

*Please mark X to indicate your tutorial section.
Failure to do so will result in a deduction of 5 marks.*

UNIVERSITY OF TORONTO

FACULTY OF APPLIED SCIENCE AND ENGINEERING

Final Exam

20 April 2015

APS 104S

INTRODUCTION TO MATERIALS AND CHEMISTRY

Exam Type B

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TUT 01	
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NAME: _____
Last First

STUDENT NO: _____

INSTRUCTIONS:

- This is a Type B examination. Only non-programmable calculators are allowed.
- Answer all seven questions.
- All work is to be done on the pages of this booklet.
- When answering the questions **include all the steps** of your work on these pages and then **fill the answer in the respective boxes**. For additional space, you may use the back of the preceding page.
- Do not unstaple this exam booklet.
- A Formula Sheet and the periodic table are attached to the end of this exam booklet; if you wish, you may tear-off these sheets *only*.

Q1	/20
Q2	/20
Q3	/20
Q4	/20
Q5	/20
Q6	/20
Q7	/20
Total	/140

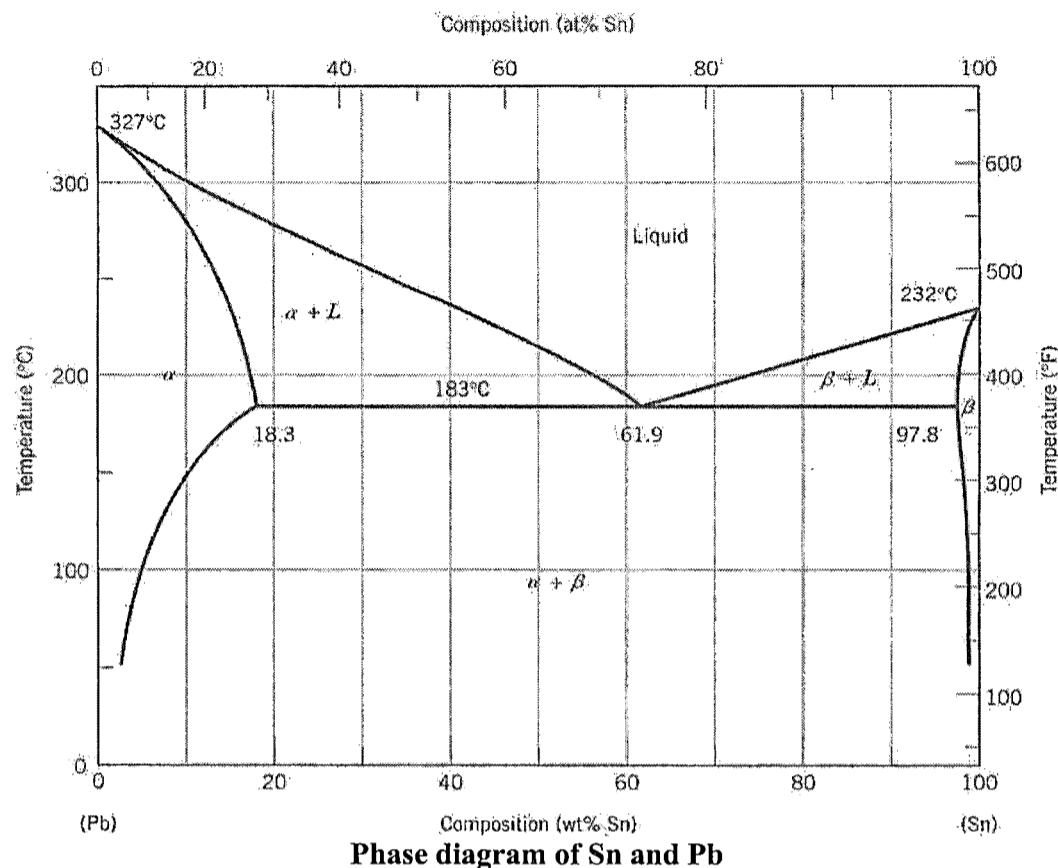
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Problem 1. Binary Phase Diagrams

A phase diagram of tin and lead is shown below.

For Part 1a-1d, we examine the slow cooling of a 30 wt% Sn-70 wt% Pb mixture from the liquid phase to 150 °C.



1a. What is the temperature at which the first solid phase is formed. [2 pts]

1b. What is the composition of the last drop of liquid in the alloy before complete solidification. [2 pts]

1c. Determine the i) phase(s), ii) their respective weight fractions, and iii) their composition(s) of the phases when the temperature reaches 150 °C.

[2 pts] Phase(s):

[2 pts] Weight Fraction(s):

[2 pts] Composition(s) of each phase:

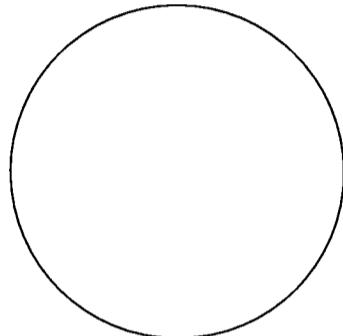
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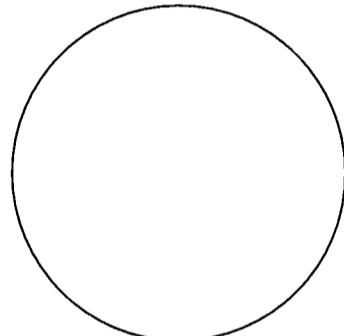
- 1d. What is the minimum weight fraction of β in the mixture containing only solid phases that can be formed from the 30 wt% Sn-70 wt% Pb during the cooling process (from liquid phase to 150 °C)? [2 pts]

- 1e. Consider cooling a second sample with 75% Sn from the liquid phase to 100°C.

- i) Sketch the microstructure at T = 184°C. Label all of the phases present. [2 pts]



- ii) Sketch the microstructure at T = 182°C. Label all of the phases present. [2 pts]

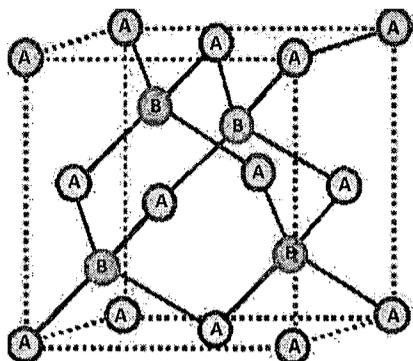


- iii) At T = 182°C, calculate the weight fractions of the solid solution and the eutectic phase. [4 pts]

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Problem 2: Crystal Structures

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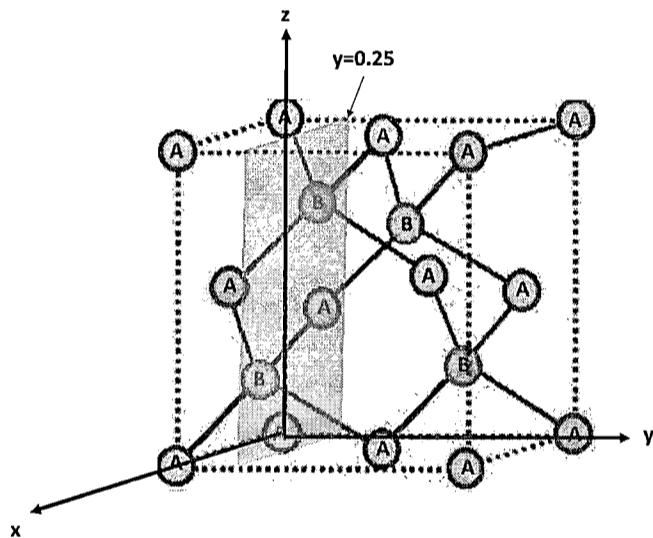
The crystal structure of Mercury(II) Telluride ($\text{Hg}^{2+}\text{Te}^{2-}$) is shown below. The radius of Mercury(II) ion is 116 pm and that of the Telluride ion is 211 pm.



2a. Name the crystal structure. _____ [2 pts]

2b. The coordination number of atom A in the figure is _____ [2 pts]

2c. The Planar (Miller) Indices of the plane highlighted below are: [2 pts]



2d. The planar density (PD) is defined as:

$$\text{PD} = \frac{\text{number of atoms centered on a plane}}{\text{area of plane}}$$

Determine the planar density of the plane in Part 2c, in atom nm⁻². [4 pts]

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2e. Determine the theoretical density of HgTe, in g cm⁻³. [6 pts]

2f. As the ionic radius for cation-to-anion increases, the appropriate crystal structures change from (select the correct answer): [4 pts]

- a. Sodium chloride, cesium chloride, zincblende
- b. Cesium chloride, zincblende, sodium chloride
- c. Zincblende, sodium chloride, cesium chloride
- d. Cesium chloride, sodium chloride, zincblende

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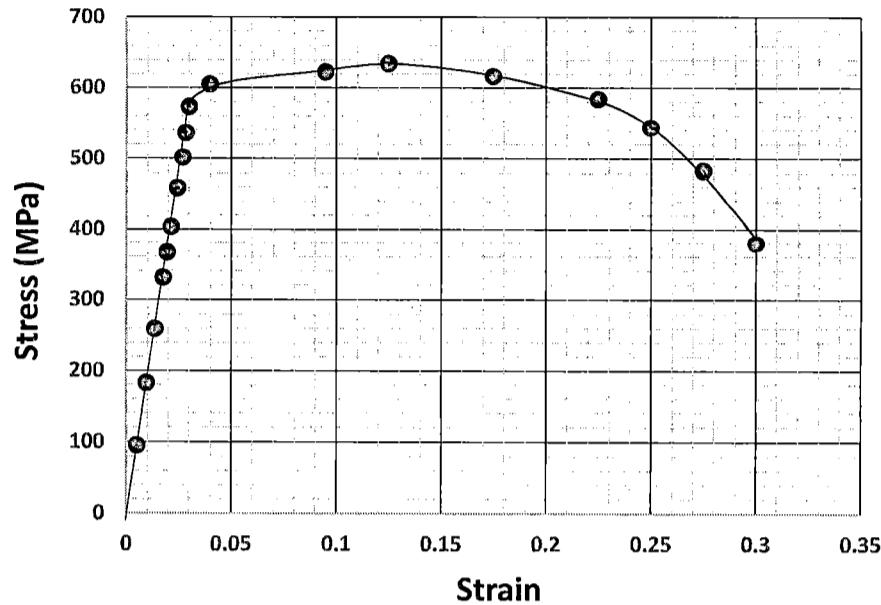
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Problem 3: Mechanical Properties

You are evaluating a bronze alloy specimen with a cross-sectional area of 500 mm^2 and length of 6 mm.

You are given:

- 1) stress-strain behavior (see figure below) and
- 2) the Poisson's ratio for this material is 0.30



Stress-strain behavior of a bronze alloy specimen.

3a. What is the maximum load (in N) that can be sustained by the specimen? [2pts]

3b. What is the maximum load (in N) that can be applied to the bronze alloy specimen without plastic deformation? [2 pts]

3c. Determine the specimen cross-sectional area when the specimen is pulled in tension with a force of 200 000 N. [4 pts]

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3d. What is the ductility, in percent of elongation? [4 pts]

3e. How do you determine the toughness of this sample? [2 pts]

3f Calculate the toughness of the sample. [2pts]

3g. Select the correct answer: [4 pts]

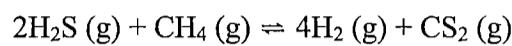
- i. Brittle materials generally never exhibit higher tensile strengths than ductile materials
- ii. During plastic deformation, the bonds between original atom neighbors are broken and new bonds are formed.
- iii. Ceramics typically absorb large amount of energy than metal before their catastrophic fracture.
- iv. When porosity increases, the flexural strength also increases accordingly.

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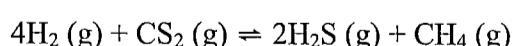
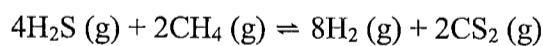
Problem 4: Equilibrium and ΔG°

4(a) A 1-L vessel initially contains 0.2 M $\text{CH}_4(\text{g})$ and 0.8 M $\text{H}_2\text{S}(\text{g})$ at 973 K. Assume the process given below reaches equilibrium when 30% of the $\text{CH}_4(\text{g})$ reacts with the $\text{H}_2\text{S}(\text{g})$ to produce $\text{H}_2(\text{g})$ and $\text{CS}_2(\text{g})$ products, according to:



Calculate the equilibrium constants (K_c and K_p) and ΔG° for this reaction at 973 K [6 pts].

4(b) Calculate K_c for the following related chemical equations at 973 K [4 pts].



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4(c) If K_p for the reaction “ $2\text{H}_2\text{S}(\text{g}) + \text{CH}_4(\text{g}) \rightleftharpoons 4\text{H}_2(\text{g}) + \text{CS}_2(\text{g})$ ” is 3.02×10^{-5} at 25°C , and also using the results from part a), calculate $\Delta H^\circ_{\text{reaction}}$ (assumption: $\Delta H^\circ_{\text{reaction}}$ is independent of temperature) [6 pts].

4(d) How would the equilibrium position change, if the following actions are performed on the reaction “ $2\text{H}_2\text{S}(\text{g}) + \text{CH}_4(\text{g}) \rightleftharpoons 4\text{H}_2(\text{g}) + \text{CS}_2(\text{g})$ ” system? Circle the correct response [4 pts].

- | | | | |
|---|----------------------|---------------------|----------------------|
| 1) Addition of iron mixed with metal oxides catalyst | <i>move to right</i> | <i>move to left</i> | <i>doesn't shift</i> |
| 2) Decreasing temperature | <i>move to right</i> | <i>move to left</i> | <i>doesn't shift</i> |
| 3) Increasing the volume of the vessel | <i>move to right</i> | <i>move to left</i> | <i>doesn't shift</i> |
| 4) Increasing the partial pressure of $\text{CS}_2(\text{g})$ | <i>move to right</i> | <i>move to left</i> | <i>doesn't shift</i> |

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Problem 5: Thermodynamics

One mole of an ideal diatomic gas is compressed from an initial pressure and temperature of 1 bar and 300 K to a final pressure of 4 bar in three different reversible process paths given below. For each path, calculate w, q, ΔU , ΔH , and ΔS for the process.

(a) the process is adiabatic [7 pts].

(b) the process takes place at constant volume [7 pts].

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(c) the process takes place isothermally [6 pts].

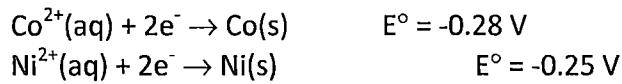
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Problem 6: Electrochemistry

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A voltaic cell with Ni/Ni²⁺ and Co/Co²⁺ half-cells has the following initial concentrations: [Ni²⁺]=0.80 M; [Co²⁺] = 0.20 M.

Standard Reduction Potentials at 25 °C



(a) Write the overall reaction that occurs spontaneously under standard conditions and circle the reducing agent in the equation. [3 pts]

(b) Write the cell notation for the voltaic cell that incorporates the above reaction. [2 pts]

(c) What is the initial E_{cell}? [3 pts]

(d) What is [Ni²⁺] when E_{cell} reaches 0.03 V? [4 pts]

(e) What are equilibrium concentrations of the ions? [5 pts]

(f) If the cell was run from the initial conditions to equilibrium at 10A, how many hours will it take to reach equilibrium? Assume 1L volume in each half cell. [3 pts]

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Problem 7: Electrical Properties

Assume that Indium contributes three free electrons per atom to electrical conduction. The density of In is 7.31 g/cm^3 and its resistivity is $8.37 \times 10^{-8} \Omega \cdot \text{m}$.

(a) What is the electron mobility of indium? [10 pts]

(b) How long would an In wire of 0.1 mm diameter have to be to have a resistance of 50Ω ? [4 pts]

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(c) Silicon has the following properties:

	E_g	n_i	μ_e	μ_h
units	eV	m^{-3}	$m^2/V \cdot s$	$m^2/V \cdot s$
Si	1.10	1.3×10^{16}	0.135	0.045

Calculate the conductivity of intrinsic Silicon. [4 pts]

(d) Which of the following statements is true? Circle the correct answer. [2 pts]

- Electrons and holes contribute equally to conductivity in intrinsic Si
- Electrons contribute more than holes to conductivity in intrinsic Si
- Holes contribute more than electrons to conductivity in intrinsic Si

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FORMULAE & CONSTANTS (You may tear this sheet off.)

$$R = 8.3145 \text{ J}\cdot\text{K}^{-1} \text{ mol}^{-1} = 0.08320574587 \text{ L}\cdot\text{atm}\cdot\text{K}^{-1} \text{ mol}^{-1} = 0.083145 \text{ L}\cdot\text{bar}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$$

$$1 \text{ atm} = 101.325 \text{ kPa} = 1.01325 \text{ bar} = 14.696 \text{ psi} = 760 \text{ Torr} = 760 \text{ mmHg}$$

$$N_A = 6.022 \times 10^{23} \text{ mol}^{-1} \quad k = 8.62 \times 10^{-5} \text{ eV/K} \quad 1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}$$

$$T(\text{K}) = T(\text{°C}) + 273.15 \text{ K} \quad F = 9.6485309 \times 10^4 \text{ C mole}^{-1} \quad e = 1.60217733 \times 10^{-19} \text{ C}$$

$$\text{STP: } 273.15\text{K, 1 atm} \quad \text{SATP: } 298.15\text{K, 1 bar} \quad 1\text{L atm} = 101.325 \text{ J}$$

Mechanical properties

$$E = \frac{\sigma}{\epsilon} \quad \sigma = \frac{F}{A} \quad \epsilon = \frac{\Delta l}{l} \quad \tau = \frac{F}{A} \quad \tau = G\gamma \quad U_r = \frac{1}{2} \sigma_Y \epsilon_Y \quad \% \text{CW} = \left(\frac{A_0 - A_d}{A_0} \right) \times 100 \quad G = E/(2(1+\nu))$$

$$\nu = -\frac{\epsilon_L}{\epsilon} = -\frac{\epsilon_x}{\epsilon_z} = -\frac{\epsilon_y}{\epsilon_z}$$

Electrical properties

$$V = IR \quad \rho = \frac{RA}{l} \quad \sigma = \frac{1}{\rho} \quad v_d = \mu_e E \quad \sigma = n|e|\mu_e$$

$$\sigma = n|e|\mu_e + p|e|\mu_h$$

Electrochemistry

$$E = E^\circ - \frac{RT}{nF} \ln Q \quad E = E^\circ - \frac{0.0592}{n} \log Q \quad \text{at } 25^\circ\text{C} \quad I = \frac{nC}{t}$$

Ideal gas equation of state: $PV = nRT$

First law, closed systems

$$\Delta U = q + w \quad dU = dq + dw$$

$$dw = -P_{\text{ext}} dV$$

$$dU = nC_v dT$$

$$H \equiv U + PV$$

$$dH = nC_p dT$$

$$\text{For ideal gases, } C_{p,m} = C_{v,m} + R$$

$$\text{Solids, Liquids, } C_{p,m} = C_{v,m}$$

$$G \equiv H - TS$$

$$dS = \frac{dQ_{\text{reversible}}}{T}$$

For a process at constant temperature

$$\Delta G = \Delta H - T\Delta S$$

For an isothermal reversible process (ideal gas):

$$W_{\text{rev}} = - \int_{V_1}^{V_2} \frac{nRT}{V} dV = -nRT \ln \frac{V_2}{V_1} = -nRT \ln \frac{P_1}{P_2}$$

Adiabatic reversible process (ideal gas):

$$P_1 V_1^\gamma = P_2 V_2^\gamma \quad T_1 V_1^{(\gamma-1)} = T_2 V_2^{(\gamma-1)} \quad T_1 P_1^{[(1-\gamma)/\gamma]} = T_2 P_2^{[(1-\gamma)/\gamma]} \quad \left(\frac{\bar{C}_p}{\bar{C}_v} \right) = \gamma$$

$$\frac{T_2}{T_1} = \left(\frac{V_2}{V_1} \right)^{-R/\bar{C}_v} \quad \frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{R/\bar{C}_p}$$

v_i : stoichiometric coefficient

Assuming no phase change, constant C_p

$$\Delta H^\circ_{\text{rxn}} = \sum v_i * \Delta H^\circ_{f,i} + \Delta C_p * (T - 25^\circ\text{C})$$

$$\Delta C_p = \sum v_i * C_{p,i}$$

For solids or liquids:

$$\text{Phase transition } \Delta S_{\text{trans}} = \frac{\Delta H_{\text{trans}}}{T_{\text{trans}}}$$

$$\Delta S^\circ(T_2) = \Delta S^\circ(T_1) + \int_{T_1}^{T_2} \Delta C_p \frac{dT}{T}$$

$$\Delta S = nR \ln \frac{V_f}{V_i} \quad (\text{isothermal})$$

$$\Delta S = nC_v \ln \frac{T_f}{T_i} \quad (\text{change in T at const V})$$

$$\Delta S = nC_p \ln \frac{T_f}{T_i} \quad (\text{change in T at const P})$$

Standard entropy of reaction $\Delta S^\circ_{\text{rxn}} = \sum v_i * S_m^\circ_i$

$$\Delta S = n\bar{C}_p \ln \left(\frac{T_2}{T_1} \right) - nR \ln \left(\frac{P_2}{P_1} \right)$$

$$\Delta S = n\bar{C}_v \ln \left(\frac{T_2}{T_1} \right) + nR \ln \left(\frac{V_2}{V_1} \right)$$

Standard free energy of a reaction: $\Delta G^\circ_{\text{rxn}} = \sum v_i * \Delta G^\circ_{f,i}$ or $\Delta G^\circ_{\text{rxn}} = \Delta H^\circ_{\text{rxn}} - T\Delta S^\circ_{\text{rxn}}$

$$\Delta G^\circ = -RT \ln K$$

$$\ln \left(\frac{K_p(T_1)}{K_p(T_2)} \right) = -\frac{\Delta H_{\text{reaction}}^\circ}{R} \left(\frac{1}{T_1} - \frac{1}{T_2} \right) \quad (\text{assuming } \Delta H_{\text{reaction}}^\circ \text{ independent of } T)$$

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Total free energy of the reaction $aA + bB \Rightarrow cC + dD$

$$\Delta G_{rxn} = \Delta G_{rxn}^{\theta} + RT \ln(Q)$$

where

$$where Q = \left[\frac{a_C^c a_D^d}{a_A^a a_B^b} \right] \text{ where } a = \text{activity}$$

$$\Delta G_{rxn} = \Delta G_{rxn}^{\theta} + RT \ln(Q_p),$$

$$Q_p = \frac{\left(\frac{P_C}{P^\circ} \right)^c \left(\frac{P_D}{P^\circ} \right)^d}{\left(\frac{P_A}{P^\circ} \right)^a \left(\frac{P_B}{P^\circ} \right)^b}$$

