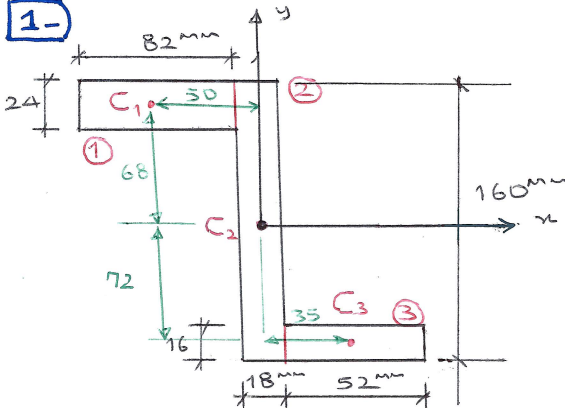




Problem Set 9 (PS9)

Solution

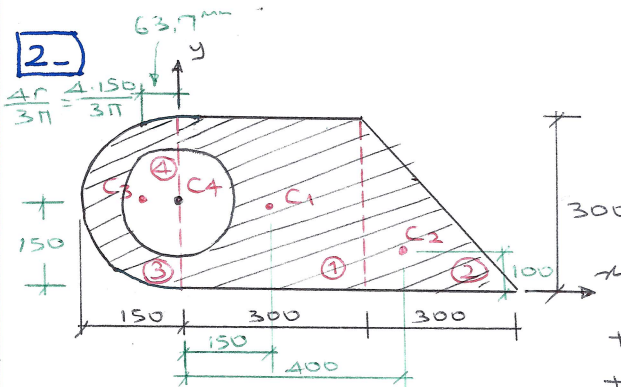


- First, divide the section into parts. Locate C_i of each part. Use a tabular solution.

$$\bar{x} = \frac{\sum A_i x_i}{\sum A_i} = \frac{-69280}{5680} = -12,2 \text{ mm}$$

$$\bar{y} = \frac{\sum A_i y_i}{\sum A_i} = \frac{73920}{5680} = 13,0 \text{ mm}$$

Part	$A_i (\text{mm}^2)$	$x_i (\text{mm})$	$y_i (\text{mm})$	$A_i x_i (\text{mm}^3)$	$A_i y_i (\text{mm}^3)$
1	$82 \cdot 24 = 1968$	-50	68	-98400	133824
2	$160 \cdot 18 = 2880$	0	0	0	0
3	$52 \cdot 16 = 832$	35	-72	29120	-59904
Σ	5680			-69280	73920



Answer:

Q1

- Need to do subtraction here

- Determine all parts to be considered.

- + ①: square ($300 \times 300 \text{ mm}^2$)
- + ②: triangle
- + ③: half circle ($r = 150 \text{ mm}$)
- ④: full circle ($r = 100 \text{ mm}$)

- Locate C of all parts.

- Use a tabular solution.

Part	$A_i (\text{mm}^2)$	$x_i (\text{mm})$	$y_i (\text{mm})$	$A_i x_i (\text{mm}^2)$	$A_i y_i (\text{mm}^2)$
1	$300 \cdot 300 = 90000$	150	150	$13,5 \cdot 10^6$	$13,5 \cdot 10^6$
2	$300 \cdot 300 / 2 = 45000$	400	100	$18,0 \cdot 10^6$	$4,50 \cdot 10^6$
3	$\pi \cdot 150^2 / 2 = 35343$	-63,7	150	$-2,25 \cdot 10^6$	$5,30 \cdot 10^6$
-4	$-\pi \cdot 100^2 = -31416$	0	150	-0	$-4,71 \cdot 10^6$
Σ	$138,9 \cdot 10^3$			$29,25 \cdot 10^6$	$18,59 \cdot 10^6$

$$\bar{x} = \frac{\sum A_i x_i}{\sum A_i} = \frac{29,25 \cdot 10^6}{138,9 \cdot 10^3} = 210,6 \text{ mm}$$

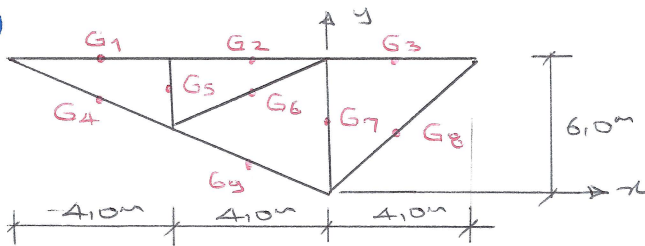
$$\bar{y} = \frac{\sum A_i y_i}{\sum A_i} = \frac{18,59 \cdot 10^6}{138,9 \cdot 10^3} = 133,8 \text{ mm}$$



3-

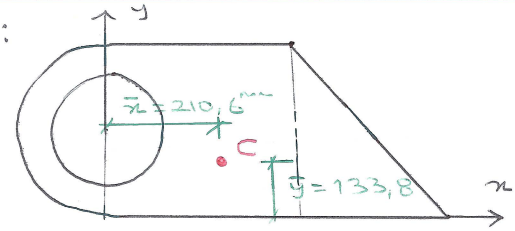
• $W = 8.9 = 20 \text{ kg/m} \cdot 10 \text{ m/s}^2 = 200 \text{ N/m}$

i-)



Answer:

Q2

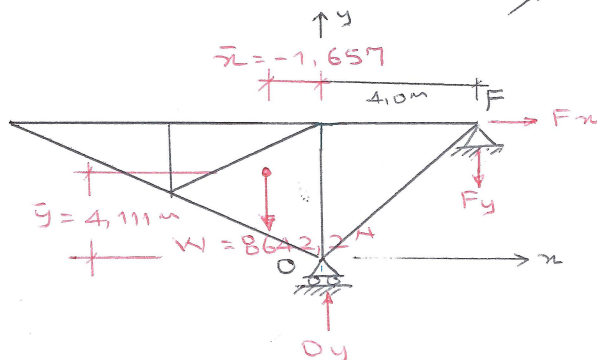


Part	$W_i \text{ (N)}$	$x_i \text{ (m)}$	$y_i \text{ (m)}$	$W_i x_i \text{ (N}\cdot\text{m)}$	$W_i y_i \text{ (N}\cdot\text{m)}$
1	$4.0 \text{ m} \cdot 200 \text{ N/m} = 800 \text{ N}$	-6.0	6.0	-4800	4800
2	800	-2.0	6.0	-1600	4800
3	800	2.0	6.0	1600	4800
4	$5.0 \text{ m} \cdot 200 \text{ N/m} = 1000$	-6.0	4.5	-6000	4500
5	$3.0 \cdot 200 = 600$	-4.0	4.5	-2400	2700
6	1000	-2.0	4.5	-2000	4500
7	$6.0 \cdot 200 = 1200$	0	3.0	0	3600
8	$7.21 \cdot 200 = 1442.2$	2.0	3.0	2884.4	4326.6
9	1000	-2.0	1.5	-2000	1500
$\Sigma =$	8642.2			-14315.6	35526.6

• $\bar{x} = \frac{\Sigma W_i x_i}{\Sigma W_i} = \frac{-14315.6}{8642.2} = -1.657 \text{ m}$

• $\bar{y} = \frac{\Sigma W_i y_i}{\Sigma W_i} = \frac{35526.6}{8642.2} = 4.111 \text{ m}$

ii-)



• $\Sigma M_F = 0$

$O_y \cdot 4.0 \text{ m} = 8642.2 \text{ N} \cdot (4.0 + 1.657)$
 $\Rightarrow O_y = 12222.2 \text{ N} (\uparrow)$

• $\Sigma F_y = 0$

$\Rightarrow F_y = 12222.2 - 8642.2 = 3580.0 \text{ N} (\downarrow)$

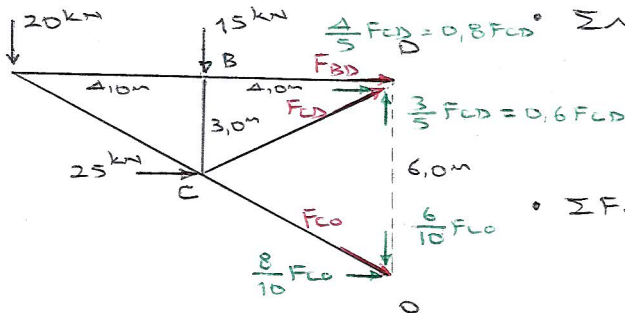
• $\Sigma F_x = 0$

$\Rightarrow F_x = 0$

• check: $\Sigma M_O = 8642.2 \cdot 1.657 - 3580.0 \cdot 4.0 \approx 0$ OK ✓

(iii)

First, look at members BD, CD, and CO. Try avoiding finding support rxns. Get a section cut just at the left of member DO.



$$\frac{4}{5} F_{CD} = 0,8 F_{CD} \quad \Sigma M_D = 0 \Rightarrow 15 \cdot 4,0 + 20 \cdot 8,0 + 25 \cdot 3,0 + 0,8 F_{CO} \cdot 6,0 = 0$$

$$\Rightarrow F_{CO} = -61,5 \text{ kN (C)}$$

$$\Sigma F_y = 0 \Rightarrow 0,6 F_{CD} - 20 - 15 - 0,6 F_{CO} = 0$$

$$\Rightarrow F_{CD} = -3,1 \text{ kN (C)}$$

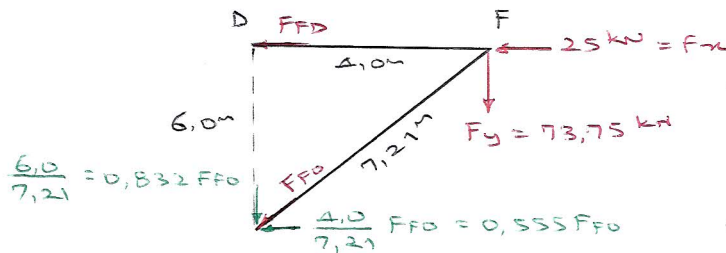
$$\Sigma F_x = 0 \Rightarrow 0,8 F_{CD} + 0,8 F_{CO} + 25 + F_{BD} = 0$$

$$\Rightarrow F_{BD} = 26,7 \text{ kN (T)}$$

Then look at members DF and OF. Need to find the support rxn at F.

$$\Sigma M_O = 0 \Rightarrow 20 \cdot 8^m + 15 \cdot 4^m = 25 \cdot 3^m + F_y \cdot 4,0 - 25 \cdot 6 \Rightarrow F_y = 73,75 \text{ kN}$$

F_x (↓)



$$\Sigma F_y = 0 \Rightarrow 0,832 F_{FO} + 73,75 = 0$$

$$\Rightarrow F_{FO} = -88,6 \text{ kN (C)}$$

$$\Sigma F_x = 0 \Rightarrow 25 + 0,555 F_{FO} + F_{FD} = 0$$

$$\Rightarrow F_{FD} = 24,2 \text{ kN (T)}$$

check results at point O.

$$\Sigma F_x = 0 \Rightarrow 0,8 F_{CO} - 0,555 F_{FO} = 0,027 \text{ kN} \approx 0 \quad \boxed{\text{OK}} \checkmark$$