

# TANA: Precise and Practical Sampling-based Side channel Information Leakage Quantification

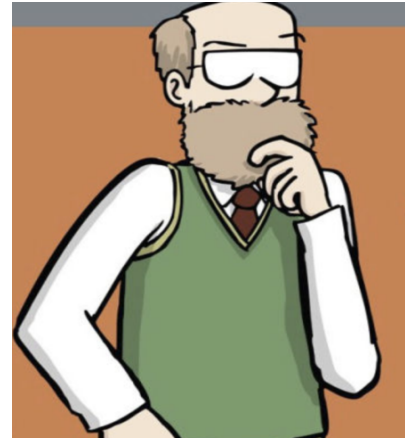
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# What is side-channel attack ?

A side-channel attack is any attack that allows attackers to infer some sensitive information based on non-functional characteristics.



A naïve Ph.D. student



A prestigious professor

# Side-channel attack

Secret: whether your advisor is in the office

What you can do:

1. Ask your advisor (Not a good idea)



Attacker



Victim

# Side-channel attack

Secret: whether your advisor is in the office

What you can do:

1. Ask your advisor (Not a good idea)

Insight:

Your advisor always drives to work.

The parking lot is shared with you.

# Side-channel attack

Secret: whether your advisor is in the office

What you should do:

1. Go to the parking lot
2. Find your advisor's vehicle



# Address-based Side Channels

Side-channels in computer systems: timing, power, CPU usage, cache ...

```
unsigned char key = input();  
// 4 bits information  
unsigned char temp = key/2;  
if (temp == 0xb)  
// branch 0 execution 2s  
else  
// branch 1 execution 1s
```

Secret-dependent control-flow transfers

```
T[1024];  
// Lookup tables with 1024 entries  
index = key % 1024;  
temp = T[index]  
// Secret-dependent memory access
```

Secret-dependent memory accesses

Cache-based: Prime + Probe, Flush + Reload, Flush + Evict  
Memory-based: Controlled-channel attack, page-table attack

# Side-channel Vulnerability Detections

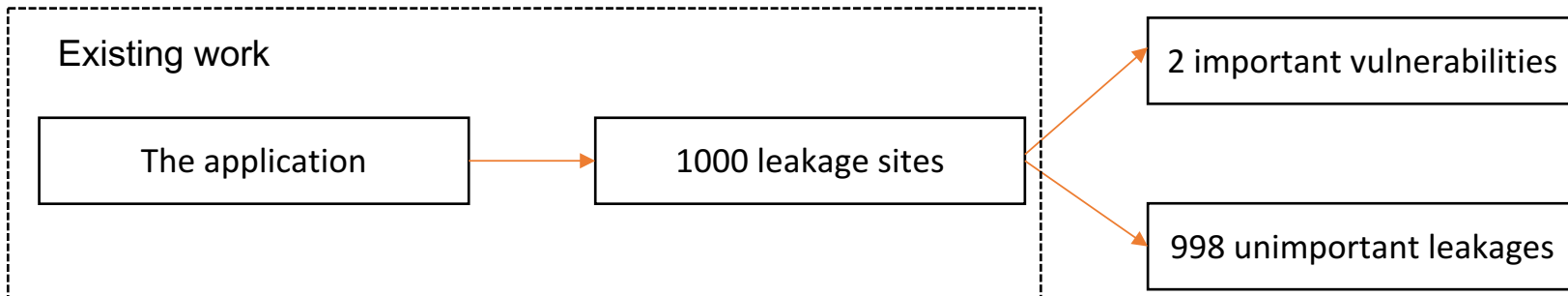
Software countermeasures:

- Find vulnerabilities
  - It's hard. Real cryptosystems are complicated
    - OpenSSL 281K LoC
  - Those vulnerabilities are architecture-dependent
  - Existing works: CacheAudit, CacheD, DATA, CacheS.
- Fix vulnerabilities
  - It's also hard. Side-channel vulnerabilities are inevitable.
  - Many vulnerabilities are unpatched.

# Motivation

## Existing works:

- False positives
  - e.g., 2248 potential leakages for RSA in OpenSSL, 1510 of them were dismissed
- Report many insensitive leakages
- Only on one leakage site



**Our Objective: Identify and quantify address-based side-channels precisely.**



# An example

```
unsigned char k1, k2;  
...  
t1 = T[k1 % 8];           // Leakage 1  
if(k1 > 127)              // Leakage 2  
    A();  
if(k2 + k1 > 127)        // Leakage 3  
    B();
```

An attacker:

1. knows which element the code read
2. knows if the code runs A(), B()

| Leakage       | 1 | 2 | 3 | 1,2 | 1,3 | 2,3 |
|---------------|---|---|---|-----|-----|-----|
| Leaked (bits) | 3 | 1 | 1 | 4   | 4   | 2   |

Table 1. Leakage Summary

# Overview

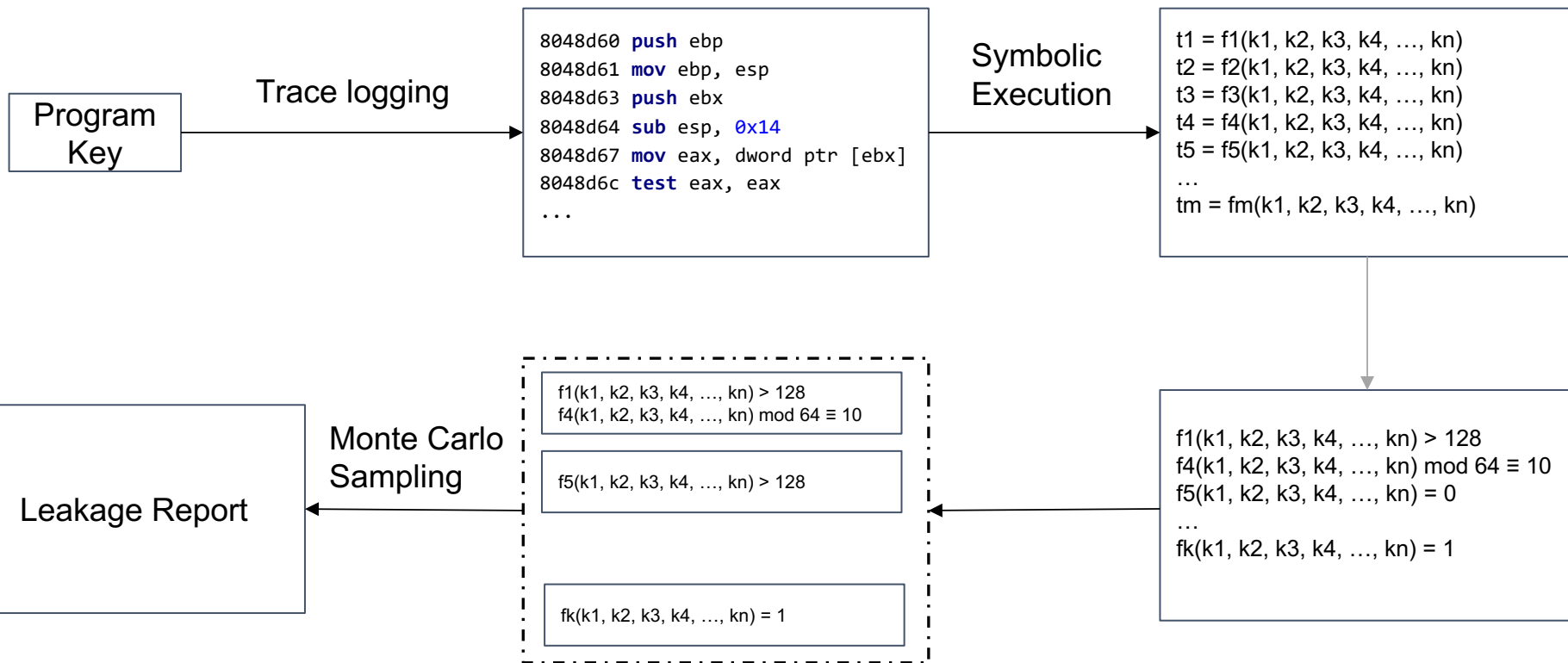


Figure 1. TANA architecture

# Challenges

- Information Leakage Definition
  - Existing work: Shannon entropy and mutual information
  - Number of different observations
- Leakage Dependence
  - Real-world applications may have multiple information leakages sites
  - Some leakages are dependent
- Scalability
  - We want to quantify information leakages in real-world applications
  - e.g. RSA implementations OpenSSL have thousands of lines -> 1 million instructions
  - The performance is important

# Challenge 1: Information Leakage Definition

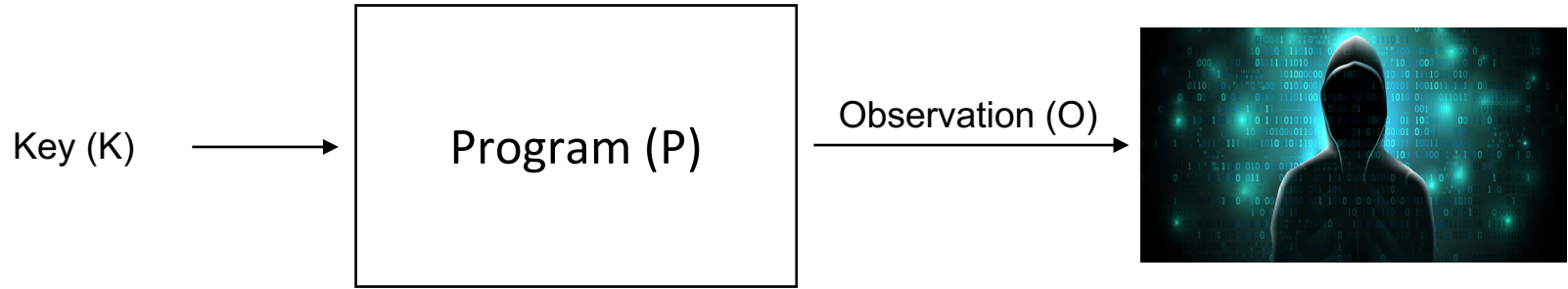


Figure 2. Observation Model

Observations:

1. Secret-dependent control-flow transfers
2. Secret-dependent memory access

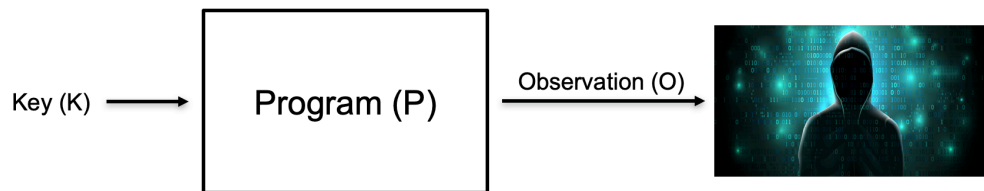
# Previous Information Leakage Definition

Mutual Information (MI):

$$MI = I(K; O) = H(O) - H(O|K) = H(O) = \sum_{o_i \in O} P(o_i) \log_2 P(o_i)$$

Maximal Leakage (ML):

$$ML = \log_2 |O|$$



```
unsigned char key = input();  
// key = [0 ... 255]  
if(key = 128)  
    A(); // branch 1  
else if (key < 64)  
    B(); // branch 2  
else if (key < 128)  
    C(); // branch 3  
else  
    D(); // branch 4
```

| Branch      | 1               | 2                | 3                | 4                 |
|-------------|-----------------|------------------|------------------|-------------------|
| Possibility | $\frac{1}{256}$ | $\frac{64}{256}$ | $\frac{63}{256}$ | $\frac{128}{256}$ |

$$MI = \frac{1}{256} \log_2 \frac{1}{256} + \frac{64}{256} \log_2 \frac{64}{256} + \frac{63}{256} \log_2 \frac{63}{256} + \frac{128}{256} \log_2 \frac{128}{256} = 1.7 \text{ bits}$$

$$ML = \log_2 4 = 2 \text{ bits}$$

# Challenge 1: Information Definition

```
// Dummy password checker
unsigned char key = input();
// key = [0 ... 255]
if(key = 128)
    A(); // branch 1
else if (key < 64)
    B(); // branch 2
else if (key < 128)
    C(); // branch 3
else
    D(); // branch 4
```

Suppose an attacker knows the code run branch 1, then he knows the key equals to 128.

Mutual Information: 1.7 bits

Max Leakage: 2 bits

Problem: Both methods neglect the input key and give an “average” estimate.

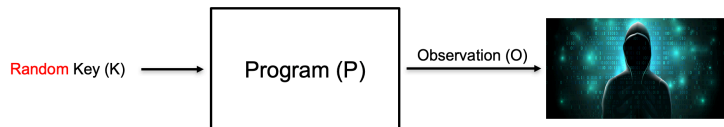


Figure 3. Mutual Information

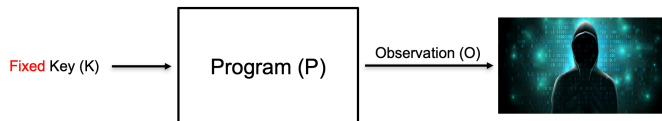


Figure 4. Real Attack

# Challenge 1: Information Leakage Definition

**Definition.** Given a program  $P$  with the input set  $K$ , an adversary has the observation  $o$  when the input  $k \in K$ . We denote it as

$$P(k) = 0$$

The leakage  $L_{ko}$  based on the observation is

$$L_{ko} = \log_2 |K| - \log_2 |K^o|$$

where

$$K_o = \{k' \mid k' \in K \text{ and } P(k') = o\}$$

Basic idea: counting the number of observations that have the same memory-access pattern.

```
// Dummy password checker
unsigned char key = input();
// key = [0 ... 255]
if(key == 128)
    A(); // branch 1
else if (key < 64)
    B(); // branch 2
else if (key < 128)
    C(); // branch 3
else
    D(); // branch 4
```

Example:

$$\begin{aligned} |K| &= 256 & |K_1| &= 1 & |K_2| &= 64 \\ L_{ko1} &= \log_2 256 - \log_2 1 = 8 \text{ bits} \\ L_{ko2} &= \log_2 256 - \log_2 64 = 2 \text{ bits} \end{aligned}$$

# Challenge 2: Leakage Dependence

- Suppose one program has two leakage sites A and B.

- Independent Leakage
- Mutual Exclusive Leakage
- Dependent Leakage

Leakage A:

$$\begin{cases} 0 \leq k_1 \\ k_1 \leq 255 \\ 3k_1 + k_2 > 127 \end{cases}$$

Leakage B:

$$\begin{cases} 0 \leq k_2 \\ k_2 \leq 255 \\ k_1 - 3k_2 > 0 \end{cases}$$

Leakage A and B :

$$\begin{cases} 0 \leq k_1 \\ k_1 \leq 255 \\ 3k_1 + k_2 > 127 \\ k_1 - 3k_2 > 0 \end{cases}$$

```
unsigned char k1, k2, t1, t2;
t1 = k1 + 2*k2;
t2 = 2*k1 - k2;
if(t2 + t1 > 127) // Leakage A
    A();
if(t2 - t1 > 0)   // Leakage B
    B();
```

if  $L_{(k_1 k_2)A} + L_{(k_1 + k_2)B} = L_{(k_1 + k_2)AB}$ ,  
then A and B are independent



# Challenge 3: Scalability

We want to quantify information leakages from real-world applications.

The performance suffers from the following aspects:

- Symbolic Execution
  - IR explosion
- Monte Carlo Sampling
  - #P problem

# Challenge 3: Scalability (Symbolic Execution)

- Why symbolic execution (SE) is slow?
  - Path Explosion ✓
  - Constraint Solving ✓
  - Intermediate Languages (IR) ?

## Why symbolic execution uses IR?

test eax, eax →

- Support many architecture platform.
  - X86, ARM, MIPS
- Easy to implement
  - X86, more than 1000 instructions
  - Side effects

```
STR R_EAX:32, , V_00:32
STR 0:1, , R_CF:1
AND V_00:32, ff:8, V_01:8
SHR V_01:8, 7:8, V_02:8
SHR V_01:8, 6:8, V_03:8
XOR V_02:8, V_03:8, V_04:8
SHR V_01:8, 5:8, V_05:8
SHR V_01:8, 4:8, V_06:8
XOR V_05:8, V_06:8, V_07:8
XOR V_04:8, V_07:8, V_08:8
SHR V_01:8, 3:8, V_09:8
SHR V_01:8, 2:8, V_10:8
XOR V_09:8, V_10:8, V_11:8
SHR V_01:8, 1:8, V_12:8
XOR V_12:8, V_01:8, V_13:8
XOR V_11:8, V_13:8, V_14:8
XOR V_08:8, V_14:8, V_15:8
AND V_15:8, 1:1, V_16:1
NOT V_16:1, , R_PF:1
STR 0:1, , R_AF:1
EQ V_00:32, 0:32, R_ZF:1
SHR V_00:32, 1f:32, V_17:32
AND 1:32, V_17:32, V_18:32
EQ 1:32, V_18:32, R_SF:1
STR 0:1, , R_OF:1
```

# Challenge 3: Scalability (Monte Carlo Sampling)

- The problem is #P-Hard.
- The number of satisfying assignments might be exponentially small.

$$\circ \text{ e.g., } F(K) = \begin{cases} k_1 = 1 \\ 120 < k_2 < 123 \\ k_3 = 3 \\ k_4 = 4 \\ k_5 = 5 \end{cases} \quad k_1, k_2, k_3, k_4, k_5 \in [0, 255]$$

Total search space:  $2^{40}$

Only two satisfying assignments

Solution: Markov Chain Monte Carlo Sampling (MCMC)

Chernoff bound:  $N \geq \Theta\left(\frac{\log \delta}{p \varepsilon^2}\right)$  to get an  $(\delta, \varepsilon)$  approximation scheme

# Implementation

- 15k LoC of C++11
- Trace Collection
  - Intel Pin Tool
- Symbolic Execution
  - arithmetic, bitwise, logical, control-transfer
  - Not support: AVX, floating number, AES-NI
- Information Leakage Computation

# Evaluation (Not finished)

- Real-world cryptosystems:
  - OpenSSL 0.9.7 1.1.1
  - mbedTLS 2.5 2.15
  - Libjpeg
- Performance
  - CacheD 5 hours
  - 30s found 8 secret-dependent memory access for the DES in mbedTLS 2.5

# Summary

Identify and quantify address-based side-channels leakages precisely

- A trace-based method that models each leakage site with math formulas.
- We quantify the information leakages based on the number of secrets that satisfy the constrain.
- Most of leakages found by recent works are hard to be exploited. (Need to be confirmed)