

MASTER TEACHER'S GUIDE

Unit Title: The Final Empirical Proof (Week 3)

This module is the culmination of the No-Cloning Theorem study. Students execute the definitive lab, using advanced single-qubit gates (RY,P) and the **Bloch Sphere** to visually and empirically prove that a CNOT cannot universally clone an arbitrary, unknown quantum state ($|\psi\rangle$).

Field	Detail
Target Audience	Tier 4 - Advanced Level
Design Principle	Visual and Empirical Proof. Link the Week 2 mathematical derivations to the visual reality of State Corruption .
Learning Progression	Mathematical Proof → Visual Modeling (Bloch Sphere) → Universal Conclusion (No-Cloning).
Duration	1 Week (approx. 4×60–90 minute sessions)
Teacher Guidance	Proficiency in using RY and Phase gates to map arbitrary points on the Bloch sphere is required.

2. Pedagogical Framework: The Visual Argument

This unit forces students to use the primary visualization tool (the Bloch Sphere) as the final, unassailable evidence against the possibility of a Universal Cloning Machine.

Focus Area	Objective (The student will be able to...)	Bloom's Level
Computational Logic	Use RY and P gates to initialize an arbitrary unknown state ($ \psi\rangle$) on the Bloch Sphere.	Creating
Visual Analysis	Visually compare the final state of the Target qubit (q1) to the Input qubit (q0) on the Bloch Sphere to demonstrate corruption.	Evaluating

Synthesis	Formulate a generalized conclusion that links the No-Cloning Theorem to the security of Quantum Cryptography (BB84).	Creating, Evaluating
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3. Core Activity: The Universal Cloning Failure Lab

A. The Geometry of Failure (The Bloch Sphere)

Concept	Action	Key Observation
Arbitrary State	Use the $R_Y(\theta)$ and $P(\lambda)$ gates to move the input qubit (q_0) to a random point in the X-Y plane.	The complexity of the unknown state is essential, it is not an eigenstate of the CNOT's measuring basis.
The CNOT's Corruption	Apply the CNOT gate (Control q_0 , Target q_1).	When q_0 is measured in a superposition of $ 0\rangle$ and $ 1\rangle$, the CNOT forces q_1 into a state that is unrelated to $ \psi\rangle$, corrupting the target.
Final Proof	Students compare q_0 's final position (post-CNOT) with q_1 's final position on the Bloch Sphere.	Neither q_0 nor q_1 is in the original state $ \psi\rangle$. The state has been transformed into a single entangled system.

4. Exemplary Lesson Plan: Universal Quantum Clone Failure

Module: Applied Lab 2

This lesson uses the lab outlined in the initial prompt, placing it here to finalize the empirical proof of the theorem.

Composer Lab: Universal Quantum Clone Failure

Objective	To empirically prove the No-Cloning Theorem by visually demonstrating the failure of the CNOT gate to copy an arbitrary state.
Required Resources	IBM Quantum Composer, Bloch Sphere Visualization Tool, Tier 4 Worksheet (for recording RY/P settings).

Step-by-Step Instructions

Part 1: State Preparation ($|\psi\rangle$)

- 1. **Initialize Canvas:** Start with two qubits, q0 (Input) and q1 (Target), both at $|0\rangle$.
- 2. **Define $|\psi\rangle$:** Prepare q0 in an arbitrary non-basis state (e.g., $RY(\pi/3)$ followed by $P(\pi/2)$).
- 3. **Visualization Check:** Use the Bloch Sphere to confirm q0's location. q1 must remain at the North Pole ($|0\rangle$).

Part 2: Attempting the Clone (The Visual Failure)

- 1. **The Naive Copy:** Apply a **CNOT gate** ($q0 \rightarrow q1$).
- 2. **Observe Failure: Crucially, do not add measurement gates initially.** The Bloch Sphere viewer will show the resulting entangled state's representation.
 - o **Visual Test:** Observe q0 and q1. If the CNOT *had* worked, both spheres would show the exact same position as the initial $|\psi\rangle$.
 - o **Expected Result:** The Bloch Sphere for q1 will show a corrupted or undefinable state (often collapsed to the origin/center if the input state is in superposition), proving it is not a copy.
- 3. **Confirmation (Measurement):** Add measurement gates. The resulting 50/50 probabilities confirm the state's entangled nature (as derived in Week 2), but the Bloch Sphere provided the immediate, visual proof of corruption.

5. Conclusion and Next Steps

This **Tier 4, Week 3** module successfully concludes the theoretical and empirical foundation for quantum information security. The visual confirmation of state corruption (failure to clone) serves as the central security tenet.

The immediate next phase of development will focus on **Tier 4, Week 4** (Protocols), where students use the Bell state ($|\Phi+\rangle$) they learned to create in Week 2 as the **necessary resource** to circumvent the No-Cloning limitation via **Quantum Teleportation** and **Superdense Coding**.

6. Resources for Curriculum Implementation (Week 3)

Resource Name	Type	Purpose in Curriculum
Exemplary Lesson Plan	Universal Quantum Clone Failure	Step-by-step guidance for setting up arbitrary states.

IBM Quantum Composer	Visual Tool (Web)	Core platform for all Lab activities.
Bloch Sphere Visualization	Visual Tool (Graphical)	The essential tool for visually confirming state corruption.
Tier 4 Worksheets	Cloning Attempts	Assignments for recording the input (RY,P) settings and the final Bloch Sphere output positions.
Qiskit Textbook	Quantum Gates	Reference for RY and P gate definitions (rotation vs. phase shift).