## Discussion 7

Hash Indexes & Project 3 Intro EECS 484

#### Logistics

- Homework 3 due Nov 3 at 11:55 PM EST
- Project 3 due Nov 10 at 11:55 PM EST
- Midterm exam in the process of grading
  - Please do not discuss the exam
- Today
  - Indexing & Hash index
  - Intro to MongoDB (project 3)
  - MapReduce (project 3)

# Indexing

#### Indexes

- Our database has lots of nice data
  - How do we get the data as fast as possible
    - Indexing!
- Indexes are a type of data structure that allow us to search for, insert, and delete data in a table
  - Take an input k (not necessarily a key for the table, just a search key)
    - Set of columns
    - If search key contains a primary key then we call it the primary index
      - Otherwise it is the secondary index
  - Find data entries k\* for each k
    - Can have more than one data entry per search key k



#### Records

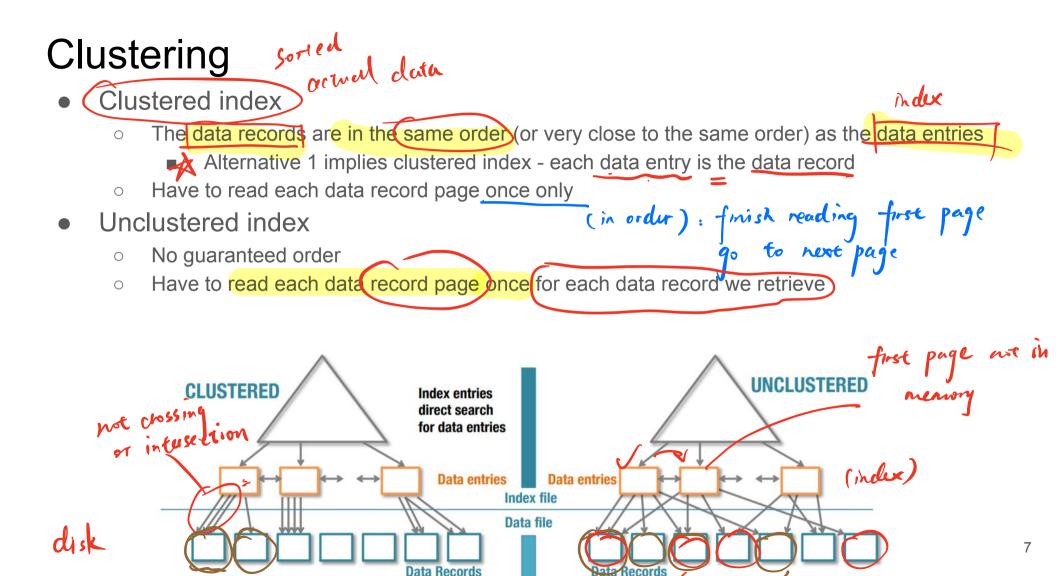
- All data are stored in a unit of space called a page
  - Multiple records can exist in a page
  - Often times needs multiple pages to fit all records in a table
- Pages don't have to be always full
  - Clustered indexes may keep pages ¾ full to make inserting and deletion faster

#### Data Entries k\*

- Take search key k and find data entries k\* (from the index file) for k
- Alternative 1: Data entry k\* is the actual record itself
   Only 1 k\* can be resolved using Alternative 1 (no way to handle duplicates)
   Alternative 2: Data entry k\* is the resolved using Alternative 1 (no way to handle duplicates)
- Alternative 2: Data entry k\* is (k, rid) where rid is the record ID for the record with the search key k

  | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | Search key k | S
- Alternative 3: Data entry k\* is (k, list of rids) where each rid is the record ID for the record with the search key k

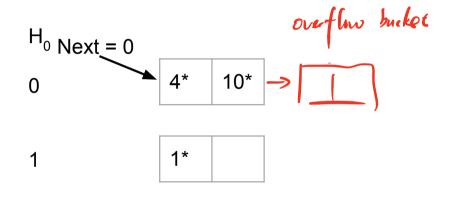
One entiry points to one reard, one page Contains many records, to feech one record you need to access the whole page



read same record multiple times

take binary transformation
$$N = 2$$
and look at last
$$H_{i}(x) = x \pmod{N * 2^{i}}$$
Level = 0
$$2 \text{ bits}$$

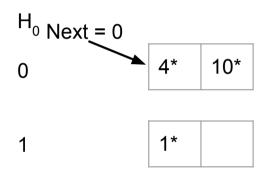
- Family of hash functions
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Ho: last 2 bits

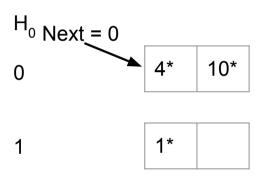
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$$N = 2$$
  
 $H_i(x) = x \pmod{N * 2^i}$   
Level = 0  
 $H_0(x) = x \pmod{N * 2^0} = x \pmod{2}$ 



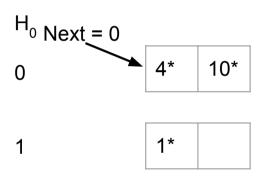
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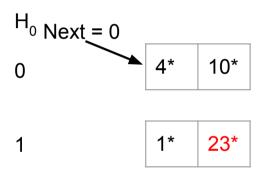


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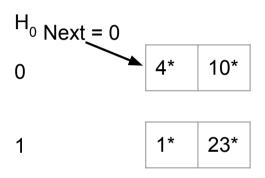
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• Done :)

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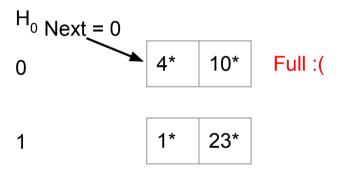


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- Insert 12\*

$$\circ$$
 H<sub>0</sub>(12) = 12 (mod 2) = 0 mod 2 = 0b0

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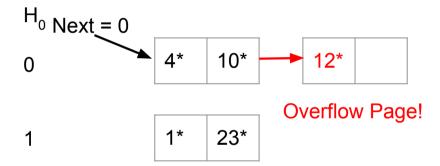
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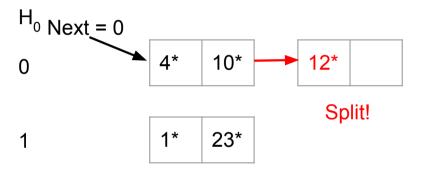
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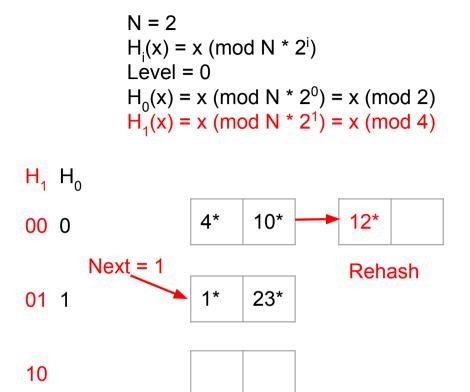


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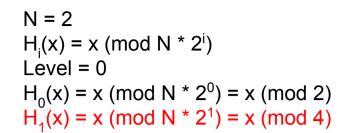
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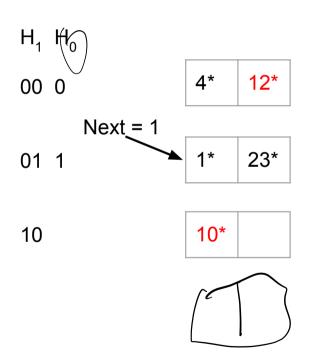


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$$\circ$$
 H<sub>0</sub>(12) = 12 (mod 2) = 0 mod 2 = 0b0

- Rehash 4\*, 10\*, 12\*
  - $\circ$  H<sub>1</sub>(4) = 4 (mod 4)= 0 mod 4 = 0b00
  - $\circ$  H<sub>1</sub>(10) = 10 (mod 4) = 2 mod 4 = 0b10
  - $\circ$  H<sub>1</sub>(12) = 12 (mod 4) = 0 mod 4 = 0b00

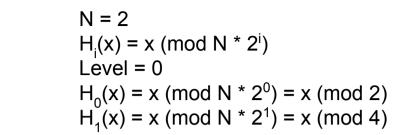


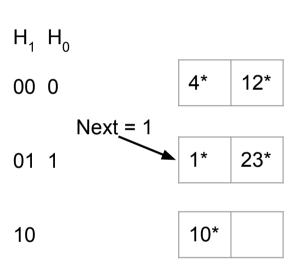


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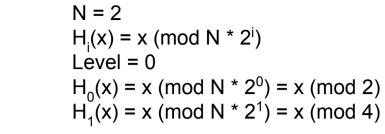
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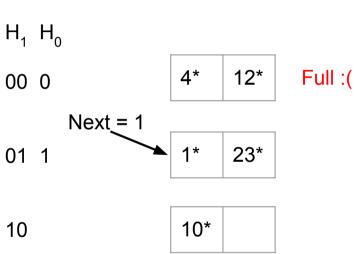
Done :)



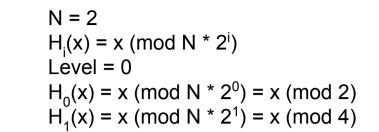


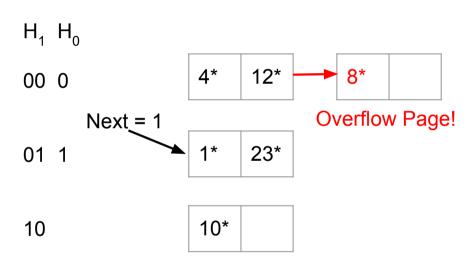
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  - $\circ$  H<sub>1</sub>(8) = 8 (mod 4) = 0 mod 4 = 0b00



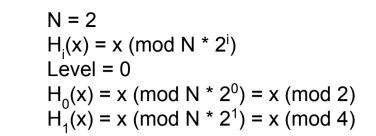


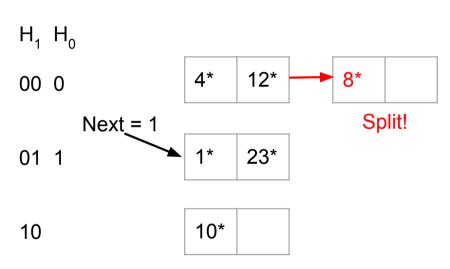
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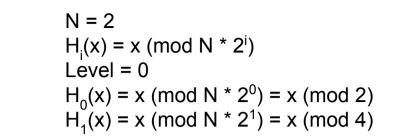


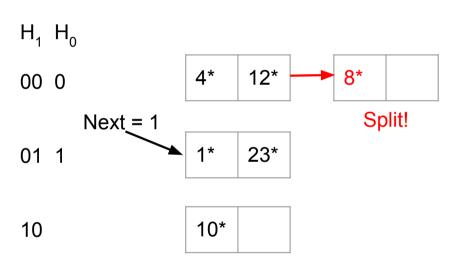
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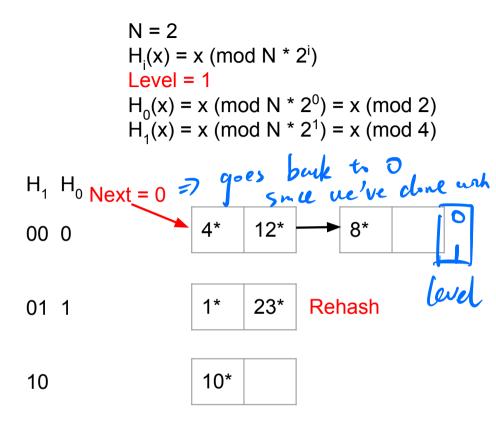


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  - $\circ$  H<sub>4</sub>(8) = 8 (mod 4) = 0 mod 4 = 0b00
  - Remember we split the next node always even though it might not be overflow

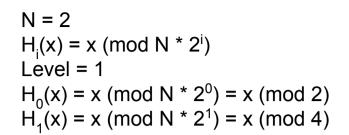




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  - $\circ$  H<sub>4</sub>(8) = 8 (mod 4) = 0 mod 4 = 0b00
  - $\circ$  H<sub>4</sub>(1) = 1 (mod 4) = 1 mod 4 = 0b01
  - $\circ$  H<sub>1</sub>(23) = 23 (mod 4) = 3 mod 4 = 0b11





01 1 1\*

10 10\*

11 23\*

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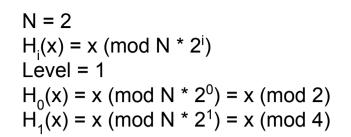
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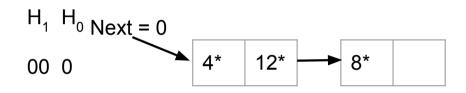
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Still have overflow page; that's ok





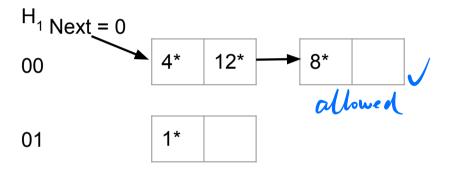
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  - $\circ$  H<sub>1</sub>(23) = 23 (mod 4) = 3 mod 4 = 0b11
  - Still have overflow page; that's ok
  - One :)

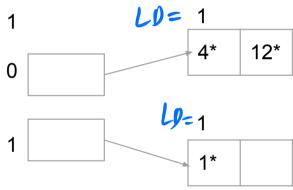
$$N = 2$$
  
 $H_i(x) = x \pmod{N \cdot 2^i}$   
Level = 1  
 $H_0(x) = x \pmod{N \cdot 2^0} = x \pmod{2}$   
 $H_1(x) = x \pmod{N \cdot 2^1} = x \pmod{4}$ 



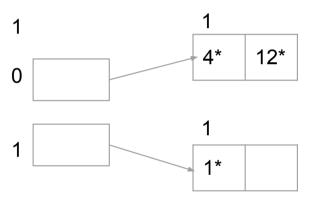


- Use directory of pointers
  - Split on overflow
  - Once we're out of room in directory, double size 60 1
  - Global depth = number of bits considered globally
  - Local depth = number of bits considered locally

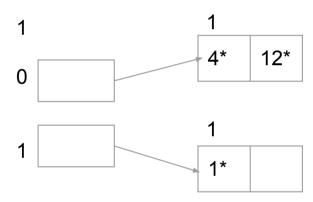
COD 2 LD



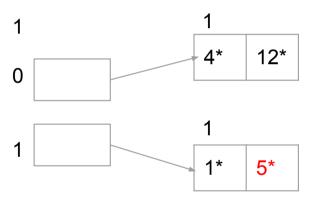
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  - Global depth = number of bits considered globally
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- Insert 5\*



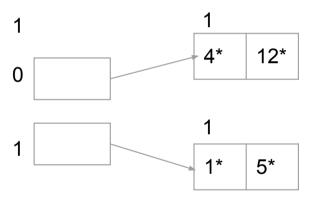
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  - o 5=0b10<u>1</u>



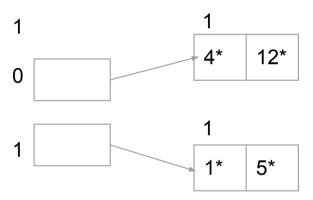
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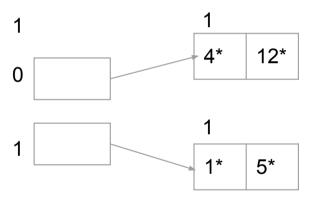
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- Insert 5\*
  - o 5=0b101
  - o Done:)



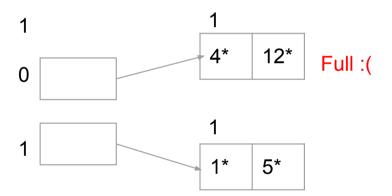
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  - Global depth = number of bits considered globally
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- Insert 10\*



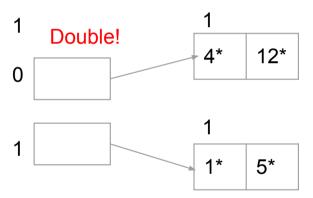
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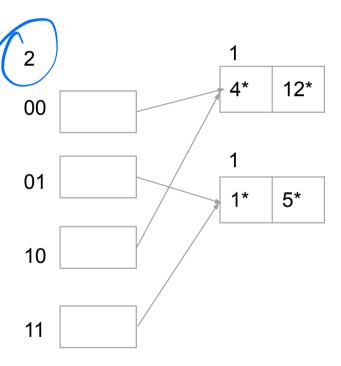
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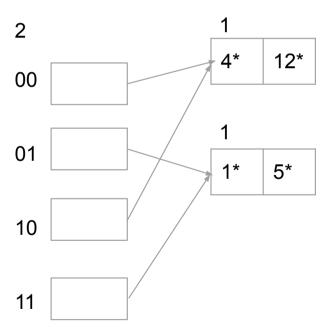
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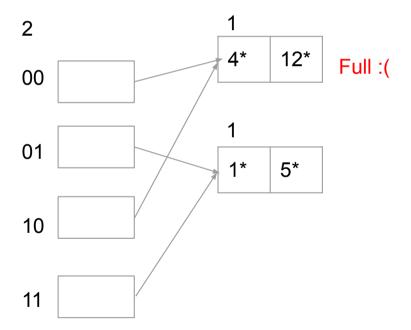
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- Insert 10\*
  - o 10=0b1010
  - New directories point to "Split image"



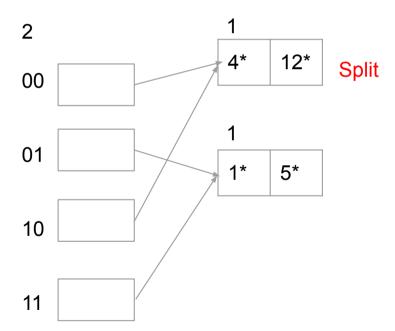
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  - New directories point to "Split image"
  - Try to insert again



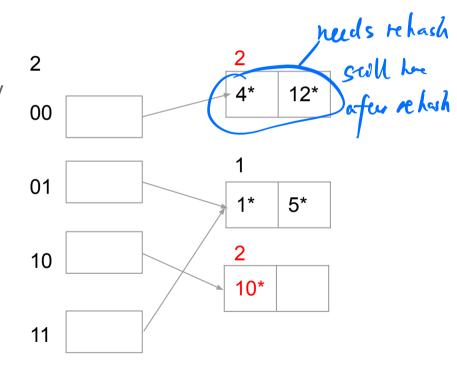
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  - New directories point to "Split image"
  - Try to insert again



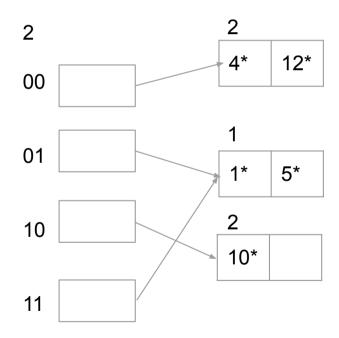
- Use directory of pointers
  - Split on overflow
  - o Once we're out of room in directory, double size
  - Global depth = number of bits considered globally
  - Local depth = number of bits considered locally
- Insert 10\*
  - o 10=0b1010
  - New directories point to "Split image"
  - Try to insert again



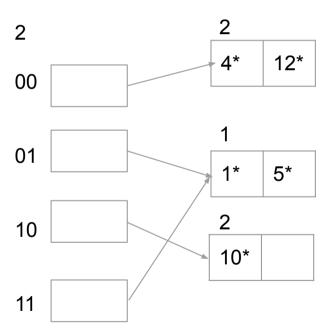
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  - Split on overflow
  - Once we're out of room in directory, double size
  - Global depth = number of bits considered globally
  - Local depth = number of bits considered locally
- Insert 10\*
  - o 10=0b1010
  - New directories point to "Split image"
  - Try to insert again



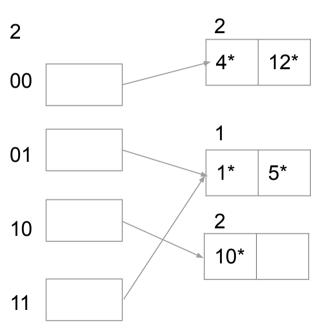
- Use directory of pointers
  - Split on overflow
  - Once we're out of room in directory, double size
  - Global depth = number of bits considered globally
  - Local depth = number of bits considered locally
- Insert 10\*
  - o 10=0b1010
  - New directories point to "Split image"
  - Try to insert again
  - Opening Done :)



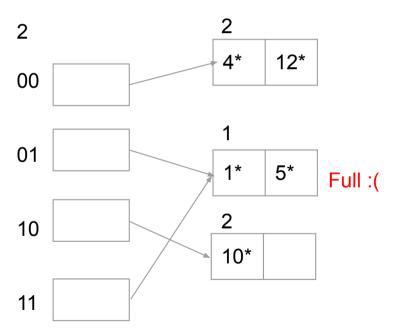
- Use directory of pointers
  - Split on overflow
  - Once we're out of room in directory, double size
  - Global depth = number of bits considered globally
  - Local depth = number of bits considered locally
- Insert 7\*



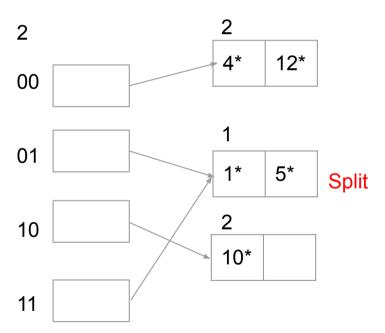
- Use directory of pointers
  - Split on overflow
  - Once we're out of room in directory, double size
  - Global depth = number of bits considered globally
  - Local depth = number of bits considered locally
- Insert 7\*
  - o 7=0b111



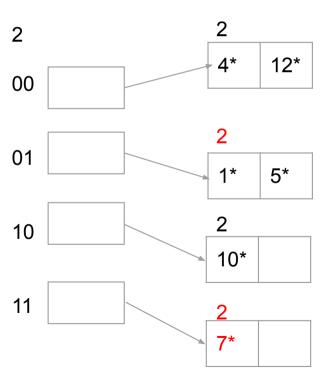
- Use directory of pointers
  - Split on overflow
  - Once we're out of room in directory, double size
  - Global depth = number of bits considered globally
  - Local depth = number of bits considered locally
- Insert 7\*
  - o 7=0b111



- Use directory of pointers
  - Split on overflow
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- Use directory of pointers
  - Split on overflow
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- Use directory of pointers
  - Split on overflow
  - Once we're out of room in directory, double size
  - Global depth = number of bits considered globally
  - Local depth = number of bits considered locally
- Insert 7\*
  - o 7=0b111
  - o Done:)



2

00

01

4\*

1\*

12\*

5\*

#### Hashing Overview

- Directory size can double in extendible hashing
  - Linear hashing only adds one bucket at a time
  - Global depth >= local depth always
  - # pointers to any specific bucket ₹2<sup>GD-LD</sup>
  - Overflow pages only in rare cases (unavoidable collisions)
- Linear Hashing only adds one bucket at a time
  - Better memory usage
  - Doesn't avoid overflow pages in many cases
    - Over time we minimize overflow pages



Hash browns < hash tables

# MongoDB and NoSQL

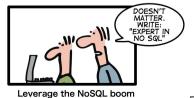
#### **NoSQL**

- Not Only SQL!
  - Non relational databases
  - Use very different data structures compared to traditional relational databases
- Reading: <a href="https://www.mongodb.com/nosql-explained">https://www.mongodb.com/nosql-explained</a>
- Different data models used by different distributions
- Data in a common set doesn't need to adhere to a schema

HOW TO WRITE A CV







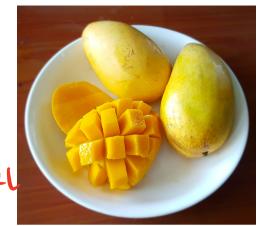
### MongoDB

- Instead of rows we have documents
  - Fields and values
    - I.E "Age": "7"





- Use Javascript instead of SQL to interact
- Data is in JSON
- https://docs.mongodb.com/manual/reference/sql-comparison/



#### **JSON**

- JavaScript Object notation
- {Key: Value}
  - o var data = {("Name": "Alice"), ("Major": CS"), "University": "UofM", "Hobby": "Beating MSU");
  - Can have nested key values as well:
- Can have nested key values as well:

  {"Location": {"City": "Ann Arbor", "State": "Michigan", "Country": "USA"}};

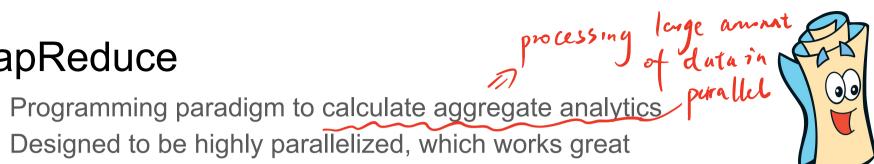
  eve data by data["Name"]

  \*\*Alica"
- Retrieve data by data["Name"]
  - Returns "Alice"
- JSON Objects are not ordered



note: JSON has nothing to do with Jason Momoa, but again, they sound similar

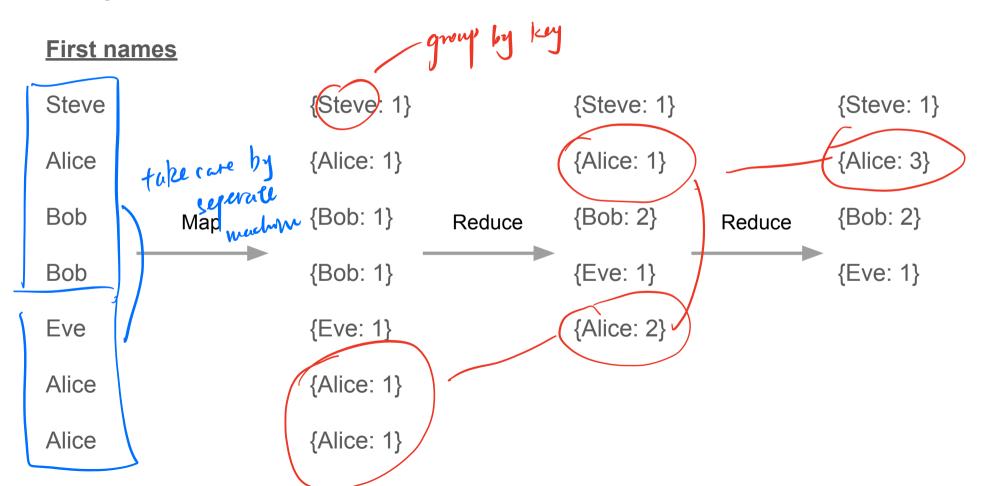
- Designed to be highly parallelized, which works great when we have a large set of data and many processors
  - Historically performed on Hadoop (distributed storage) framework
- Often performs worse compared to an equivalent serial algorithm working on a single machine
  - But we will use it anyway with MongoDB in P3, to get practice with the paradigm



- Needed for queries 7 and 8
- Mapper
  - Run on each record
  - o Emits(a key and a value) interminde of key-value
- Reducer
  - Run on each mapped object
  - o Combine values in aggregate that share key to get value of interest
  - It's possible to have multiple calls to reduce!
- Finalizer
  - Specific to MongoDB
  - Performs any last calculations before returning in final form

grouping:

kry [x, j, ]



# Project 3 Intro

### Project 3

- Part A: Java code to export database to JSON
  - Need to perform this on CAEN just like in Project 2
- Part B: MongoDB Queries
  - You can run entirely on your local machine (requires installing MongoDB)
    - We won't be able to help with specific installation issues though
  - Use the eecs484 server through CAEN
    - Set up your project on CAEN and edit the Makefile as specified in the spec
    - Run commands which will connect to a MongoDB server setup for you on the eecs484 server
  - Write the queries!
    - Lots of helpful references in the spec to various MongoDB documentation

#### General Tips

- Try to focus on getting the solution correct rather than doing it in the fanciest way
  - Yes you can use an aggregate, group, out pipeline or you can iterate a couple times
  - No efficiency tests
  - No private tests
  - Most important thing: make sure you understand how and why your code works
- Take the time to get familiar with Javascript
  - Documentation will be your best friend
- Query 5 is the hardest
  - Has a similar concept to how you dealt with the friends relation in Query 6 on Project 2
    - Completely different code but similar work around needed

## Query 7

I key is month

- Find number of users born in each month using map reduce
- Mapper
  - Given access to a user (this) what can we return that will give us useful information?
  - Emit Tuple: (key, value)
  - Hint: Think about a way to mark that this user was born in this month.

#### Reducer

- Given access to a set of values that correspond to a key, how do we combine these values?
- Return value
  - Should match the same time of value output by the mapper
- Hint: The value output at the end of this method should be the number of users (that we know of) born in the month denoted by key

#### Finalizer

- Get the final answers for each key ready to return
- No change needed for query 7:)

## Query 8

city as the key

- Find average friend count per city
- Mapper
  - Given access to a user (this) what can we return that will give us useful information?
  - Emit Tuple: (key, value)
  - Hint: Value can be a tuple in it of itself!
- Reducer
- & don't calculate aug in reducer Given access to a set of values that correspond to a key, how do we combine these values?
  - Return value should match the same type of value output by the mapper
  - Hint: The reducer can be called multiple times during execution
    - We can take intermediate sums, but not intermediate averages
- Finalizer
  - Get the final answers for each key ready to return
  - Small change needed for query 8 0
  - Hint: We can't compute an average in the reducer, but we can in the finalizer 0

Calculate here

- Find average of (5, 3) 9, 5, 13) given that they all map to the same key
  - Incorrect solution:
    - Reducer: Find average of 5 and 3 (4)
    - Reducer: Find average of 9 and 5 and 13 (9)
    - Reducer: Find the average of the averages (gives us 6.5 when the real answer is 7)
  - Correct solution
    - Reducer: sums 5 and 3, and outputs 8
    - Reducer: sums 9 and 5 and 13, and outputs 27
    - Reducer: sums 8 and 27, and outputs 35
    - Finalizer: computes the average 35/5 to output 7 as the average

## Get started on HW4 and Project 3!