



UNIVERSITY OF TORONTO
FACULTY OF APPLIED SCIENCE & ENGINEERING

DATE
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NAME
Prof. J. A. Packer

COURSE NO.

COURSE NAME

CIV100F: Mechanics

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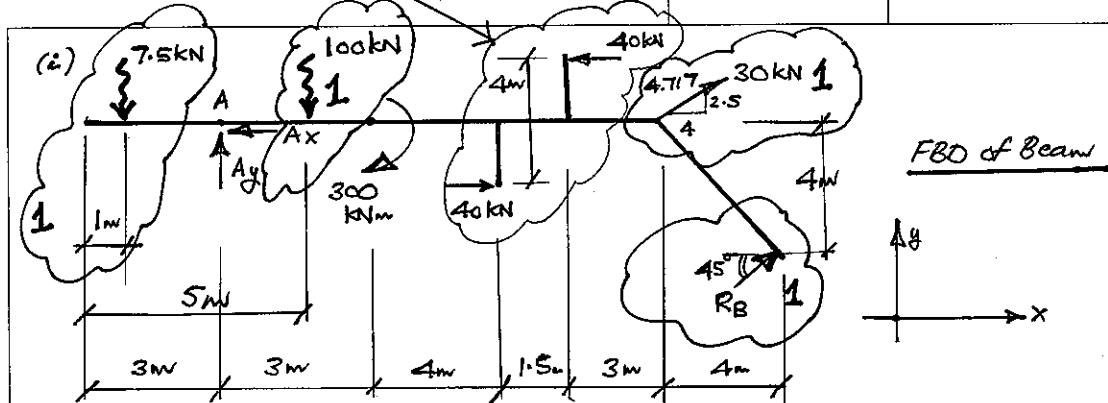
MIDTERM.

Q1.

Can also be
shown as

160kNm

4.



FBD of Beam

2.

$$(ii) \sum M_A = 0 \Rightarrow -7.5(2) + 100(2) + 300 - 40(4) - \left(\frac{2.5}{4.717}\right)(30)(11.5) - R_B \cos 45^\circ (4) - R_B \cos 45^\circ (15.5)$$

1.

$$\therefore 325 - 182.85 - 19.5 \cos 45^\circ \cdot R_B = 0$$

$$\therefore R_B = \frac{7.2897}{\cos 45^\circ} = \frac{10.31 \text{ kN}}{\frac{1}{2}} \quad \text{Reaction @ B.}$$

1.

$$\sum F_x = 0 \Rightarrow -A_x + \left(\frac{4}{4.717}\right)(30) + (10.31) \cos 45^\circ = 0 \quad \therefore A_x = 32.7 \text{ kN} \leftarrow$$

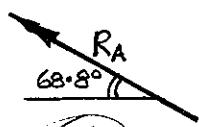
1.

$$\sum F_y = 0 \Rightarrow -7.5 + A_y - 100 + \left(\frac{2.5}{4.717}\right)(30) + R_B \cos 45^\circ = 0 \quad \therefore A_y = 84.3 \text{ kN} \uparrow$$

1.

$$\therefore \text{Reaction @ A} = \sqrt{32.7^2 + 84.3^2} = \underline{90.4 \text{ kN}}$$

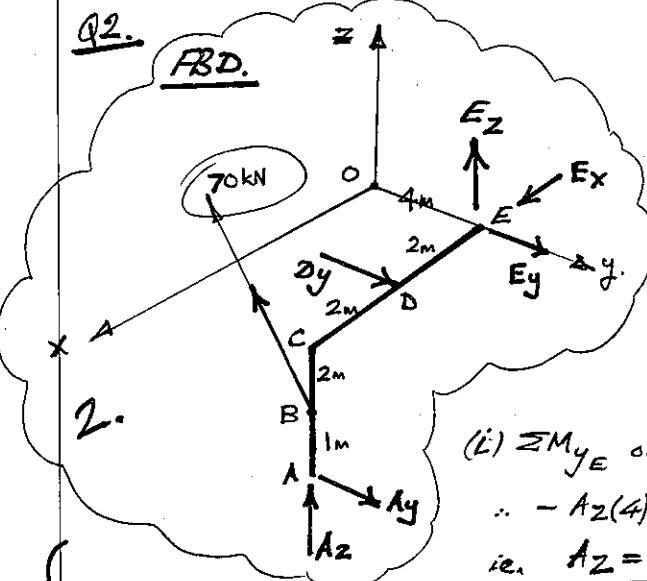
$\Sigma = 10$





Q2.

FBD.



$$\text{Length of BF} = \sqrt{(4)^2 + (-4)^2 + (6)^2} \\ = 7.4833 \text{ m}$$

$$\therefore F_{BF_x} = \left(\frac{2}{7.4833}\right)(70) = 18.708 \text{ kN}$$

$$\therefore F_{BF_y} = \left(\frac{-4}{7.4833}\right)(70) = -37.417 \text{ kN}$$

$$\therefore F_{BF_z} = \left(\frac{6}{7.4833}\right)(70) = 56.125 \text{ kN}$$

$$(i) \sum M_{y_E} \text{ or line } OE = 0$$

$$\therefore -A_2(4) - 18.708(2) - 56.125(4) = 0 \therefore A_2 = -65.48 \text{ kN}$$

$$\text{i.e. } A_2 = 65.5 \text{ kN}$$

$$(ii) \sum M_{x_E} \text{ or line } EC = 0 \Rightarrow A_y(3) - 37.417(2) = 0 \therefore A_y = 24.945 \text{ kN}$$

$$\text{i.e. } A_y = 24.9 \text{ kN}$$

$$(iii) \sum M_{z_E} = 0 \Rightarrow D_y(2) + 24.945(4) - 18.708(4) - 37.417(4) = 0 \\ \therefore D_y = 24.944 \text{ kN} \quad \text{i.e. } D_y = 24.9 \text{ kN}$$

$$(iv) \sum F_x = 0 \Rightarrow E_x + 18.708 \text{ kN} = 0 \therefore E_x = 18.71 \text{ kN}$$

$$(v) \sum F_y = 0 \Rightarrow E_y + 24.944 + 24.9 - 37.417 = 0 \therefore E_y = -12.427 \quad \text{i.e. } E_y = 12.43 \text{ kN}$$

$$(vi) \sum F_z = 0 \Rightarrow E_z - 65.5 + 56.125 = 0 \therefore E_z = 9.38 \quad \text{i.e. } E_z = 9.38 \text{ kN}$$

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$$\therefore \text{Reaction at } A = (24.9\hat{j} - 65.5\hat{k}) \text{ kN}$$

$$\text{Reaction at } D = 24.9\hat{j} \text{ kN}$$

$$\text{Reaction at } E = (-18.71\hat{i} - 12.43\hat{j} + 9.38\hat{k}) \text{ kN}$$

OR

Alternatively, for steps (i), (ii) & (iii) above, $\sum M_E = 0$ and vector cross products can be used ($\vec{r} \times \vec{F}$,

$$\text{i.e. } \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 4 & 0 & -2 \\ 18.71 & -37.42 & 56.13 \end{vmatrix} + \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 0 & 0 \\ 0 & D_y & 0 \end{vmatrix} + \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 4 & 0 & -3 \\ 0 & A_y & A_2 \end{vmatrix} = 0$$

\downarrow
to 70kN

\downarrow
to D_y

\downarrow
to h.

$$\text{i.e. } (-74.84\hat{i} - 261.94\hat{j} - 149.68\hat{k}) + (20y\hat{k}) + (3A_y\hat{i} - 4A_2\hat{j} + 4A_y\hat{k}) = 0$$

$$\text{i.e. } (-74.84 + 3A_y)\hat{i} + (-261.94 - 4A_2)\hat{j} + (-149.68 + 4A_y)\hat{k} = 0$$

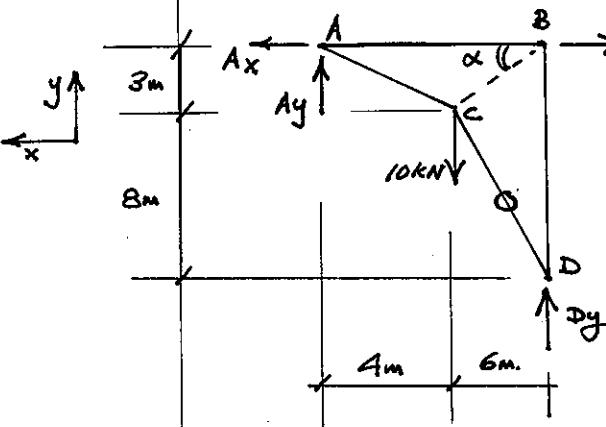
$= 0$

$= 0$

$= 0$



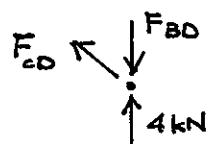
Q3. (a) FBD of Whole Truss



$$\alpha = 26.565^\circ$$

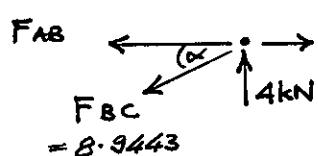
$$\begin{aligned}\sum M_A = 0 \Rightarrow 10(4) - Dy(10) = 0 \therefore Dy = 4 \text{ kN} \quad \uparrow \frac{1}{2} + \frac{1}{2} \\ \sum F_y = 0 \Rightarrow Ay + 4 - 10 = 0 \therefore Ay = 6 \text{ kN} \quad \uparrow \frac{1}{2} + \frac{1}{2} \\ \sum F_x = 0 \Rightarrow Ax - 10 = 0 \therefore Ax = 10 \text{ kN} \quad \leftarrow \frac{1}{2} + \frac{1}{2}\end{aligned}$$

FBD of Joint D:

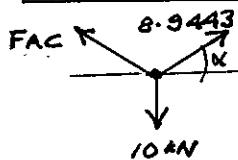


$$\begin{aligned}\sum F_x = 0 \Rightarrow F_{CD} = 0 \quad \frac{1}{2} + \frac{1}{2} \\ \sum F_y = 0 \Rightarrow F_{BD} = 4 \text{ kN C.} \quad \frac{1}{2} + \frac{1}{2}\end{aligned}$$

FBD of Joint B:



FBD of Joint C:



$$\sum F_y = 0 \Rightarrow F_{BC} \sin \alpha = 4 = 0$$

$$\begin{aligned}\therefore F_{BC} = 8.94 \text{ kN T.} \quad \frac{1}{2} + \frac{1}{2} \\ \sum F_x = 0 \Rightarrow F_{AB} + 8.94 \cos \alpha - 10 = 0 \\ \therefore F_{AB} = 2.00 \text{ kN T.} \quad \frac{1}{2} + \frac{1}{2}\end{aligned}$$

$$\sum F_x = 0 \Rightarrow 8.000 - F_{AC} \left(\frac{4}{5}\right) = 0$$

$$\therefore F_{AC} = 10.000 \text{ kN T.} \quad \frac{1}{2} + \frac{1}{2}$$

1/2 for Magnitude
1/2 for Direction or sense.

Check @ Joint A:



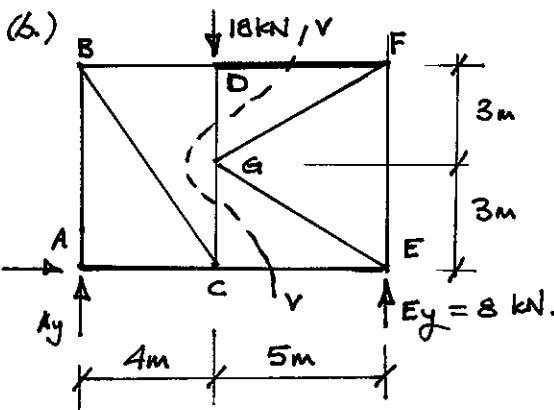
$$\sum F_x = 10 - 2 - 10\left(\frac{4}{5}\right) = 0 \checkmark$$

$$\sum F_y = 6 - 10\left(\frac{3}{5}\right) = 0 \checkmark$$

Solution Correct: ✓

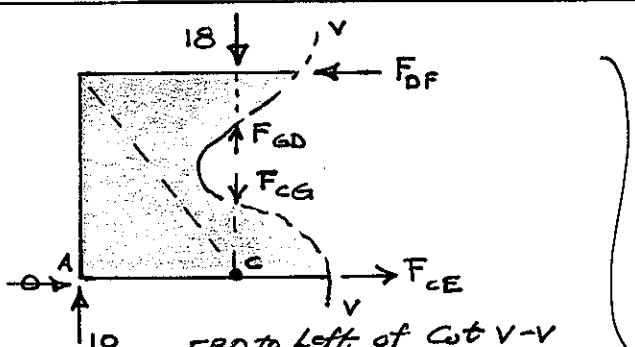
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Not necessary but a good check



FBD of Whole Truss

$$\begin{aligned}\sum M_A = 0 \Rightarrow 18(4) - Ey(9) = 0 \\ \therefore Ey = 8 \text{ kN} \\ \therefore Ay = 10 \text{ kN} \quad \& Ax = 0.\end{aligned}\quad \left\{ \frac{1}{2} \right.$$



Section V-V actually produces 4 unknown forces, but 3 unknown forces have lines of action that pass through point C!

$$\begin{aligned}\therefore \sum M_C = 0 \Rightarrow 10(4) - F_{DF}(6) = 0 \\ \therefore F_{DF} = 6.67 \text{ kN C.}\end{aligned}\quad \left. \frac{1}{2} \right)$$

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