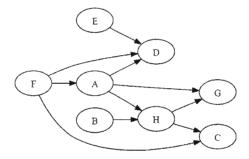
due: 02.02.2023 at 23:55

# **Bayesian Networks for Inference**

## Exercise H11.1: Directed Acylic Graphs (DAG) (h

(homework, 4 points)

Consider the following DAG:



- (a) (1 point) Give a possible topological sorting of the nodes in this DAG.
- (b) (2 point) The joint distribution of the corresponding n random variables can be factorized as

$$P(X) = \prod_{i}^{n} P(X_i | \text{parents}(X_i))$$
.

Write down the factorization for this DAG.

(c) (1 point) Indicate which nodes belong to the Markov blanket of node A and create the moral graph of the DAG.

#### **Exercise H11.2: Software**

#### (homework, 2 points)

Familiarize yourself with software packages for your programming language of choice (e.g., gRain<sup>1</sup> for R or BayesNetToolbox<sup>2</sup> for Matlab or BayesPy / pgmpy<sup>3</sup> for Python).

Implement the "water sprinkler" Bayesian network example in the tutorial by K. Murphy<sup>4</sup>. What is the probability that the sprinkler was active (S=true) after observing that the grass is wet (W=true)? What is the probability after the additional observation that it rained recently (R=true)?

## **Exercise H11.3: Construction of a DAG**

### (homework, 4 points)

Consider the binary random variables B (Burglary), E (Earthquake), A (Alarm), and R (Radio broadcast) which can all take values that are either "true" (t) or "false" (f).

Assume our knowledge about their co-occurrence is given by the (conditional) probabilities:  $P(B=t)=0.01, P(E=t)=10^{-6}, P(R=t|E=f)=0, P(R=t|E=t)=1,$  and

B	E	P(A = t B = b, E = e)
f	f	0.001
f	t	0.41
t	f	0.95
t	t	0.98

- (a) (1 point) Create a DAG representing the corresponding factorization of the joint distribution.
- (b) (2 points) Implement the DAG with a software package of your choice (see above) and calculate P(A=t), P(A|R=t), P(B=t|A=t) and P(B=t|A=t).
- (c) (1 point) Explain the phenomenon of *explaining away* using the examples obtained in (b).

Total 10 points.

<sup>1</sup> gRain http://cran.r-project.org/web/views/gR.html

<sup>&</sup>lt;sup>2</sup> BayesNetToolbox http://code.google.com/p/bnt

<sup>&</sup>lt;sup>3</sup> BayesPy http://www.bayespy.org/intro.html . Alternative Python packages that may be easier to use are https://pgmpy.org/ and https://github.com/eBay/bayesian-belief-networks

<sup>&</sup>lt;sup>4</sup> K. Murphy. A brief introduction to graphical models and Bayesian networks. http://people.cs.ubc.ca/~murphyk/Bayes/bnintro.html