

MIE 100S Quiz 1a Jan 12, 2015

First name and Last name printed correctly as seen on ROSI (1 mark)

Legibility and neatness (1 mark)

$$\text{Given: } a = \frac{175 \text{ m}}{v^2 \text{ s}^2} \text{ and } v_0 = 30 \frac{\text{m}}{\text{s}}$$

$$\begin{aligned} \frac{dv}{dt} &= a \\ \frac{dv}{dt} &= \frac{175}{v^2} \\ \int v^2 dv &= \int 175 dt \\ \frac{1}{3} v^3 &= 175t + C \end{aligned}$$

Can determine constant from initial conditions:

$$v_0 = v(t = 0) = 30 \frac{\text{m}}{\text{s}}$$

Plugging into equation above:

$$\begin{aligned} \frac{1}{3} (30)^3 &= 175(0) + C \\ C &= 9000 \end{aligned}$$

and therefore  $v$  is given by:  $v = \sqrt[3]{525t + 27000}$

$$\text{and } t \text{ is given by: } t = \frac{v^3}{525} - \frac{9000}{175}$$

$$a) v(t = 4) = \sqrt[3]{525(4) + 27000} = 30.76 \text{ m/s}$$

4 marks

$$b) t(v = 50) = \frac{50^3}{525} - \frac{9000}{175} = 186.67 \text{ s}$$

4 marks