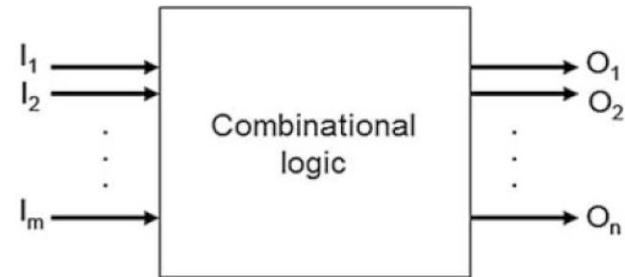


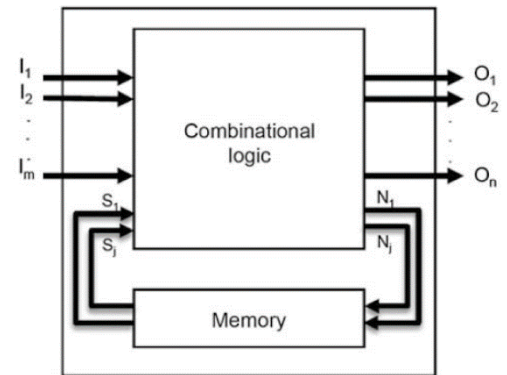
## CEG3155: DGD 1

**Review****Combinational Logic**

- Outputs depend only on the present inputs, i.e. no memory elements.
- Examples:
  - Multiplexers, demultiplexers, encoders, and decoders.
  - Adders, subtractors, multipliers, shifters, comparators, and ALUs.

**Sequential Logic**

- Outputs depend not only on the present inputs but also on past inputs.
- A memory element is used to store the state of the previous inputs.
- Sequential circuits are usually designed using a Finite State Machine (FSM).
- Examples:
  - Flip-flops, and counters.

**IEEE 1164 Standard**

- A technical standard published by the IEEE in 1993. ([https://perso.telecom-paristech.fr/guilley/ENS/20171205/TP/tp\\_syn/doc/IEEE\\_VHDL\\_1164-1993.pdf](https://perso.telecom-paristech.fr/guilley/ENS/20171205/TP/tp_syn/doc/IEEE_VHDL_1164-1993.pdf))
- It describes the logic values to be used in Electronic Design Automation (EDA) tools.
- Defines the following primary data types:

Character	Value
'U'	Uninitialized
'X'	Strong unknown value
'0'	Strong zero
'1'	Strong one
'Z'	High impedance
'W'	Weak unknown
'L'	Weak zero
'H'	Weak one
'_'	Don't care

- In VHDL, this standard is embodied in the std\_logic\_1164 package.

## Questions

### Question 1

Consider the function  $f(x_1, x_2, x_3) = m(2, 3, 4, 6, 7)$ , use the truth table below to identify the Sum-of-Products (SoP) and Product-of-Sums (PoS).

	$x_1$	$x_2$	$x_3$	Minterms	Maxterms
0	0	0	0	$m_0 = \overline{x_1} \overline{x_2} \overline{x_3}$	$M_0 = x_1 + x_2 + x_3$
1	0	0	1	$m_1 = \overline{x_1} \overline{x_2} x_3$	$M_1 = x_1 + x_2 + \overline{x_3}$
2	0	1	0	$m_2 = \overline{x_1} x_2 \overline{x_3}$	$M_2 = x_1 + \overline{x_2} + \overline{x_3}$
3	0	1	1	$m_3 = \overline{x_1} x_2 x_3$	$M_3 = x_1 + \overline{x_2} + x_3$
4	1	0	0	$m_4 = x_1 \overline{x_2} \overline{x_3}$	$M_4 = \overline{x_1} + x_2 + \overline{x_3}$
5	1	0	1	$m_5 = x_1 \overline{x_2} x_3$	$M_5 = \overline{x_1} + x_2 + x_3$
6	1	1	0	$m_6 = x_1 x_2 \overline{x_3}$	$M_6 = \overline{x_1} + \overline{x_2} + x_3$
7	1	1	1	$m_7 = x_1 x_2 x_3$	$M_7 = \overline{x_1} + \overline{x_2} + \overline{x_3}$

Identify the SoP, and PoS terms, and prove that  $f(x_1, x_2, x_3)$  can be expressed by SoP or PoS.

### Question 2

Use algebraic manipulation to show that for three input variables  $x_1, x_2, x_3$ :

$$\sum m(1, 2, 3, 4, 5, 6, 7) = x_1 + x_2 + x_3$$

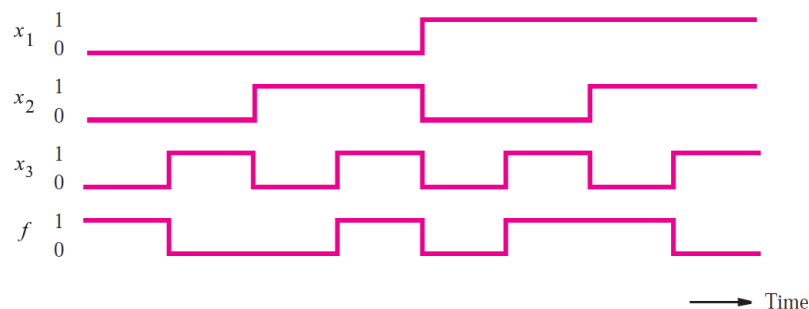
### Question 3

Perform the following operations in binary, where numbers are signed and represented in 2's complement form. Then, get the corresponding decimal number.

- $00000110 + 00001101$
- $11111010 - 11110011$
- $1100 + 1010$

### Question 4

For the timing diagram in the Figure, synthesize the function  $f(x_1, x_2, x_3)$  in the simplest sum-of-products form.



**Question 5**

Draw the circuit described by the following VHDL code.

```
architecture SomeCode of SomeEntity is
    signal sig1, sig2, out1: std_logic;
begin
    out2 <= not out1;
    sig2 <= (c xor d);
    out1 <= (sig1 and sig2);
    sig1 <= (a and b) or c;
end SomeCode;
```

**Question 6**

Write VHDL code to implement the function  $f(x_1, x_2, x_3) = m(0, 1, 2, 3, 4, 5)$ .

**Question 7**

Design 1-bit full adder in VHDL:

- Show timing diagrams of the sum and carry-out bits for all possible values of inputs.
- Show structural implementation of it.