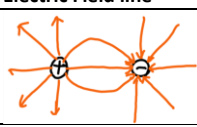
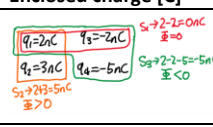
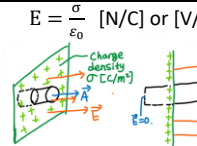
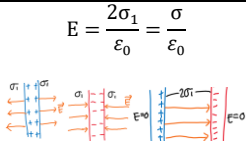
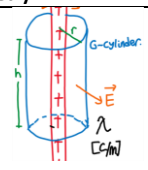
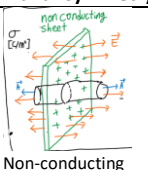
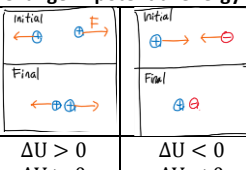
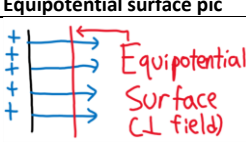
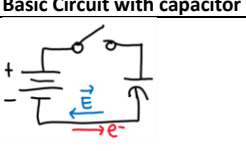
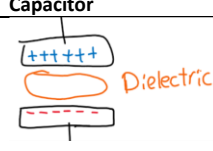
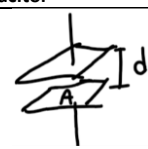


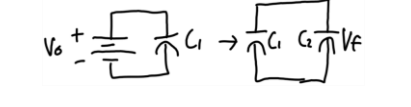




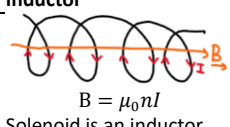


Coulomb's Law $F_{qQ} = \frac{1}{4\pi\epsilon_0} \frac{Qq}{r^2} \hat{r}$ $\epsilon_0 = 8.854 \cdot 10^{-12} [C^2/Nm^2]$ $k = 8.99 \cdot 10^9 [Nm^2/C^2]$	Electric Fields $E_Q = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} \hat{r}$	Electric Field line 	Electric Flux [Nm²/C] $\Phi_{net} = \oint_S E \cdot dA$ $= \oint_S E \cdot dA \cdot \cos(E dA)$	Enclosed charge [C]  $q_{enc} = \epsilon_0 \Phi_{net}$ $= \epsilon_0 \oint_S E \cdot dA$	Gaussian surface Sphere: 1 gaussian surf Cylinder: 3 gaussian surf Cube: 6 gaussian surf $dA = dA\hat{n} (\hat{n} \perp A)$
Isolated conductor $E = 0$ Cavity walls, inside isolated conductor, in metal (charges all reside at surface)	External elec. field $E = \frac{\sigma}{\epsilon_0} [N/C] \text{ or } [V/m]$ 	Two conducting planes $E = \frac{2\sigma_1}{\epsilon_0} = \frac{\sigma}{\epsilon_0}$ 	Charge Density (linear, surface, volume) Linear density λ $q_{tot} = \int \lambda(x) dx$ Surface density σ $q_{tot} = \iint \sigma(x, y) dxdy$ Volume density ρ $q_{tot} = \iiint \rho(x, y, z) dxdydz$		Spherical Symmetry $E_{ext} = \left(\frac{q}{4\pi\epsilon_0 R^3}\right) r$ r - radius of gauss surf R - radius of sphere q - charge enclosed $E_{int} = 0$
Cylindrical symmetry $E = \frac{\lambda}{2\pi\epsilon_0 r}$  $q_{enc} = \lambda h$ $= \epsilon_0 \oint_S E \cdot dA$	Planar symmetry  Non-conducting sheet (charge density of sigma) $E = \frac{\sigma}{2\epsilon_0}$ $\phi = \phi_1 + \phi_2 = 2EA$	Change in potential energy  $\Delta U > 0$ $\Delta V > 0$ Force applied $\Delta U < 0$ $\Delta V < 0$ Field does work	Potential Energy and Electric Potential $\Delta U = U_f - U_i$ $= W_{qappl} = -W_{field} [J]$ $= q(V_f - V_i) = -qE\Delta S$ $\Delta V = V_f - V_i [V]$ $= \frac{\Delta U}{q} = - \int_i^f E dS = -E\Delta x$		$\Delta V = - \int_i^f E dS$ $= \frac{Q}{4\pi\epsilon_0} \left(\frac{1}{r_2} - \frac{1}{r_1}\right)$
Voltage and Potential Energy $V_{r>\infty} = \frac{Q}{4\pi\epsilon_0 r}$ $U = \frac{Qq}{4\pi\epsilon_0 r}$ Voltages can be added up each other (scalar)	Equipotential surface pic 	Basic Circuit with capacitor 	Capacitor  *Metal plates > separation of charge *Dielectric > increase capacitance *Capacitor is charged	Capacitance $C = \frac{q}{V} [F]$ q - charge stored in one plate: not total charge!	
Parallel plate capacitor $E = \frac{Q}{A\epsilon_0}$ $V = \frac{Q}{A\epsilon_0} d$ $C_{pp} = \frac{A\epsilon_0}{d}$ (Ignore dielectric) 	Cylindrical Capacitor $E = \frac{Q}{2\pi\epsilon_0 L r} \hat{r}$ $V = \frac{Q}{2\pi\epsilon_0 L} \ln\left(\frac{b}{a}\right)$ $C_{cyl} = \frac{2\pi\epsilon_0 L}{\ln(b/a)}$ a is smaller radius, b is larger radius, L is height, r is radius of gaussian surface	Spherical capacitor $E = \frac{Q}{4\pi\epsilon_0 r^2} \hat{r}$ $V = \frac{Q}{4\pi\epsilon_0} \left(\frac{1}{a} - \frac{1}{b}\right)$ $C_{sphy} = \frac{4\pi\epsilon_0 ab}{b-a}$ $C_{single_sphy} = 4\pi\epsilon_0 r$	Parallel Capacitor  $Q_T = Q_1 + Q_2 + \dots$ $V_T = V_1 = V_2 = \dots$ $Q_T = C_T V$ $C_T = C_1 + C_2 + \dots$	Series Capacitor  $Q_T = Q_1 = Q_2 = \dots$ $V_T = V_1 + V_2 + \dots$ $\frac{1}{C_T} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$	Energy in capacitor $U = \int dU = \int q dV = \int CV dV$ $U = \frac{1}{2} CV^2 = \frac{1}{2} \frac{q^2}{C}$ $= \frac{1}{2} qV$
Energy Density $U_{pp} = \frac{U}{Volume} = \frac{U}{Ad} = \frac{CV^2}{2Ad}$ $= \frac{kA\epsilon_0 E^2 d^2}{2d} \frac{1}{Ad} = \frac{1}{2} k\epsilon_0 E^2$	Capacitance + dielectric Increase area + decrease distance + dielectric = high capacitance  $V_f = \frac{c_1}{c_1 + c_2} V_0$	$C_{pp} = \frac{k\epsilon_0 A}{d}$ $C_{cyl} = \frac{2\pi k\epsilon_0 L}{\ln\left(\frac{b}{a}\right)}$ $C_{sphy} = \frac{4\pi k\epsilon_0 ab}{b-a}$ k : dielectric constant ($k > 1$)	Ohm's Law and current $R = \frac{V}{I} [\Omega]$ $I = \frac{dq}{dt} [A]$ $= q_0 N A v_d$ $Q = q_0 N A L [C]$ $= q_0 N A v_d t$	Current Density $I = \iint J dA = JA$ $J = nq_0 v_d [A/m^2]$	Resistivity/Conductivity $\rho = \frac{ E }{ J } [\Omega m]$ $J = \frac{1}{\rho} E = \sigma E$ $\sigma = \frac{1}{\rho} [1/\Omega m]$ $R = \frac{El}{JA} = \rho \frac{l}{A}$
Power in Electric Fields $U = qRI$ $Power = \frac{dU}{dt}$ $Power = I^2 R = \frac{V^2}{R} = VI [W]$	Parallel Circuit ()  $V_T = V_1 = V_2 = \dots$ $I_T = I_1 + I_2 + \dots$ $\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$ $\Sigma I = 0$	Series Circuit (<->)  $V_T = V_1 + V_2 + \dots$ $I_T = I_1 = I_2 = \dots$ $R_T = R_1 + R_2 + \dots$ $\Sigma V = 0$	Magnetic Force $F_B = q(v \times B)$ $= Bqv \sin \theta$ θ is $\angle(v, B)$	Magnetic Field  Measured in [T]	Magnetic field 'inside'? $I_{tot} = \pi R^2 J_0$ $I_{enc} = \iint J dA = \pi r^2 J_0$ $(dA = r dr d\theta)$ $\oint_C B dS = \mu_0 I_{enc} = 2\pi Br$ $B = \frac{\mu_0 I_{tot} r}{2\pi R^2}$
Biot-Savart Law $dB = \frac{\mu_0 I (dS \times \hat{r})}{4\pi r^2}$ $\mu_0 = 4\pi \cdot 10^{-7} [H/m]$	Ampere's Law $\oint_C B dS = \mu_0 I_{enc} = \oint_C B \cos(B, dS) dS$ $B = \frac{\mu_0 I}{2\pi R}$	Magnetic field due to current Infinite wire $B = \frac{\mu_0 I}{4\pi} \int_{-\infty}^{\infty} \frac{\sin \theta}{r^2} dx$ $B = \frac{\mu_0 I}{2\pi R}$  Semi-infinite wire $B = \frac{\mu_0 I}{4\pi} \int_0^{\infty} \frac{\sin \theta}{r^2} dx$ $B = \frac{\mu_0 I}{4\pi R}$	Magnetic force (wire) $F_B = I(L \times B)$ $= BIL \sin \theta$ θ is $\angle(L, B)$	Force between two parallel currents $F = \frac{\mu_0 I_a I_b}{2\pi d}$ $\frac{\mu_0}{2\pi} = 2 \cdot 10^{-7}$	Solenoids $I_{enc} = nhI$ $\mu_0 I_{enc} = \mu_0 nhI = Bh$ $B = \mu_0 nI$ $(n = \text{number of loops/m})$ $(I = \text{current on the loop})$
Magnetic flux $\Phi_B = \iint B dA [Wb]$ $\Phi_B = BA = \mu_0 nIA$	EMF (Faraday/Lenz) $\epsilon = -(N) \frac{\partial \Phi_B}{\partial t} = -(N) \frac{\partial}{\partial t} \iint B dA$ Faraday's law - $\epsilon \propto \frac{\partial \Phi_B}{\partial t}$ Lenz' law - Direction of induced I and ϵ against induced B		EMF/current in loops $\epsilon = -(N)(N) B v_x l$ $I = \frac{(N) B v_x l}{R}$ I is induced by induced B	Power dissipated $P = VI = \frac{V^2}{R} = I^2 R = \frac{N^2 B^2 v^2 l^2}{R}$	Series Inductor $V_T = L_T \frac{dI}{dt}$ $L_T = L_1 + L_2 + \dots$
Inductor  $B = \mu_0 nI$ Solenoid is an inductor.	Inductance $L = \frac{N\Phi_B}{I} [H]$ $L = n^2 A l \mu_0$ $L = \frac{BAN}{I} = NAn\mu_0$ $(N = nl)$	Self-induction (ϵ_L) $\epsilon_L = -N \frac{\partial \Phi_B}{\partial t}$ $= -L \frac{d}{dt} I(t)$ $V_L = -\epsilon_L = L \frac{d}{dt} I(t)$	Energy in magnetic field $U = qV$ $dU = Vdq = qdV$ $Power = \frac{dU}{dt} = IV$ $dU = ILdI$ $U = \frac{1}{2} LI^2$	Ohm's law & power $V(t) = R I(t)$ $P(t) = V(t)I(t) = R I(t)^2 = \frac{(v(t))^2}{R}$ $R > 0 > V(t) = R I(t) = 0$ $R = \infty > I(t) = \frac{V(t)}{R} = 0$	Parallel inductor $V = L \frac{dI}{dt}$ $\frac{V}{L_T} = \frac{V}{L_1} + \frac{V}{L_2} + \dots$ $\frac{1}{L_T} = \frac{1}{L_1} + \frac{1}{L_2} + \dots$

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