

- # 1
1. $\pi_{\text{Firstname}} (\text{Passengers} \bowtie \text{Tickets} \bowtie (\sigma_{\text{Departure time} < 12} (\text{Flights})))$
 2. $\pi_{\text{Destination, PlaneID}} (\text{Flights}) / \pi_{\text{planeID}} (\text{Planes})$
 3. $\pi_{\text{FlightID}} (\text{Tickets} \bowtie (\sigma_{\text{FirstName} = 'Isabella'} (\text{Passengers})))$
 $- \pi_{\text{FlightID}} (\text{Flights} \bowtie (\sigma_{\text{Airline} = 'Delta'} (\text{Planes})))$

- # 2.
1. $\{id, name, GPA, major, school\}$. $id \rightarrow name, GPA, major, school$ $GPA \rightarrow major$ $school \rightarrow major$
 $name, major \rightarrow id$
 id is the key, anything can give id is candidate key. $name, major \rightarrow id$ $name, school \rightarrow name, major$
 $GPA, name \rightarrow name, major$.
 candidate keys: $\{id\}$, $\{name, major\}$, $\{name, school\}$ $\{GPA, name\}$.

2. The relation is in 3NF since for dependencies in the form $X \rightarrow A$: $GPA \rightarrow major$, $school \rightarrow major$
 $name, major \rightarrow id$ $major$ is part of key ($name, major$) and id is superkey
3. The relation is not in BCNF because for dependencies $GPA \rightarrow major$ $school \rightarrow major$ $major$ is not superkey
 and $major$ is clearly not a subset of GPA nor $school$
4. $GPA \rightarrow major$ is violated with $(3.8, \text{English}) \neq (3.8, \text{Astronomy})$ $school \rightarrow major$ is violated
 with $(\text{Engineering, CS}) \neq (\text{Engineering, Aerospace})$.

- # 3
1. C BD is superkey, it qualifies for both of them
 2. B A is not superkey so not BCNF but A is part of AD and so for the 3NF
 3. $AC \Rightarrow F$

$$R_1 = \{A, C, F\}$$

$$R_2 = \{A, B, C, D, E\}$$

$$F_1 = \{AC \Rightarrow F\}$$

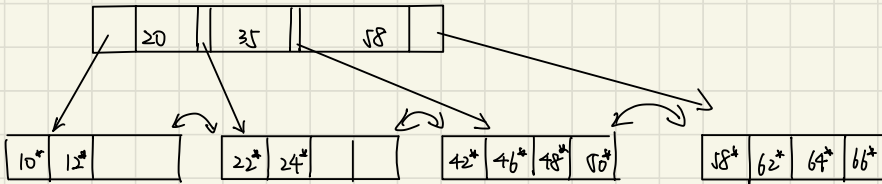
$$F_2 = \{A \Rightarrow B, BD \Rightarrow ACE\}$$

4. A $R_1 \cap R_2 = A_C \rightarrow R_1$

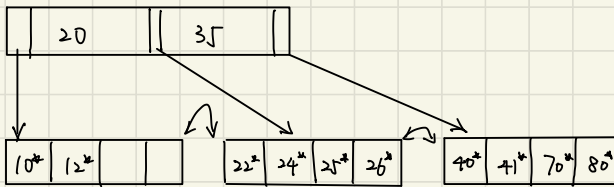
5. B. $DF \rightarrow CE$ across 2 tables.

4.

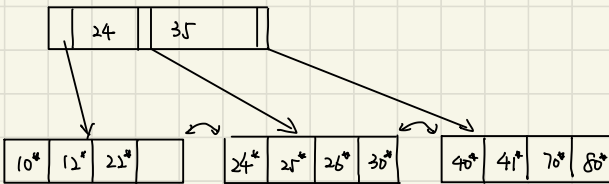
1. redistribute to the right.



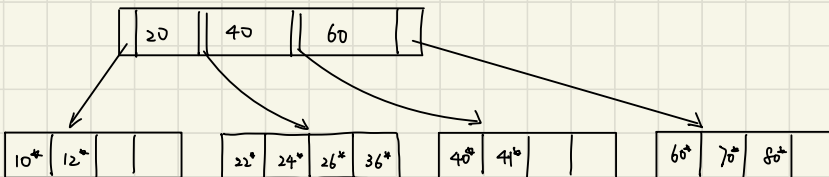
2. Insert 25^*



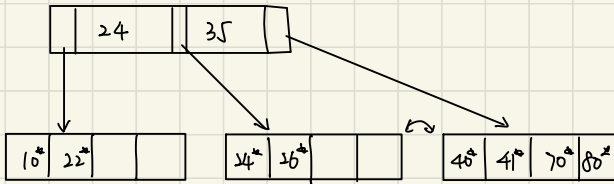
Insert 30^* redistribute to left.



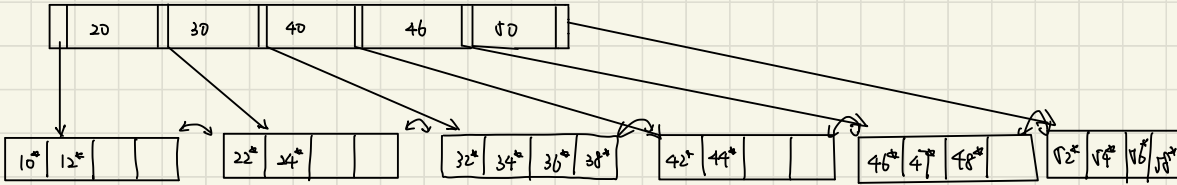
3. split



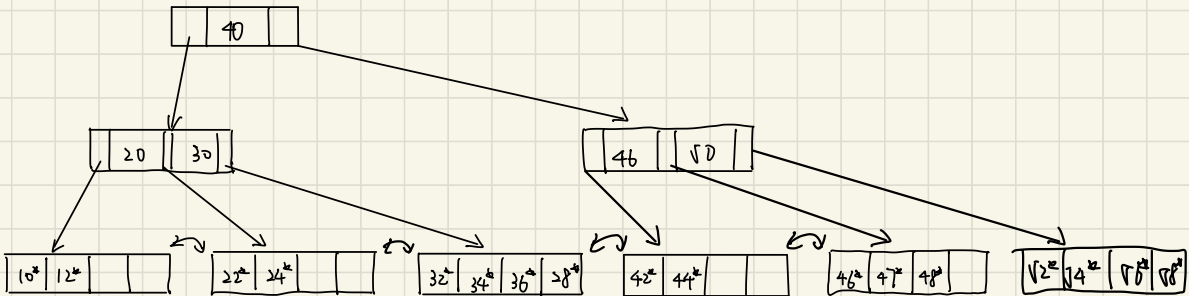
4. redistribute from the right



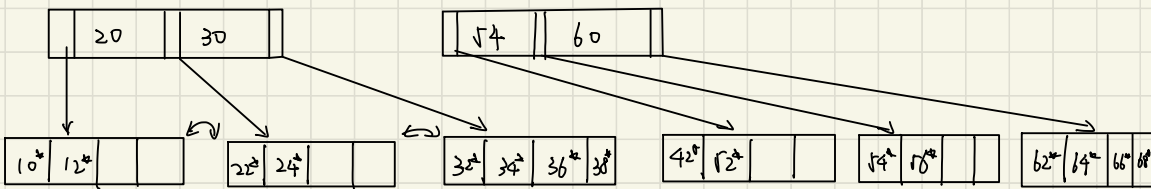
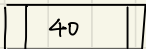
5. split.



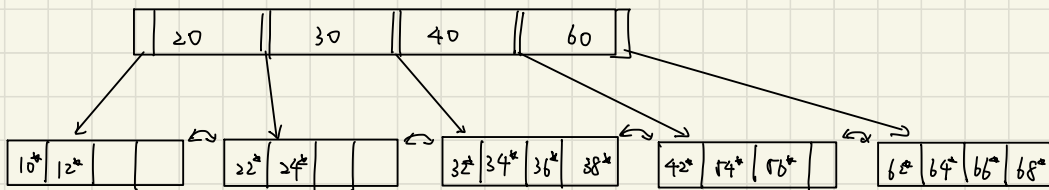
move 40 up



6. delete 44 redistribute from right.



delete & merge.



5.

1. $N=2$ having 4 buckets need to split twice and reaching level = 1 need to trigger split when

next = $N-1 = 1$

minimum Insert will be Insert 2 values to bucket of hash value = 1

splitting bucket for $h_0=0$ and bucket for $h_0=1$

① Insert 3. H_0

00 0 20*
10 1 Next=1 \rightarrow 11* 13* \rightarrow 3*

② Insert 5. H_1, H_0

00 0 Next=0 [20*]
01 1 [13* 5*]
10 []
11 [11* 3*]

level 0. $N=2$

2.1

H_0 Next=0
0 [20* 22*]
1 [11* 13*]

2.2

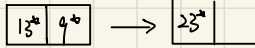
 H_1 H_0

00

0

| Next = 1

10

level 0. $N=2$ level = 1. $N=2$

2.3.

 H_1

00

Next = 0

01

10

11



2.4

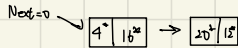
 H_1 H_0

00 0

01 1

10

11

level 1. $N=2$ level 1. $N=2$

2.5

 H_2 H_1

000 00

001 01

010 10

011 11

100

