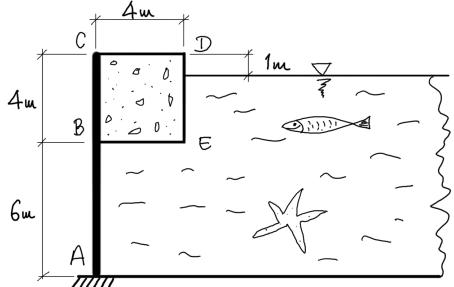


# CIV100F/APS160F – Mechanics: Final Exam 2016

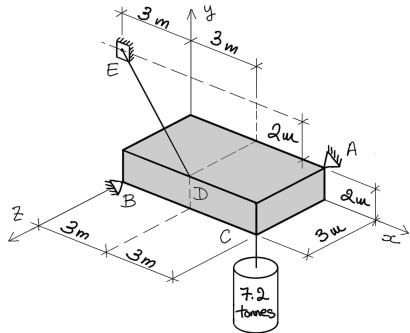
## Question 1

The structure  $ABCDE$  is used to prevent fresh water from flowing out of the long channel on the right. The weight of vertical panel  $ABC$  may be neglected and  $BCDE$  is made of reinforced concrete with a density of  $2,400 \text{ kg/m}^3$ . Determine the reaction force components at the fixed base  $A$ .



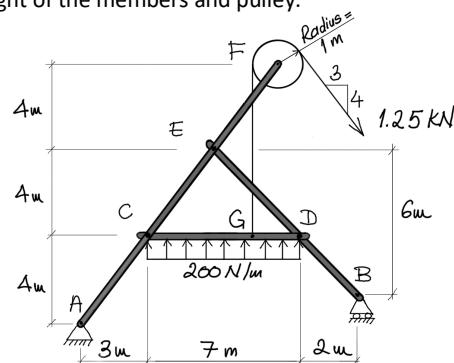
## Question 2

The rectangular prism is made of a solid, homogenous material having a density of  $1,400 \text{ kg/m}^3$  and must support a cylindrical container at  $C$ . The prism is supported by a cable  $DE$  and by ball-and-socket joints at  $A$  and  $B$ . The support at  $E$  lies in the  $x-y$  plane. Determine the magnitude of the force in cable  $ED$ . Express the force in cable  $ED$  in Cartesian vector format.



## Question 4

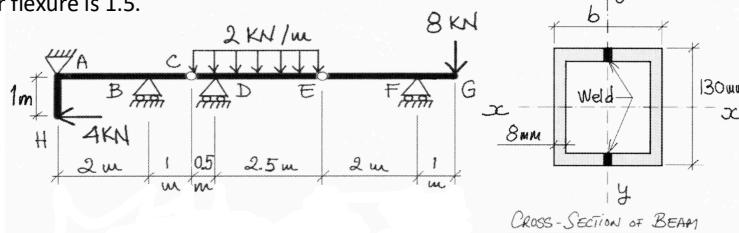
The three straight members in the structure shown are pin-connected and the pulley is frictionless. The rope is attached at one end to member  $CD$ , at  $G$ . Determine the components of all the forces acting on member  $ACEF$ . Present your answers on a separate free-body diagram of member  $ACEF$ . Neglect the weight of the members and pulley.



## Question 3

The hinged beam illustrated below is made of three rigid segments, connected by pins at  $C$  and  $E$ .  
 (a) Draw the shear force and bending moment diagrams in the space reserved below, indicating the values at  $A$ ,  $B$ ,  $C$ ,  $D$ ,  $E$ ,  $F$  and  $G$ , as well as any potential local maxima and minima;

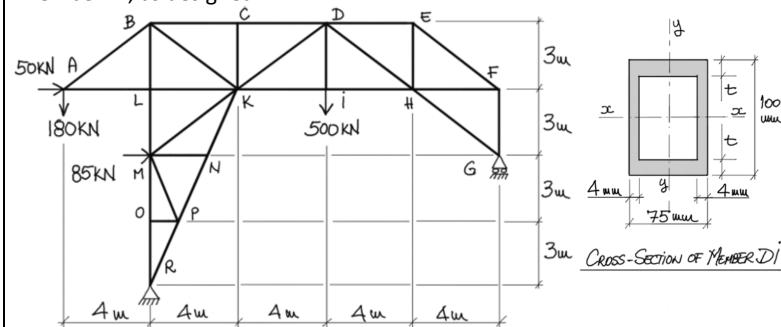
(b) The beam is made of two *identical* C-shaped bent plates, welded ‘toe-to-toe’ to form a hollow rectangle, as shown in the cross section. Before bending, each plate can be cut in multiples of 10 mm. Determine the width,  $b$ , of the beam such that it can safely carry the loads applied. The beam material is Grade 6061-T4 aluminium with a yield stress of 110 MPa and the required load factor for flexure is 1.5.



## Question 5

Illustrated below is a portal crane used in a ship-building yard. While lifting materials, the crane is also affected by wind loading. The forces acting on the crane from both lifting and wind are as illustrated.

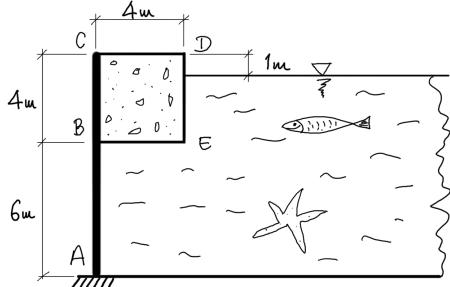
- (a) Find the forces in members  $DE$ ,  $DI$ ,  $IK$  and  $KL$  of the truss;
- (b) Member  $DI$  is to be constructed from a built-up steel hollow section constructed from four plates welded together, as indicated in the cross section. Determine the minimum plate thickness,  $t$ , considering that the material is available in one millimetre intervals. The yield stress for steel is 350 MPa and the load factor for axial tension is 1.1;
- (c) Knowing that the modulus of elasticity for steel is 200,000 MPa, determine the elongation of member  $DI$ , as designed.



# CIV100F/APS160F – Mechanics: Final Exam 2016

## Question 1

The structure  $ABCDE$  is used to prevent fresh water from flowing out of the long channel on the right. The weight of vertical panel  $ABC$  may be neglected and  $BCDE$  is made of reinforced concrete with a density of  $2,400 \text{ kg/m}^3$ . Determine the reaction force components at the fixed base  $A$ .

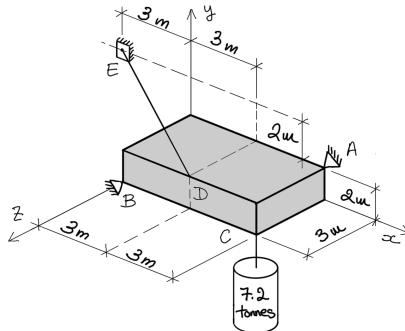


### Answers:

$$\begin{aligned} A_x &= 397 \text{ kN/m} \rightarrow \\ A_y &= 259 \text{ kN/m} \uparrow \\ M_A &= 674 \text{ kNm/m} \curvearrowright \end{aligned}$$

## Question 2

The rectangular prism is made of a solid, homogenous material having a density of  $1,400 \text{ kg/m}^3$  and must support a cylindrical container at  $C$ . The prism is supported by a cable  $DE$  and by ball-and-socket joints at  $A$  and  $B$ . The support at  $E$  lies in the  $x$ - $y$  plane. Determine the magnitude of the force in cable  $ED$ . Express the force in cable  $ED$  in Cartesian vector format.

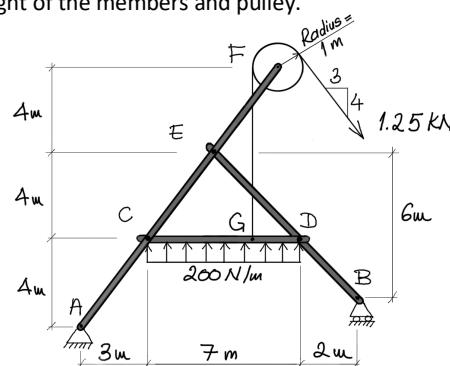


### Answers:

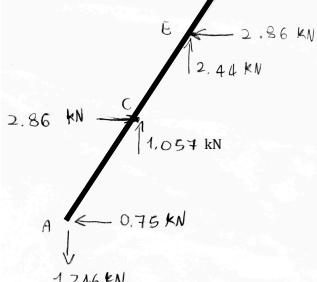
$$\begin{aligned} T_{ED} &= 123.6 \text{ kN (Tension)} \\ \vec{T}_{ED} &= -105.9\hat{i} + 35.3\hat{j} - 53.0\hat{k} \text{ kN} \end{aligned}$$

## Question 4

The three straight members in the structure shown are pin-connected and the pulley is frictionless. The rope is attached at one end to member  $CD$ , at  $G$ . Determine the components of all the forces acting on member  $ACEF$ . Present your answers on a separate free-body diagram of member  $ACEF$ . Neglect the weight of the members and pulley.



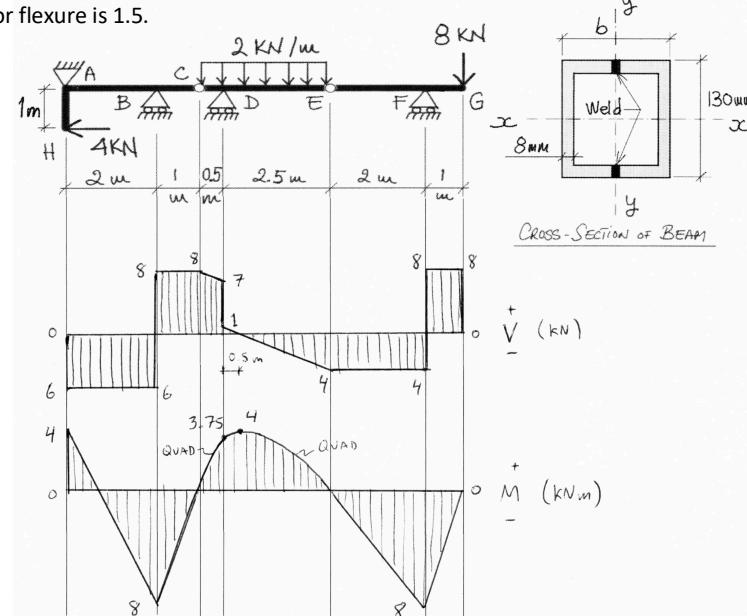
### Answer:



## Question 3

The hinged beam illustrated below is made of three rigid segments, connected by pins at  $C$  and  $E$ . (a) Draw the shear force and bending moment diagrams in the space reserved below, indicating the values at  $A$ ,  $B$ ,  $C$ ,  $D$ ,  $E$ ,  $F$  and  $G$ , as well as any potential local maxima and minima;

(b) The beam is made of two *identical* C-shaped bent plates, welded ‘toe-to-toe’ to form a hollow rectangle, as shown in the cross section. Before bending, each plate can be cut in multiples of 10 mm. Determine the width,  $b$ , of the beam such that it can safely carry the loads applied. The beam material is Grade 6061-T4 aluminium with a yield stress of 110 MPa and the required load factor for flexure is 1.5.



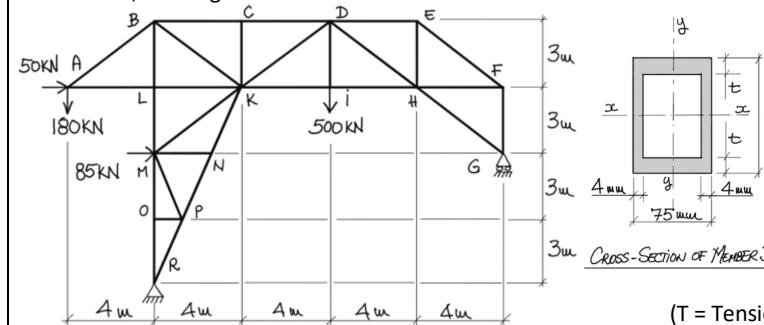
### Answer:

$$b = 90.0 \text{ mm}$$

## Question 5

Illustrated below is a portal crane used in a ship-building yard. While lifting materials, the crane is also affected by wind loading. The forces acting on the crane from both lifting and wind are as illustrated.

- Find the forces in members  $DE$ ,  $DI$ ,  $IK$  and  $KL$  of the truss;
- Member  $DI$  is to be constructed from a built-up steel hollow section constructed from four plates welded together, as indicated in the cross section. Determine the minimum plate thickness,  $t$ , considering that the material is available in one millimetre intervals. The yield stress for steel is 350 MPa and the load factor for axial tension is 1.1;
- Knowing that the modulus of elasticity for steel is 200,000 MPa, determine the elongation of member  $DI$ , as designed.



### Answers:

$$\begin{aligned} F_{DE} &= 353 \text{ kN (C)} \\ F_{DI} &= 500 \text{ kN (T)} \\ F_{IK} &= 707 \text{ kN (T)} \\ F_{KL} &= 290 \text{ kN (C)} \\ t &= 6.00 \text{ mm} \\ \Delta_{DI} &= +4.68 \text{ mm} \\ (\text{T} &= \text{Tension}; \text{C} = \text{Compression}) \end{aligned}$$