

UNIVERSITY OF TORONTO
FACULTY OF APPLIED SCIENCE AND ENGINEERING

FINAL EXAMINATION, APRIL 2006

First Year – Industrial and Mechanical Engineering Programs

ECE 110H1 S – ELECTRICAL FUNDAMENTALS

Exam. Type: A

Examiners – L. de Windt and B. Wang

NAME : (PLEASE PRINT)	<div style="border-bottom: 1px solid black; height: 1.2em; margin-bottom: 5px;"></div> FAMILY NAME	<div style="border-bottom: 1px solid black; height: 1.2em; margin-bottom: 5px;"></div> GIVEN NAME
STUDENT NUMBER :		

EXAMINATION TYPE : Type A – Paper for which no data are permitted other than the information printed on the examination paper.

CALCULATORS : ONLY Non-programmable scientific type allowed (models as specified in the Faculty Calendar).

DURATION : 2.5 hours

- INSTRUCTIONS :
- DO NOT UNSTAPLE THIS EXAM. BOOK.
 - Answer all six questions.
 - All six questions are of equal weight.
 - All work is to be done on these pages. Show methods, compute numerical results when requested and state units.
 - Place your final answer in the corresponding box. You may use the back of the preceding page for rough work.

$e = 1.6 \times 10^{-19} \text{C}, \quad \epsilon_o = 8.85 \times 10^{-12} \text{ F/m}, \quad \mu_o = 4\pi \times 10^{-7} \text{ H/m}$
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Question	Mark
1	
2	
3	
4	
5	
6	
Total	

Part A

If the net electric field at location p in Figure 1A, is zero, what is q_3 ?

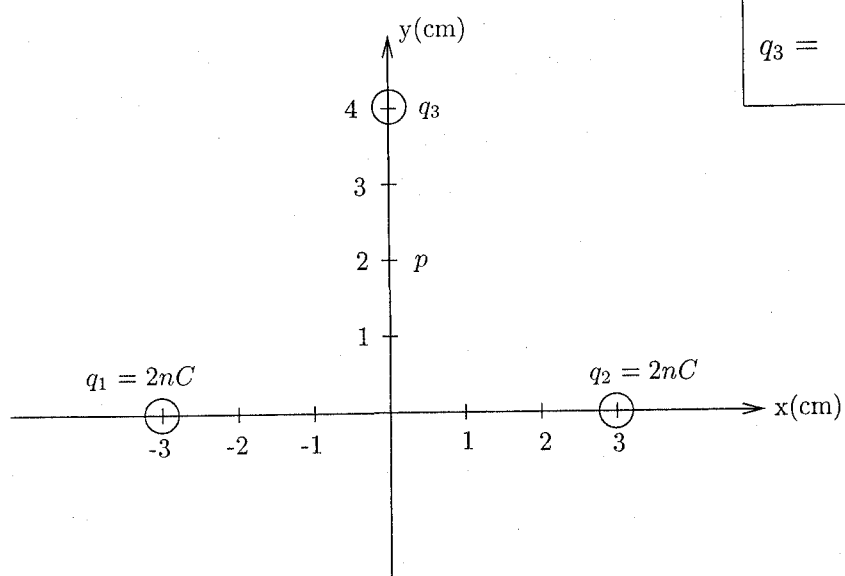


Figure 1A

$q_3 =$

Part B

Two point charges, $+Q$ and $-Q$, are placed in a region of space where the magnetic field \vec{B} is uniform and points in the $-Z$ direction. The charges are moving in parallel in the x direction with speed v . The distance between the point charges is r , as shown in Figure 1B. Find the expression of the speed v , for which the distance r between the charges is not changing in time.

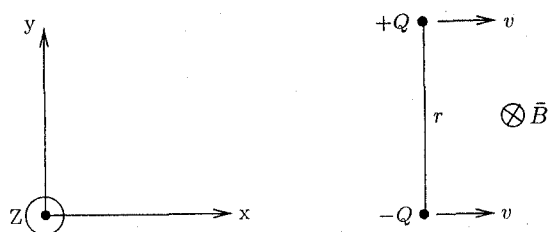


Figure 1B

$v =$

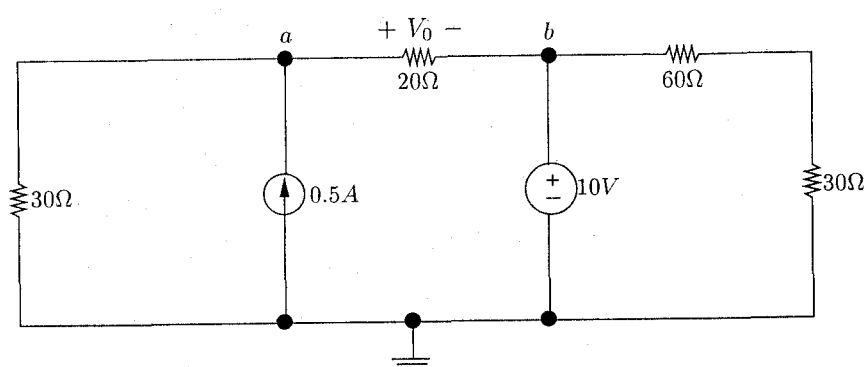


Figure 2

Part A

- (i) Find the voltage, V_0 in Figure 2.
- (ii) How much power is supplied by the 0.5A current source?

$$V_0 =$$

$$P_{0.5A} =$$

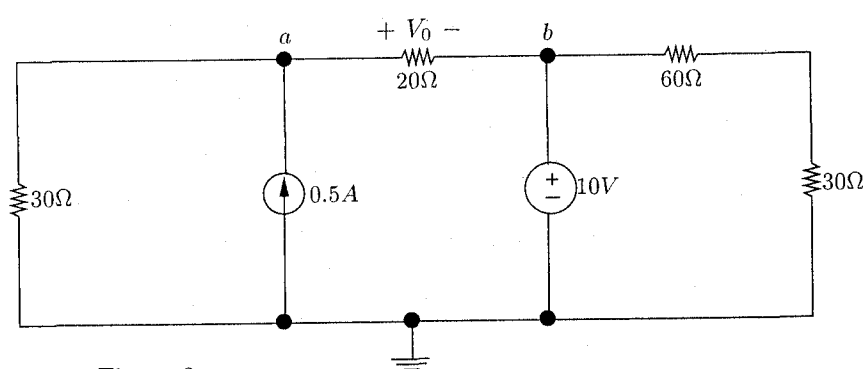


Figure 2

Part B

- (i) Remove the 20Ω load from the circuit in Figure 2, then find the Thevenin equivalent circuit between the terminals a and b .
- (ii) What is the maximum power that the circuit can deliver to a load?

Thevenin equivalent circuit

$P_{\max} =$

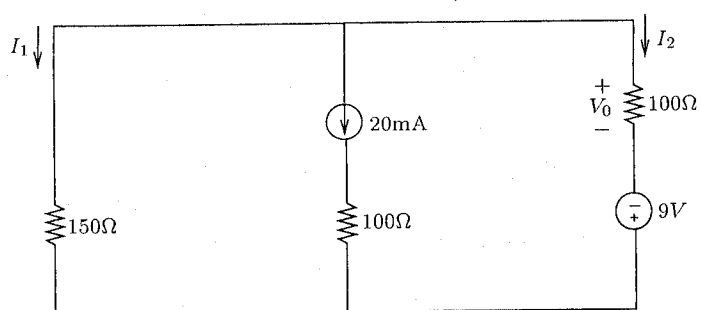


Figure 3

Part A

For the circuit shown in Figure 3, what is the contribution of the 20mA source to the current, I_1 , what is the contribution of the 9V source to the current, I_2 .

$$I_1 =$$

$$I_2 =$$

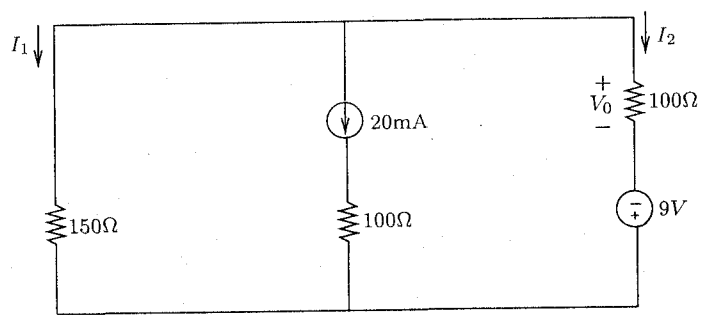


Figure 3

Part B

For the circuit shown in Figure 3, find the voltage, V_0 .

$V_0 =$

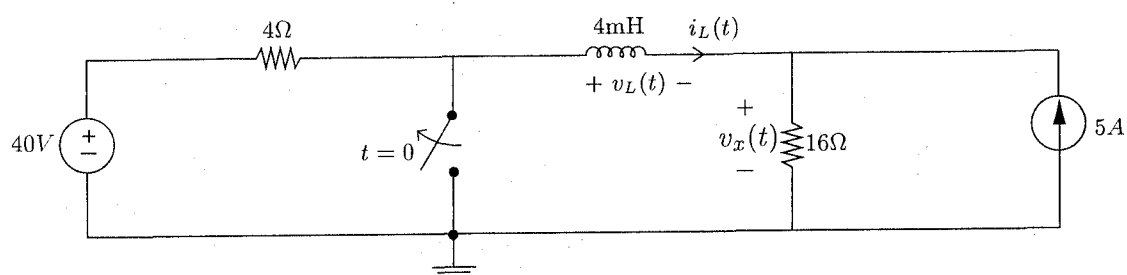


Figure 4

For the circuit shown in Figure 4, the switch has been closed for a long time before opening at $t = 0$. Determine:

- i) $i_L(0^-)$
 $i_L(0^+)$
 $v_x(0^-)$
 $v_L(0^+)$
 $i_L(\infty)$

$$i_L(0^-) =$$

$$i_L(0^+) =$$

$$v_x(0^-) =$$

$$v_L(0^+) =$$

$$i_L(\infty) =$$

- ii) The time constant τ for $t \geq 0^+$
 $i_L(t)$ for $t \geq 0^+$
 $v_L(t)$ for $t \geq 0^+$

$$\tau =$$

$$i_L(t) =$$

$$v_L(t) =$$

Part A

Design an inverting voltage amplifier with a voltage gain of -4 . You only have access to five $10k\Omega$ resistors and one operational amplifier. Assume the operational amplifier is ideal. Try to minimize the number of resistors used. Determine the input resistance of the inverting amplifier.

$$R_{in} =$$

Part B

For the circuit shown in Figure 5, the operational amplifiers are ideal and operating in their linear regions. Determine:

- i) The current gain i_0/i_s
- ii) The output voltage v_0

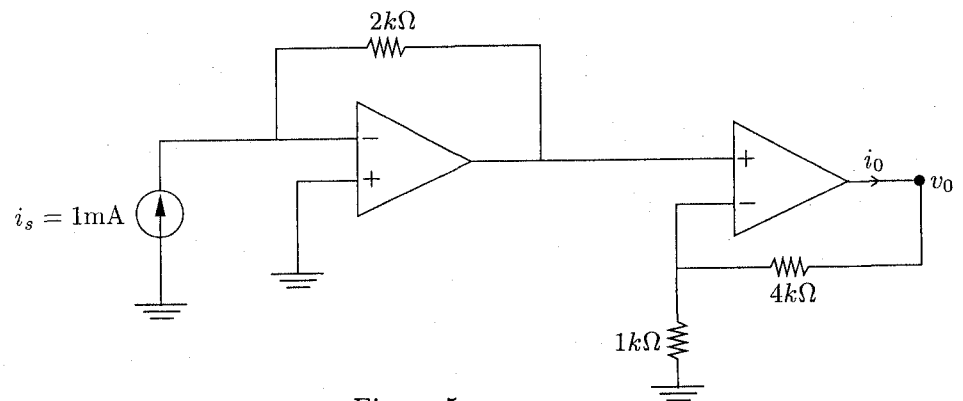


Figure 5

$$i_0/i_s =$$

$$v_0 =$$

Question 6

An industrial load operates at 38.4kW, 0.8 lagging power factor as shown in Figure 6. The load voltage is $240\angle 0^\circ \text{ V}_{\text{RMS}}$. The real and reactive power losses in the transmission line are 2kW and 3kVAR, respectively. Determine:

- i) The phasor current I
- ii) The impedance of the transmission line Z_{LINE}
- iii) The phasor voltage V_g

I

$Z_{\text{LINE}} =$

$V_g =$

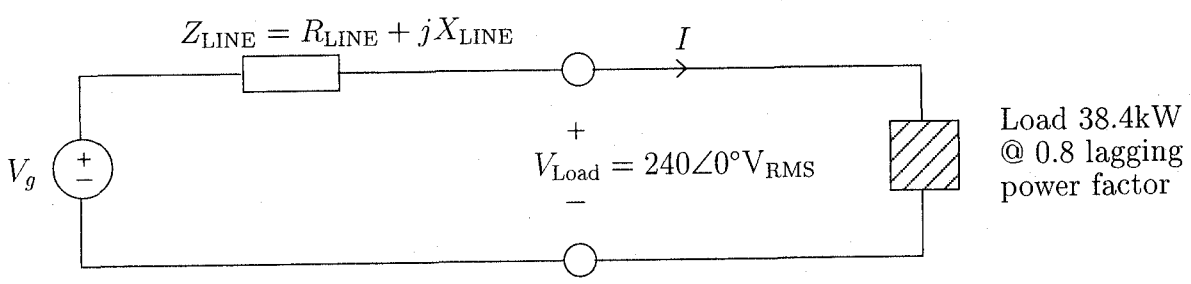


Figure 6