-------|
| A                   | $A_3$ | $A_2$ | $A_1$ | $A_0$ | $A_3^+$              | $A_2^+$ | $A_1^+$ | $A_0^+$ | $J_3$       | $K_3$ | $J_2$       | $K_2$ | $J_1$       | $K_1$ | $J_0$       | $K_0$ |
| 0                   | 0     | 0     | 0     | 0     | 0                    | 0       | 0       | 1       | 0           | x     | 0           | x     | 0           | x     | 1           | x     |
| 1                   | 0     | 0     | 0     | 1     | 0                    | 0       | 1       | 0       | 0           | x     | 0           | x     | 1           | x     | x           | 1     |
| 2                   | 0     | 0     | 1     | 0     | 0                    | 0       | 1       | 1       | 0           | x     | 0           | x     | x           | 0     | 1           | x     |
| 3                   | 0     | 0     | 1     | 1     | 0                    | 1       | 0       | 0       | 0           | x     | 1           | x     | x           | 1     | x           | 1     |
| 4                   | 0     | 1     | 0     | 0     | 0                    | 1       | 0       | 1       | 0           | x     | x           | 0     | 0           | x     | 1           | x     |
| 5                   | 0     | 1     | 0     | 1     | 0                    | 1       | 1       | 0       | 0           | x     | x           | 0     | 1           | x     | x           | 1     |
| 6                   | 0     | 1     | 1     | 0     | 0                    | 1       | 1       | 1       | 0           | x     | x           | 0     | x           | 0     | 1           | x     |
| 7                   | 0     | 1     | 1     | 1     | 1                    | 0       | 0       | 0       | 1           | x     | x           | 1     | x           | 1     | x           | 1     |
| 8                   | 1     | 0     | 0     | 0     | 1                    | 0       | 0       | 1       | x           | 0     | 0           | x     | 0           | x     | 1           | x     |
| 9                   | 1     | 0     | 0     | 1     | 1                    | 0       | 1       | 0       | x           | 0     | 0           | x     | 1           | x     | x           | 1     |
| 10                  | 1     | 0     | 1     | 0     | 1                    | 0       | 1       | 1       | x           | 0     | 0           | x     | x           | 0     | 1           | x     |
| 11                  | 1     | 0     | 1     | 1     | 1                    | 1       | 0       | 0       | x           | 0     | 1           | x     | x           | 1     | x           | 1     |
| 12                  | 1     | 1     | 0     | 0     | 1                    | 1       | 0       | 1       | x           | 0     | x           | 0     | 0           | x     | 1           | x     |
| 13                  | 1     | 1     | 0     | 1     | 1                    | 1       | 1       | 0       | x           | 0     | x           | 0     | 1           | x     | x           | 1     |
| 14                  | 1     | 1     | 1     | 0     | 1                    | 1       | 1       | 1       | x           | 0     | x           | 0     | x           | 0     | 1           | x     |
| 15                  | 1     | 1     | 1     | 1     | 0                    | 0       | 0       | 0       | x           | 1     | x           | 1     | x           | 1     | x           | 1     |

$$J_0 = K_0 = 1$$

$$J_1 = K_1 = A_0$$

$$J_2 = K_2 = A_0 A_1$$

$$J_3 = K_3 = A_0 A_1 A_2$$



# Outline

- Decoders, Multiplexers
- Registers + Common sense design strategies
  - Register with Parallel Load
  - Shift Registers
  - Bidirectional Shift Register with Parallel Load
- Binary Counters
  - **Binary Counter with Parallel Load**

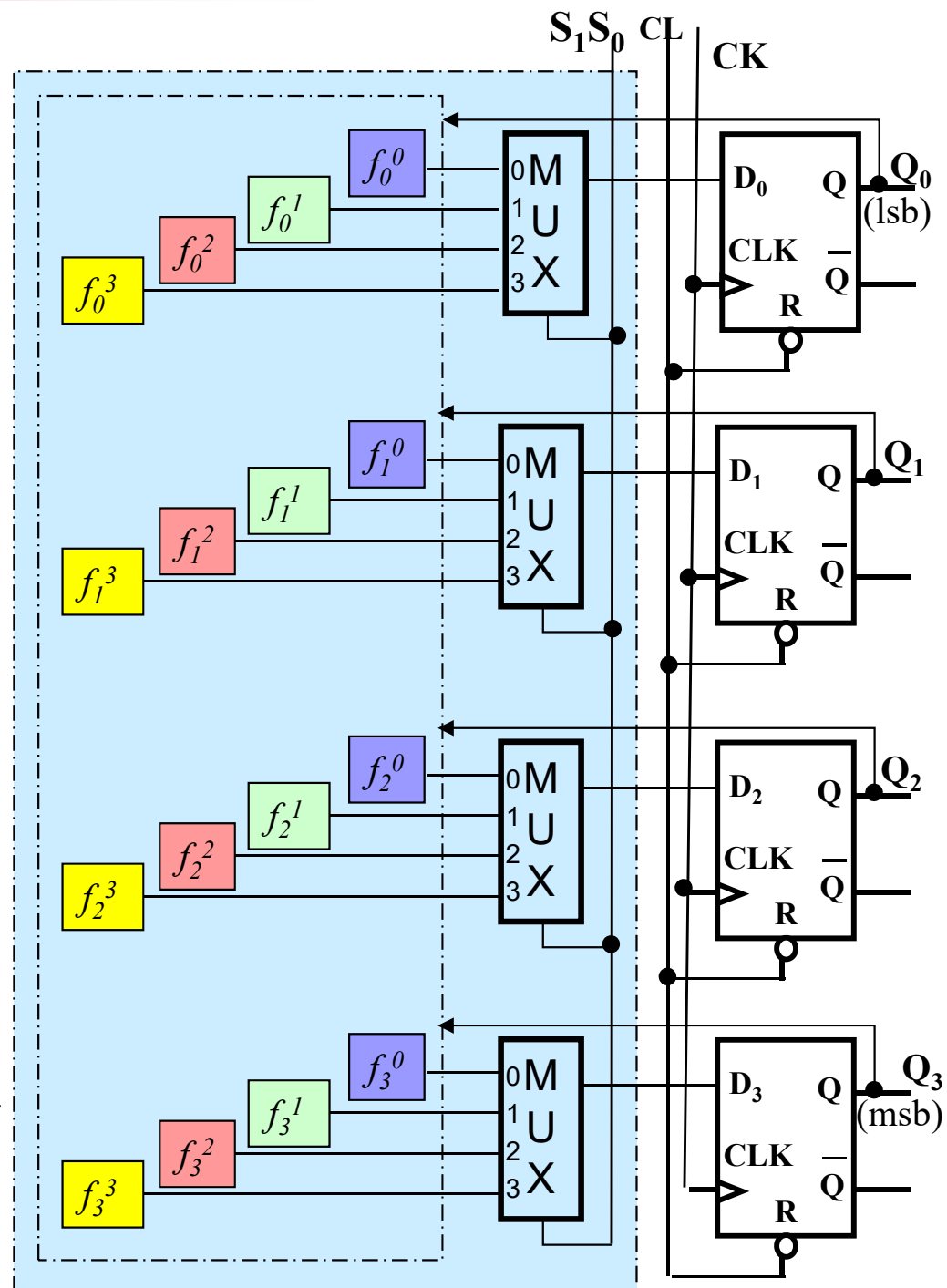
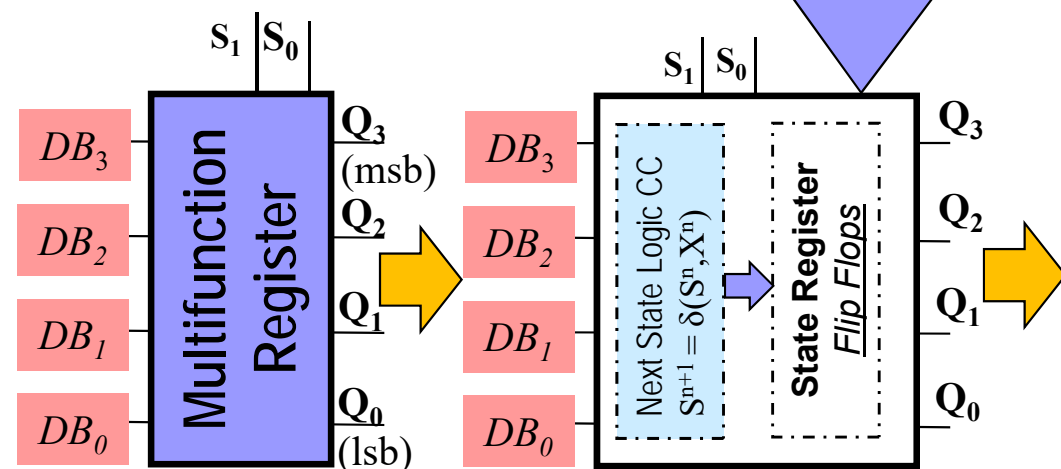
## ◆ Top-down design

### Multifunction Register with D-Flip Flops

| $S_1 S_0$ | $Q_k^{n+1}$ | Function |
|-----------|-------------|----------|
| 0 0       | $Q_k^n$     | Store    |
| 0 1       | $N_k$       | Count up |
| 1 0       | $DB_k$      | Load     |
| 1 1       | 0           | Clear    |

 $k = \{0, 1, 2, 3\}$ 

Multifunction Register  
implemented as a Sequential Circuit



# Multifunction Register

|         | $S_1 S_0$ | $D_k = Q_k^{n+1}$ | Function |
|---------|-----------|-------------------|----------|
| $(f^0)$ | 0 0       | $Q_k^n$           | Store    |
| $(f^1)$ | 0 1       | $N_k$             | Count up |
| $(f^2)$ | 1 0       | $DB_k$            | Load     |
| $(f^3)$ | 1 1       | 0                 | Clear    |

Use the “Common sense” design approach,  
(where obvious) or:

D- FF's excitation equation:  $D^n = Q^{n+1}$  (1)

**Store** ( $f^0$ ):  $Q^{n+1} = Q^n$  (2) to be implemented with D-FF

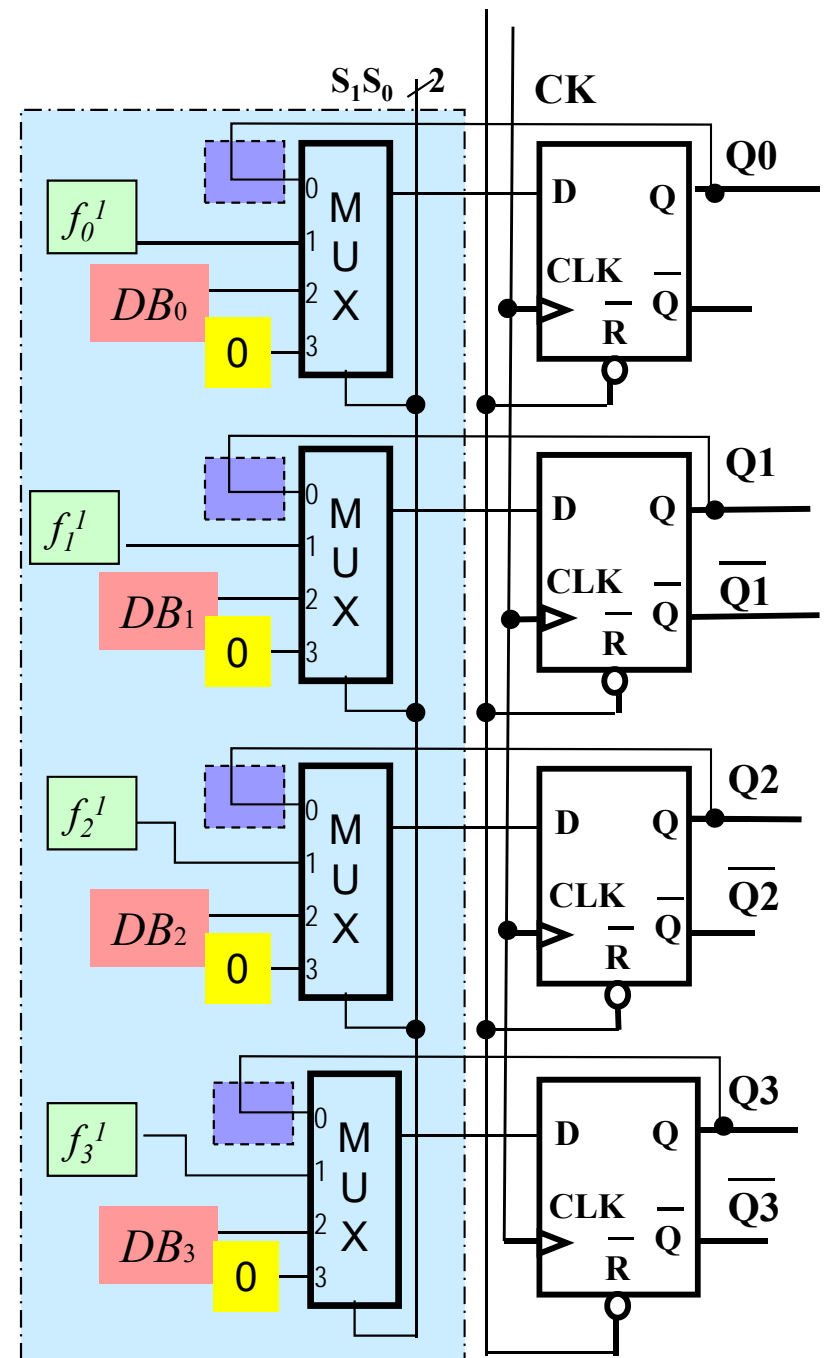
From (1), (2)  $\Rightarrow D^n = Q^{n+1} = Q^n$  i.e.,  $D_k = Q_k$ ,  $k = \{0, 1, 2, 3\}$

**Clear** ( $f^3$ ):  $Q^{n+1} = 0$  (3) with D-FF

From (1), (3)  $\Rightarrow D^n = 0$  i.e.,  $D_k = 0$ ,  $k = \{0, 1, 2, 3\}$

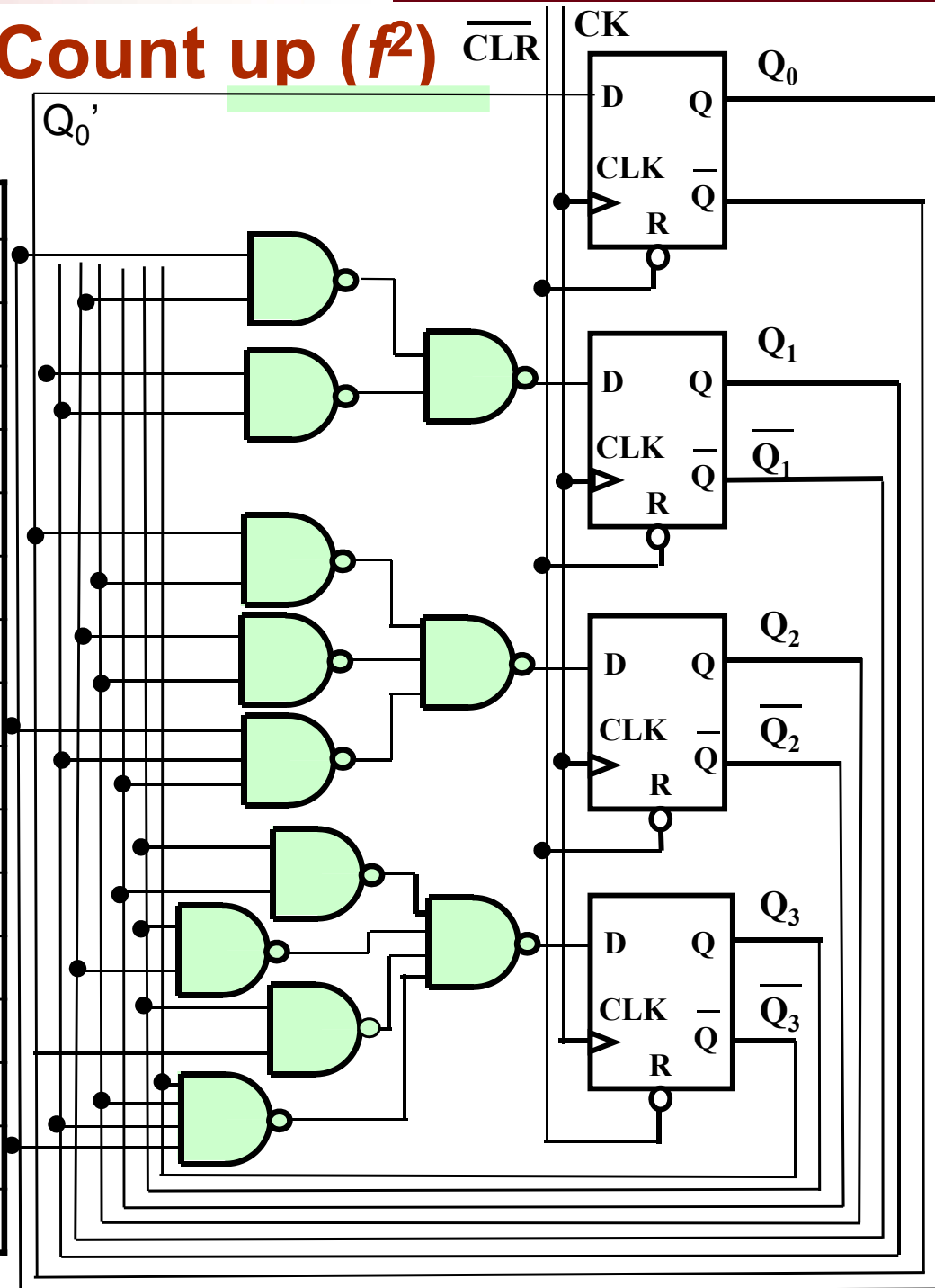
**Load** ( $f^2$ ):  $Q^{n+1} = DB^n$  (4) with D-FF

From (1), (4)  $\Rightarrow D^n = DB^n$ , i.e.,  $D_k = DB_k$ ,  $k = \{0, 1, 2, 3\}$



# Multifunction Register - Count up ( $f^2$ )

| $Q_3$ | $Q_2$ | $Q_1$ | $Q_0$ | $Q_3^+$ | $Q_2^+$ | $Q_1^+$ | $Q_0^+$ | $D_3$ | $D_2$ | $D_1$ | $D_0$ |
|-------|-------|-------|-------|---------|---------|---------|---------|-------|-------|-------|-------|
| 0     | 0     | 0     | 0     | 0       | 0       | 0       | 1       | 0     | 0     | 0     | 1     |
| 0     | 0     | 0     | 1     | 0       | 0       | 1       | 0       | 0     | 0     | 1     | 0     |
| 0     | 0     | 1     | 0     | 0       | 0       | 1       | 1       | 0     | 0     | 1     | 1     |
| 0     | 0     | 1     | 1     | 0       | 1       | 0       | 0       | 0     | 1     | 0     | 0     |
| 0     | 1     | 0     | 0     | 0       | 1       | 0       | 1       | 0     | 1     | 0     | 1     |
| 0     | 1     | 0     | 1     | 0       | 1       | 1       | 0       | 0     | 1     | 1     | 0     |
| 0     | 1     | 1     | 0     | 0       | 1       | 1       | 1       | 0     | 1     | 1     | 1     |
| 0     | 1     | 1     | 1     | 1       | 0       | 0       | 0       | 1     | 0     | 0     | 0     |
| 1     | 0     | 0     | 0     | 1       | 0       | 0       | 1       | 1     | 0     | 0     | 1     |
| 1     | 0     | 0     | 1     | 1       | 0       | 1       | 0       | 1     | 0     | 1     | 0     |
| 1     | 0     | 1     | 0     | 1       | 0       | 1       | 1       | 1     | 0     | 1     | 1     |
| 1     | 0     | 1     | 1     | 1       | 1       | 0       | 0       | 1     | 1     | 0     | 0     |
| 1     | 1     | 0     | 0     | 1       | 1       | 0       | 1       | 1     | 1     | 0     | 1     |
| 1     | 1     | 0     | 1     | 1       | 1       | 1       | 0       | 1     | 1     | 1     | 0     |
| 1     | 1     | 1     | 0     | 1       | 1       | 1       | 1       | 1     | 1     | 1     | 1     |
| 1     | 1     | 1     | 1     | 0       | 0       | 0       | 0       | 0     | 0     | 0     | 0     |

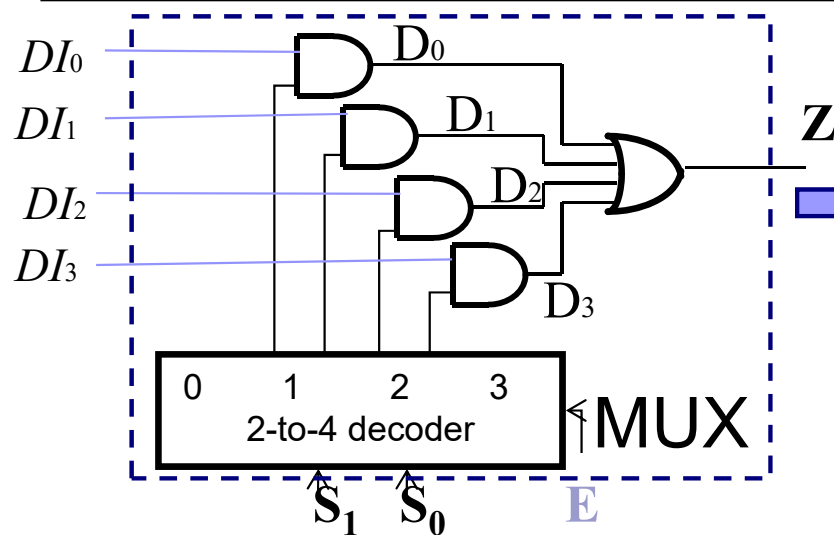


[illegible]

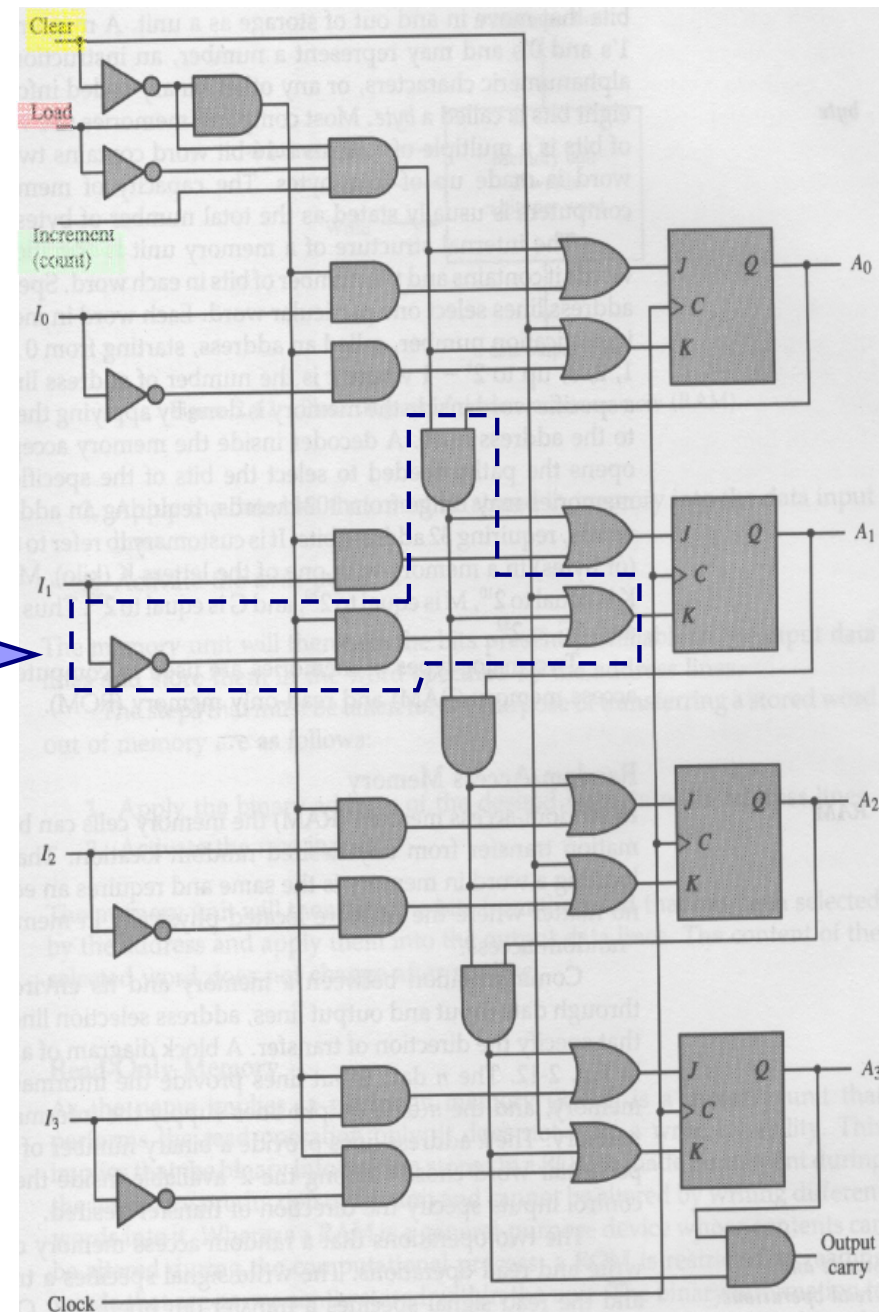
| $A_1 A_0$ | $D_k = Q_k^{n+1}$ | Function |
|-----------|-------------------|----------|
| 0 0       | $Q_k^n$           | Store    |
| 0 1       | $N_k$             | Count up |
| 1 0       | $DB_k$            | Load     |
| 1 1       | 0                 | Clear    |

# 4-bit Binary Counter with Parallel Load & Synchronous Clear with JK FF

|         | $A_1 A_0$ | $Q_k^{n+1}$ | Function             | $k = \{0,1,2,3\}$ |
|---------|-----------|-------------|----------------------|-------------------|
| $(f_0)$ | 0 0       | $Q_k^n$     | Store = No change    |                   |
| $(f_1)$ | 0 1       | $N_k$       | Increment (Count up) |                   |
| $(f_2)$ | 1 0       | $DB_k$      | Load                 |                   |
| $(f_3)$ | 1 1       | 0           | Clear                |                   |



| Clock | Clear | Load | Increment | Operation            |
|-------|-------|------|-----------|----------------------|
| ↑     | 0     | 0    | 0         | No change            |
| ↑     | 0     | 0    | 1         | Increment count by 1 |
| ↑     | 0     | 1    | x         | Load inputs          |
| ↑     | 1     | x    | x         | Clear outputs to 0   |



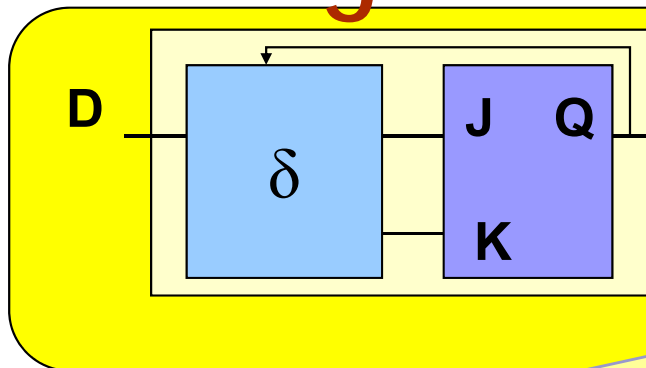


# Design D-Latch using JK FF

**START HERE**

JK Excitation Table

| $Q^t$ | $Q^{t+\Delta t}$ | $J^t$ | $K^t$ |
|-------|------------------|-------|-------|
| 0     | 0                | 0     | x     |
| 0     | 1                | 1     | x     |
| 1     | 0                | x     | 1     |
| 1     | 1                | x     | 0     |



| $D$ | $Q^n$ | $Q^{n+1}$ |
|-----|-------|-----------|
| 0   | 0     | 0         |
| 0   | 1     | 0         |
| 1   | 0     | 1         |
| 1   | 1     | 1         |

**Given:**  
D-Latch  
Characteristic  
Table

**Step 1: Initial  
State table**

**State table** of Sequential  
Circuit to be Designed

| $D$ | $Q^n$ | $Q^{n+1}$ | $J$ | $K$ |
|-----|-------|-----------|-----|-----|
| 0   | 0     | 0         | 0   | x   |
| 0   | 1     | 0         | x   | 1   |
| 1   | 0     | 1         | 1   | x   |
| 1   | 1     | 1         | x   | 0   |

**Excitation table** for  
Sequential Circuit to be Designed

**Step 3**

| $J$ | $D$ | $Q^n$ | 0              | 1              |
|-----|-----|-------|----------------|----------------|
| 0   | 0   | 0     | 0 <sup>0</sup> | 0 <sup>1</sup> |
| 1   | 1   | 0     | 1 <sup>2</sup> | x <sup>3</sup> |

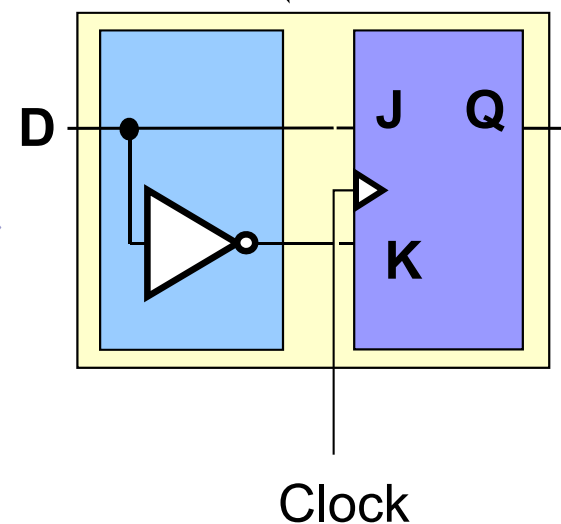
| $K$ | $D$ | $Q^n$ | 0              | 1              |
|-----|-----|-------|----------------|----------------|
| 0   | 0   | 0     | x <sup>0</sup> | 1 <sup>1</sup> |
| 1   | 1   | 0     | x <sup>2</sup> | 0 <sup>3</sup> |

**Step 4: SR input  
equations**

$$J = D$$

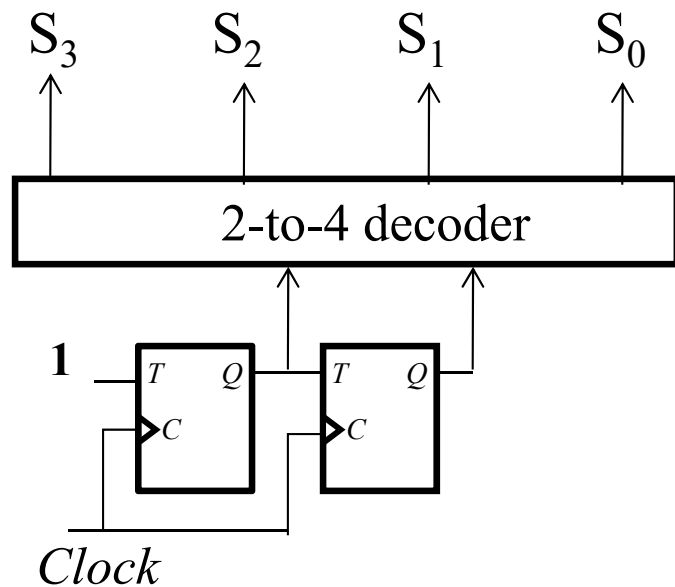
$$K = \bar{D}$$

**Step 5**

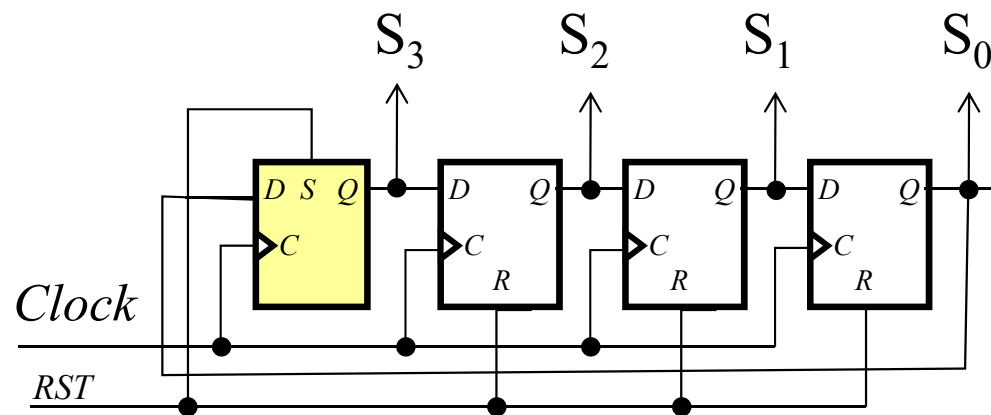


## State Encoding mod 4 counter

**Full Encoding:**  
BINARY COUNTER



**1-hot Encoding:**  
RING COUNTER





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Canada's university

# Memory Unit

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Université d'Ottawa | University of Ottawa

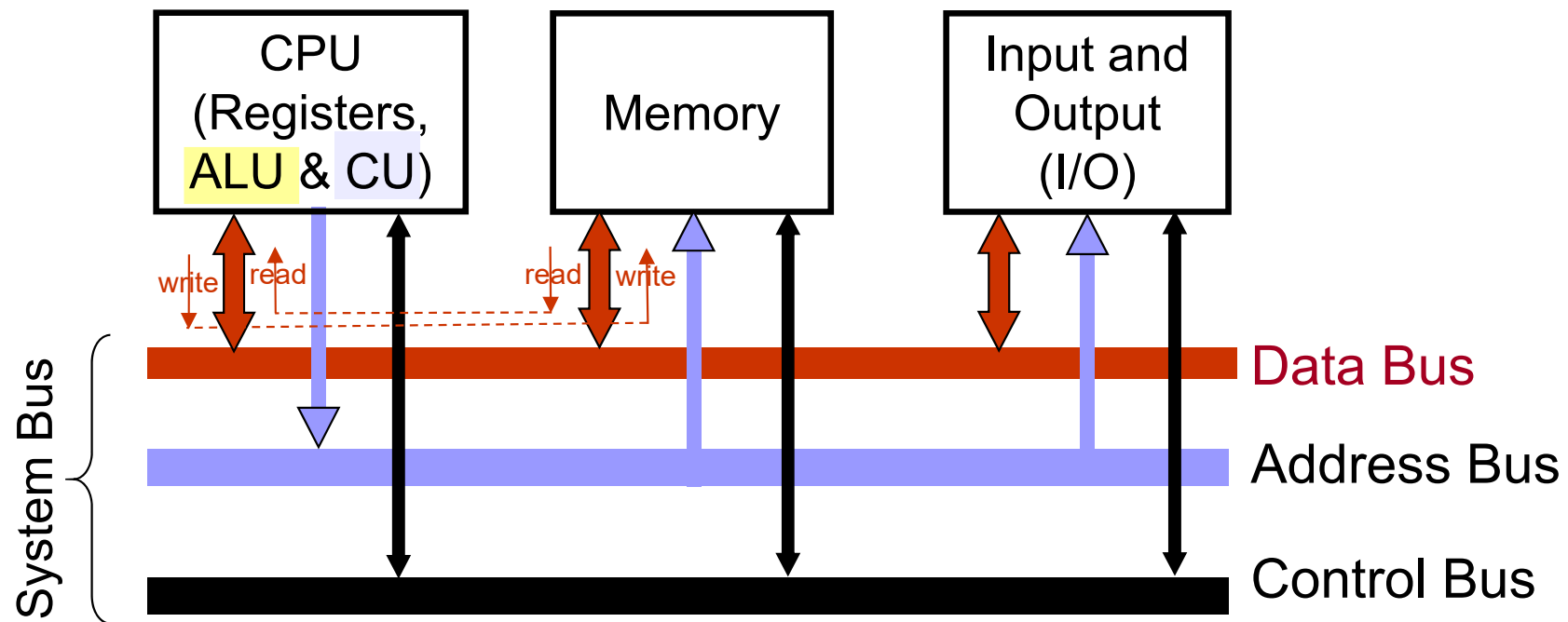
[www.uOttawa.ca](http://www.uOttawa.ca)



# Outline

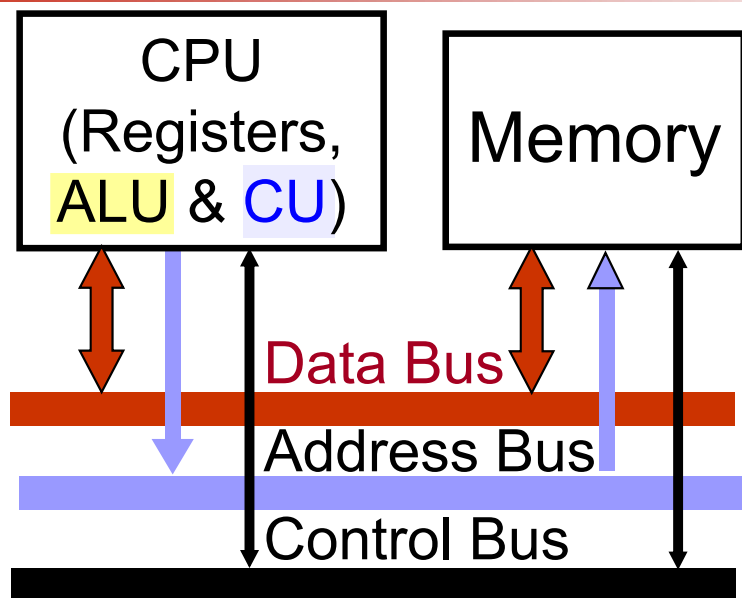
- The System Bus Model of a Computer
- Memory general Characteristics
- RAM (Random Access Memory)
- ROM (Read Only Memory)
- Memory design
- Memory hierarchy

# The System Bus Model of a Computer

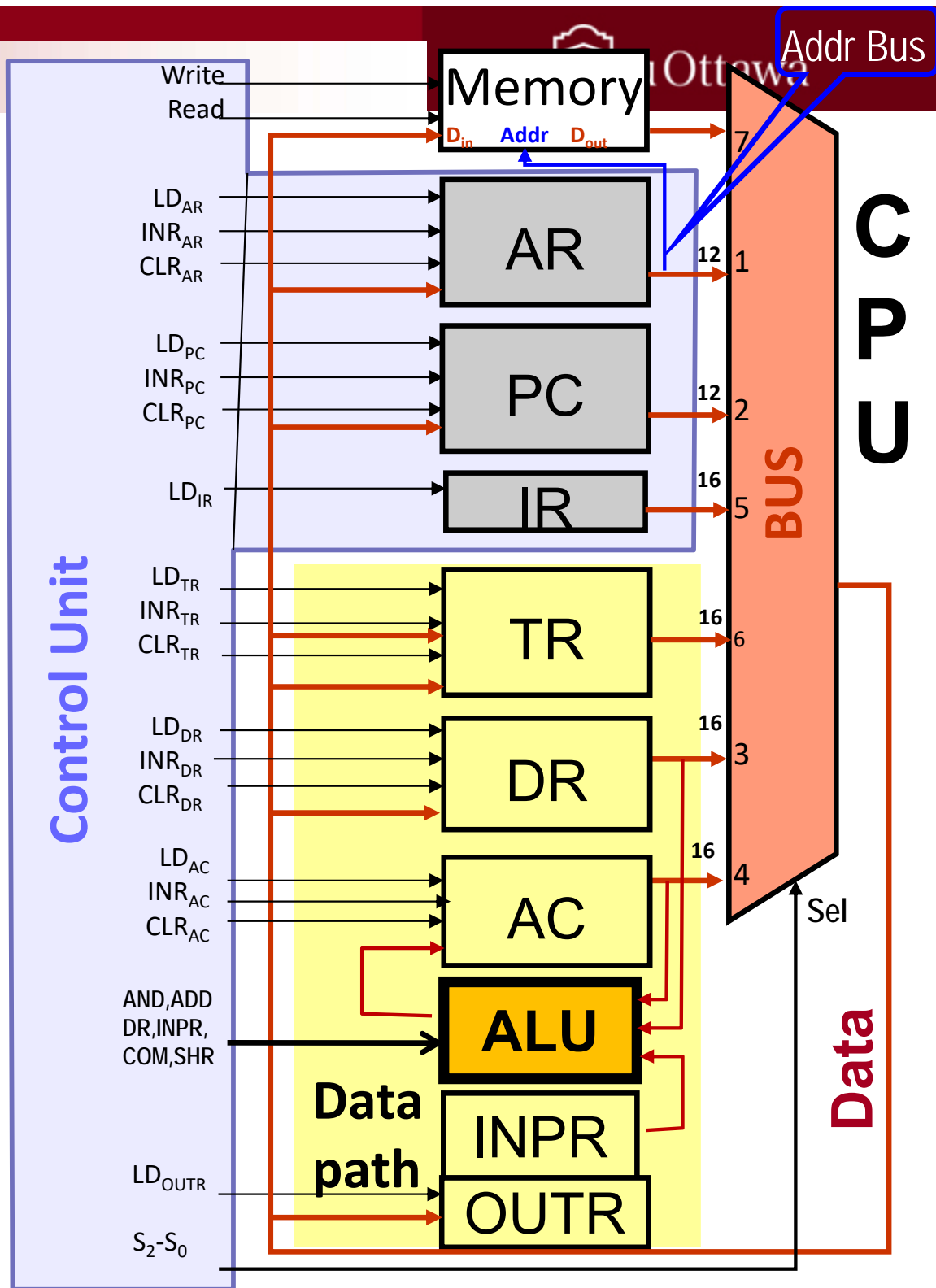


- The bus connects the CPU with other parts and reduces connections
- CPU puts address on the Bus and memory or I/O block receive address.
- Each instruction is **fetched** into the CPU from memory (read sequentially, i.e., one instruction at a time) and then **executed** mostly by the ALU.
- Control Unit manages transfer of instructions & data through the Control Bus
- The output is displayed on output device such as CRT

## BASIC COMPUTER



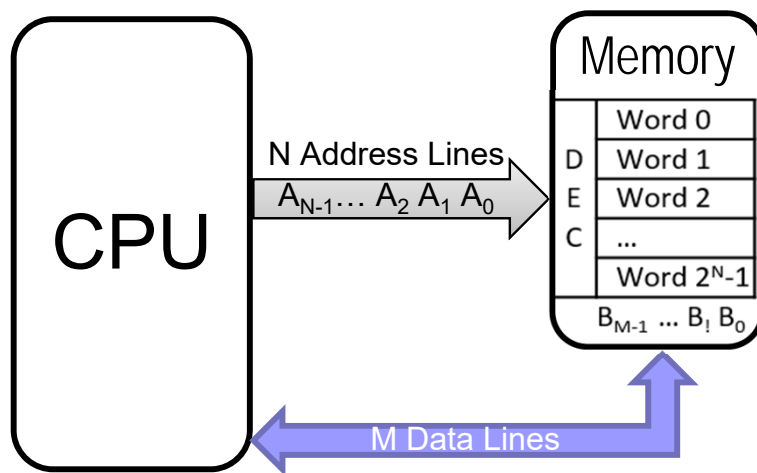
Most registers of the Basic Computer are implemented on the basis of the logic diagram of the multifunctional registers designed before.



# Memory

- A computer has a Central Processing Unit (CPU) and a memory.
- The memory stores the data and the CPU can read (extract or fetch) the data from computer memory for processing, or, it can write (store) the data onto the computer memory.
- The memory can be seen as a set of registers of the same length that store binary data, called “words”. Each memory location (i.e., such a register) stores a word and has an address.

- The computer uses the address lines to locate the specific data word in the computer memory. Also, it uses the data lines to write a word into the memory location specified by the address lines, or to read a stored word from a memory location, also specified by the address lines, as shown in the figure.



- It can be noted from the figure above that the address lines run from CPU to memory, i.e., the address lines are unidirectional, and the data lines are bidirectional, i.e. CPU uses the data lines to both read from memory, or to write the data onto the memory.

# Memory Unit

- Memories are collection of *registers* together with associated circuits needed to transfer information in and out of storage.
- The memory stores binary information in groups of bits called **words**.
- Each *memory location* (register) holds one “word” that
  - ☐ can be read or written into the memory
  - ☐ is assigned a **unique** identification number called an **address**
    - addresses are represented as binary vectors, consecutively numbered
    - if *address* is encoded with  $k$  bits, memory can have a capacity of  $2^k$  words
- *Data* is transferred to/from memory in multiples of words; i.e., it is NOT possible to read or write more or less bits than the size of the word
- One can access memory using only one address at a time, while simultaneous readings and writings are not possible
- A word in memory may contain any type of binary information that fits its size (e.g., a number, an instruction code, a memory address, or one or more alphanumeric characters)
- The internal structure of a memory is specified by the number of words it contains and the number of bits in each word.

| Address<br>K bits | Location=<br>M bit<br>word |
|-------------------|----------------------------|
| 0000              | WORD 0                     |
| 0001              | WORD 1                     |
| 0010              | WORD 2                     |
| 0011              | WORD 3                     |
| ...               | ...                        |
| $(2^k-1)_2$       | WORD $2^k-1$               |



# Memory Capacity

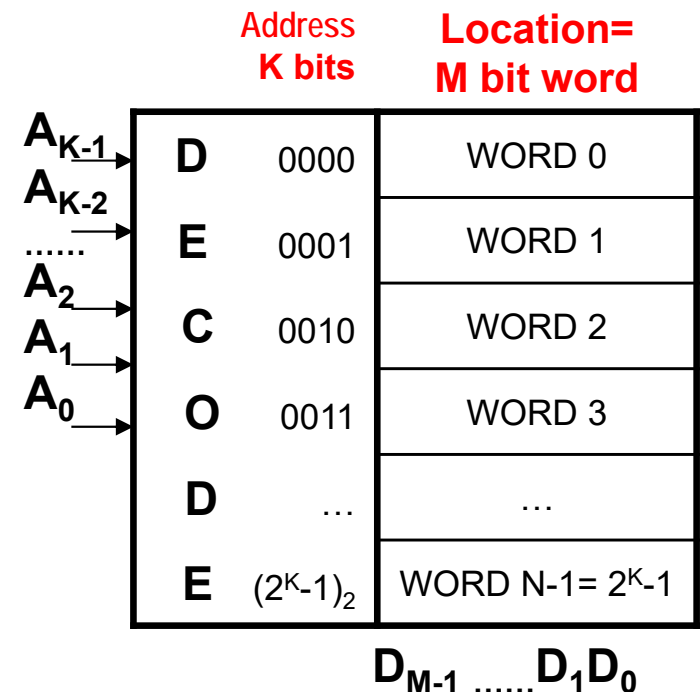
- Capacity = memory size = amount of data (measured in bits, bytes, words) stored in a memory.

- The memory size is generally specified as:

**N x M**

where,

- N is the number of words stored in memory
- M is the length (number of bits) of each word
- K address lines, with  $2^K = N$ , allows accessing any of the N words
- For example, a memory chip of capacity 1024 x 8 means that the memory is capable of storing 1024 words where each word is of 8 bits or 1 byte.
- Further, in order to address 1024 x 8 memory words, 10 address lines are required ( $2^{10} = 1024$ )



# Data

|                        |  |
|------------------------|--|
| Bit                    | 0  |
| Nibble                 | 0110   |
| Byte                   | 10110000   |
| 16-bit word (halfword) | 11001001 01000110  |
| 32-bit word            | 10110100 00110101 10011001 01011000  |
| 64-bit word (double)   | 01011000 01010101 10110000 11110011<br>11001110 11101110 01111000 00110101   |
| 128-bit word (quad)    | 01011000 01010101 10110000 11110011<br>11001110 11101110 01111000 00110101<br>00001011 10100110 11110010 11100110<br>10100100 01000100 10100101 01010001 |

- A byte is a group of 8 bits       $\Rightarrow 16 \text{ bits} = 2 \text{ bytes}$        $32 \text{ bits} = 4 \text{ bytes}$
- $1K(\text{kilo}) = 2^{10}$        $1M(\text{mega}) = 2^{20}$        $1G(\text{giga}) = 2^{30}$
- $\Rightarrow 64K = 2^6K = 2^6 \times 2^{10} = 2^{16}$

# MEMORIES

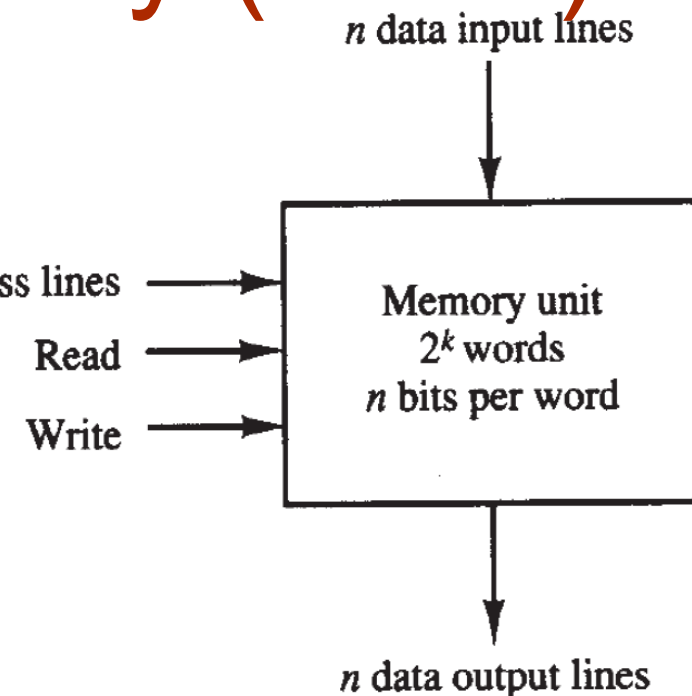
## Memory Technologies:

- Random Access Memory (RAM) - volatile
  - Static RAM (SRAM) – latches in an array of registers
  - Dynamic RAM (DRAM) – MOSFET “capacitors”
- Read Only Memory (ROM) – permanent (not programmable)
- Programmable ROM (PROM) – “fuse” principle
- EPROM – permanent, but erasable & reprogrammable
  - UV-EPROM
  - EEPROM
    - FLASH memory – erase all cells of the memory array at once
    - EEPROM – erase smaller blocks of the whole array

# Random-Access Memory (RAM)

■ Accessing the RAM is achieved through

- data input and output lines,
- address lines (to select which word in the memory is to be accessed), and
- control lines that specify the type of access (Read, Write) and, as such, the direction of information transfer.



■ The internal structure of a memory is specified by the number of words it contains and the number of bits in each word ( $n$ ).

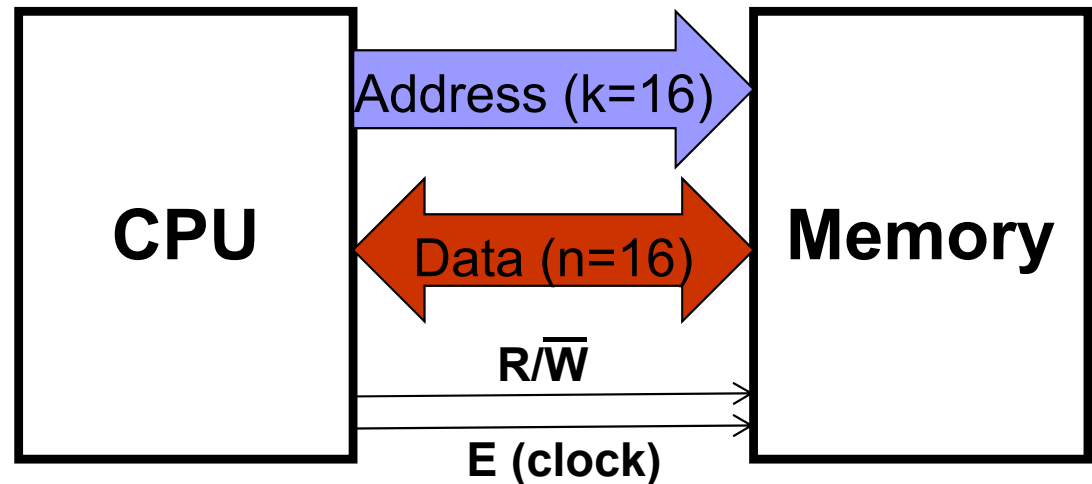
■ **Memory Capacity** = the total amount of stored information that a storage device can hold. It is expressed as a quantity of bits, bytes or words

■ For a memory unit with  $k$  address lines, there exists a maximum of  $2^k$  different words ( $n$ -bit long) with addresses ranging from 0 to  $2^k - 1$ ;

- e.g. a memory with 16 address lines has a capacity of  $2^{16}$  words ( $2^6 \cdot 2^{10} = 64$  k-words).

■ The time duration for accessing any word in RAM is independent of where that word is physically located in the memory. Thus the word “random-access memory”.

# Address, Data and Control Buses



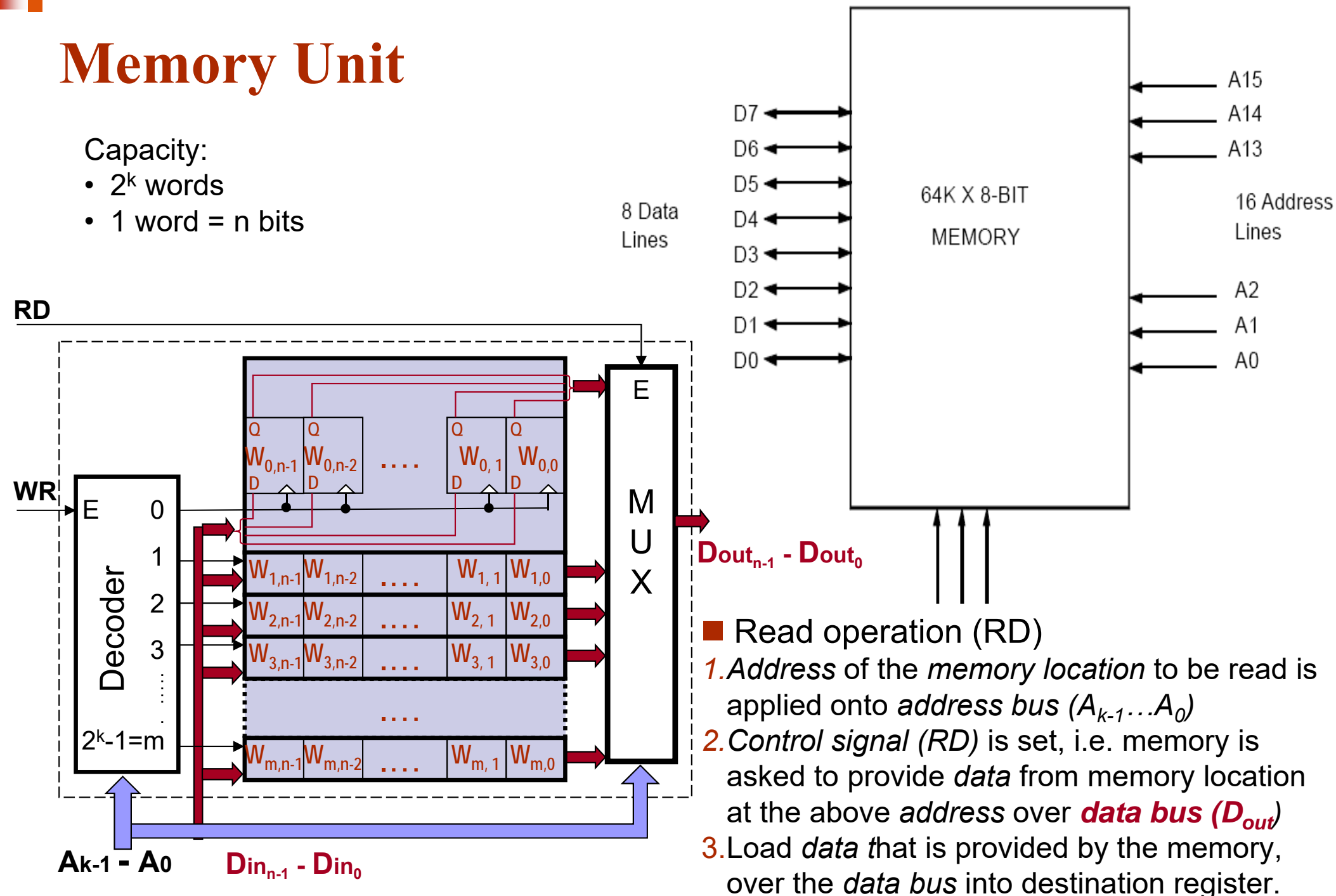
Example: if CPU has

- $k = 16$  bit **address bus**; i.e., CPU can access  $2^{16}$  memory locations
- $n = 16$  bit **data bus**; i.e., CPU can access one word of 16 bits (2 bytes) @ one memory location at a time,
- There are two types of operations a RAM can perform: **Read** and **Write**. These are specified by the control inputs (*Read* and *Write*)
- $R/\overline{W}$  tells memory if CPU is reading or writing
  - $R/\overline{W}$  high  $\Rightarrow$  Read
  - $R/\overline{W}$  low  $\Rightarrow$  Write

# Memory Unit

Capacity:

- $2^k$  words
- 1 word =  $n$  bits



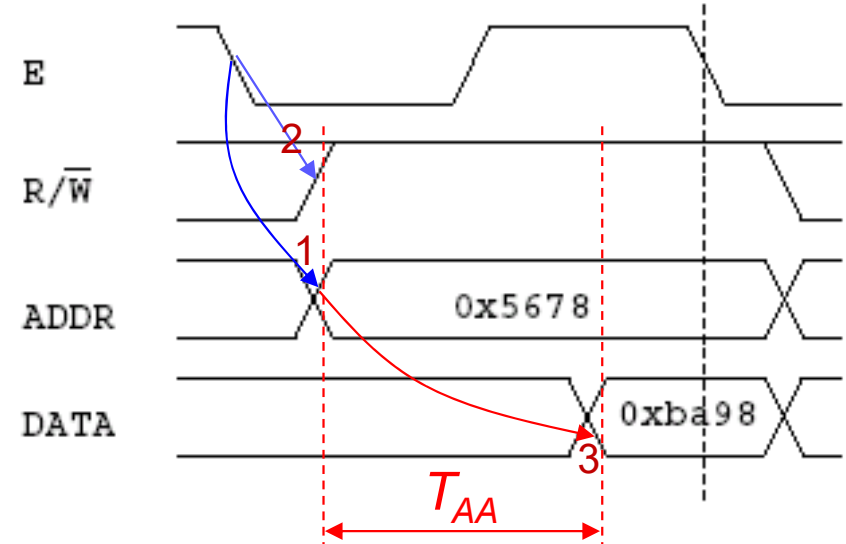
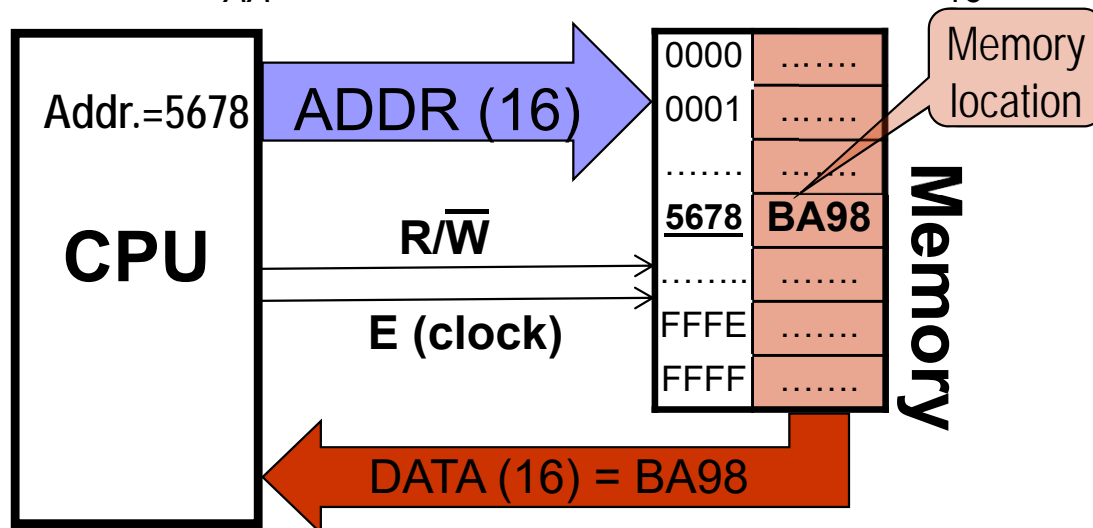
# Read Cycle

The steps to be taken to fetch a word out of RAM (read operation) are:

1. the *address* of the *memory location* which is to be read is applied onto the address lines ADDR.
2. the  $R/\overline{W}$  (Read/Write) control line is brought to high (1) to indicate a **read**
3. after **access time**  $T_{AA}$ , the memory will put on the *Data bus* the **DATA** read from the memory location specified by ADDR.

**Example:** Assuming that the memory location with address  $5678_{16}$  stores  $BA98_{16}$ , a CPU Read Cycle from that address will take place as follows:

1. CPU sends Address  $5678_{16}$  (0101 0110 0111 1000) over 16 ADDR lines to Memory
2. CPU asserts  $R/\overline{W}=1$  meaning it wants to read the content of location at address  $5678_{16}$
3. After  $T_{AA}$  memory sends to CPU  $BA98_{16}$ , i.e., the contents of memory location  $5678_{16}$



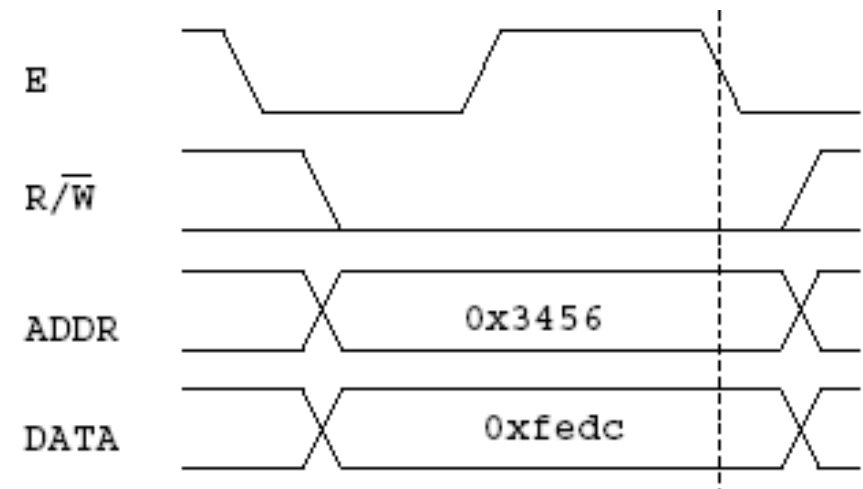
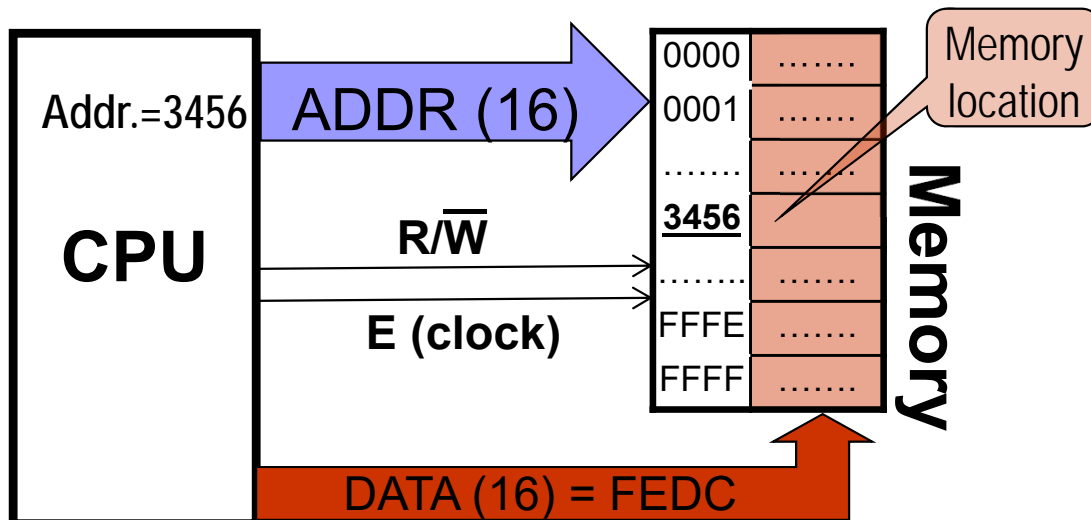
# Write Cycle

The steps to be taken to store a word into RAM (write operation) are the following:

1. CPU applies the binary vector address (**ADDR**) of the desired memory location into the address lines;
2. apply the **DATA** bits, that must be stored in memory, into the data input lines;
3. bring the  $\overline{R/W}$  (Read/Write) line low to indicate a **write** (activate the *Write* control input).

In the below example, the CPU expects that the memory location at the given address will latch the data on the falling edge of the E-clock, at the latest.

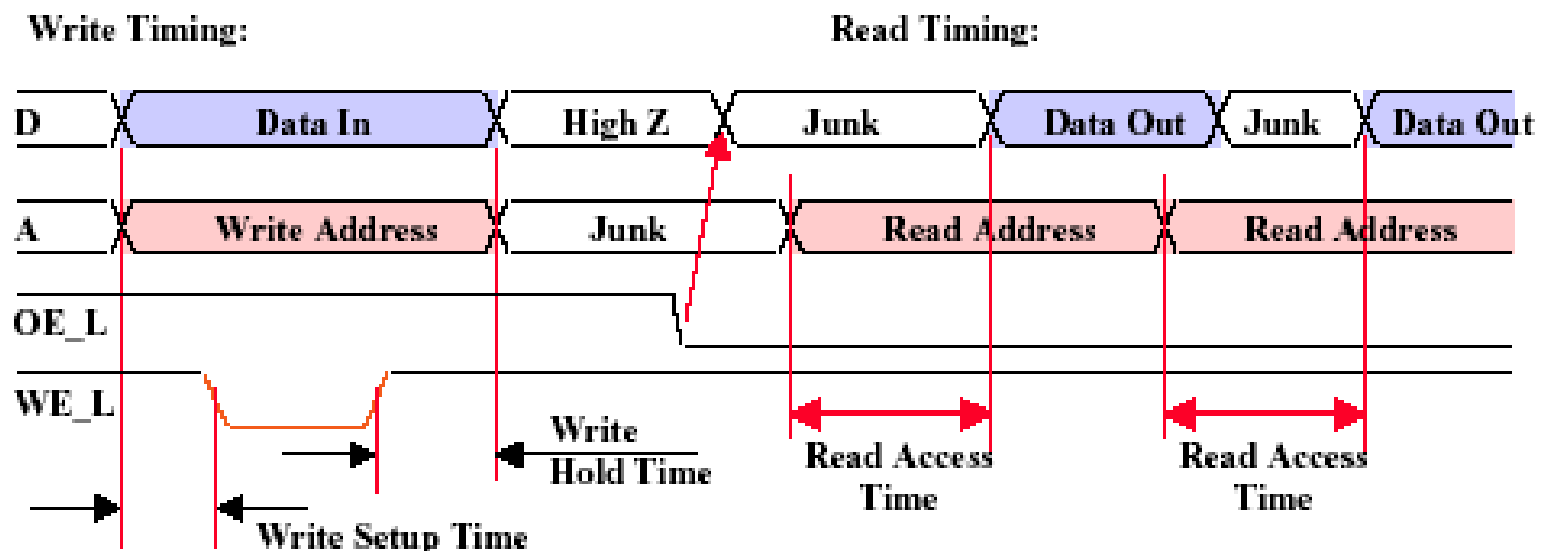
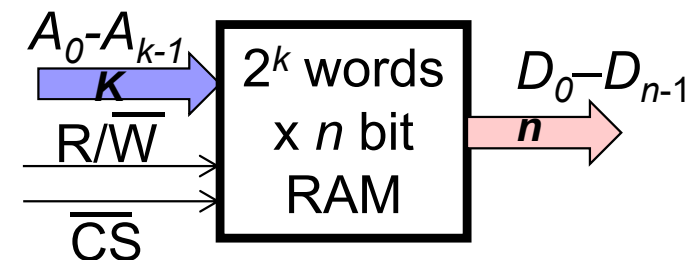
Example: Write 0xfedc to memory location at address 0x3456





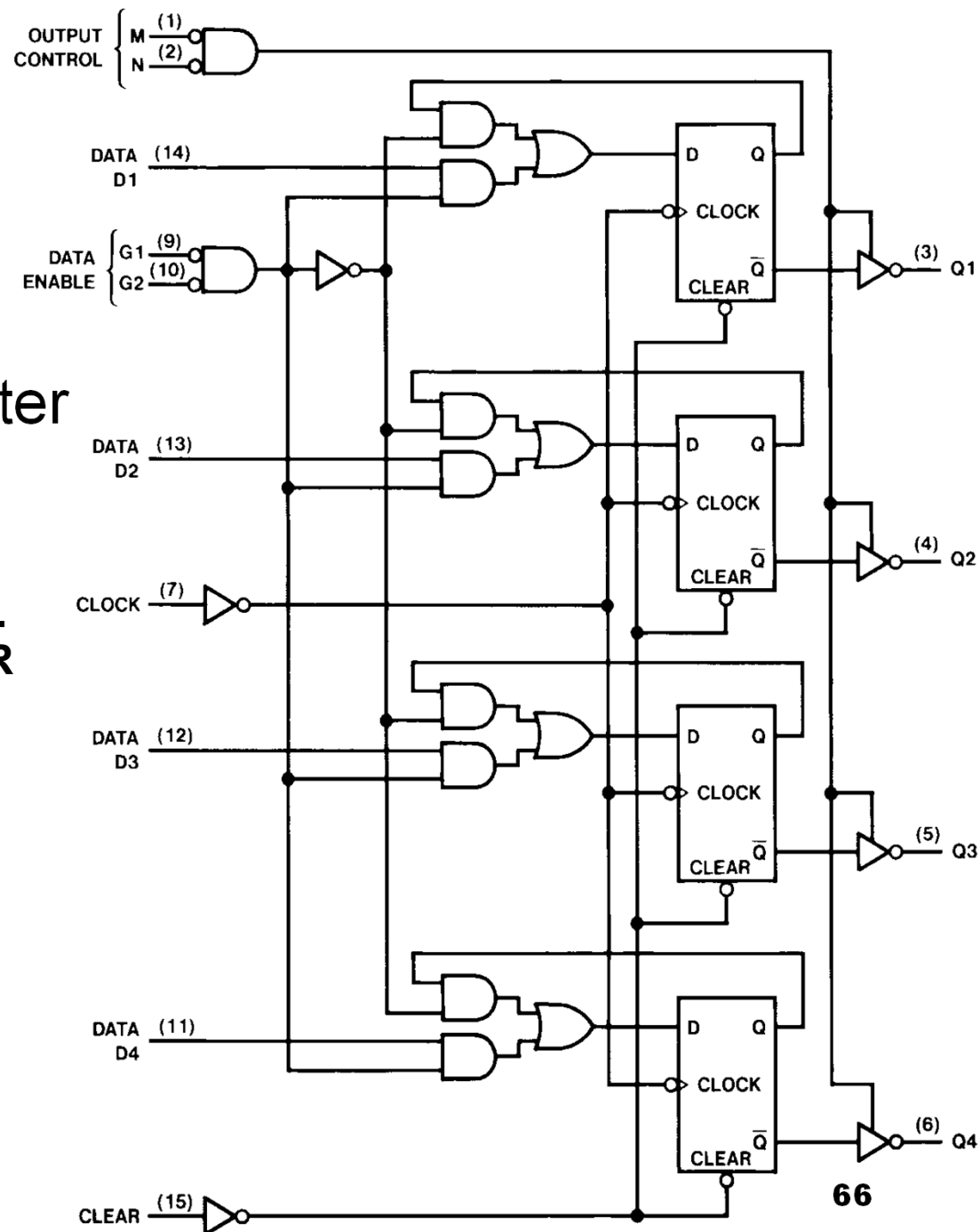
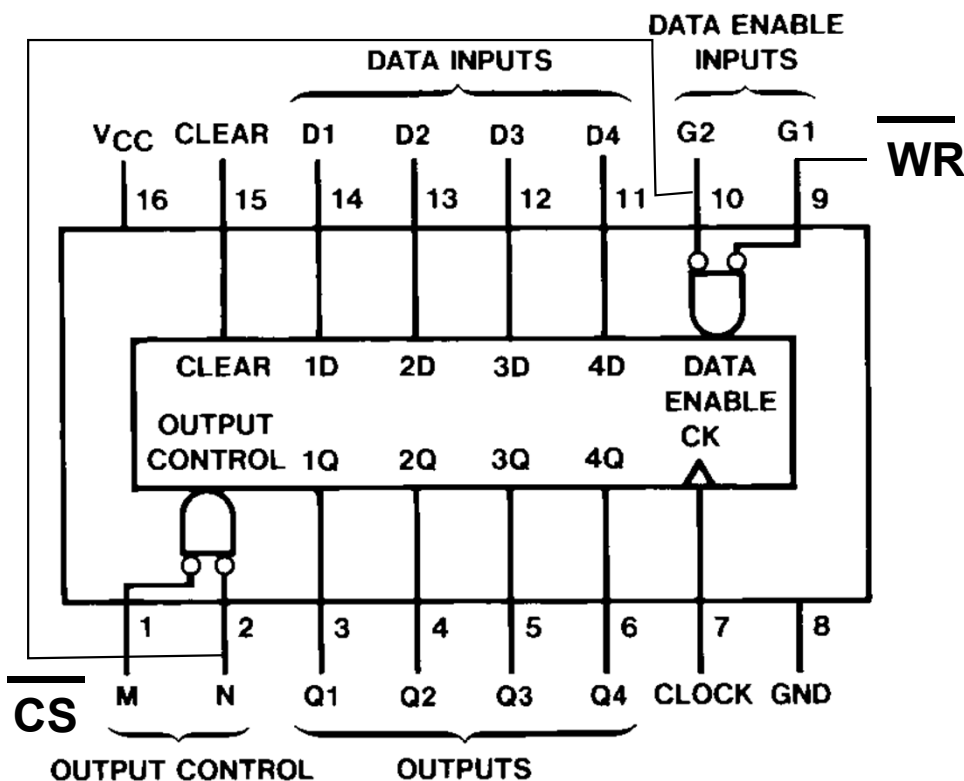
# RAM Timing

- The **access time** ( $T_{AA}$ ) is defined for reading, as the time delay from the moment when the address lines are made available to the time when the data become available at the output
- When reading data from a chip, after time period  $T_{AA}$ ,  $n$ -bit data word appears on data lines  $D_0 - D_{n-1}$
- When writing data to a chip the data lines must also be held for *Write Hold Time*



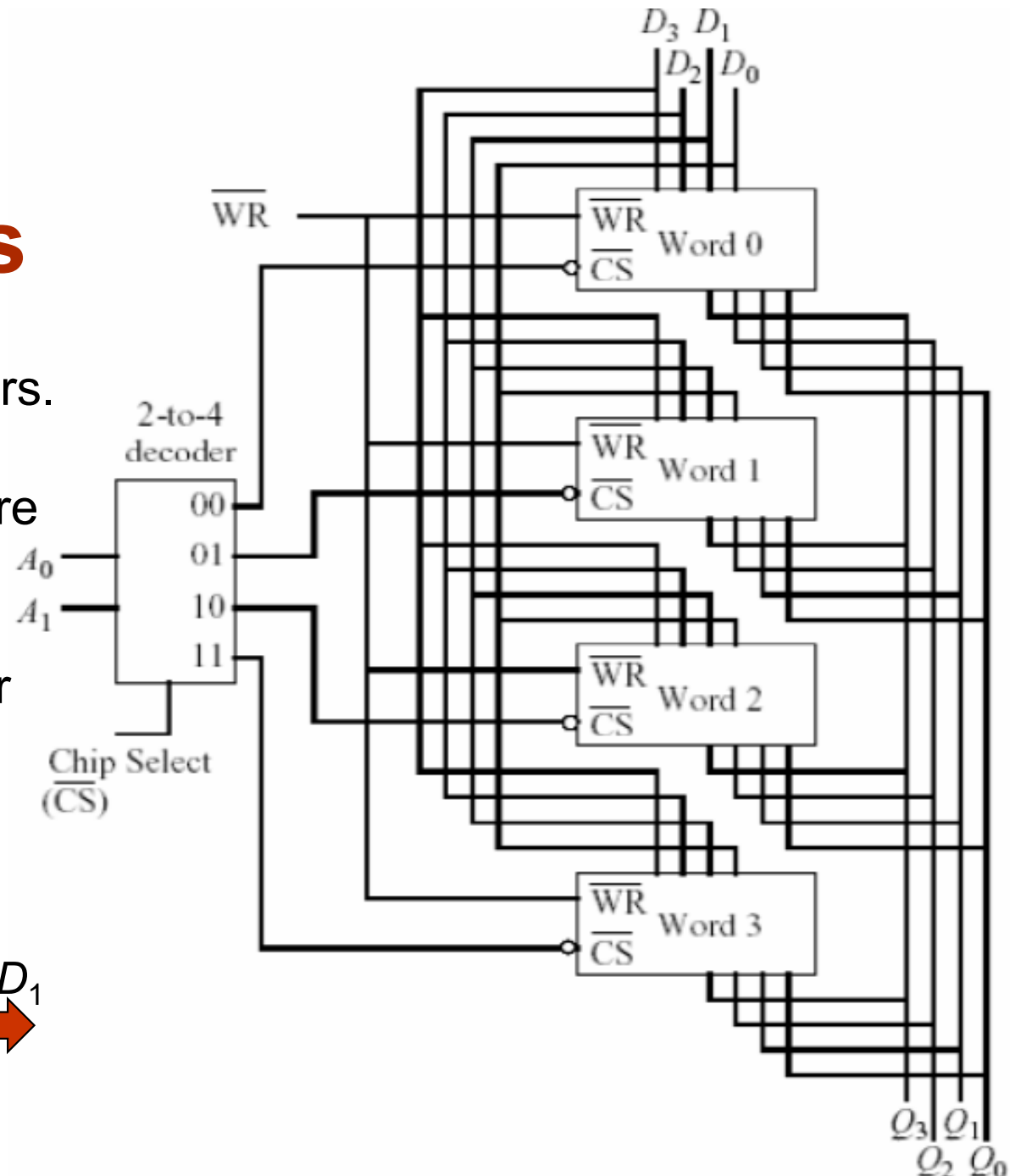
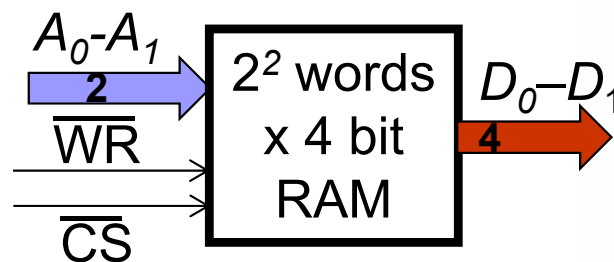
# RAM that stores 4-bit words

## ■ Basic “brick:” 74LS173 TRI-STATE 4-Bit D-Type Register



# RAM module of 4 words of 4 bits

- RAM is a collection of registers.
- Four bit registers (such as 74LS173) can be used to store the words
- Using address vector  $A_1, A_0$ , one word can be selected for reading or writing out of  $2^2$  memory locations



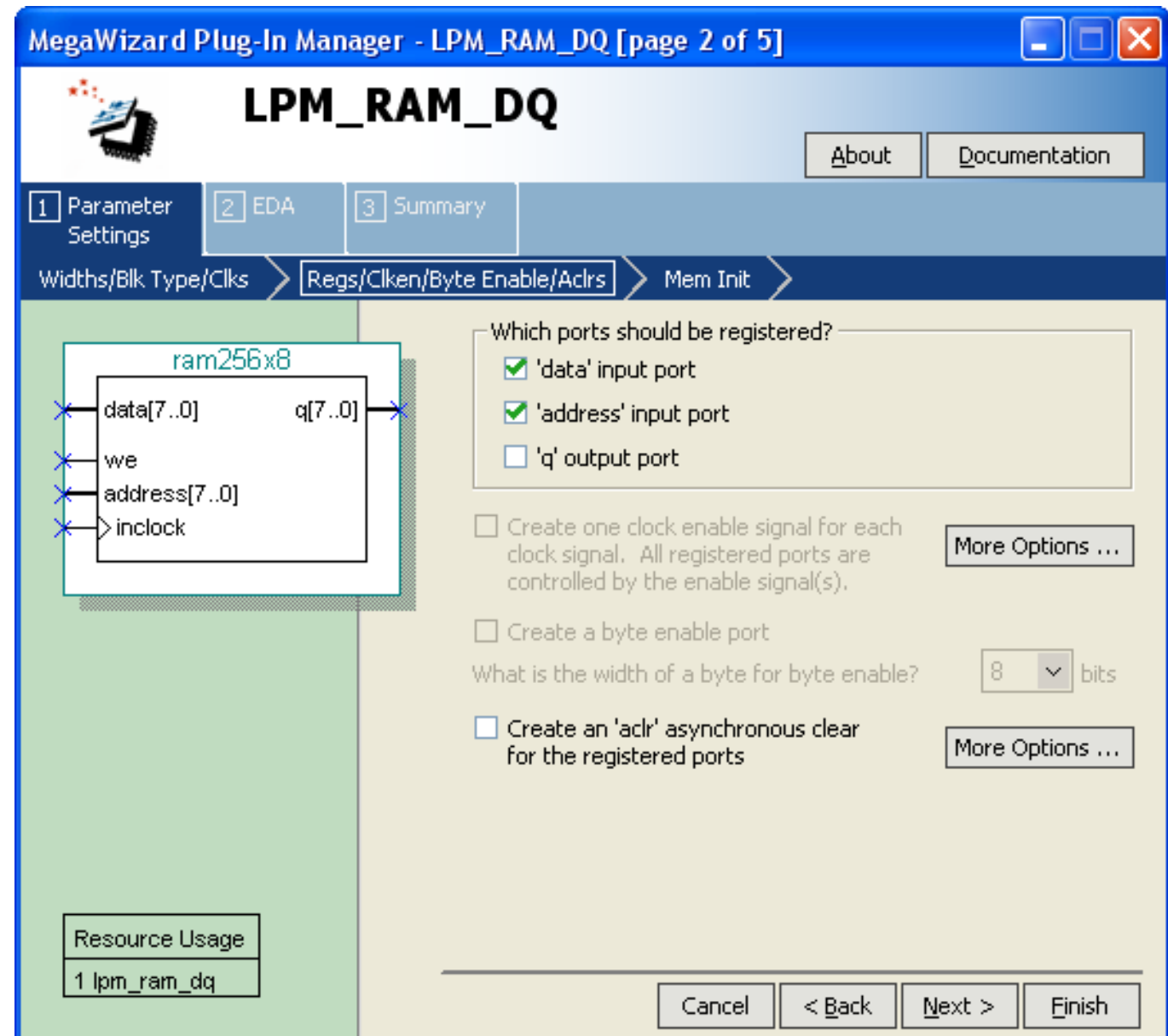
# Altera memory module (ram256x8)

## Capacity:

- 256 words
- 8-bit long

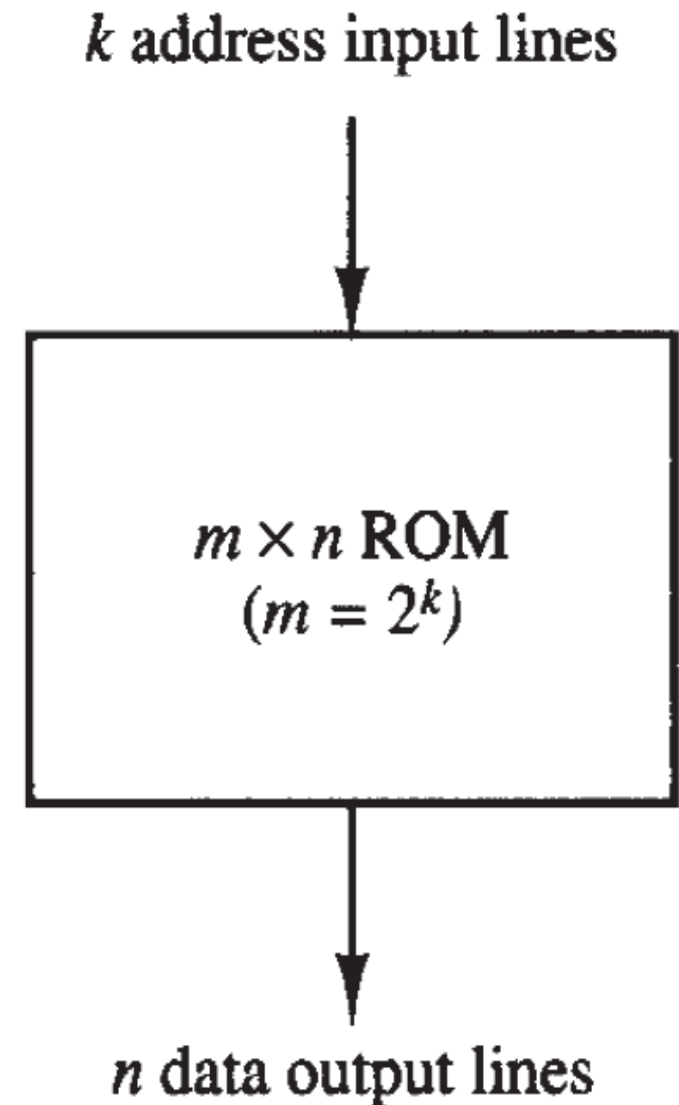
## Interface:

- Data in: data[7..0]
- Data out: q[7..0]
- address[7..0]
- inclock
- we



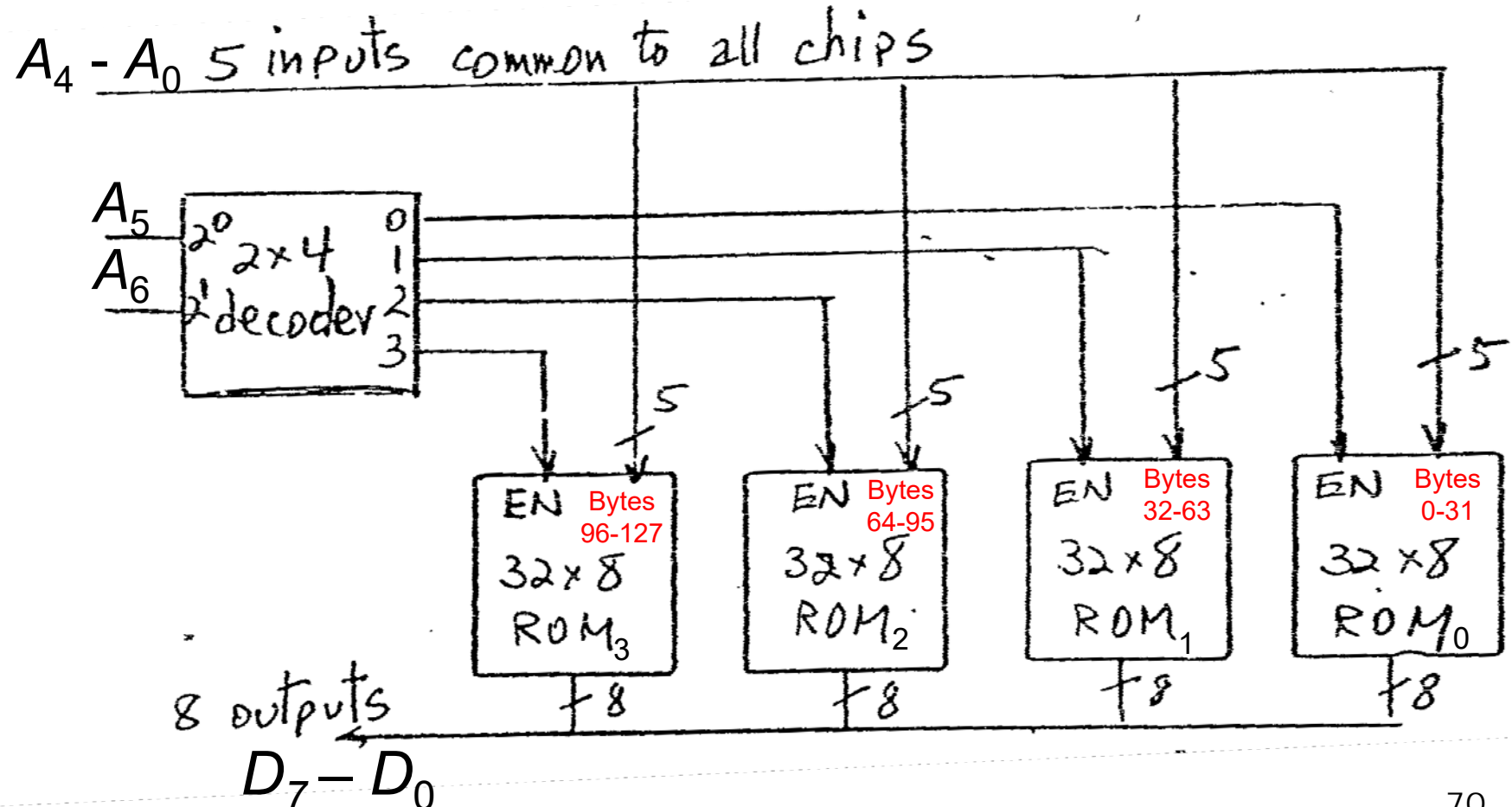
# Read-Only Memory (ROM)

- A Read-Only Memory (ROM) is a memory unit that can only perform read operations (it does not have a “write” capability).
- As such, a typical ROM has no data input lines nor control inputs.
- An  $m \times n$  ROM is an array of binary cells organized into  $m (= 2^k)$  words of  $n$  bits each, where  $k$  is the number of address bits.
- A ROM is classified as a combinational circuit.
- Figure: Block diagram of a typical ROM



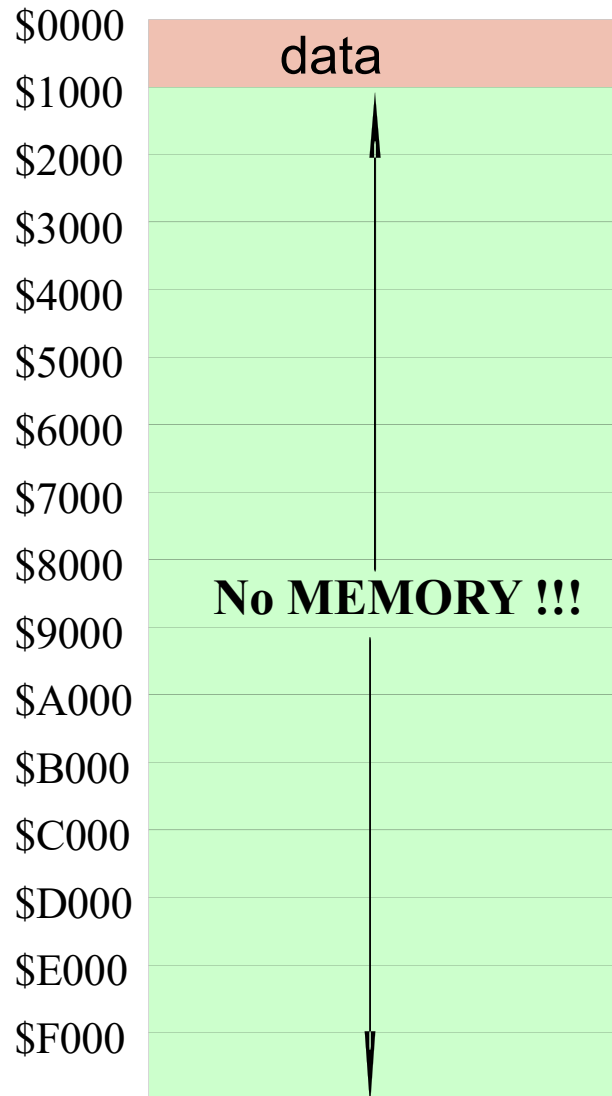
# ROM

Given a  $32 \times 8$  ROM chip with an enable input, show the external connections necessary to construct a  $128 \times 8$  ROM with four chips and a decoder.



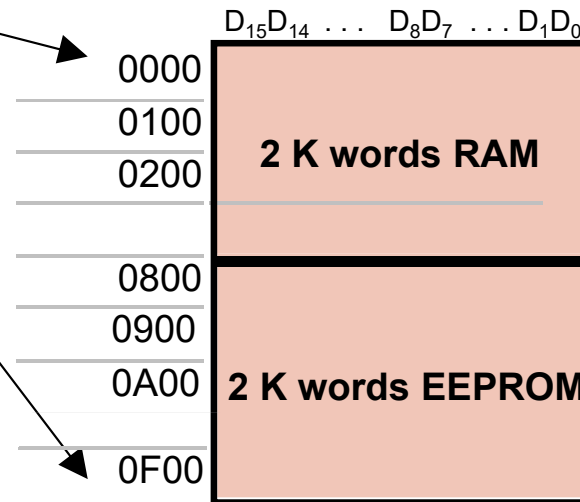
# Memory Map

address



Memory **map** shows how all memory addresses are used:

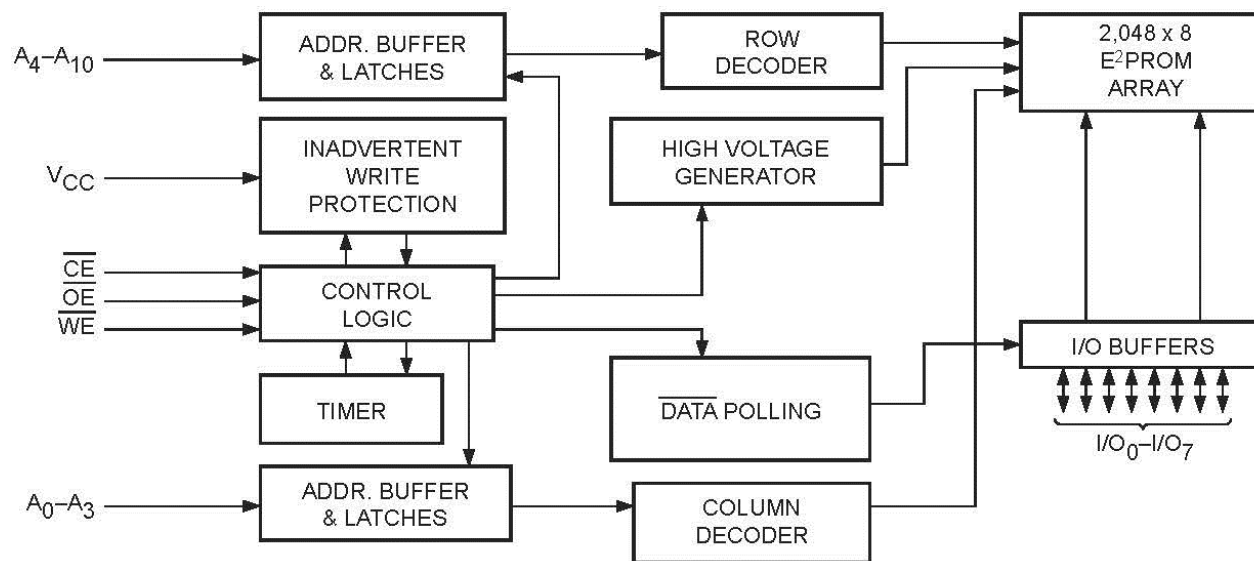
- A region may contain RAM
- Other region contains ROM
- Some regions may contain nothing



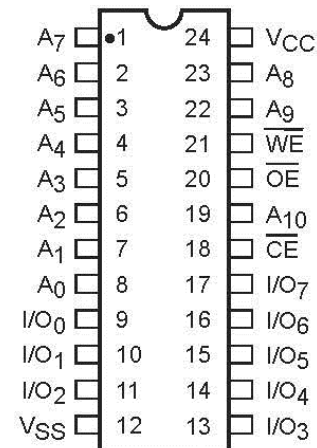
- ✓ Mano's **Basic Computer** has 12 bits for Address, so, its memory space is 4-kwords of 16 bits (2 bytes) each word, as shown above.
- ✓ Since this CPU has a 16 bit bus, it may have provisions for further expanding the memory to 64 k-words. Still, we want to build a memory as follows:
  - 1 K word RAM mapped to \$0000 - \$03FF
  - 1 K word RAM (\$0400 to \$07FF)
  - 2 K word EEPROM (\$0800 to \$0FFF)
  - 60 k words of **NOTHING** (\$1000 to \$FFFF)



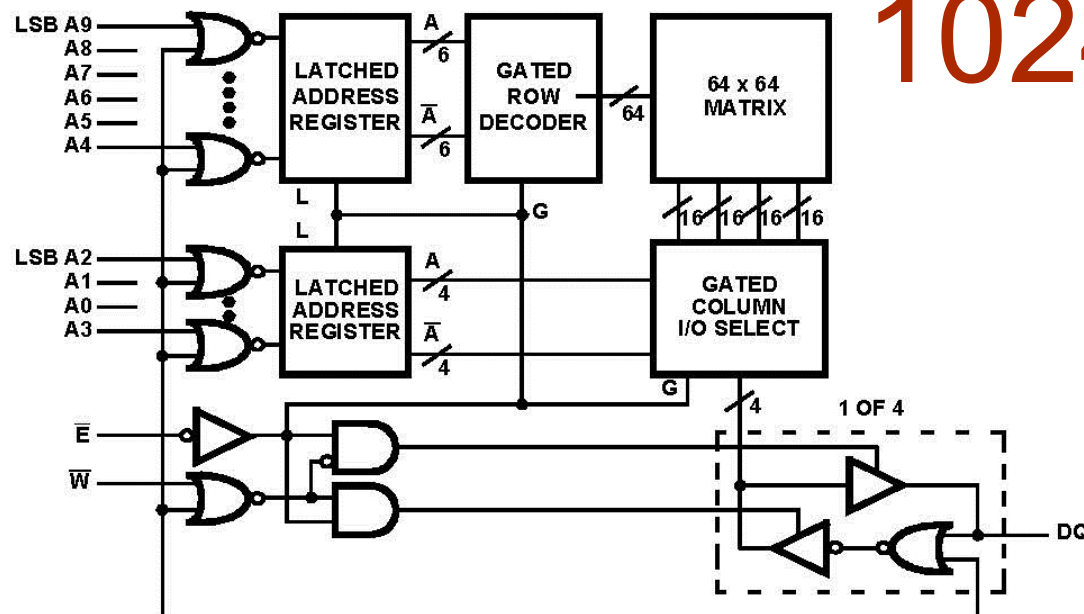
# 2048 x 8 CMOS E2PROM



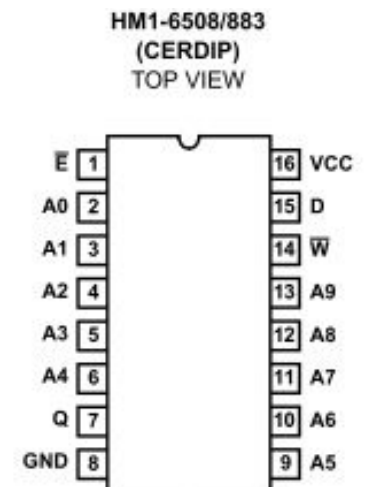
| Pin Name                           | Function            |
|------------------------------------|---------------------|
| A <sub>0</sub> -A <sub>10</sub>    | Address Inputs      |
| I/O <sub>0</sub> -I/O <sub>7</sub> | Data Inputs/Outputs |
| $\overline{CE}$                    | Chip Enable         |
| $\overline{OE}$                    | Output Enable       |
| $\overline{WE}$                    | Write Enable        |
| V <sub>cc</sub>                    | 5V Supply           |
| V <sub>ss</sub>                    | Ground              |
| NC                                 | No Connect          |



# 1024x4 CMOS RAM



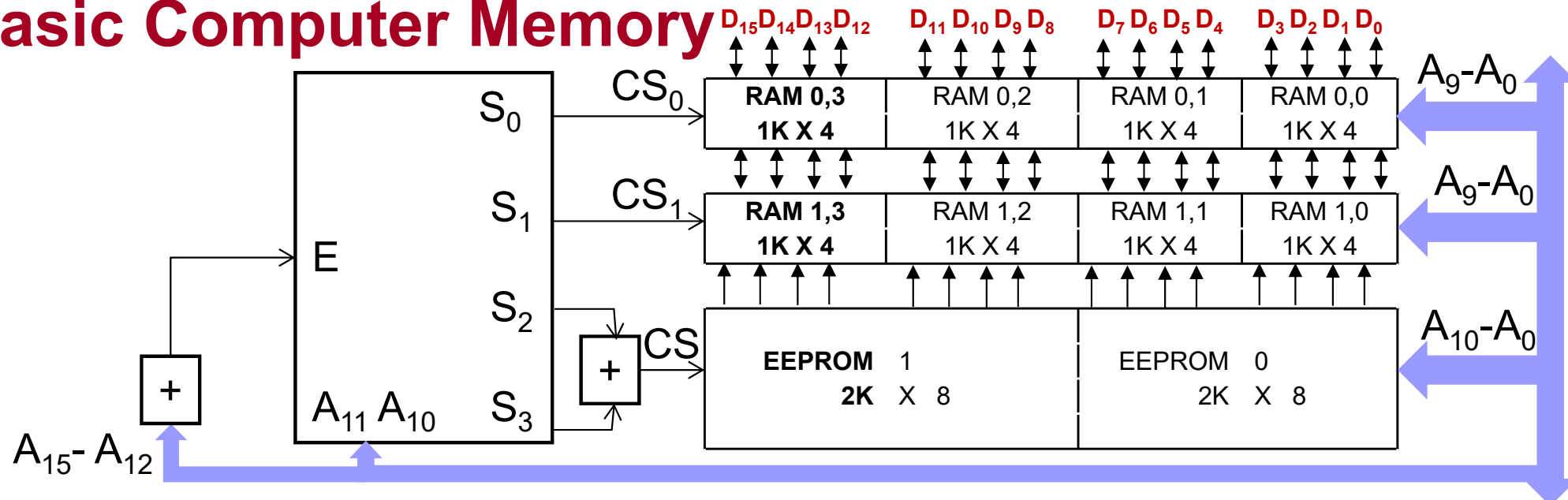
| PIN            | DESCRIPTION   |
|----------------|---------------|
| A              | Address Input |
| $\overline{E}$ | Chip Enable   |
| $\overline{W}$ | Write Enable  |
| D              | Data Input    |
| Q              | Data Output   |



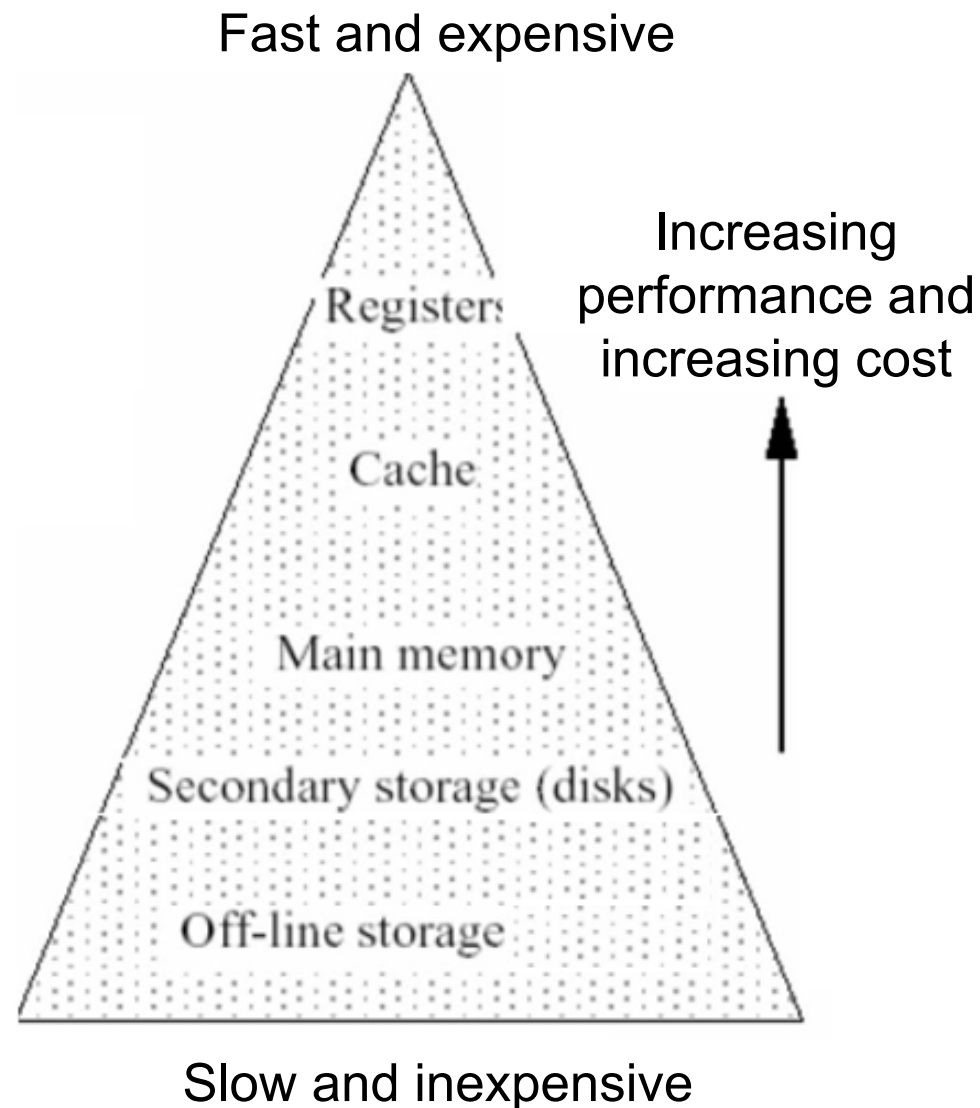


| ADDR | ADDR (HEX) | $A_{15}A_{14}A_{13}A_{12}$ | $A_{11}A_{10}A_9A_8$ | $A_7A_6A_5A_4$ | $A_3A_2A_1A_0$ | $D_{15}D_{14}D_{13}D_{12}$ | $D_{11}D_{10}D_9D_8$ | $D_7D_6D_5D_4$     | $D_3D_2D_1D_0$    |
|------|------------|----------------------------|----------------------|----------------|----------------|----------------------------|----------------------|--------------------|-------------------|
| 0    | 0000       | 0 0 0 0                    | 0 0 0 0              | 0 0 0 0        | 0 0 0 0        |                            |                      |                    |                   |
| 1    | 0001       | 0 0 0 0                    | 0 0 0 0              | 0 0 0 0        | 0 0 0 1        | RAM 0,3<br>1K X 4          | RAM 0,2<br>1K X 4    | RAM 0,1<br>1K X 4  | RAM 0,0<br>1K X 4 |
| ...  | ...        | ...                        | ...                  | ...            | ...            |                            |                      |                    |                   |
| 1023 | 03FF       | 0 0 0 0                    | 0 0 1 1              | 1 1 1 1        | 1 1 1 1        |                            |                      |                    |                   |
| 1024 | 0400       | 0 0 0 0                    | 0 1 0 0              | 0 0 0 0        | 0 0 0 0        |                            |                      |                    |                   |
| 1025 | 0401       | 0 0 0 0                    | 0 1 0 0              | 0 0 0 0        | 0 0 0 1        | RAM 1,3<br>1K X 4          | RAM 1,2<br>1K X 4    | RAM 1,1<br>1K X 4  | RAM 1,0<br>1K X 4 |
| ...  | ...        | ...                        | ...                  | ...            | ...            |                            |                      |                    |                   |
| 2047 | 07FF       | 0 0 0 0                    | 0 1 1 1              | 1 1 1 1        | 1 1 1 1        |                            |                      |                    |                   |
| 2048 | 0800       | 0 0 0 0                    | 1 0 0 0              | 0 0 0 0        | 0 0 0 0        |                            |                      |                    |                   |
| 2049 | 0801       | 0 0 0 0                    | 1 0 0 0              | 0 0 0 0        | 0 0 0 1        |                            |                      |                    |                   |
| ...  | ...        | ...                        | ...                  | ...            | ...            |                            |                      |                    |                   |
| ...  | 0BFF       | 0 0 0 0                    | 1 0 1 1              | 1 1 1 1        | 1 1 1 1        | EEPROM 1<br>2K X 8         |                      | EEPROM 0<br>2K X 8 |                   |
| ...  | 0C00       | 0 0 0 0                    | 1 1 0 0              | 0 0 0 0        | 0 0 0 0        |                            |                      |                    |                   |
| ...  | 0C01       | 0 0 0 0                    | 1 1 0 0              | 0 0 0 0        | 0 0 0 1        |                            |                      |                    |                   |
| ...  | ...        | ...                        | ...                  | ...            | ...            |                            |                      |                    |                   |
| 4095 | 0FFF       | 0 0 0 0                    | 1 1 1 1              | 1 1 1 1        | 1 1 1 1        |                            |                      |                    |                   |

## Basic Computer Memory



# Memory Hierarchy

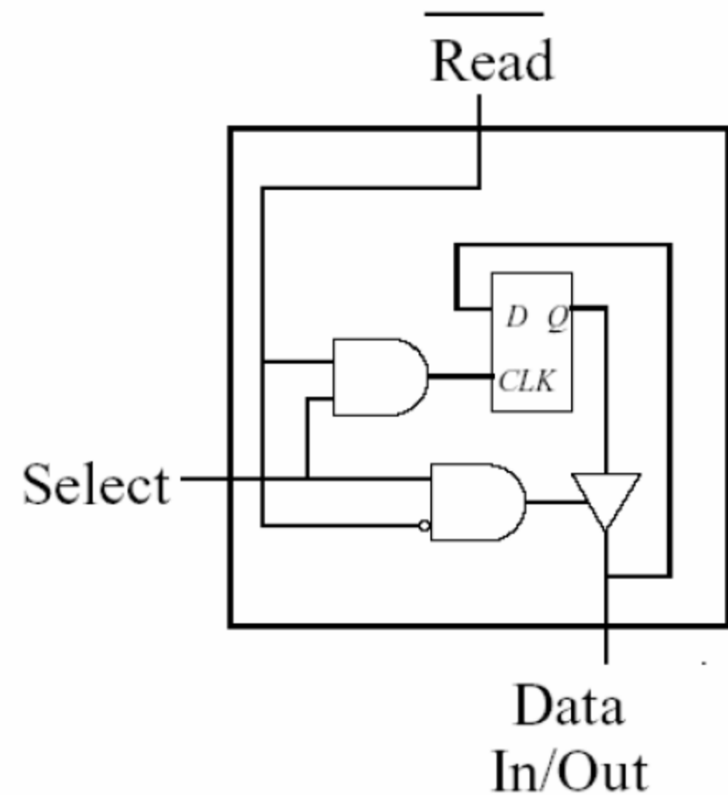


# Annex

# Static RAM (SRAM) cell

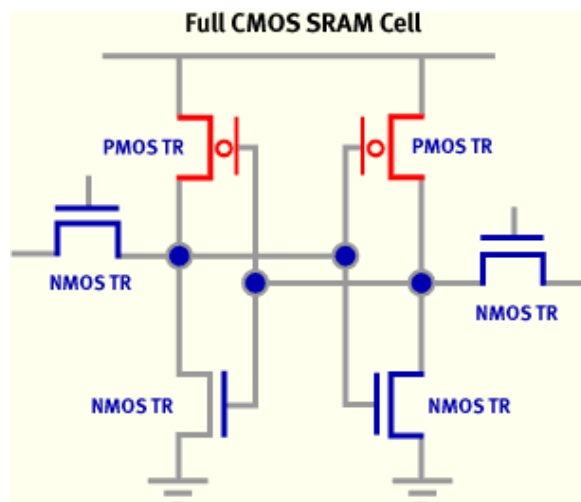
- Any location can be accessed in the same amount of time (RAM - Random Access Memory)
- The RAM chip based on D flip-flop with logic to allow the cell to select, read and written
- **Static** = a current flows through a branch of the latch
- Bi-directional line for data in and data out.
- RAM - static, content of each location persist as long as power is ON (volatile)

SRAM Cell  
logic diagram



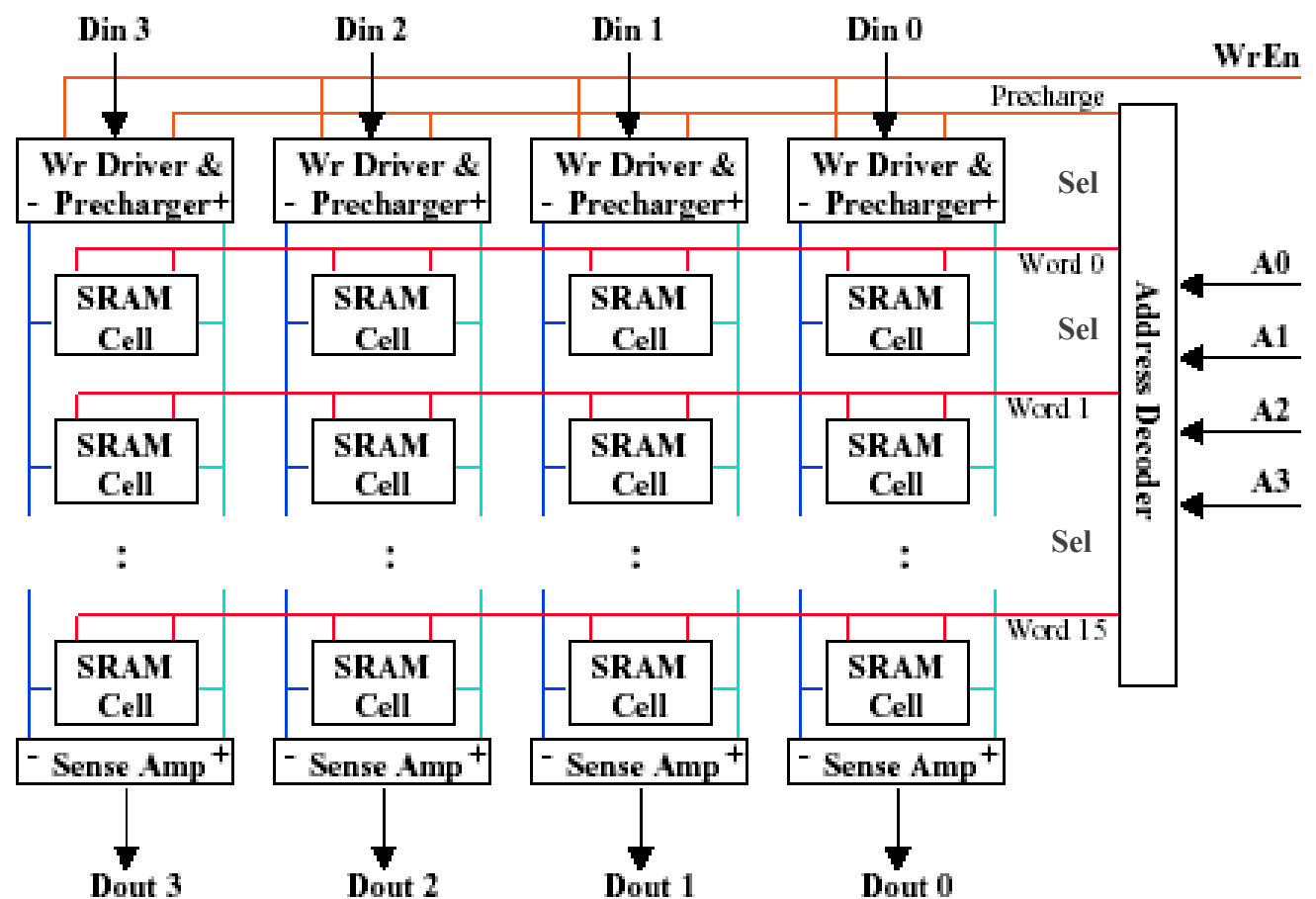
# SRAM (Static RAM )

## 6-T SRAM Cell electronic diagram

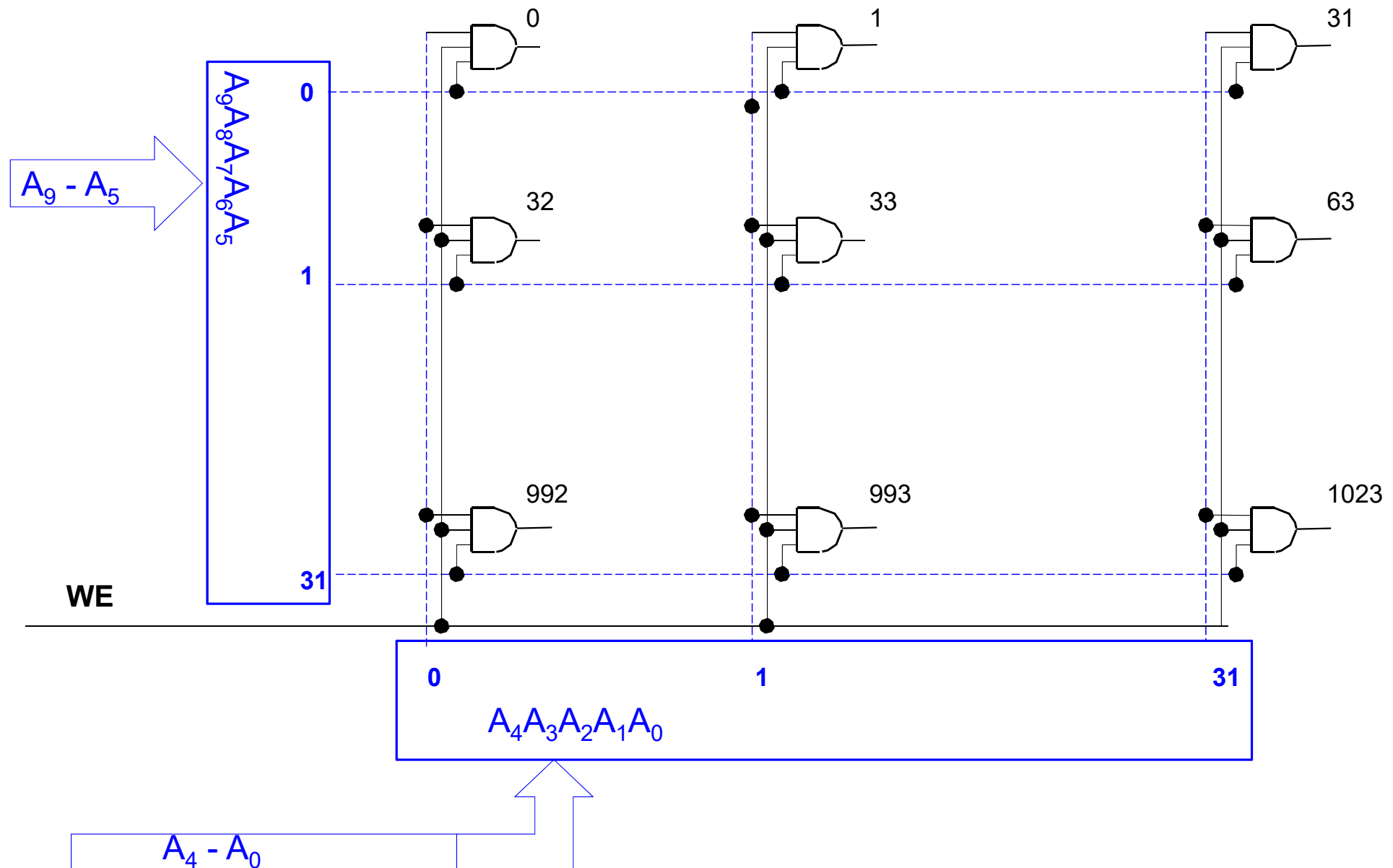


- Static: a current flows through a branch of the latch
- content will last “forever” (until lose power)
- Low density, high power, expensive, fast

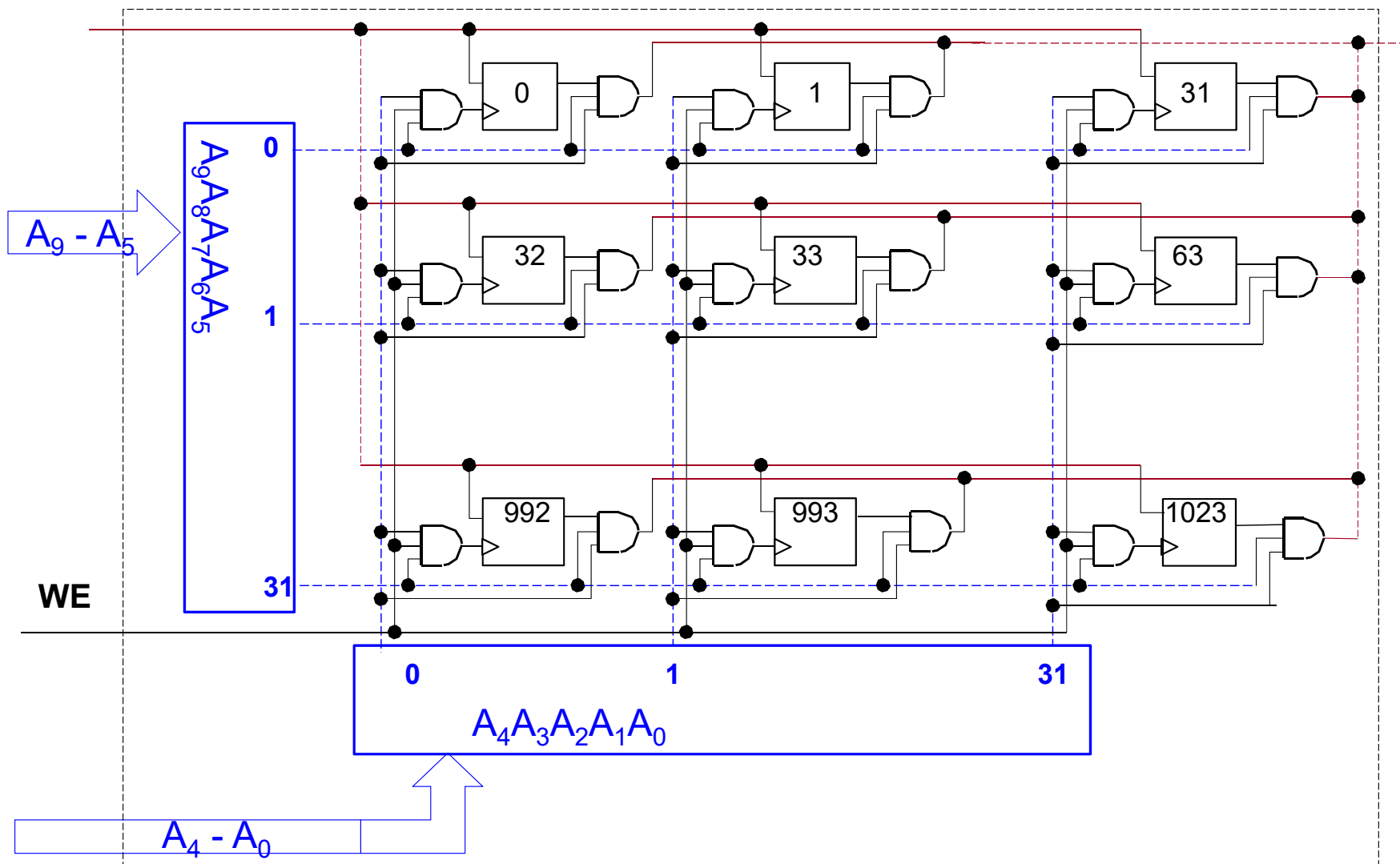
## SRAM block diagram



# Address Decoder = Matrix-type

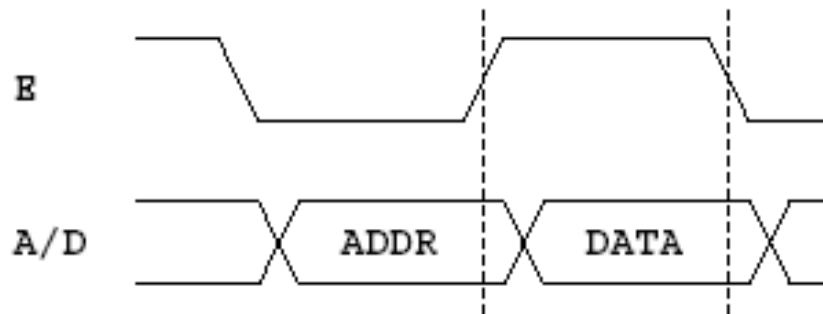


# 1 K x 1-Bit RAM module



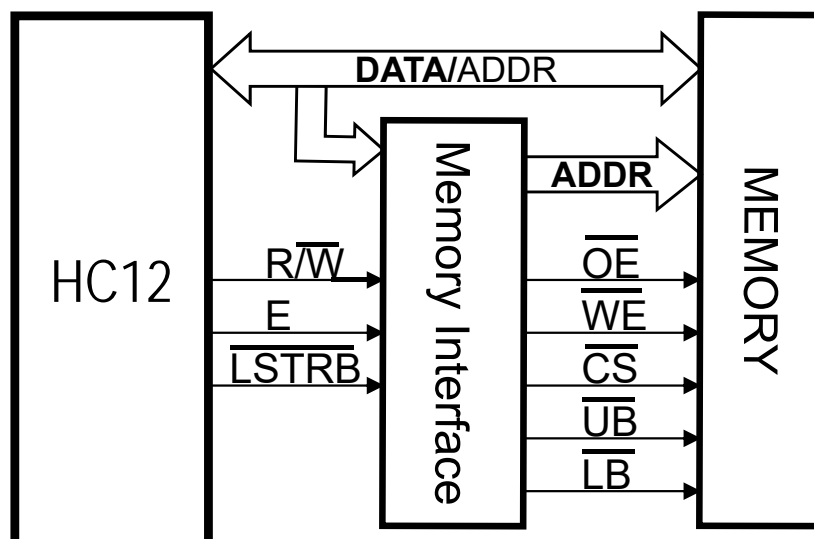
# Multiplexed Address/Data Bus

There are microprocessors which do not have enough pins for the number of signals they carry, such that they share the same pins for different functions by time-multiplexing signals. e.g., HC12 uses the same pins for DATA/ADDR as follows:



When the E-clock is

- low** => the sixteen DATA/ADDR lines (AD15-0) are used for **address**
- high** => the sixteen DATA/ADDR lines (AD15-0) are used for **data**



CS - Chip Select

WE - Write Enable

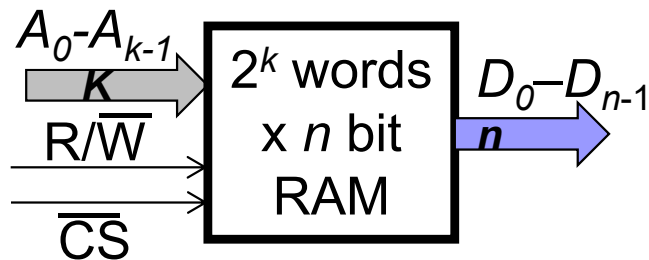
OE - Output Enable (Read)

UB - High (upper) Byte Enable

LB - Lower Byte Enable

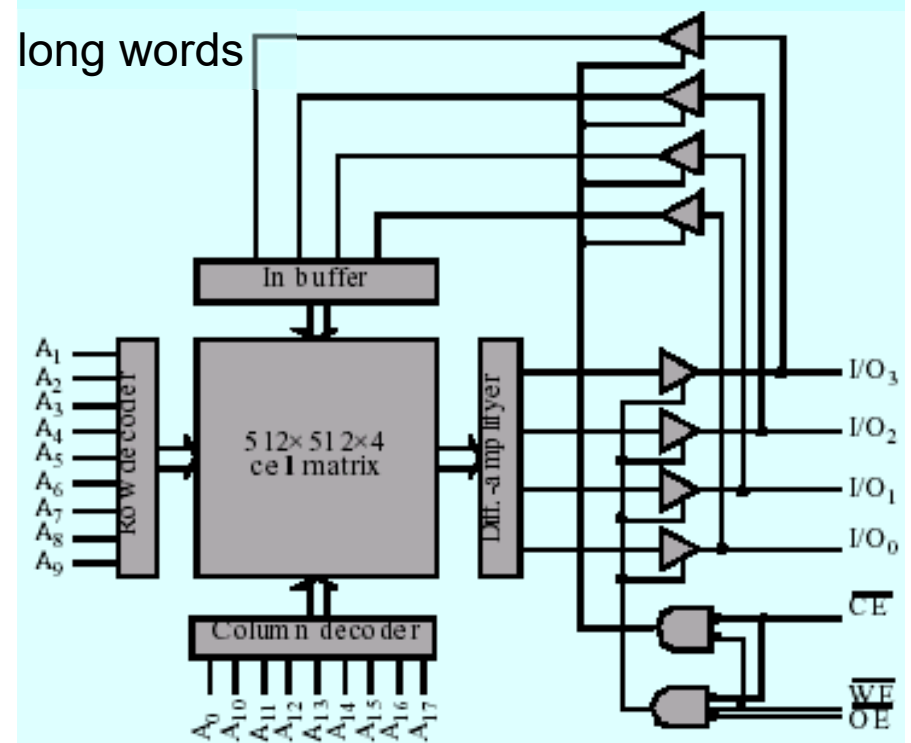


# SRAM Chip



- $k$ -bit address lines 0 to  $k-1$  is applied to  $A_0 - A_{k-1}$  (in the next figure  $k = 18$ )
- $\overline{CS}$  chip select (active low) and
- $R/\overline{W}$  high  $\Rightarrow$  Read;  $R/\overline{W}$  low  $\Rightarrow$  Write
- Data lines (I/O) are bi-directional
- Address lines  $A_0 - A_{k-1}$  contains address. The address lines are decoded into one of  $2^k$  locations
- Each location has  $n$ -bit word (here  $n = 4$ )
- The chip therefore has a capacity of  $2^k \times n$  bits
  - here:  $2^{18} \times 4$  bits = 256 k-word ( $2^{18} = 2^8 \times 1024$ ) of 4-bit long words

SRAM: 256 k-word ( $2^{18} = 2^8 \times 1024$ )  $n=4$ -bit



# DRAM (Dynamic RAM)

## 1-Transistor Cell

### Write:

1. Drive bit line
  2. Select row
- => C charges at bit-line voltage

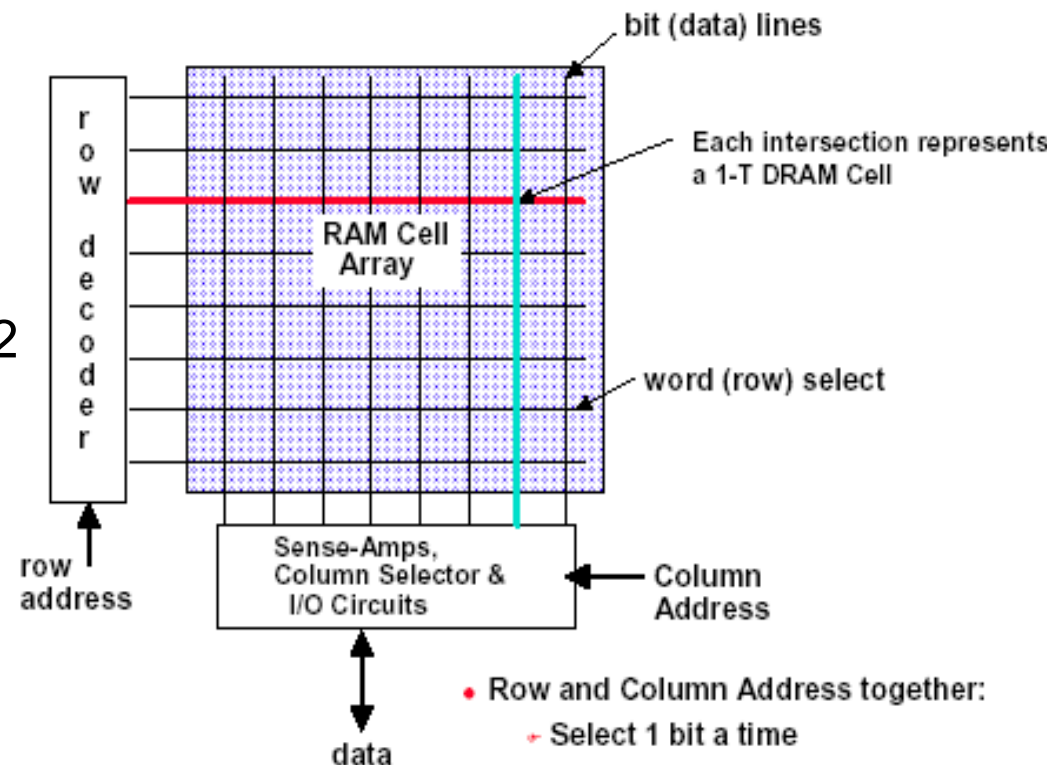
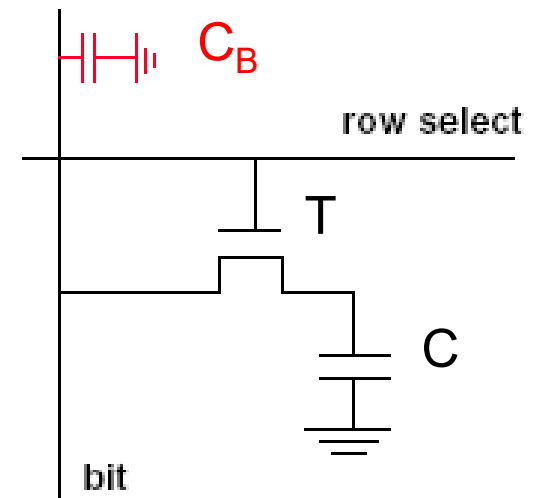
### Read:

1. Precharge bit line to  $V_{DD}/2$
2. Select row
3. Cell (C) and bit line ( $C_B$ ) share charges  
 → Very small voltage changes on the bit line  

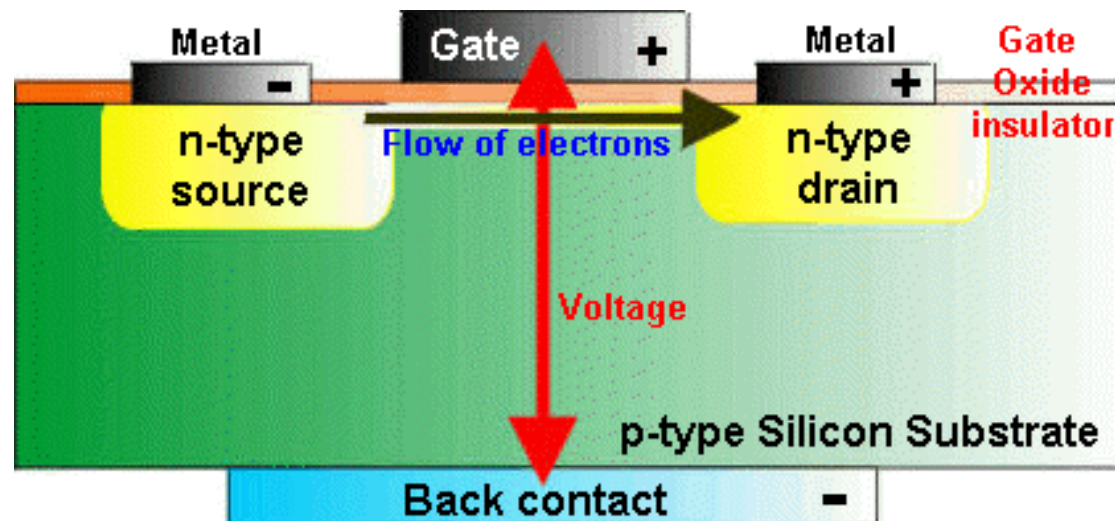
$$V_B = V_{DD}/2 [1 \pm C_B/(C + C_B)]$$
4. Sense amplifiers compare  $V_B$  with  $V_{DD}/2$   
 → Can detect changes of ~1 M electrons
5. Write: restore the voltage value on  $C_B$  and, as such, on C since  $C_B$  and C are connected together over transistor T

### Refresh

1. It's a dummy read to every cell.

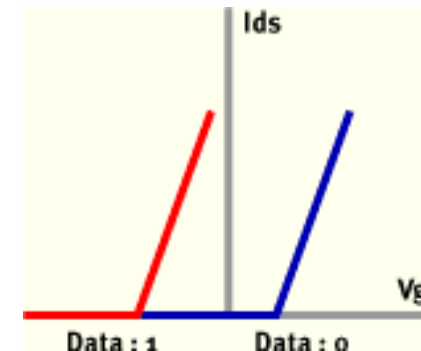
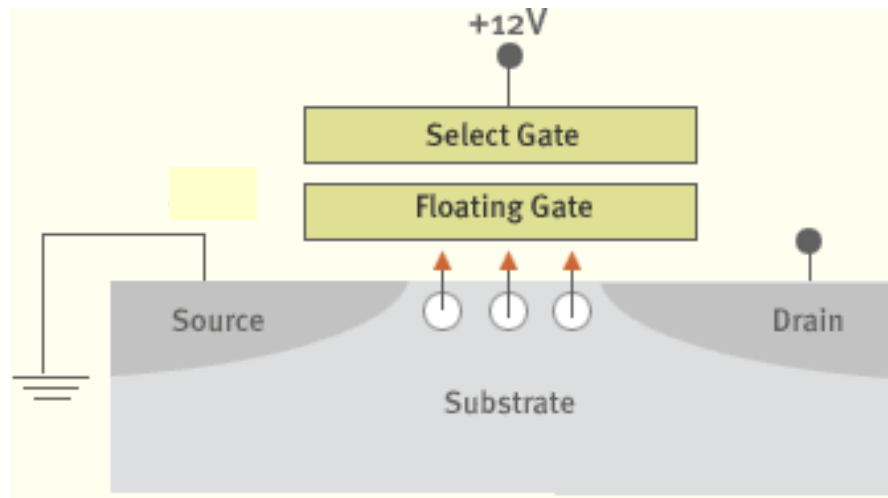


# EPROM CELL



# Programming EPROM Cell

- Changing a Flash Memory cell or bit to a zero is called programming.
- As electrons travel from the source to the drain through the substrate, the electric field generated by **high voltage** on the **select gate** causes some of the highest energy electrons to jump the gap and collect on the floating gate. The electrons now present on the floating gate counteract the voltage on the select gate and prevent the flash memory cell from turning on.
- No current flows from drain to source, resulting in a zero on the memory output pin.



# Erasing EEPROM Cell

- Memory cells must be erased before they can be overwritten.
- The generated electric field pulls electrons from the floating gate. Flash memories erase all cells in the array at the same time. EEPROM memories erase in smaller blocks.
- After "Erase Operation", a cell has data "1" and its threshold voltage becomes negative.

