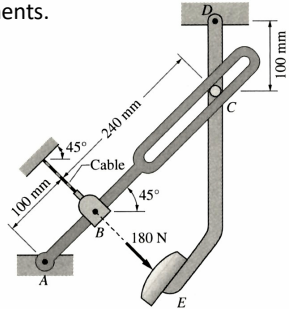


# CIV100F/APS160F – Mechanics: Final Exam 2017

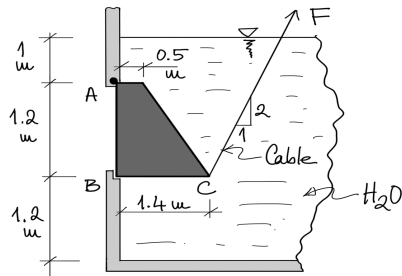
## Question 2

Determine the tension in the cable at  $B$  when the 180 N force is applied to the pedal at  $E$ . Also, calculate the reaction force components at the pins at  $A$  and  $D$ . If the cable at  $B$  has a diameter of 7.0 mm and the yield stress of the cable material is 70 MPa, determine the actual load (safety) factor for the cable. In your opinion, is this a 'safe' design? In all your calculations, neglect friction and the mass of the components.



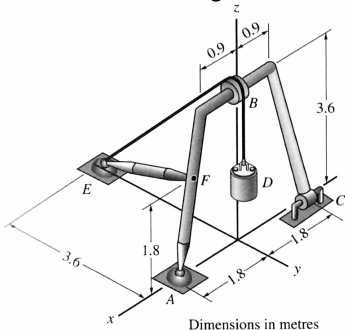
## Question 3

The fresh water channel illustrated can be emptied by opening the 6,300 kg solid gate  $ABC$  (represented in cross-section). The gate is 5 m wide (into the paper), is pinned at  $A$ , rests against the vertical wall at  $B$  and can be operated by pulling on the cable attached to it at  $C$ . Determine the minimum magnitude of the force,  $F$ , required to open the gate.



## Question 5

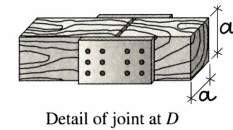
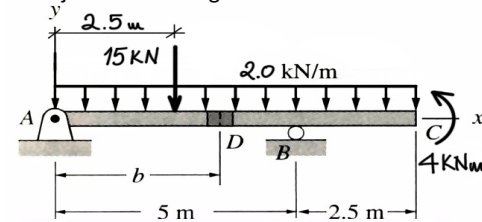
The frame shown is supported by a ball-and-socket joint at  $A$  and a pin at  $C$ . (The pin is similar to a ball-and-socket joint that was modified to allow translation in the  $x$ -direction.) The strut  $EF$  has a ball-and-socket joint at each end. The cable  $EBD$  runs over a small frictionless pulley at  $B$  and carries a 2,700 N weight at  $D$ . Neglecting the weight of the members, determine the force exerted by member  $EF$  on the frame at  $F$  and the magnitude of the total reaction at  $C$ .



## Question 1

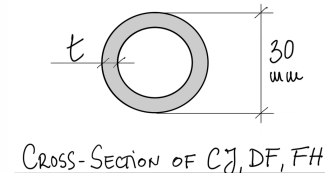
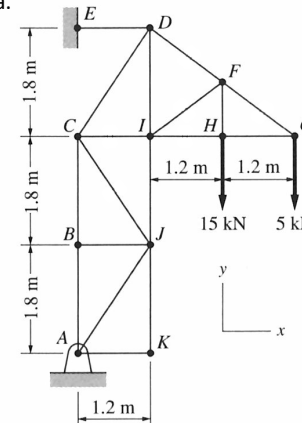
The 7.5 m-long timber floor beam, having a square cross-section, is to be designed to carry the loads shown. Because only 5 m-long timbers are available, the beam is to be fabricated from two pieces connected together by a nailed joint,  $D$ . You are required to:

- In the space provided, draw the shear force and bending moment diagrams for the beam indicating the values at points  $A$ ,  $B$ , and  $C$ , and any potential local maxima and minima;
- If wood has a strength of 30 MPa, in both tension and compression, determine the required size,  $a$ , for the beam such that it can safely carry the floor loads. The load factor for timber in bending is 1.67; and
- Determine the distance  $b$  for the most advantageous position of the joint  $D$ , knowing that nailed joints are strong in shear but weak in bending.



## Question 4

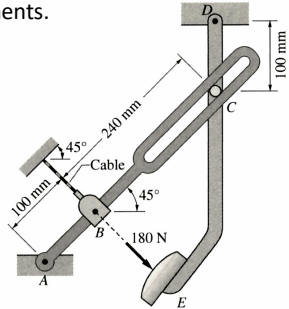
Determine the force in members  $BC$ ,  $CJ$ ,  $DF$ ,  $FH$ ,  $HI$  and state if the members are in tension or compression. Members  $CJ$ ,  $DF$  and  $FH$  are to be fabricated using the same circular hollow section having an external diameter of 30 mm and a yield stress of 150 MPa. Knowing that the load factor for members in axial tension is 1.5, determine the minimum wall thickness of the cross-section,  $t$ , such that the three members are safe. The wall thickness can be selected in 0.5 mm increments. Also, what is the elongation of member  $DF$ ? The modulus of elasticity for the material is 69,000 MPa.



# CIV100F/APS160F – Mechanics: Final Exam 2017

## Question 2

Determine the tension in the cable at  $B$  when the 180 N force is applied to the pedal at  $E$ . Also, calculate the reaction force components at the pins at  $A$  and  $D$ . If the cable at  $B$  has a diameter of 7.0 mm and the yield stress of the cable material is 70 MPa, determine the actual load (safety) factor for the cable. In your opinion, is this a 'safe' design? In all your calculations, neglect friction and the mass of the components.

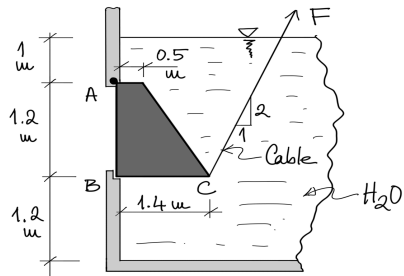


### Answers:

$$\begin{aligned} T_B &= 2,690 \text{ N (Tension)} \\ A_x &= 1,340 \text{ N} \rightarrow & A_y &= 1,340 \text{ N} \uparrow \\ D_x &= 432 \text{ N} \rightarrow & D_y &= 432 \text{ N} \downarrow \\ \text{L.F.} &= 1.00 - \text{Recommend to redesign} \end{aligned}$$

## Question 3

The fresh water channel illustrated can be emptied by opening the 6,300 kg solid gate  $ABC$  (represented in cross-section). The gate is 5 m wide (into the paper), is pinned at  $A$ , rests against the vertical wall at  $B$  and can be operated by pulling on the cable attached to it at  $C$ . Determine the minimum magnitude of the force,  $F$ , required to open the gate.

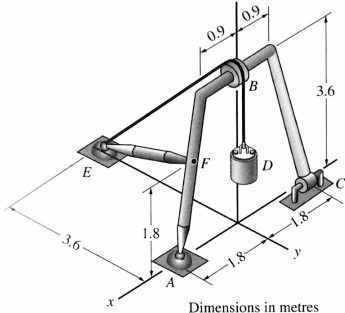


### Answer:

$$F_{\text{MIN}} = 37.2 \text{ kN (Tension)}$$

## Question 5

The frame shown is supported by a ball-and-socket joint at  $A$  and a pin at  $C$ . (The pin is similar to a ball-and-socket joint that was modified to allow translation in the  $x$ -direction.) The strut  $EF$  has a ball-and-socket joint at each end. The cable  $EBD$  runs over a small frictionless pulley at  $B$  and carries a 2,700 N weight at  $D$ . Neglecting the weight of the members, determine the force exerted by member  $EF$  on the frame at  $F$  and the magnitude of the total reaction at  $C$ .



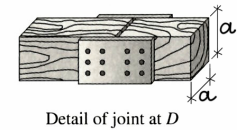
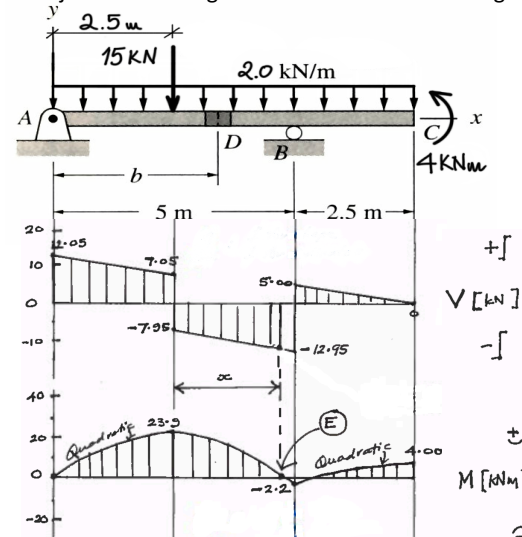
### Answers:

$$\begin{aligned} \vec{F}_{EF} &= 1,430\vec{i} + 3,820\vec{j} + 1,910\vec{k} \text{ N} \\ R_C &= 1,430 \text{ N} \end{aligned}$$

## Question 1

The 7.5 m-long timber floor beam, having a square cross-section, is to be designed to carry the loads shown. Because only 5 m-long timbers are available, the beam is to be fabricated from two pieces connected together by a nailed joint,  $D$ . You are required to:

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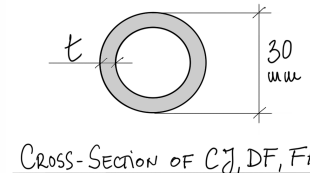
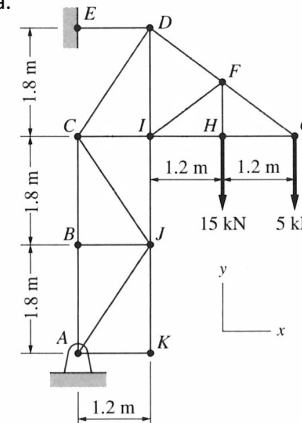


### Answers:

$$\begin{aligned} a &= 200 \text{ mm} \\ b &= 4.82 \text{ m} \\ &\text{(Place joint D at point E, where } M = 0) \end{aligned}$$

## Question 4

Determine the force in members  $BC$ ,  $CJ$ ,  $DF$ ,  $FH$ ,  $HI$  and state if the members are in tension or compression. Members  $CJ$ ,  $DF$  and  $FH$  are to be fabricated using the same circular hollow section having an external diameter of 30 mm and a yield stress of 150 MPa. Knowing that the load factor for members in axial tension is 1.5, determine the minimum wall thickness of the cross-section,  $t$ , such that the three members are safe. The wall thickness can be selected in 0.5 mm increments. Also, what is the elongation of member  $DF$ ? The modulus of elasticity for the material is 69,000 MPa.



### Answers:

$$\begin{aligned} F_{BC} &= 5.00 \text{ kN (C)} \\ F_{CJ} &= 18.18 \text{ kN (T)} \\ F_{DF} &= 20.8 \text{ kN (T)} \\ F_{FH} &= 15.00 \text{ kN (T)} \\ F_{HI} &= 6.67 \text{ kN (C)} \end{aligned}$$

(T = Tension; C = Compression)

$$\begin{aligned} t &= 2.50 \text{ mm} \\ \Delta_{DF} &= +2.10 \text{ mm} \end{aligned}$$