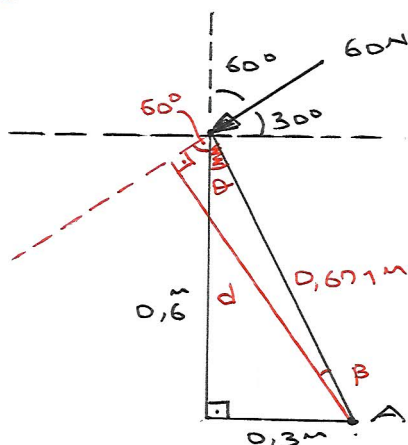




1- (i) Using the Resultant Force Given :

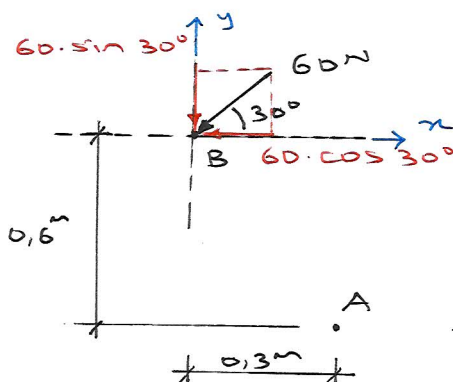


$$\begin{aligned} \theta &= \tan^{-1}\left(\frac{0.3}{0.6}\right) = 26.56^\circ \\ \beta &= 30 - \theta = 3.44^\circ \\ d &= 0.671 \cdot \cos 3.44^\circ = 0.67 \text{ m} \end{aligned}$$

$$\Rightarrow M_A = 60 \text{ N} \cdot 0.67 \text{ m} = 40.187 \text{ N}\cdot\text{m}$$

Answer : $M_A = 40 \text{ N}\cdot\text{m}$ (ccw)

(ii) Using the components :



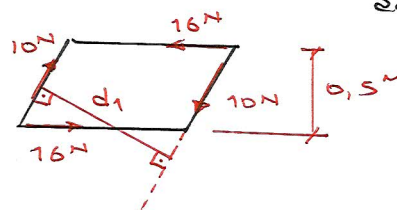
$$\begin{aligned} \Rightarrow M_A &= 60 \cdot \cos 30 \cdot 0.6 + 60 \cdot \sin 30 \cdot 0.3 \\ &= 40.177 \text{ N}\cdot\text{m} \end{aligned}$$

Answer : $M_A = 40 \text{ N}\cdot\text{m}$ (ccw)

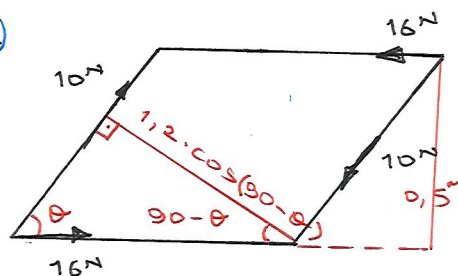
note : components method is typically easier to apply.

2- (i) $M = 16 \text{ N} \cdot 0.5 \text{ m} = 8.0 \text{ N}\cdot\text{m}$ (ccw) (independent of any point)

(ii) $16 \text{ N} \cdot 0.5 = 10 \text{ N} \cdot d_1$
 $\Rightarrow d_1 = 0.8 \text{ m}$



(iii)

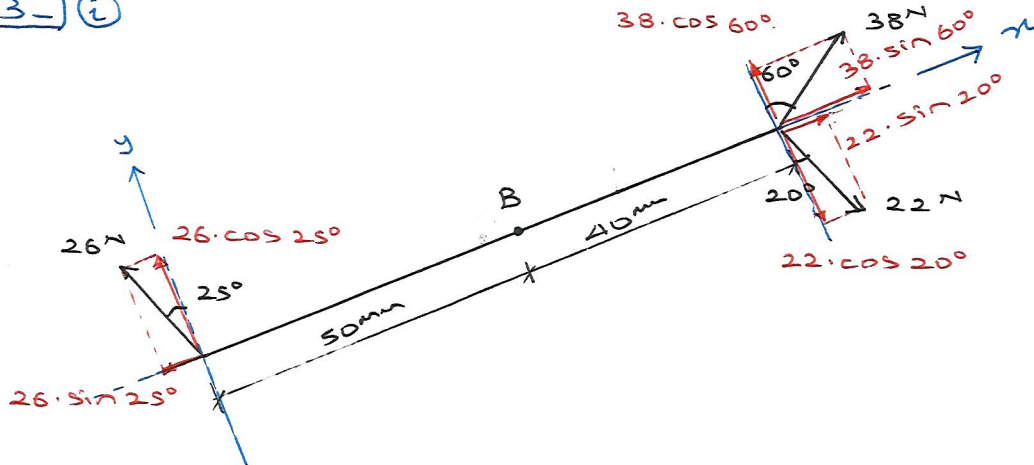


$$\begin{aligned} \Rightarrow 10 \text{ N} \cdot 1.2 \cos(90 - \theta) - 16 \cdot 0.5 \text{ m} &= 2.1 \text{ N}\cdot\text{m} \\ \Rightarrow \theta &= 57.32^\circ \end{aligned}$$

Answer : $\theta = 57^\circ$



3- i



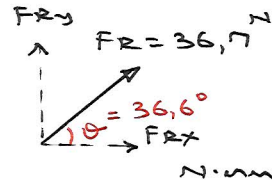
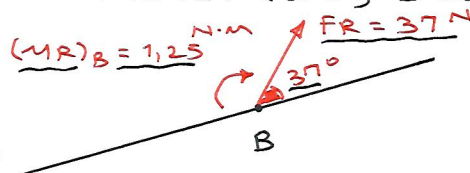
$$\bullet F_{Rx} = 38 \sin 60^\circ + 22 \sin 20^\circ - 26 \sin 25^\circ = 29,45 \text{ N}$$

$$\bullet F_{Ry} = 38 \cos 60^\circ - 22 \cos 20^\circ + 26 \cos 25^\circ = 21,89 \text{ N}$$

$$\bullet (M_R)_B = 38 \cos 60^\circ \cdot 40 \text{ mm} - 22 \cos 20^\circ \cdot 40 \text{ mm} - 26 \cos 25^\circ \cdot 50 \text{ mm} = -1245,1 \text{ N}\cdot\text{mm}$$

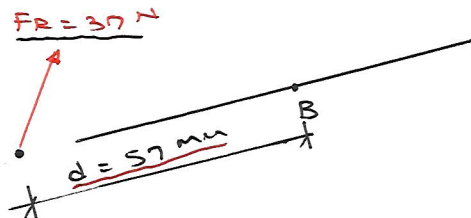
NOTE: I selected x and y axes such that 3 components will not create moment. (only 3 components along y needed)

Answer:



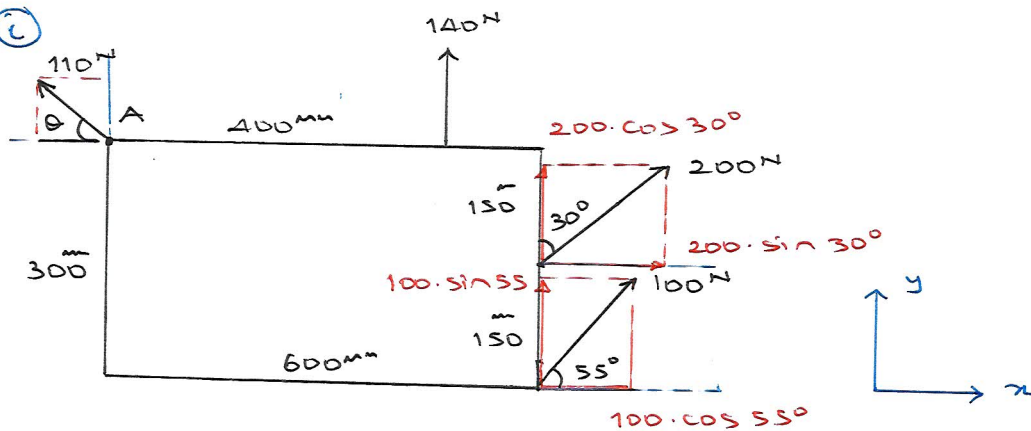
ii- $(M_R)_B = F_{Ry} \cdot d \Rightarrow 1245,1 = 21,89 \cdot d \Rightarrow d = 56,88 \text{ mm}$

Answer:



NOTE: to have $(M_R)_B$ CW, must place F_R to the left of point B.

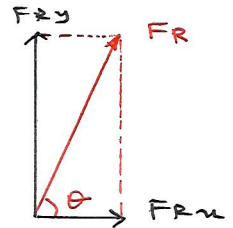
4- i





4-i-cont'd

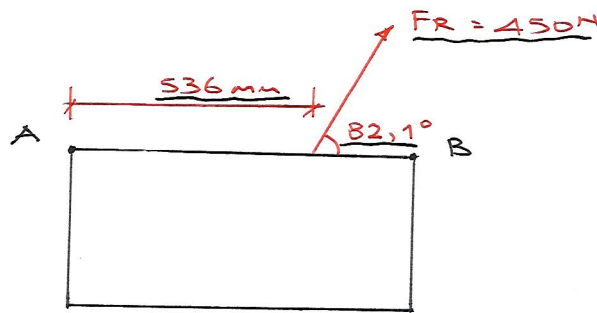
- $F_{Rx} = 200 \cdot \sin 30^\circ + 100 \cdot \cos 55^\circ - 110 \cdot \cos 30^\circ = 62,1 \text{ N} \rightarrow$
- $F_{Ry} = 200 \cdot \cos 30^\circ + 100 \cdot \sin 55^\circ + 110 \cdot \sin 30^\circ + 140 = 450,1 \text{ N} \uparrow$
- $\Rightarrow F_R = \sqrt{F_{Rx}^2 + F_{Ry}^2} = 454,4 \text{ N}$
- $\Theta = \tan^{-1}(F_{Ry} / F_{Rx}) = 82,14^\circ$



- $(M_R)_A = (200 \cdot \cos 30^\circ + 100 \cdot \sin 55^\circ) \cdot 600 \text{ mm} + 140 \cdot 400 \text{ mm} + 200 \cdot \sin 30^\circ \cdot 150 \text{ mm} + 100 \cdot \cos 55^\circ \cdot 300 \text{ mm} = 241279,46 \text{ N} \cdot \text{mm}$

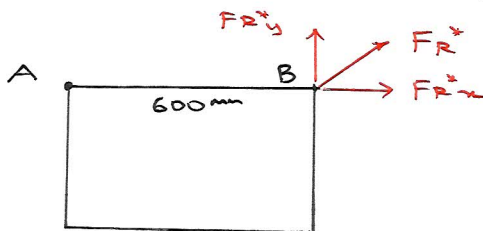
- $(M_R)_A = F_{Ry} \cdot d \Rightarrow 241279,46 = 450,1 \cdot d \Rightarrow d = 536,1 \text{ mm}$

Answer:



$F_R^* \neq F_R$

(ii) Changing Θ will not change $(M_R)_A$. Find F_R^* at B to create the same $(M_R)_A$.



- $(M_R)_A = F_{Ry}^* \cdot 600 \text{ mm}$
- $\Rightarrow F_{Ry}^* = 402,13 \text{ N}$

• In the original system, resultant vertical force must be equal to F_{Ry}^* .

- $200 \cos 30^\circ + 100 \sin 55^\circ + 140 + 110 \cdot \sin \Theta = F_{Ry}^* = 402,13 \text{ N}$
- $\Rightarrow \sin \Theta = 0,06254 \Rightarrow \Theta = 3,65^\circ$

Answer: $\Theta = 3,65^\circ$

• note: F_{Rx} will not create any moment at A; therefore, we did not use it.