

MIE 100S Quiz 1a Jan 12, 2015

First name and Last name printed correctly as seen on ROSI (1 mark)  
Legibility and neatness (1 mark)

$$\text{Given: } a = \frac{175}{v^2} \frac{m}{s^2} \text{ and } v_0 = 30 \frac{m}{s}$$

$$\begin{aligned}\frac{dv}{dt} &= a \\ \frac{dv}{dt} &= \frac{175}{v^2} \\ \int v^2 dv &= \int 175 dt \\ \frac{1}{3} v^3 &= 175t + C\end{aligned}$$

Can determine constant from initial conditions:

$$v_0 = v(t = 0) = 30 \frac{m}{s}$$

Plugging into equation above:

$$\begin{aligned}\frac{1}{3}(30)^3 &= 175(0) + C \\ C &= 9000\end{aligned}$$

and therefore  $v$  is given by:  $v = \sqrt[3]{525t + 27000}$

$$\text{and } t \text{ is given by: } t = \frac{v^3}{525} - \frac{9000}{175}$$

a)  $v(t = 4) = \sqrt[3]{525(4) + 27000} = 30.76 \text{ m/s}$

4 marks

b)  $t(v = 50) = \frac{50^3}{525} - \frac{9000}{175} = 186.67 \text{ s}$

4 marks