Homework 2 of Computational Mathematics

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1.
$$x^3 = x + 1 \implies x^2 = 1 + \frac{1}{x} \implies x = \sqrt{1 + \frac{1}{x}} = g(x)$$
. $p_1 = g(p_0) = \sqrt{1 + 1} = \sqrt{2} \approx 1.414$. $p_2 = g(p_1) = \sqrt{1 + \frac{1}{\sqrt{2}}} \approx 1.3065$. $p_3 = g(p_2) \approx 1.324$ is the answer that we want to find.

2. Let
$$a_0 = 1, b_0 = 4$$
. $f(a_0) = -2, f(b_0) = f(2.5) = 14.125$