# Dual Graph Attention Networks for Deep Latent Representa of Multifaceted Social Effects in Recommender Systems

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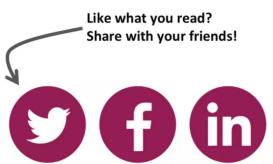




### Problem







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(a)

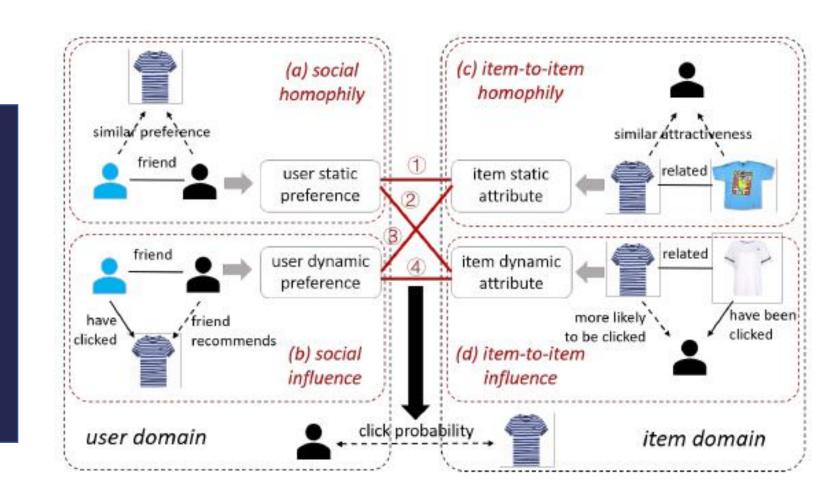




#### Motivation

#### four-fold social effects:

- social homophily
- social influence
- item-to-item homophily
- item-to-item



#### Related Works

Trust Propagation

Use the rating/clicking of friends to estimate the rating/clicking of the targeted user

Trust Matrix Factorization

Adopt latent user preference factor to retrieve the matrix of social trust

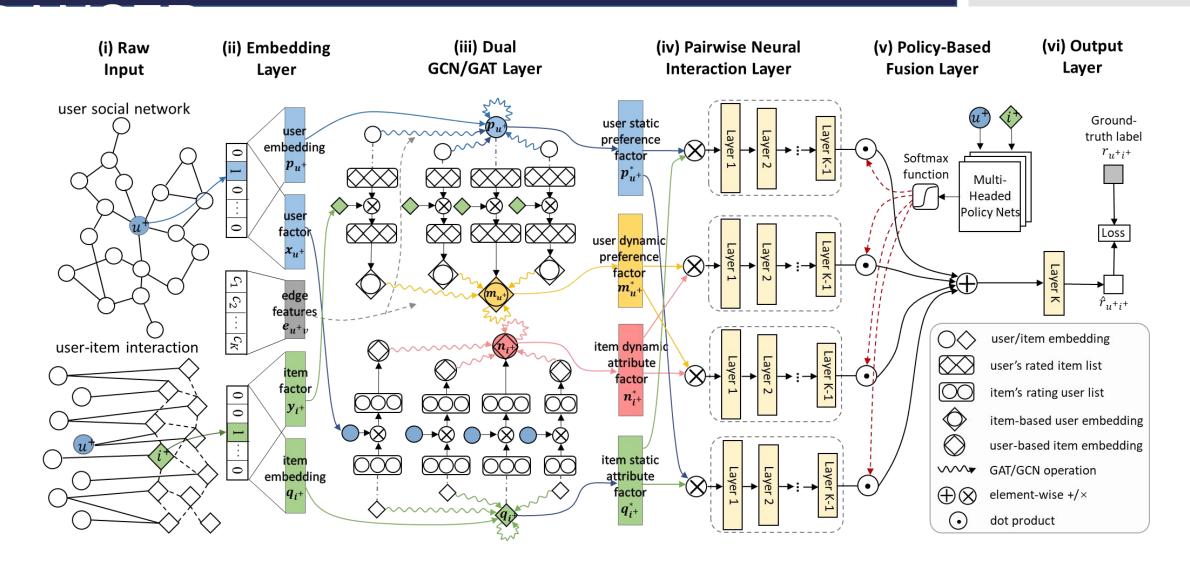
Trust Graph Regularization

Constrain the representations of neighbored users in social network to be similar

Trust Network Embedding

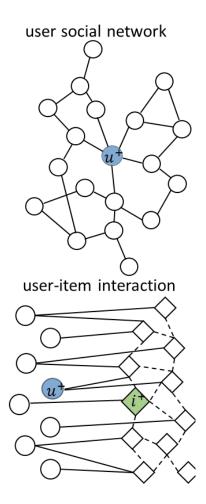
Treat user-item interaction network and social network as a whole network and use network embedding technique to encode the topology information as low-dimension features

### Our Model:



### Raw Input

#### (i) Raw Input



 $\begin{array}{ll} \text{user social} & G_U \\ \text{network} \\ \text{user-item interaction matri} \mathcal{R} \end{array}$ 

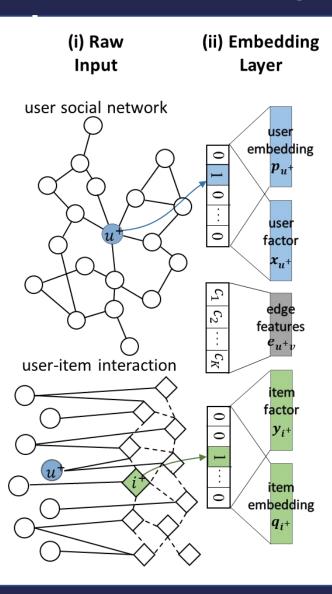
define item implicit network as  $G_I = (V_I, E_I)$ 

graph

similarity coefficients ij of item i and item j: number of users who clicked both items

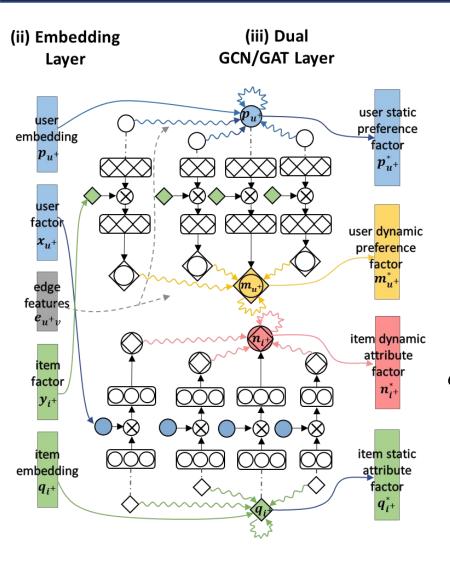
item i is related to item j if  $s_{ij} > \tau$ 

### Embedding



user embedding  $\mathbf{P} = \{\mathbf{p}_u\}_{D \times M}$  item embedding  $\mathbf{Q} = \{\mathbf{q}_i\}_{D \times N}$  user factor  $\mathcal{X}_i = \{\mathbf{x}_v | v \in R_U(i)\}$  item factor  $\mathcal{Y}_u = \{\mathbf{y}_j | j \in R_I(u)\}$  edge features  $e_{u,v}$ 

### Dual GCN/GAT Layer



#### GAT to capture social influence (user domain)

$$\mathcal{Y}_{u}^{i+} = \{\mathbf{y}_{i} \otimes \mathbf{y}_{i+} | j \in R_{I}(u)\}$$

$$m_{ud}^{i^+} = \max_{j \in R_I(u)} \{ y_{jd} \cdot y_{i^+d} \}, \forall d = 1, ..., D \qquad \alpha_{uv}^P = \frac{attn_U(\mathbf{W}_{p\mathbf{p}_u}, \mathbf{W}_{p\mathbf{p}_v}, \mathbf{W}_E \mathbf{e}_{uv})}{\sum_{w \in \Gamma_U(u)} attn_U(\mathbf{W}_{p\mathbf{p}_u}, \mathbf{W}_{p\mathbf{p}_w}, \mathbf{W}_E \mathbf{e}_{uv})}$$

$$\alpha_{uv}^{P} = \frac{attn_{U}(\mathbf{W}_{p\mathbf{p}_{u}}, \mathbf{W}_{p\mathbf{p}_{v}}, \mathbf{W}_{E}\mathbf{e}_{uv})}{\sum_{\mathbf{q} \neq tm} \mathbf{W}_{\mathbf{q}} \mathbf{W}_{\mathbf{q}} \mathbf{W}_{\mathbf{q}} \mathbf{w}_{\mathbf{q}}}$$

 $\mathbf{P}^* = \sigma(\mathbf{A}_P(G_U)\mathbf{P}\mathbf{W}_P^T + \mathbf{b}_n)$ 

GAT to capture social

homophily (user domain)

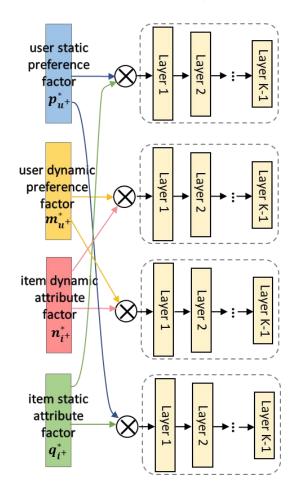
$$M_{i^+}^* = \sigma(\mathbf{A}_M(G_U)\mathbf{M}\mathbf{W}_M^T) + \mathbf{b}_{\mathbf{M}}, \mathbf{A}_M(G_U) = \{\alpha_{uv\hat{M},i^+\}_{M\times M}}\}$$

$$\alpha_{uv,i^{+}}^{M} = \frac{\operatorname{attn}_{U}(\mathbf{W}_{M}\mathbf{m}_{u}^{i^{+}}, \mathbf{W}_{M}\mathbf{m}_{v}^{i^{+}}, \mathbf{W}_{M}\mathbf{E}\mathbf{e}_{uv})}{\sum\limits_{w \in \Gamma_{U}(u)} \operatorname{attn}_{U}(\mathbf{W}_{M}\mathbf{m}_{u}^{i^{+}}, \mathbf{W}_{M}\mathbf{m}_{w}^{i^{+}}, \mathbf{W}_{M}\mathbf{E}\mathbf{e}_{uv})}$$

Formulas of GAT in item domain are similar

### Pairwise Neural Interaction Layer

#### (iv) Pairwise Neural Interaction Layer



# Multi-layer fully-connected neural networks

$$\mathbf{s}_a = \phi_K^a(\cdots \phi_2^a(\phi_1^a(\mathbf{z}_0[a]]))$$

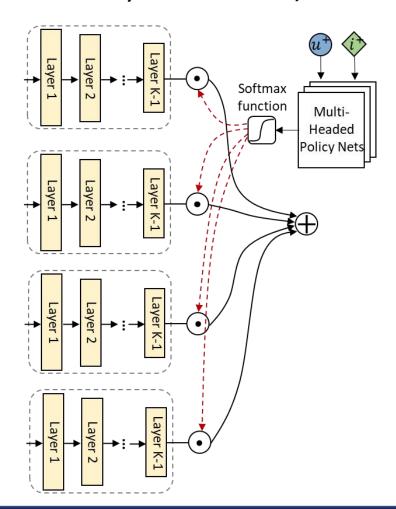
$$\phi_k^a(\mathbf{z}_{k-1}) = \tanh(\mathbf{W}_k^a \mathbf{z}_{k-1}^a + \mathbf{b}_k^a), k \in [1, K-1]$$

$$\mathbf{z}_0 = [\mathbf{p}_\mathbf{u}^* \oplus \mathbf{q}_\mathbf{i}^*, \mathbf{p}_\mathbf{u}^* \oplus \mathbf{n}_\mathbf{i}^*, \mathbf{m}_\mathbf{u}^* \oplus \mathbf{q}_\mathbf{i}^*, \mathbf{m}_\mathbf{u}^* \oplus \mathbf{n}_\mathbf{i}^*]$$

### Policy-Based Fusion Layer

#### (iv) Pairwise Neural Interaction Layer

#### (v) Policy-Based Fusion Layer

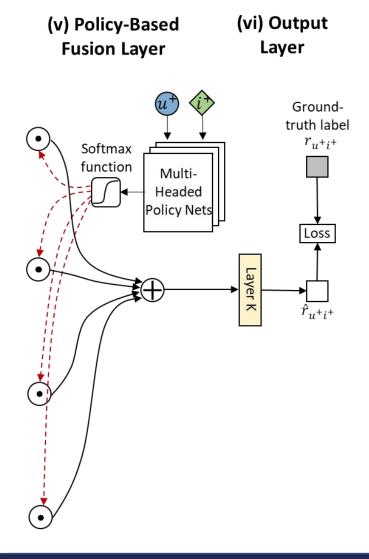


$$e_{\gamma} = \mathbf{W}_F^2 \tanh(\mathbf{W}_F^1(\mathbf{p}_u||\mathbf{q}_i) + \mathbf{b}_F^1) + \mathbf{b}_F^2.$$

$$p(\gamma|\mathbf{p}_u, \mathbf{q}_i) = \frac{\exp(e_\gamma)}{\sum_{a=1}^4 \exp(e_a)}$$

$$\mathbf{s} = \mathbb{E}_{\gamma \sim p(\gamma | \mathbf{p}_u, \mathbf{q}_i)}(\mathbf{s}_{\gamma}) = \sum_{\gamma=1}^{4} (p(\gamma | \mathbf{p}_u, \mathbf{q}_i) \cdot \mathbf{s}_{\gamma})$$

### Output Layer



A fully-connected layer without activation function

implicit

feedback:

explicit feedback:

$$\mathcal{L}_1 = -\sum_{(u,i)} r_{ui} \log \hat{r}_{ui} + (1 - r_{ui}) \log(1 - \hat{r}_{ui})$$

$$\mathcal{L}_1 = \sum_{(u,i)} ||\hat{r}_{ui} - r_{ui}||^2$$

### Training

## Mini-Batch & Sampling

Sample neighbored nodes

Truncate history sequence

B(u,i) interaction pairs for each training

 $F_U(u)$   $F_I(i)$  Neighbored nodes for user and item

 $R_I(v)$   $R_U(j)$  History sequence for user and item

Uniformly sample F neighbored nodes for each user and item

Truncate recent C clicked items for each user

Truncate recent C infected users for each item

 $F_U(u)$   $F_I(i)$  Size  $B \times F$  for one batch

 $R_I(v)$   $R_U(j)$  Size  $B \times F \times C$  for one batch

### Training

#### Local-Graph Aware Regularization

L1 regularization

$$\mathcal{L}_{2} = \sum_{u} (||p_{u}|| + ||x_{u}||) + \sum_{i} (||q_{i}|| + ||y_{i}||).$$

$$\mathcal{L}_{2} = \frac{1}{2} \sum_{(u,i)} [||\mathbf{p}_{u}|| + ||\mathbf{x}_{u}||] + ||\sum_{v \in \Gamma_{U}(u)} \frac{1}{|F_{U}(v)|} (||\mathbf{p}_{v}|| + ||\mathbf{x}_{v}||)$$

$$+ ||\mathbf{q}_{i}|| + ||\mathbf{y}_{i}|| + \sum_{j \in \Gamma_{I}(j)} \frac{1}{|F_{I}(j)|} (||\mathbf{q}_{j}|| + ||\mathbf{y}_{j}||)$$

final loss function

$$\mathcal{L} = \mathcal{L}_1 + \lambda \mathcal{L}_2$$

### Training

### **Policy Gradient**

I-th policy network  $\ p_l(\gamma|\mathbf{p}_u,\mathbf{q}_i)$ 

draw  $\gamma \sim Multi(p_l(\gamma|\mathbf{p}_U,\mathbf{q}_i))$ 

$$\mathcal{R}(p_u, q_i, \gamma) = -\mathcal{L}(\mathbf{s}_{\gamma})$$

maximize the expected reward

$$\mathbb{E}_{\gamma \sim p(\gamma|p_u,q_i)}(\mathcal{R}(p_u,q_i,\gamma))$$

calculate gradient

$$\nabla_{\theta} \mathbb{E}_{\gamma \sim p_{\theta}(\gamma | \mathbf{p}_{u}, \mathbf{q}_{i})} (\mathcal{R}(\mathbf{p}_{u}, \mathbf{q}_{i}, \gamma))$$

$$\simeq \frac{1}{4} \sum_{\gamma} \nabla_{\theta} \log p_{\theta}(\gamma | \mathbf{p}_{u}, \mathbf{q}_{i}) \mathcal{R}(\mathbf{p}_{u}, \mathbf{q}_{i}, \gamma)$$

### Justification of Dual GATS

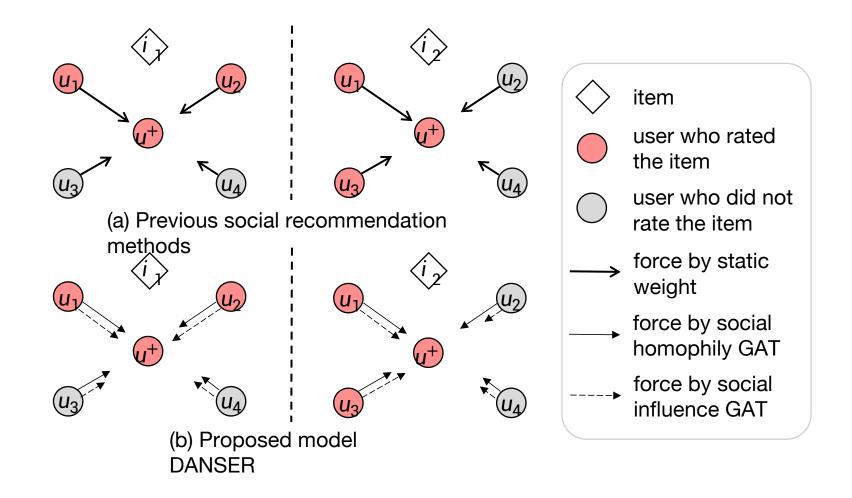




Table 1: Statistics of three datasets.

Dataset	#users	#items	#interactions	#relationships
Epinions	49,290	139,738	664,824	487,181
WeChat	~200,000	~100,000	~4,000,000	~2,000,000

#### **Evaluation Protoc**

Data partition For Epinions, randomly 80% for training and 20% for testing

For Wechat, sequentially 90% for training, 10% for testing

Evaluation metrics For Epinions, *MAPE* and *RMSE* for accuracy of 1~5 score prediction

For Wechat, *Precision@10* and *AUC* for accuracy of 0-1 classification

Implementation Python with Tensorflow + GTX 1080 GPU with 8G memory

### Competitive Method

Collaborative filtering SVD++Basic collaborative filtering method

> Dual embedding method – IJCAI'18 **DELF**

Social recommendation Trust propagation — SIGIR'11 TrustPro

> TrustMF Trust matrix factorization – IJCAI'13

> TrustSVD Trust matrix factorization – AAAI'15

**NSCR** Graph regularization – SIGIR'17

Network embedding – AAAI'18 **SREPS** 

**Table1:** Comparative results for Epinions and Wechat. For MAE, RMSE, the smaller value is better and vice versa for P@10, AUC.

	Epinions		WeChat	
	MAE	RMSE	P@10	AUC
SVD++ [15]	0.8321	1.0772	0.0653	0.7304
DELF [2]	0.8115	1.0561	0.0752	0.7818
TrustPro [37]	0.9130	1.1124	0.0561	0.6482
TrustMF [36]	0.8214	1.0715	0.0625	0.7005
TrustSVD [10]	0.8144	1.0492	0.0664	0.7325
NSCR [31]	0.8044	1.0425	0.0736	0.7727
SREPS [16]	0.8014	1.0393	0.0725	0.7745
DANSER	0.7781	1.0268	0.0823	0.8165
Impv. <sup>1</sup>	2.87%	1.25%	9.33%	4.48%

<sup>&</sup>lt;sup>1</sup> The improvement compares DANSER with the best competitor (underlined).

**Table2:** Ablation study of components in proposed method

	Epir	nions	WeChat		
	MAE	RMSE	P@10	AUC	
DualEMB	.7920(1.7%) <sup>1</sup>	1.0363(0.7%)	.0794(3.6%)	.7992(2.2%)	
<b>DualGCN</b>	.7840(0.7%)	1.0335(0.4%)	.0814(1.1%)	.8102(0.8%)	
userGAT	.7858(0.9%)	1.0364(0.7%)	.0813(1.2%)	.8136(0.4%)	
itemGAT	.7919(1.7%)	1.0335(0.4%)	.0813 (1.2%)	.8138(0.3%)	
DANSER-w	.8191(4.9%)	1.0659(3.4%)	.0820(0.4%)	.8151(0.2%)	
DANSER-m	.8211(5.2%)	1.0681(3.6%)	.0815(1.0%)	.8144(0.3%)	
DANSER-a	.8232(5.4%)	1.0710(3.9%)	.0814 (1.1%)	.8140(0.3%)	
DANSER-c	.8091(3.8%)	1.0659(3.4%)	.0809(1.7%)	.8118(0.6%)	
DANSER	0.7787	1.0292	0.0823	0.8165	

<sup>&</sup>lt;sup>1</sup> The ratio indicates the impv. comparing DANSER with corresponding variant.

### Case Study

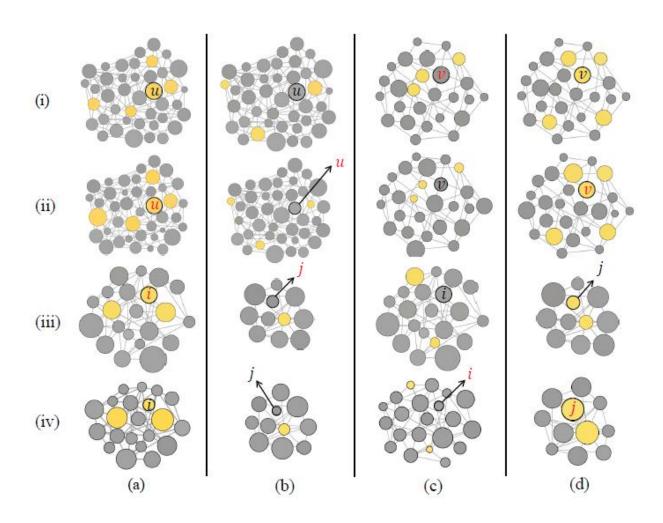


Figure3: Visualization of the four GAT's weights for a case study

### Conclusions

Our contributions can be summarized as follows

- i) General Aspects: 4 different social effects in recommendation (heterogeneous and dynamic)
- ii) Novel Methodologies: GAT + policy fusion
- iii) Multifaceted Experiments: comparison + ablation study + parameter sensitivity + interpretable visualization

#### Available sources

Paper & Codes:

https://github.com/echo740/DANSER

Contact us: echo740@sjtu.edu.cn

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