## Linear Model Project

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## Question 1

In this problem, Let  $\mathbf{y}$  denote stiffness  $(lb/in^2)$  and  $\mathbf{X}$  denote the design matrix. Since here we have 30 observations, the dimension of  $\mathbf{y}$  is  $30 \times 1$ . Then we have:

$$\mathbf{y} = \begin{pmatrix} 2622\\22148\\26751\\18036\\96305\\\vdots\\49499\\25312 \end{pmatrix}_{30 \times 1}$$

\

$$\mathbf{X} = \begin{pmatrix} 1 & 15.0 \\ 1 & 14.5 \\ 1 & 14.8 \\ 1 & 13.6 \\ 1 & 25.6 \\ \vdots & \vdots \\ 1 & 16.7 \\ 1 & 15.4 \end{pmatrix}_{30 \times 2}$$

Before running into questions, we firstly want to show

$$result1: \mathbf{X'X} = \begin{bmatrix} 30 & 464.1 \\ 464.1 & 8166.29 \end{bmatrix}$$
$$result2: (\mathbf{X'X})^{-1} = \begin{bmatrix} 0.2758892 & -0.0156791 \\ -0.0156791 & 0.001013517 \end{bmatrix}$$
$$result3: \mathbf{X'y} = \begin{bmatrix} 1017405 \\ 19589339 \end{bmatrix}$$

, and

$$result4: s^2 = 165242295.59$$

Below is my code to show these four results.

```
## [,1] [,2]
## [1,] 30.0 464.10
## [2,] 464.1 8166.29
```