

UNIVERSITY OF TORONTO  
FACULTY OF APPLIED SCIENCE AND ENGINEERING

FINAL EXAMINATION, APRIL 2006

First Year – Industrial and Mechanical Engineering Programs

ECE 110H1 S – ELECTRICAL FUNDAMENTALS

Exam. Type: A

Examiners – L. de Windt and B. Wang

NAME : (PLEASE PRINT)	FAMILY NAME	GIVEN NAME
STUDENT NUMBER :		

EXAMINATION TYPE : Type A – Paper for which no data are permitted other than the information printed on the examination paper.

CALCULATORS : ONLY Non-programmable scientific type allowed (models as specified in the Faculty Calendar).

DURATION : 2.5 hours

- INSTRUCTIONS :
- DO NOT UNSTAPLE THIS EXAM. BOOK.
  - Answer all six questions.
  - All six questions are of equal weight.
  - All work is to be done on these pages. Show methods, compute numerical results when requested and state units.
  - Place your final answer in the corresponding box. You may use the back of the preceding page for rough work.

$$e = 1.6 \times 10^{-19} \text{ C}, \quad \epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}, \quad \mu_0 = 4\pi \times 10^{-7} \text{ H/m}$$

Question	Mark
1	
2	
3	
4	
5	
6	
Total	

**Part A**

If the net electric field at location  $p$  in Figure 1A, is zero, what is  $q_3$ ?

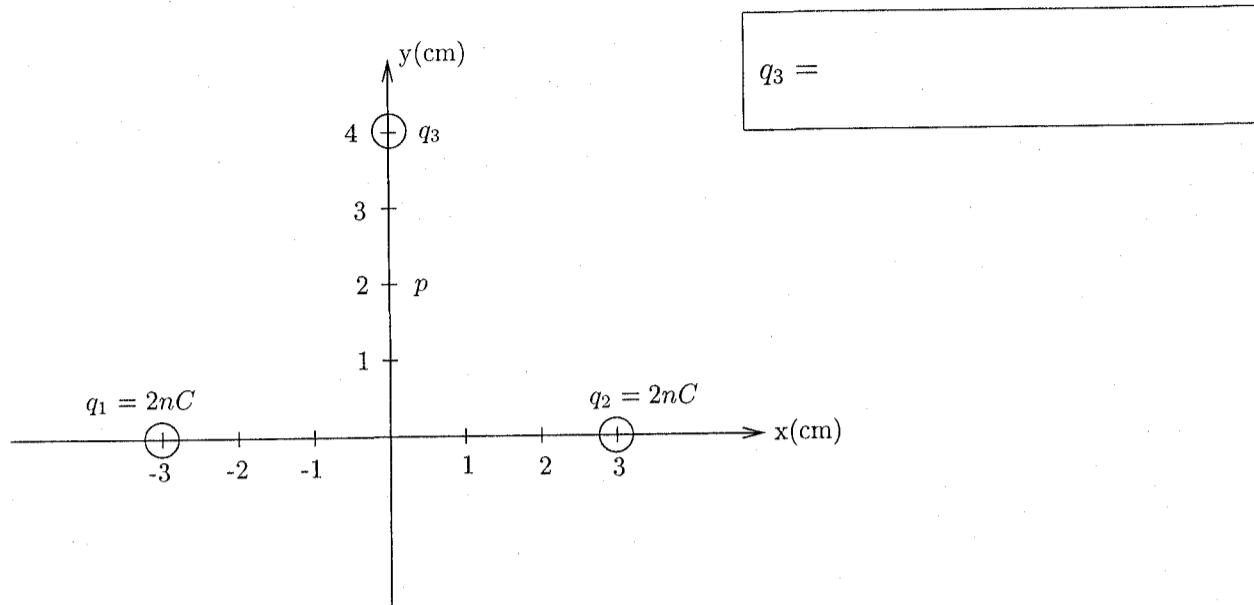


Figure 1A

Part B

Two point charges,  $+Q$  and  $-Q$ , are placed in a region of space where the magnetic field  $\vec{B}$  is uniform and points in the  $-Z$  direction. The charges are moving in parallel in the  $x$  direction with speed  $v$ . The distance between the point charges is  $r$ , as shown in Figure 1B. Find the expression of the speed  $v$ , for which the distance  $r$  between the charges is not changing in time.

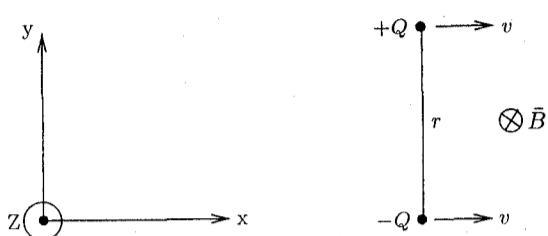


Figure 1B

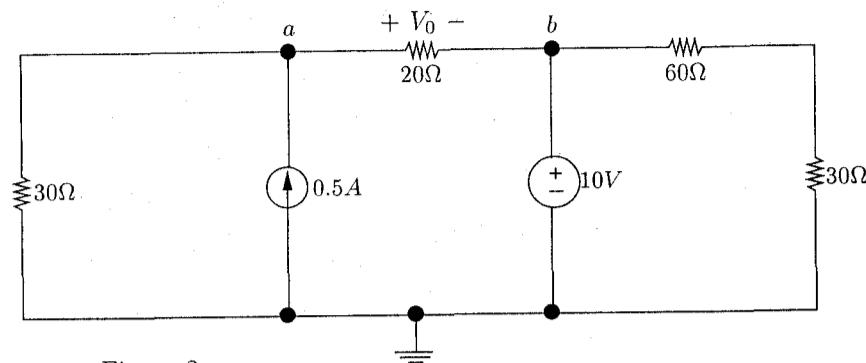


Figure 2

Part A

- (i) Find the voltage,  $V_0$  in Figure 2.
- (ii) How much power is supplied by the  $0.5A$  current source?

$$V_0 =$$

$$P_{0.5A} =$$

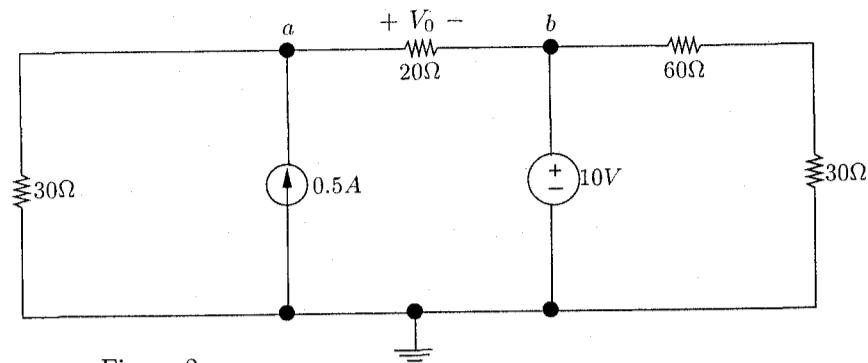


Figure 2

Part B

- Remove the  $20\Omega$  load from the circuit in Figure 2, then find the Thevenin equivalent circuit between the terminals  $a$  and  $b$ .
- What is the maximum power that the circuit can deliver to a load?

Thevenin equivalent circuit

$P_{\max} =$

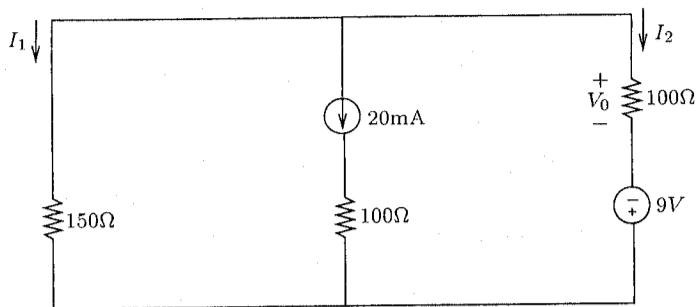


Figure 3

**Part A**

For the circuit shown in Figure 3, what is the contribution of the 20mA source to the current,  $I_1$ , what is the contribution of the 9V source to the current,  $I_2$ .

$$I_1 =$$

$$I_2 =$$

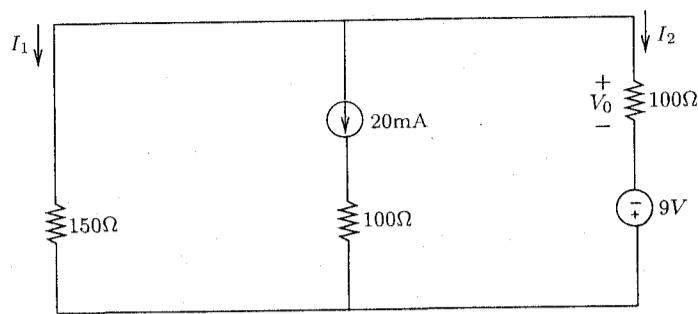


Figure 3

**Part B**

For the circuit shown in Figure 3, find the voltage,  $V_0$ .

$$V_0 =$$

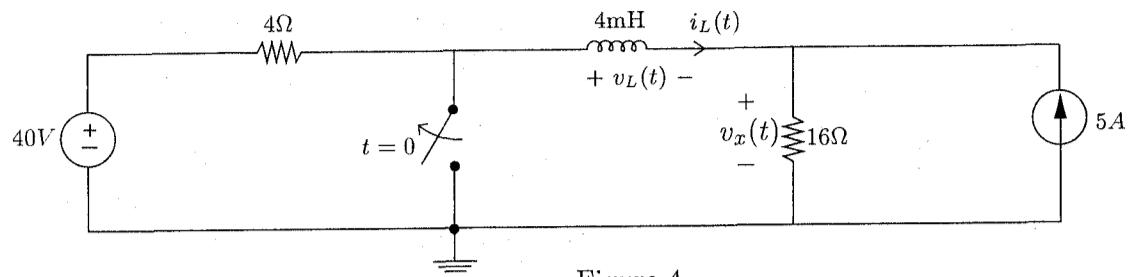


Figure 4

For the circuit shown in Figure 4, the switch has been closed for a long time before opening at  $t = 0$ . Determine:

- i)  $i_L(0^-)$
- $i_L(0^+)$
- $v_x(0^-)$
- $v_L(0^+)$
- $i_L(\infty)$

$$i_L(0^-) =$$

$$i_L(0^+) =$$

$$v_x(0^-) =$$

$$v_L(0^+) =$$

$$i_L(\infty) =$$

- ii) The time constant  $\tau$  for  $t \geq 0^+$
- $i_L(t)$  for  $t \geq 0^+$
- $v_L(t)$  for  $t \geq 0^+$

$$\tau =$$

$$i_L(t) =$$

$$v_L(t) =$$

**Part A**

Design an inverting voltage amplifier with a voltage gain of  $-4$ . You only have access to five  $10k\Omega$  resistors and one operational amplifier. Assume the operational amplifier is ideal. Try to minimize the number of resistors used. Determine the input resistance of the inverting amplifier.

$$R_{in} =$$

**Part B**

For the circuit shown in Figure 5, the operational amplifiers are ideal and operating in their linear regions. Determine:

- i) The current gain  $i_0/i_s$
- ii) The output voltage  $v_0$

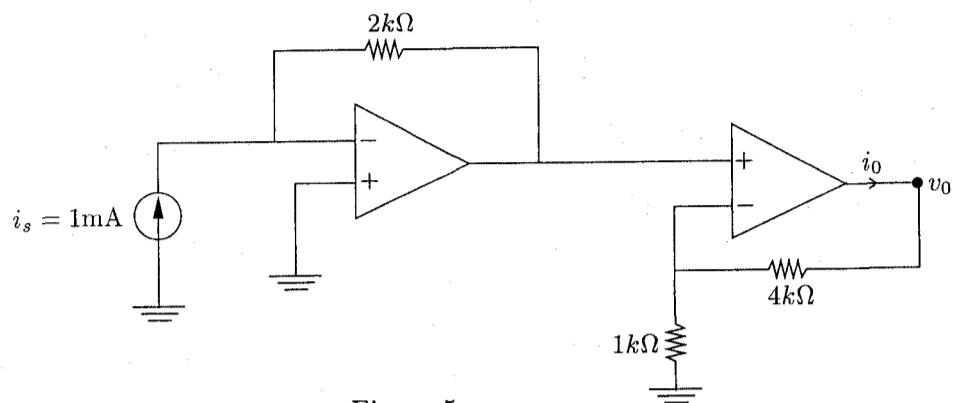


Figure 5

$$i_0/i_s =$$

$$v_0 =$$

Question 6

An industrial load operates at 38.4kW, 0.8 lagging power factor as shown in Figure 6. The load voltage is  $240\angle 0^\circ \text{ V}_{\text{RMS}}$ . The real and reactive power losses in the transmission line are 2kW and 3kVAR, respectively. Determine:

- i) The phasor current  $I$
- ii) The impedance of the transmission line  $Z_{\text{LINE}}$
- iii) The phasor voltage  $V_g$

$I$
$Z_{\text{LINE}} =$
$V_g =$

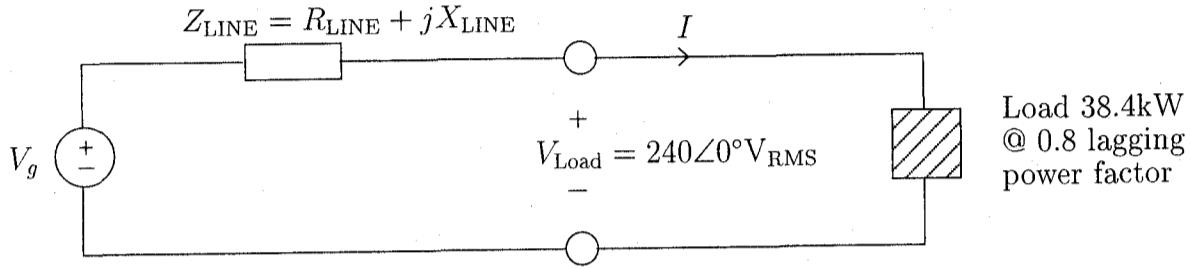


Figure 6