

HKUST Jockey Club IAS, PTC, 2023

High-Quality Axions in a Class of Chiral U(1)Gauge Theories

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Strong CP and Axion

Frameworl

QCD Axio

Fuzzy DM

i uzzy Divi

Axion

Summary

High-Quality Axions in a Class of Chiral U(1) Gauge Theories

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Why axion?

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Strong CP problem?

$$\mathcal{L}\supset ar{ heta}G ilde{G}$$
 , $ar{ heta}<10^{-10}$

Why $\bar{\theta}$ is so small?

► Peccei-Quinn mechanism:

anomalous global
$$U(1)$$
 $\stackrel{SSB}{\longrightarrow}$ shift symmetry $\frac{a}{F_a} \rightarrow \frac{a}{F_a} + \delta_{PQ}$

$$\stackrel{anomaly}{\longrightarrow} \quad \mathcal{L} \supset \left(\bar{\theta} + \frac{a}{F_a}\right) G \tilde{G} \stackrel{instanton}{\longrightarrow} \quad V(a) \sim \cos\left(\bar{\theta} + \frac{a}{F_a}\right)$$

► *CP*-invariance · · ·



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► Observed Cosmological Constant

$$\Lambda_{
m obs} \simeq 10^{-120} M_{
m Pl}^4$$

- \bullet If it is the potential of a scalar, the mass must be extremely small, $\sim 10^{-33}\,\text{eV}.$
- Fuzzy Dark Matter

$$m \sim 10^{-20} \text{--} 10^{-19} \, \text{eV}$$

All of them could be Nambu-Goldstone boson! Axion!



Axion Quality Problem

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Summar

 $U(1)_{PQ}$ is a global symmetry, which could easily be explicitly broken at least by gravity (wormhole).

Suppose the axion belongs to $\Phi \sim e^{ia/F_a}$, then

$$g \xrightarrow{\Phi^n} \xrightarrow{\langle \Phi \rangle \sim F_a} \Delta V(a) = M_{\rm Pl}^4 \left(\frac{F_a}{M_{\rm Pl}} \right)^n \cos \left(\frac{a}{F_a} + \underbrace{\beta}_{\text{arg } g} \right)$$

$$V=V(a)+\Delta V(a) \stackrel{ar{ heta}<10^{-10}}{\longrightarrow} n>10 ext{ for } F_a\sim 10^{16}\, ext{GeV}$$

One shall suppress all terms at least up to order 10!



"Gauged" PQ symmetry

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Summary

The goal is to construct a framework that can easily have high quality axion.

Idea

- Suppose there are 2 complex scalar fields, then one has global $U(1) \times U(1)$. phase rotations
- One linear combination could be gauged, $U(1)_g$, and another one is the global $U(1)_{PQ}$.
- ▶ To have an anomalous $U(1)_{PQ}$, chiral fermions shall be introduced.



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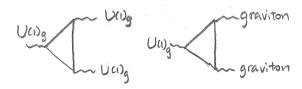
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Summarv

Introduce N pairs of chiral fermions charged under $U(1)_g$, $\{\psi_i, \overline{\psi}_i\}$, where $\psi_i \in (\mathbf{3}, 1, 0)$ and $\overline{\psi}_i \in (\mathbf{3}^*, 1, 0)$ under $SU(3)_c \times SU(2)_L \times U(1)_Y$. Anomaly cancellation condition requires that

$$\sum_i Q_i^3 = 0 \; , \qquad \sum_i Q_i = 0$$





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► Assume that 2 Higgs given all chiral fermion mass,

and only through Yukawa interaction.

TABLE I. Fermion charge assignment.

\overline{i}	1	2	3	4			k+1	k+2					
ψ_i	α_1	eta_1	α_2	β_2	 γ_1	γ_2	 δ_1	η_1	δ_2	η_2	 σ_1	σ_2	
$\overline{\psi}_i$	eta_1	$lpha_1$	β_2	α_2	 γ_1	γ_2	 η_1	δ_1	η_2	δ_2	 σ_1	σ_2	

Suppose N = k + l pairs, k pairs coupled to $\phi_1(q_1)$ and l pairs coupled to $\phi_2(q_2)$.

By proper charge assignment, one could have

$$-\frac{q_1}{q_2} = \frac{k}{l} = \frac{m}{n}$$

(n, m) are relatively prime number to each other.



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Summary

$$\mathcal{L}\supset -\phi_1\sum_i c_i\psi_i\overline{\psi}_i -\phi_2\sum_j c_j\psi_j\overline{\psi}_j$$

Interestingly, there is an anomaly-free \mathbf{Z}_{2N} symmetry, where

$$\psi_i(+1) , \quad \overline{\psi}_i(+1) , \quad \phi_{1,2}(-2) .$$

We gauge it. Will be useful later.

The lowest-order non-renormalizable operator that obey $U(1)_g$ and \mathbf{Z}_{2N} is

$$\mathcal{O} = \frac{1}{k! l!} \frac{\phi_1^k \phi_2^l}{M_{\text{Pl}}^{N-4}}$$

The \mathbf{Z}_{2N} and fermion loop.

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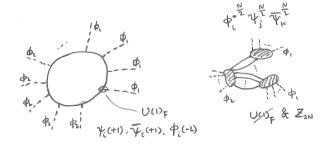
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$$\mathcal{L}_0 = -\phi_1 \sum_i c_i \psi_i \overline{\psi}_i - \phi_2 \sum_j c_j \psi_j \overline{\psi}_j$$

Accidentally, it contains a global $U(1)_F$.



- \triangleright Converging diagram does not contribute to \mathcal{O} .
- Diverging diagrams are more suppressed due to the loop factors.

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Focus on the axionic mode.

$$\phi_1 \sim \mathrm{e}^{i ilde{a}/f_1} \;, \quad \phi_2 \sim \mathrm{e}^{i ilde{b}/f_2}$$

Spontaneous symmetry breaking, $\langle \phi_1 \rangle \sim \mathit{f}_1$ and $\langle \phi_2 \rangle \sim \mathit{f}_2$.

$$|D_\mu\phi_1|^2+|D_\mu\phi_2|^2 \quad o \quad rac{1}{2}(\partial_\mu a)^2+m_A^2\left(A_\mu-rac{1}{m_A}\partial_\mu b
ight)^2.$$

where

$$\begin{pmatrix} a \\ b \end{pmatrix} = \frac{-1}{\sqrt{q_1^2 f_1^2 + q_2^2 f_2^2}} \begin{pmatrix} q_2 f_2 & -q_1 f_1 \\ q_1 f_1 & q_2 f_2 \end{pmatrix} \begin{pmatrix} \tilde{a} \\ \tilde{b} \end{pmatrix}$$

$$rac{a}{F_a} \in [0, 2\pi) \; , \quad F_a = rac{f_1 f_2}{\sqrt{m^2 f_1^2 + n^2 f_2^2}}$$



Breaking Operator

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Summary

$$\mathcal{O} = \frac{1}{k!I!} \frac{\phi_1^k \phi_2^l}{M_{\rm Pl}^{N-4}} \sim \exp\left(i \frac{aN_{\rm DW}}{F_a}\right), \quad N_{\rm DW} = {\sf GCD}[k, I]$$

Anomaly term is

$$\mathcal{L} \supset N_{\text{DW}} \frac{a}{F_2} G \tilde{G}$$

- ▶ Choosing large k and l, one could have highly suppressed O.
- ▶ Gauged \mathbf{Z}_{2N} prevent possible converging fermion loop contributing to \mathcal{O} .
- \blacktriangleright Given k and l, one needs to solve for fermion charges Q_i under

$$\sum_i Q_i^3 = 0$$

A general mathematical problem. Tricks Required!

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Summary

Take k = 3 and l = 2x, and assume that GCD[3, 2x] = 1.

$$\delta ar{ heta} \sim rac{2}{3!(2x)!} \left(rac{F_a}{M_{ ext{Pl}}}
ight)^N \left(rac{9+4x^2}{2}
ight)^{N/2} rac{M_{ ext{Pl}}^4}{m_\pi^2 F_\pi^2}$$

 \bullet $F_a=10^{12}\,\mathrm{GeV}$, x=7, $\deltaar{ heta}\sim10^{-26}$

$$\{-19,-9,-14|-17,23,-4,10,-2,8,-2,8,-2,8,-2,8,1,5\}$$

• $F_a = 10^9 \, \text{GeV}$, x = 4, $\delta \bar{\theta} \sim 10^{-23}$

$$\{-5, -3, -4 | -3, 6, 1, 2, 1, 2, 1, 2\}$$



Fuzzy DM

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Summary

Assume that $\psi_i \in (1, \mathbf{2}, 0)$ and $\overline{\psi}_i \in (1, \mathbf{2}^*, 0)$ under SM gauge group.

$$\mathcal{L} \supset N_{\mathsf{DW}} rac{a}{F_a} W ilde{W}$$

- Electroweak instanton contribution negligible without SUSY. Nomura, Watari, and Yanagida (2000)
- Potential mainly from \mathcal{O} .

$$V = \frac{\Lambda_a}{2} \left(1 - \cos \frac{aN_{\rm DW}}{F_a} \right) \; , \quad \Lambda_a = \frac{2^{2-N/2}}{k! /!} \frac{f_1^k f_2^l}{M_{\rm Pl}^{N-4}}$$



Fuzzy DM

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Summary

The mass of axion is determined by $\partial_a^2 V|_{\min}$,

$$m_a = N_{\rm DW} M_{\rm Pl} \sqrt{\frac{2}{k! I!}} \left(\frac{m^2 + n^2}{2}\right)^{N/4} \left(\frac{F_a}{M_{\rm Pl}}\right)^{-1 + N/2}$$

• k=7, l=42 and $F_a=10^{16}\,\mathrm{GeV}$ \longrightarrow $m_a=2.5\times 10^{-20}\,\mathrm{eV}.$

$$\{-21|4,3,16,-9,20,-13\}\times 7\;,\quad \textit{N}_{DW}=7$$



Quintessence Axion

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Same as the Fuzzy DM scenario, the potential is

$$V = rac{\Lambda_a}{2} \left(1 - \cos rac{a N_{
m DW}}{F_a}
ight) \; , \quad \Lambda_a = rac{2^{2-N/2}}{k! I!} rac{f_1^k f_2^I}{M_{
m Pl}^{N-4}}$$

• k=8 and I=72, $\Lambda_a=1.88\Lambda_{\rm obs}$ and $F_a/N_{\rm DW}=3.3\times 10^{16}~{\rm GeV}.$

$$\{-27|5, 1, 15, -9, 19, -13, 29, -23, 3\} \times 8, \quad N_{DW} = 8$$



Instability Problem

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Cosmic evolution

$$\ddot{a} + 3H(t)\dot{a} + \partial_a V = 0$$

Suppose $a_{\rm ini}$ locates around the bottom, $\partial_a V \sim m_a^2 a$,

$$m_a \sim \sqrt{rac{\Lambda_a N_{
m DW}}{F_a^2}} > \sqrt{N_{
m DW}} imes 10^{-33} \, {
m eV} \quad {
m for} \quad F_a \lesssim M_{
m Pl}$$

One has to put a_{ini} around the hilltop.

One needs large enough $\frac{F_a}{N_{\text{DW}}}$ to stabilize it.



New Scenario on Quintessence Axion

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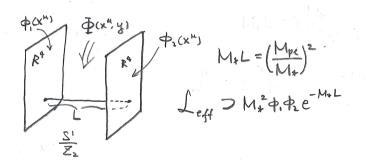
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Flat extra dimension. Fundamental scale is M_* .





New Scenario on Quintessence Axion

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Summary

$$V = \frac{\Lambda_a}{2} \left(1 - \cos \frac{a}{F_a} \right)$$

$$\Lambda_a \approx \Lambda_{\rm obs} \left(\frac{M_*}{1.47 \times 10^{17} \, {\rm GeV}} \right)^{515} , \quad F_a = \frac{M_*}{\sqrt{2}} \approx 1.04 \times 10^{17} \, {\rm GeV}$$

- ightharpoonup Gauged \mathbf{Z}_{2N} is not needed.
- Only 2 pairs of fermions are needed.
- ▶ No instability problem. $F_a > 10^{17}$ GeV.
- ▶ Simple $U(1)_g$ charge assignment.



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- ▶ High quality axion(s) could be easily constructed in this framework.
- ▶ The quality is protected by gauged $U(1)_g$ and \mathbf{Z}_{2N} .
- ▶ The QCD axion constructed under this framework has $N_{DW} = 1$.
- ▶ $N_{\rm DW} \frac{a}{F_a} W \tilde{W} \longrightarrow c_{\gamma} \frac{a}{F_a} F \tilde{F}$, quintessence axion could explain the isotropic cosmic birefringence. Lin & Yanagida (2022)
- ▶ If extra dimension is introduced, model become simpler and quintessence axion becomes more attractive.
- $ightharpoonup \phi_{1,2}$ could be identified as inflaton(s).
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Thank you!