

# **MIE100S Dynamics – Spring 2014**

**Midterm Test – February 25, 2014**

**6:15 – 7:45 p.m.**

## **General Instructions:**

- Answer all questions in the exam booklets provided.
- Print your full ROSI name, student # and TUTORIAL # on your exam booklet(s).
- All rough work must be *neatly* shown to earn credit for each question
- You must use a pen or *dark* pencil
- Answer all three questions
- Total marks on this test = 100

## **Number of Pages:**

- 4 (including cover page)

## **Permitted Aids:**

- Non-communicating/non-programmable calculator: Casio FX-991MS or Sharp EL-520X
- One 8 ½” x 11” aid sheet, any colour. You may write on both sides of the sheet.

1. A box of mass  $m = 50 \text{ kg}$  slides down a hill. At the instant before it goes over the cliff (Position A in the diagram), the speed of the box is  $17 \text{ m/s}$ , the frictional force between the box and hill is  $130 \text{ Newtons}$ , the radius of curvature of the hill is  $28 \text{ meters}$ , and the hill is sloped down at  $20 \text{ degrees}$ .

(5 marks)

- (a) Find the normal component of the acceleration ( $a_n$ ) at the instant shown in the diagram.

(15 marks)

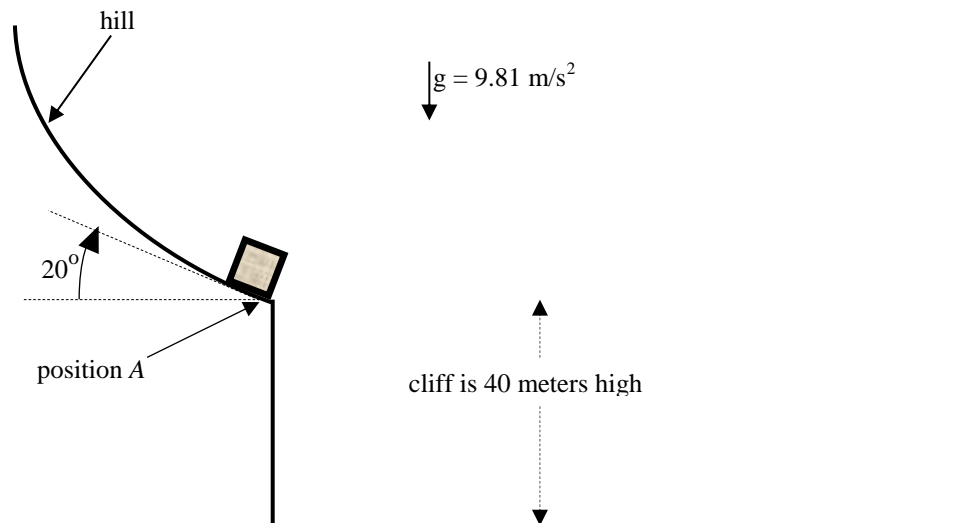
- (b) Find the coefficient of kinetic friction.

(10 marks)

- (c) What is the horizontal distance that the box will travel after it goes over the cliff of height  $40 \text{ meters}$ ?

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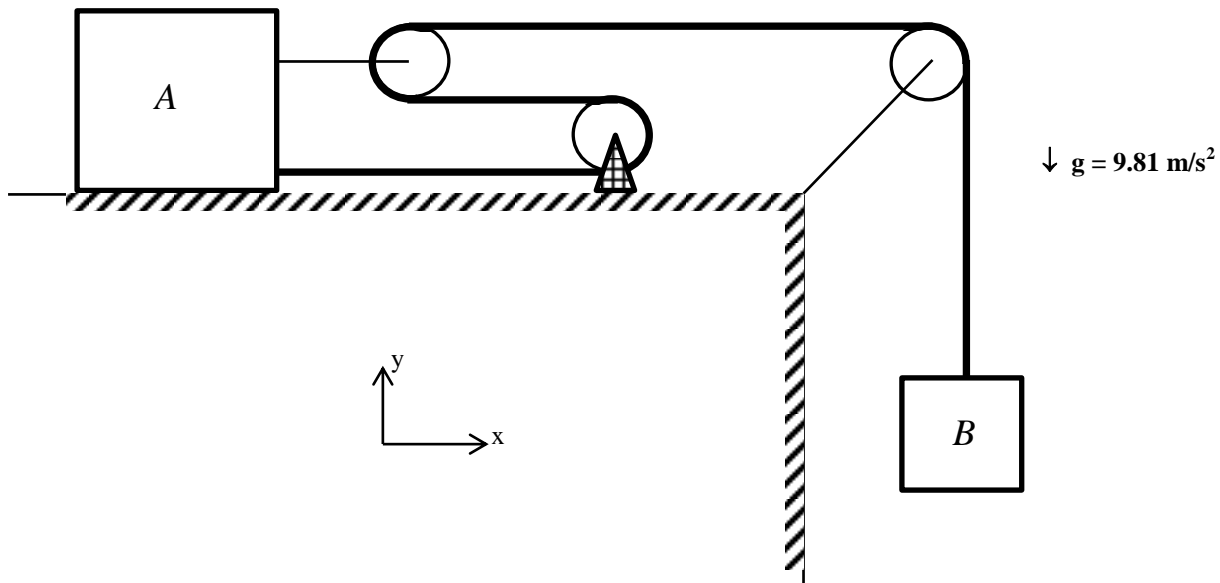


2. Crates  $A$  and  $B$  are connected by a rope and pulley system. At the instant shown in the diagram, the speed of crate  $A$  is  $0.5 \text{ m/s}$  to the right. The coefficient of kinetic friction  $\mu_k$  between the crate  $A$  and the ground is  $0.27$ .

$$\text{mass}_A = 44 \text{ kg.} \quad \text{mass}_B = 21 \text{ kg.}$$

(10 marks) (a) What is the kinetic energy of crate  $B$  at the instant shown in the diagram?

(20 marks) (b) What is the acceleration of crate  $B$  at the instant shown in the diagram?



3. Collars  $A$  and  $B$  slide on a frictionless rod as shown in the diagram. At the instant shown, collar  $B$  has a velocity of  $2 \text{ m/s}$  to the left, and collar  $A$  is sitting at rest on two platforms. The platforms are each attached to a spring and are initially held stationary with the springs compressed to an initial length  $x = 0.3 \text{ m}$ , as shown. Each spring has an unstretched (relaxed) length of  $1.5 \text{ m}$  and a spring constant of  $200 \text{ N/m}$ . The mass of collar  $A$  is  $4 \text{ kg}$  and the mass of collar  $B$  is  $5 \text{ kg}$ . Assume that the dimensions of both collars and the platforms are extremely small.

- (10 marks) (a) What is the total elastic potential energy of the two springs before the platforms are released?
- (20 marks) (b) When the platforms are released, collar  $A$  slides along the rod to point  $C$  where it collides with collar  $B$ . The two collars then stick together. What is the velocity of collars  $A$  and  $B$  immediately after they stick together, expressed in x-y coordinates?
- (10 marks) (c) How much heat is generated in the collision between collars  $A$  and  $B$ ?

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